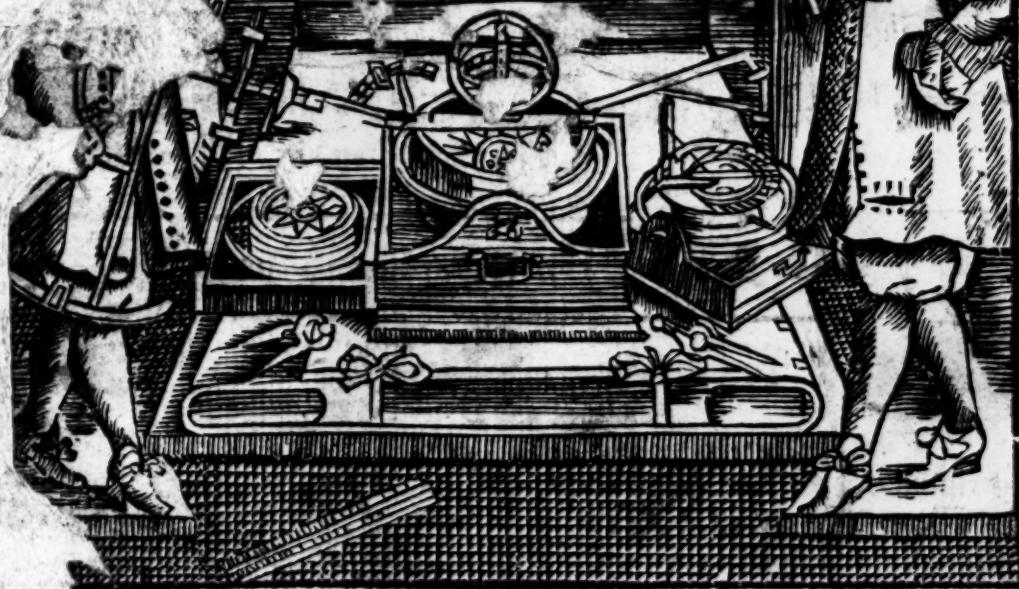


Practical
NAVIGATION,
OR
An Introduction,
to the Whole
ART.

By John Seller, Hydro-
grapher to the KING.



* 1819

Practical Navigator

OR AN

Introduction to the Who

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Practical Navigation

OR AN

Introduction to the Whole Art.

CONTAINING

The Doctrine of Plain and Spherical Triangles. Plain, Mercator, Great Circle Sailing; and Astronomical Problems. The Use of divers Instruments; as also of the Plain Chart, *Mercator's* Chart, and both Globes. Sundry Useful Tables in Navigation: And a Table of 10000 *Logarithms*, and of the *Logarithm Sines, Tangents, and Secants*. All carefully Corrected.

By John Seller, Hydrographer to the KING.

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 Paper-Books; the best Ink, and all other Stationery Ware, at Reasonable Rates.

THE
PREFACE

To all COMMANDERS of Ships, and all other Officers
and Mariners of our English Nation.

GENTLEMEN,

THE kind Acceptance of this Treatise amongst you, hath encouraged the Continuation thereof unto many Impressions; it having had the Countenance and Assistance of an able Mathematician, in several Impressions, to render it the more complete and useful, finding a general Approbation of all who are exercised in Nautical Affairs. In this Edition there hath been a Correction of several Errors, that have escaped in the former Impressions; and several Tables removed forward that were annexed. So hoping for as good success in this, as in the former Impressions, I commend it to the candid Censure of the Judicious, and rest

Yours to serve you,

JOHN SELLER.

IN Prescot Street in Goodman's-fields are taught these Mathematical Sciences: *Viz.* Arithmetick, Geometry, Algebra, Trigonometry, Navigation, Astronomy, Surveying, Gauging, Dialling, Fortification, and Gunnery; likewise the Use of the Globes, and other Mathematical Instruments, the Projection of the Sphere, and other Parts of the Mathematicks.

By JOHN COLSON.

That for our good your Talents will not hide,
 But build a House of Marblers to guide,
 What others have in many Volumes done,
 You neatly have composed all in one;
 Yet is your Book to no great Volume grown,
 Though grac'd with learned Additions of your own.
 For due to praise your Work, might be my blame,
 Fearing my Mown might dispraise the same:
 You want the learned Pens, in lofty Verse,
 Your well-deserv'd Praises to rehearse.
 Most Artists, such as I (and such as I)
 Ought to write and give the world Prosperity.
 To write (for once) my humble Muse, and let
 The Country Oak-Pipe drown the Flageolet
 And to be singing (that your name is thus
 In every part of Country useful to)
 That our Country and Country Lads
 May all the Country should echo forth your Praises
 With such praise your Work shall surely find,
 The best of kindred well, and well design'd,
 For such have done in kind: Here we find,
 That is the Art my place a curious Mind,
 The Country Carpenter: But if we much
 Your Lines observe, abundant may be
 For me sufficient; but the same to get,
 With certainty, is not discover'd yet
 Which have Performance, if that any can
 Write clearly thus, I wish you be the Man.
 For thus, my Muse, be there, and not so rude;
 And say with you well, and so conclude.
 May then your Labours (as they profit all)
 Turn to your profit, and your good withal.
 May no base Plagiarist arrogate
 That to himself, which you by pains have got.
 May never English-man be so unkind,
 As to steal your Writings, and reverse Word to find)
 To write to Strangers, what you have so forth
 Deserv'd to from their and your own Worth.
 May you be encouraged be as to write
 To publish more such useful Works as this,
 May you be happy ever in the End:
 Thus prays your humble Servant and your Friend.

Written in
 Gloucestershire.

Nathaniel Friend.

* Mr. Wright's
 Chart ascribed
 to Mr. Friend.
 † Dr. Ward's
 Invention of
 a Triangle in
 an Ellipse, and
 applied to As-
 tronomy, At-
 tributed to Co-
 pagan.

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Practical

Practical Navigation.

CHAP. I.

A Preliminary Discourse of Navigation and Arithmetick.

SECT. I. *Of the Preliminary Discourse of Navigation.*

NAVIGATION (that useful part of the *Mathematicks*) is a Science which has been highly valued by the Antients, especially by our Ancestors of this Island; it being indeed the Beauty and Bulwark of *England*, the Wall and Wealth of *Britain*, and the Bridge that joins it to the Universe.

It consists of two general Parts.

First, That which may be called the *Domestick*, or more common *Navigation*, (I mean *Coasting* or *Sailing* along the *Shore*.) This Part employs the Mariners *Compass* and *Lead*, as the chief Instruments; and for an Introduction of this kind, I refer you to the Books, Entituled, *The English Pilot*, describing the *Sea-Coasts*, *Capes*, *Soundings*, *Sands*, *Rocks*, and *Dangers*; the *Bays*, *Roads*, *Harbours*, *Rivers*, and *Ports*, in most of the known Parts of the World: *Being furnished with New and Exact Draughts and Descriptions*, collected from the Experience of divers of our *Able Navigators*; Sold by Mr. *Grierison* in *Essex-Street*.

Secondly, That which may more properly bear the Name, and principally deserves to be Entituled the *Art of Navigation*, is that part which guides the Ship in her Course through the Immense Ocean, to any part of the known World; which cannot be done unless it be determined in what place the Ship is at all times, both in respect of *Latitude* and *Longitude*; this being the principal Care of a *Navigator*, and the *Master-piece* of *Nautical Science*.

To the Commendable Accomplishment of which knowledge, these four things are subordinate Requisites:

VIZ. { ARITHMETICK,
GEOMETRY,
TRIGONOMETRY, and
The Doctrine of the SPHERES.

of the first of which (namely *arithmetick*) I shall give you a brief
 Specimen.

Arithmetick is the Art of Numbering, from the Greek Word *Arithmos*,
 which signifies Number; and in it there five especial Parts, viz. *Nu-
 meration, Addition, Subtraction, Multiplication, and Division*. Of which
 in order.

SECT. II. OF NUMERATION.

Numeration teaches how to set down any Number spoken or propo-
 sed; and to read it truly when written.

To which purpose you are to observe, That Numbers are commonly
 expressed by these Nine Figures.

¹ ² ³ ⁴ ⁵ ⁶ ⁷ ⁸ ⁹
One, Two, Three, Four, Five, Six, Seven, Eight, Nine.

And 0 which is called a Cypher, (and by some a Nought) because of
 it self it signifies nothing, yet encreases the Value of other Figures that
 stand behind it; for every Figure augments its proper Value according to
 the place it happens in, except the first: And are reckoned from the right-
 hand unto the left (and the reason is, because this Art of Numbering was
 first taught by the Oriental Nations, whose Languages are read that way)
 so that the Figure that stands farthest to the right-hand is said to be in
 the first place, the next to that to be in the second place, and so of the rest.

Any of the Nine Figures in the first place signifies only its single Value;
 in the second place, as many Tens as its own simple Value; in the third
 place, so many Hundreds, in the fourth place, so many Thousands, in
 the fifth place, so many Ten Thousands; in the sixth place, so many
 Hundred Thousands; and in the seventh place, so many Millions; as
 may appear in this following Table.

Units	1	2	3	4	5	6	7	8	9
Tens	1	2	3	4	5	6	7	8	9
Hundreds	1	2	3	4	5	6	7	8	9
Thousands	1	2	3	4	5	6	7	8	9
Ten Thousands	1	2	3	4	5	6	7	8	9
Hundred Thousands	1	2	3	4	5	6	7	8	9
Millions	1	2	3	4	5	6	7	8	9
Ten Millions	1	2	3	4	5	6	7	8	9
Hundred Millions	1	2	3	4	5	6	7	8	9

To be read this way.

The last Line of this Table is thus read, *One hundred twenty three
 Millions, four hundred fifty six thousand, seven hundred eighty nine.*

SECT.

SECT. III. OF ADDITION.

Addition is the putting together of two or more Numbers into one Sum, so that the total Value of them all may be discovered.

Example 1. In whole Numbers.

Suppose there were a Squadron of Men of War of five Ships, I demand (according to the quantity of Men in each Ship) how many Men there is in the whole Squadron?

Aboard of the biggest Ship there are	_____	500
Aboard another,	_____	450
Aboard another,	_____	362
Aboard another,	_____	278
Aboard the last,	_____	110

There are in the Squadron _____ 1700

To Add these together, begin at the first Row on the Right-hand, and say 8 and 2 is 10, set down 0 under the first; then I carry the 1 (which stands for 10) to the next Row, and say 1 and 1 is 2, and 7 is 9, and 6 is 15, and 5 is 20; then set down 0 under the second Row, and carry the 2, which is 20, to the next Row, and say 2 and 1 is 3, and 2 is 5, and 3 is 8, and 4 is 12, and 5 is 17; which 17 set down under the third Row, and the Sum is 1700, the Number of Men in the whole Squadron.

Example 2. Of Pounds, Shillings, Pence.

Now if you would know how much Money all the Captains Pay comes to for one Month.

	l.	s.	d.
Supposing that the Captain of the greatest Ship hath per Month	10	00	00
The Captain of the other Ship	08	10	00
The Captain of the other	07	10	00
The Captain of the other	06	10	00
The Captain of the last	05	00	00
	37	10	00

The Question is, *How much Money it amounts to for 1 Month?* Answer _____ 37—10—00.

To effect which you must begin at the Row of Pence, and seeing there is no Pence in the whole Row, you must set down 00 under the Row of Pence. Then proceed to the Row of Shillings, and add up the Shillings in that Row, which amounts to 30 Shillings; set down the 10 Shillings under the Row of Shillings, and carry the 20 Shillings, or one Pound, to the Row of Pounds, and say 1 and 5 is 6, and 6 is 12, and 7 is 19, and 8 is 27, and 10 is 37, which 37 set down under the Row of Pounds; and the whole Sum amounts to *Thirty Seven Pounds, Ten Shillings*, the Sum of all the Captains Pay for one Month.

SECT. IV. OF SUBTRACTION.

Subtraction (commonly called *Substraction*) is a Rule that teaches how to take any lesser Number out of a greater, so as to know how much remains.

1. Set down your greater Number, and under that your smaller, Unites under Unites, Tens under Tens, &c. and in Money each Denomination answering to its kind, as Pence under Pence, Shillings under Shillings, and Pounds under Pounds.

2. Draw a Line under them, and begin at the Right-hand, and take the lesser Number out of the greater, and set down what remains under the Line.

3. If any Figure of the smaller Number happen to be bigger than that over it, then you must borrow a Unite from the next Place, or higher Denomination, to be added to the lesser Figure, subtracting from that Sum, and subscribe the Remainder; which Unite must be added to the next place, or Denomination to be Subtracted; as will appear in the Example following.

Example.

	L.	s.	d.
Suppose I borrow	296	15	06
And I paid at several Times	125	17	04
There remains due	170	18	02

The Work is thus performed: Begin with the Row of Pence, and say 4 from 6 and there remains 2; then go to the Row of Shillings and say 17 from 15 I cannot take, then you must borrow 20 Shillings from the Row of Pounds; and say 17 from 35, and there remains 18, which 18 set under the Row of Shillings: Then proceed to the Row of Pounds, and say 1 that I borrowed and 5 is 6, 6 from 6 there remains 0, which 0 set under the first Row of Pounds; and proceed to the next, and say, 2 from 9 and there remains 7; which 7 set under the second Row, and proceed to the third Row, and say 1 from 2 and there remains 1; then is the Question finished, and there remains 170 L. 18 s. 2 d. unpaid.

And the Question stands thus,

Now to prove whether the Question is truly wrought, add the Remainder and the lower Number together; and if the total of that Addition be the same with the upper Number, then is the Work right.

	L.	s.	d.
296	15	06	
125	17	04	
170	18	02	
296	15	06	

SECT.

SECT. V. OF MULTIPLICATION.

1. **M**ultiplication teaches how to encrease the greater of two Numbers given, as often as there are Unites in the lesser ; and serves instead of many Additions.

2. In Multiplication there are three Parts.

1. The Multiplicand, or Number to be Multiplied.
2. The Multiplier, or Number by which it is Multiplied.
3. The Product made by the Multiplication.

Example.

792 Multiplicand.
32 Multiplier.

1584
2376
25344 Product.

Before you can make any Progress in this Rule, you must perfectly get the following Table by Heart.

Multiplication Table.

	1	2	3	4	5	6	7	8	9
1	1	2	3	4	5	6	7	8	9
2	2	4	6	8	10	12	14	16	18
3	3	6	9	12	15	18	21	24	27
4	4	8	12	16	20	24	28	32	36
5	5	10	15	20	25	30	35	40	45
6	6	12	18	24	30	36	42	48	54
7	7	14	21	28	35	42	49	56	63
8	8	16	24	32	40	48	56	64	72
9	9	18	27	36	45	54	63	72	81

The Use of the foregoing Table.

Note ; That on the Top and left Side are placed the 9 Digits, which are to be multiplied one by another ; and in the common Angle of meeting, you will have the Product.

Example. Suppose I would multiply 7 times 9 ; look on the left side of the Table for 7, and on the Top of the Table for 9, and in the Angle of meeting (in the Column next the right-hand) you will find 63, the Answer of the Question.

Question 1.

Question 1.

Suppose there are 1700 private Seamen in a Squadron of Ships, and they have 23 Shillings *per* Month; How much Money will pay them for one Month? Set your Numbers thus, the greater Number uppermost.

1700 Multiplicand.

23 Multiplier

5100

3400

39100 Shillings; the answer of the Question.

The Numbers being plac'd as is before directed, begin thus, and say, 3 times 0 is 0, set that under the 3, and proceed to the next Figure in the Multiplicand, and say again, 3 times 0 is 0; then set that 0 under the 2, and proceed to the next, and say, 3 times 7 is 21; set down the 1 under the 7, and bear 2 in mind, and proceed to the next Figure in the Multiplicand, and say, 3 times one is 3, and 2 that I carry is 5, set that down under the 1; then have you done with the first Product: Then go to the next Figure in the Multiplier, and proceed as you did before, and the second Product will be 3400, which must be set down under the other, only with this Caution, to move it one place more to the left hand, as you may see in the Work; then add those two Numbers together, and the Product will be 39100, which are Shillings, the whole Sum of Wages for 1700 Men for one Month.

Example 2.

In 235 Degrees, how many Minutes?

Multiply the Degrees by 60, the Number of Minutes in one Degree.

235

60

14100 Minutes.

Note, For a Contraction in this Rule, if any Number is given to be Multiplied by 10, 100, or 1000, it is but adding so many Cyphers to the Number given, and that will be the Product. As thus,

If 232 be multiplied by 10, it will produce 2320, by 100, 23200, by 1000, it will be 232000, &c.

S E C T VI. Of DIVISION.

Division teacheth to find how many times a lesser Number is contained in a greater, and sheweth what remains, supplying the use of many Subtractions. It consists of three Parts, Dividend, Divisor and Quotient. The Dividend is the Number to be divided. The Divisor is the Number to divide by, which is always lesser than the Dividend: The Quotient is the Sum produced, by shewing how many times the Divisor is contained in the Dividend. And if any thing happen to remain it is called the Remainder.

Example 1.

Of Division.

Example 1.

$$\begin{array}{r}
 \text{Dividend.} \\
 \text{Divisor } 4 \overline{) 250} \left(62 \text{ Quotient.} \right. \\
 \underline{24} \\
 10 \\
 \underline{8} \\
 2 \text{ Remainder.}
 \end{array}$$

Suppose 4684 *l.* is to be divided amongst 54 Men: How much will each Man's Share come to?

Set your Numbers in order as you see in the following Work, (which is the easiest way of Division in my Opinion) to prevent scratching of the Figures, and it will stand thus.

Example 2.

$$\begin{array}{r}
 \text{Dividend. } \textit{l.} \\
 \text{Divisor } 54 \overline{) 4684} \left(86 \text{ Quotient.} \right. \\
 \underline{432}
 \end{array}$$

$$\begin{array}{r}
 364 \\
 \underline{324} \\
 40 \\
 \underline{20}
 \end{array}$$

The Shillings in one Pound, to reduce the Remainder into Shillings.

$$\begin{array}{r}
 54 \overline{) 800} \left(14 \right. \\
 \underline{54}
 \end{array}$$

$$\begin{array}{r}
 260 \\
 \underline{216} \\
 44 \\
 \underline{12}
 \end{array}$$

The Pence in a Shilling, to reduce the Remainder into Pence.

$$\begin{array}{r}
 88 \\
 \underline{44}
 \end{array}$$

$$\begin{array}{r}
 54 \overline{) 528} \left(9 \right. \\
 \underline{486}
 \end{array}$$

The Farthings in a Penny, to reduce it into Farthings.

$$\begin{array}{r}
 42 \\
 \underline{4} \text{ } \textit{qs.} \\
 54 \overline{) 168} \left(3 \right. \\
 \underline{162} \\
 6
 \end{array}$$

Of the Rule of Three.

So that if 4684*l.* is to be divided amongst 54 Men, there is coming to each Man's share 86*l.* 14*s.* 9*d.* 3*qs.* as doth appear by the Work.

Note, That the best proof of Division is by Multiplication, thus: Multiply the Quotient by the Divisor, and add the Remainder (if any be;) and if the Product be the same with the Dividend, then is the Work right, otherwise there is some Mistake.

SECT. VII. Of the Rule of THREE.

THE Rule of Three, for its Excellent Use is called the *Golden Rule*, which teaches from three Numbers given, to find a fourth in proportion thereunto, which is done by Multiplying the second and third Numbers together, and dividing the Product by the first, and the Quotient of the said Division is the Answer of the Question.

As if 25 Tuns of Wine cost 800*l.* What shall 35 cost?

Here *Note*; That the first Number and the third must always be of the same Denomination. As if one be Pounds, Pence, Yards, Tuns, Hours, Men, &c. so respectively must the other be: And the like is to be understood by the second and the fourth, as in the following Numbers, which are thus disposed.

Tuns	Pounds	Tuns
25	800	35

This Rule is performed (after an apt disposal of the Terms) by *Multiplication* and *Division*. But note that this Rule hath two Varieties, *viz. Direct* and *Reverse*. Now for the proper disposing the Terms in any Question propounded, it is necessary to give a General Rule to know whether the Question must be wrought by the Direct Rule, or the Reverse; which is this: When in the Question more requires more, or less requires less. As in this Question:

If 25 Tuns of Wine cost 800*l.* What will 35 Tuns cost? Here it is evident that the third Term is more than the first, and therefore requires more. So in this Question:

If 750*l.* give 45*l.* Interest for a Year, What shall 50*l.* give? Here it's plain that 50*l.* is less than 750*l.* and requires less Interest. Therefore both these, and all such like Questions, must be wrought by the Rule of Three Direct, wherein the Rule is plainly thus: Multiply the second Number by the third, and divide by the first, the Quotient shall be the fourth Number sought. As in the first of these Examples, Multiply 800 by 35, and the Product is 28000; which being divided by 25, the Quotient is 1120*l.* which shews that 35 Tuns will cost 1120*l.*

The

Of the Rule of Three.

9

The Operation.

Tuns		l.		Tuns.	l.
25	—	800	—	35	Ans ^r . 1120.
		35			
		4000			
		2400			
25)	28000	(1120	l.
		25			
		30			
		25			
		50			
		50			
		0			

And so in the second Example: Multiply 50 by 45, it makes 2250 which divided by 750, the Quotient is 3; which shews that the Interest of 50l. for a Year is 3l.

The Operation.

750	—	45	—	50
		50		
750)	2250	(3

The Rule of Three Reverse, is to be used when in the third Number more requires less, or less more; and then the Rule is thus:

Multiply the first Number by the second, and divide the Product by the third, the Quotient shall be the fourth Number sought, which always (as in the direct Rule) shall be of the same Denomination with the second Number. For Instance;

If 24 Pioneers require 16 Months to dig a Retrenchment about a Town, How many Pioneers must there be employed to dig the like Trench in 4 Months?

In stating this Question you must Note, That 24, tho' it be the first named, is not to be the first Number in the Work, because the middle Term must always be of the same Denomination with that which is sought. And the three Numbers put in order stand thus.

Months	Pioneers	Months
16	—	24
		4

Here 'tis plain less requires more, that is, less Time, more Hands: Therefore it must be wrought by the Rule Reverse, and accordingly you may Multiply 24 by 16, and divide the Product by 4, the Quotient is 96; as doth appear by the Work: which is, that 96 Pioneers must be employed to finish the Trench in 4 Months.

C V o f f i c e s) The

Of the Rule of Three.

The Operation.

Months.	Pioneers.	Months.
16	24	4
	16	
	144	
	24	
	4) 384 (96 Pioneers.	
	36	
	24	
	24	
	0	

SECT. VIII.

Some Questions Answered, and the way of working them directed, serving to illustrate the foregoing Rule.

IN ADDITION.

Quest. An antient Lady being demanded, how old she was : To avoid a direct Answer, said thus, I have 9 Children, and there were three Years between the Birth of every one of them, my Eldest was born when I was 19 Years old, which is now exactly the Age of my Youngest, How old now, is the Lady ?

Ans. It is resolved by Addition thus : First, Set down her age when her first Child was born, which was 19, then add the Difference between that and the Birth of her Youngest, which is 24, and then the Age of the Youngest 19, which being added together, shews the Lady to be 62 Years of Age.

19 Her Age.

24 Difference between the Children.

19 Age of her Youngest.

62 Lady's Age.

IN SUBTRACTION.

Quest. In the Year of our Lord 1588, was the Spanish Invasion, In the Year 1706, I demand how long it is since ?

Ans. Subtract 1588 out of 1706, there remains 118, the Time since, to the Year 1706.

IN MULTIPLICATION.

Quest. How many Square Miles are there in the Circumference of the Body of the Earth, whose Circumference is 26000 Miles, and each Degree contains (according to Vulgar Computation) 69 Miles ?

Of the Rule of Three.

11

Ans. Multiply 360, by 60, (the Miles contained in one degree) and the Product is 21600 Statute Miles.

The Operation.

$$\begin{array}{r} 360 \\ \times 60 \\ \hline 21600 \end{array}$$

In DIVISION.

Quest. If the circuit of the Terrestrial Globe is 21600 Miles.

Suppose a Man travel continually in a direct Line (under one of the Greater Circles of the Sphere) 15 Miles a day : In how many days can he compass it?

Ans. Divide 21600 by 15, your Quotient will be 1440, which shews, that in so many days he may effect it, that is, in somewhat less than 4 Years.

The Operation.

$$\begin{array}{r} 15 \overline{) 21600} \\ \underline{15} \\ 60 \\ \underline{60} \\ 00 \end{array}$$

In the Rule of THREE.

Quest. A Man lent me 400 £ for 7 Months, without Interest : How much must I lend for 12 Months to retaliate his kindness?

Ans. This must be solved by the Reverse Rule of Three, and must be thus stated.

$$\begin{array}{ccc} \text{Months.} & & \text{Months.} \\ 7 & \text{---} & 12 \\ & \text{---} & \\ & 400 & \end{array}$$

Where 'tis plain that more requires less ; that is, tho' the third Number be more than the first, yet it requires a lesser Number to answer unto it than the second : Therefore you must multiply 400 by 7, and it makes 2800, which I divide by 12 (the third Number) the Quotient is 233 £ and 4 £ remaining, the 12th part of which is 6 s. 8 d. So the Answer to the Question is, That I must lend him 233 £ 6 s. 8 d. for 12 Months.

Of the Rule of Three.

The Operation.

Months $\frac{7}{400}$ Months.

$12 \overline{) 2800} (233$
 $\underline{24}$

The Operation.

20
 $\underline{4}$
 $12 \overline{) 80} (6 s.$
 $\underline{72}$
 8

40
 $\underline{36}$
 40
 $\underline{36}$

4 Which being reduced by 20, the Shillings in one Pound, and it is 80 Shillings; which being divided by 12, produceth 6 s. and 8 Remaining, which is $\frac{1}{5}$ of a Shilling, or 8 Pence.

CHAP. II.

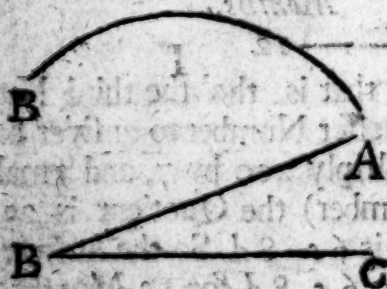
Containing sundry useful Definitions and Problems of
GEOMETRY

SECT. I. Geometrical Definitions.

A Point is that which cannot be divided, having neither Part nor Quantity, and therefore void of Length, Breadth or Depth; and is represented in the Margin, by the Letter A;

A Line is a Length, without Breadth or Thickness, and is Right; as A;

Or Curved, as B.



An Angle is the Inclination of two Lines one to another, the one touching the other, yet not so as to make one Line; as the Lines BA and BC.

A Right-lin'd Angle, is that which is contained by Right Lines, as the Angle ABC.

A Right-lin'd Angle, is either Right-Angled, or Oblique.

A *Right-Angle* is when a Right Line, standing upon a Right Line, makes the Angles on each side equal to each other ; as the Right-Angles ACD, and BCD.

An *Oblique-Angle* is either Acute, or Obtuse.

An *Acute-Angle* is less than a Right, as the Angle DEB.

An *Obtuse-Angle* is greater than a Right-Angle, as AEB.

A *Plain Figure* is contained under one Term or many.

A *Circle* is a plain Figure contained under one Term or Line, called the *Circumference*, unto which all Lines drawn from a certain Point within the Figure are equal ; and that Point is called the Center, as A.

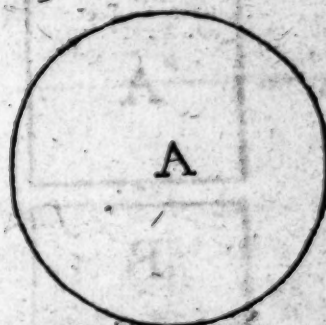
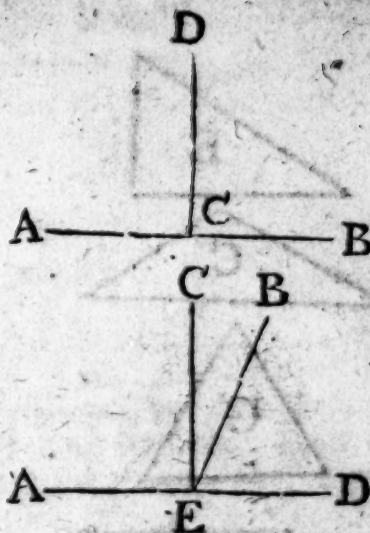
A *Right-lined Figure* is contained by Right-Lines; and is either three-sided, four-sided, or many-sided.

A *Triangle* is a three-sided Figure, and is considered either in respect of its Sides, or Angles.

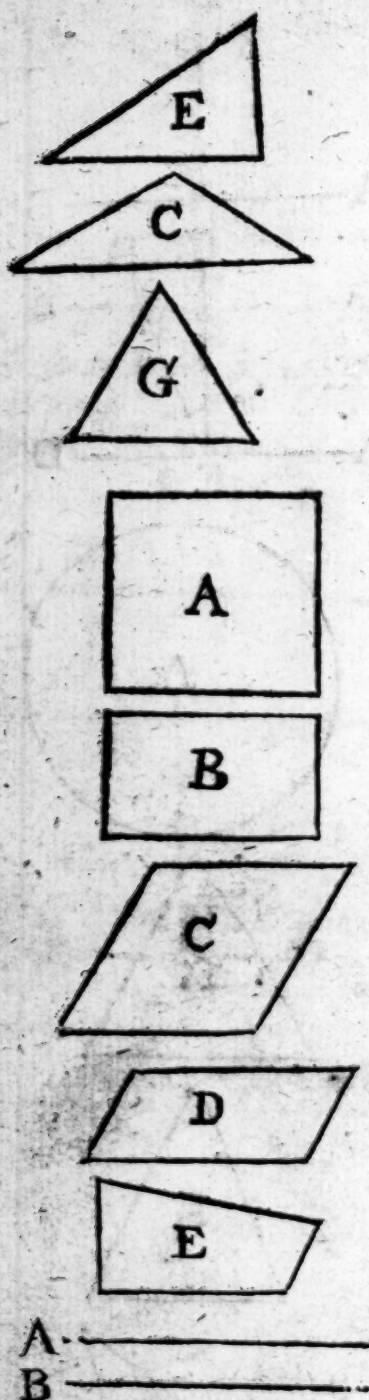
In respect of its Sides, 'tis either, *Equilateral*, having three equal Sides: as A.

Or *Equicrural*, having two equal Sides; as B.

Or *Scalenum*, having three unequal Sides as D.



Right.



In respect of its Angle, 'tis either,
Right-Angled, which hath a Right-Angle;
 as E.

Or *Oblique-Angled*, which hath no Right
 Angle, but hath two Acute-Angles, and one
 Obtuse Angle; as C.

Or three *Acute-Angles*; as G.

Of four-sided Figures.

A *Square* is that which hath four equal
 Sides, and four Right-Angles; as A.

An *Oblong* hath four Right-Angles, and
 the opposite Sides equal; as B.

A *Rhombus* hath four equal Sides, but is
 not Right-angled; as C.

A *Rhomboides* hath the opposite Sides
 and Angles equal, but is neither equal-sided
 nor Right-angled; as D.

All other four-sided Figures are called
Trapezia's, as E.

Parallel, or equi-distant Right-lines are
 such, which being the same Superficies, if
 infinitely produced, would never meet, as
 A and B.

How to raise a Perpendicular on the middle of a given Line.

LET the given Line be AB, and C be a Point therein, whereon it is required to raise a Perpendicular. First, open the Compasses to any convenient distance, and setting one foot in the point C, with the other set off on either side thereof the equal distances, CA and CB: Then opening the Compasses to any convenient (wider) distance, setting one foot in the point A, with the other strike the occult Arch at E, then with the same distance set one foot in the point B, and with the other draw the Arch F, crossing F in the point D, from whence draw the Line DC, which Line is a Perpendicular unto the given Line AB, as was required.



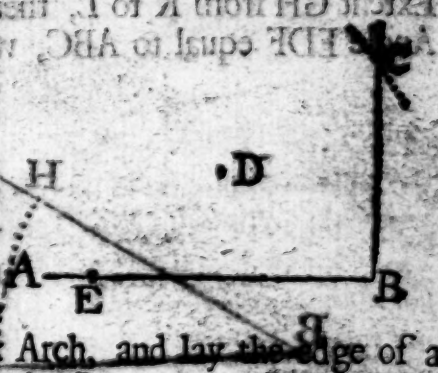
To let fall a Perpendicular from a Point assigned, to the Middle of a given Line.

Let BCD be the given Line, and A the point assigned, from whence you would have a Perpendicular let fall: First, set one foot of your Compasses in the Point A, and opening them to any convenient distance, describe the Arch of a Circle that may cut the Line BCD at E and F; then find the Middle between these, which will be the Point C, from which point draw the Line AC, which is the Perpendicular Line required.

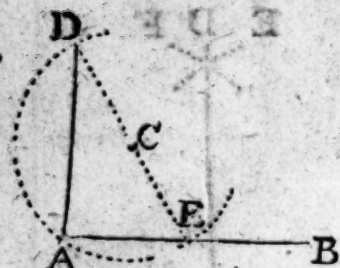


To raise a Perpendicular upon the End of a Line given.

Let the given Line be AB: First, open your Compasses to a convenient distance, and set one foot in the point B, and let the other point fall any where above the Line, as at the point D; and in that point let one foot of your Compasses remain, turning the other about, until it touch the Line AB in the point E; then turn the foot of the Compasses towards C, and draw an occult Arch, and lay the edge of a Ruler to those points E and D; and where the same edge of the Ruler doth cut the Arch C, from that point draw the Line CB, which shall be a Perpendicular at the end of the Line AB, as was required.



To let fall a Perpendicular from a Point assigned, unto the End of a given Line.



Let the Line AB be given, unto which it is required to let fall a Perpendicular from the Point D, unto the end A. First, from the Point D draw a Line unto any part of the given Line AB, which may be the Line DCE; find the middle of the Line, which is at C, place one foot of your Compasses in that Point, and extend the other unto D or E, with which distance describe the Semi-Circle DAE, which shall cut the given Line AB in the Point A; from which Point draw the Line DA, which is the Perpendicular, on the End of the given Line AB, as was required.

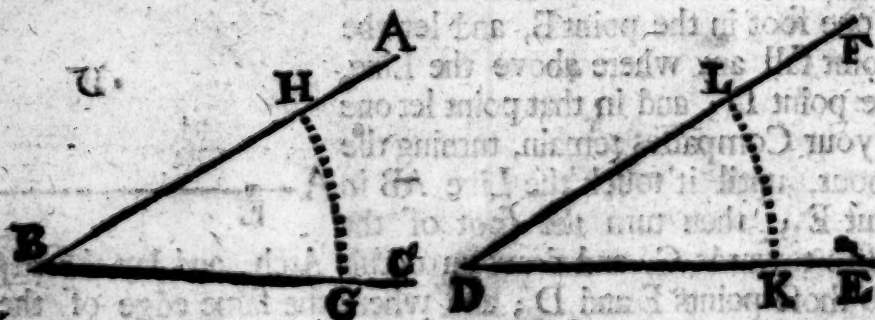
To draw a Line Parallel to a Line given.



Let AB be a Line given, whereunto it is required to draw a Parallel. First, set one foot of your Compasses in the Point C, and opening the other at pleasure draw the Arch E; then with the same Distance set one foot in the Point D, and draw the other Arch F: Lastly, lay a Ruler to the Convexities of both those Arches, and draw the Line GH, which shall be a Parallel to AB, as was required.

How to make an Angle equal to an Angle given.

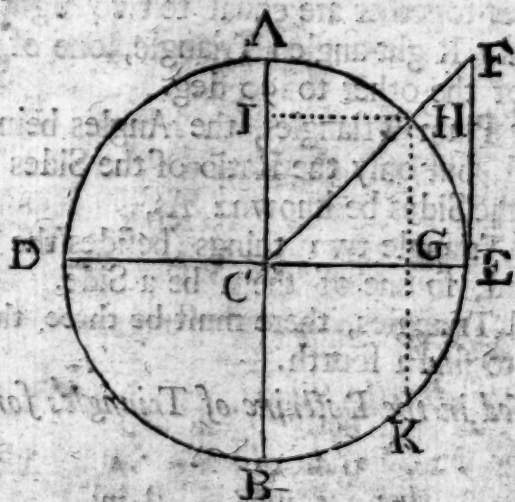
Let ABC be the given Angle, draw the Line DE, and upon B as a Center describe the Arch GH, between the Sides BA and BC, and upon the Point D, with the same Extent describe the Arch KL, and place the Extent GH from K to L, then through the Point L, draw DF: So is the Angle EDF equal to ABC, which was required.



THE Doctrine of Triangles is conversant in the Mensuration of Triangles, Plain or Spherical, comparing the Sides and Angles together, according to the known Analogies, whereby three Things being given, either Sides, Angles, or both, a fourth Side or Angle may be found.

But because the Angles, of both, Plain and Spherical-Triangles, are measured by Arches of Circles, and the Sides likewise of Spherical Triangles are themselves Arches of great Circles, therefore these Arches are in a manner *reduced into the Right-lines applied thereunto.*

A *Chord* is a Right-line drawn in a Circle, from one part of the Circumference to the other, as in the annexed Figure.



The right Sine of an Arch is half the Chord of twice that Arch, as HG being half the Chord HK, is the right Sine of the Arch HE; also of the Arch HAD, the Arch HE being the half of HEK, and the Arch HAD being half the Arch of HDK. The Sine Complement of the Arch HE is HL, equal to CG.

The *Verfed Sine* of an Arch, is that part of the Diameter, which lies between the right Sine of that Arch and the *Circumference*, for that *EF* is the *Verfed Sine* of the Arch *HE*, and *GD* the *Verfed Sine* of the Arch *HAD*.

The *Tangent* of an Arch is a Right-line touching the Arch, being Perpendicular to the Radius drawn to the Point of Contact, and concurring with a Line drawn from the Center, thro' the Term or End of that Arch; so EF is a *Tangent* of the Arch EH.

A *Secant* is that Right-line drawn from the Center of the Arch, until it meet with the *Tangent*; so CF is a *Secant* of the Arch EH.

It is to be understood that every Circle is divided into 360 equal Parts, called Degrees; every Degree into 60 Parts, called Minutes; and every Minute into 60 Parts, called Seconds, &c.

The Complement of an Arch or Angle, is commonly the Complement thereof, to (or that which makes it up) 90 deg. But if it be meant the Complement thereof to a Semi-Circle, it is expressed by saying the Complement to 180 deg.

A *Plain-Triangle* is contained under three Right-lines, and is either Right-angled or Oblique.

In all plain Triangles, two Angles being given, the third is also given: And one Angle being given, the Sum of the other two is also given, because the three Angles together are equal to two right Angles.

Therefore in a plain Right-angled Triangle, one of the acute Angles is the Complement of the other to 90 deg.

In the Solution of Plain Triangles, the Angles being only given, the Sides cannot be found, but only the Ratio of the Sides: It is therefore necessary that one of the Sides be known: As,

In a Right-angled Triangle two things (besides the Right-angle) will serve to find the third, so one of them be a Side.

In Oblique-angled Triangles, there must be three things given (one of them being a Side) to find a fourth.

Some Symbols used in the Doctrine of Triangles for Brevity's sake.

= Equal to.

-| More.

- Less.

x Multiply by, or drawn into.

• Over a Number stands for Degrees, as 12° signifies 12 deg.

• Signifies Minutes, as 12' is 12 Minutes.

cr. a Side. crs. Sides.

∠ An Angle, ∠s Angles.

Σ The Sum.

X The Difference.

S Sine

Sc. Co-Sine, or Sine Complement.

Co. Ar. Complement Arithmetical.

t. Tangent.

tc. Co-Tangent, or Tangent Complement.

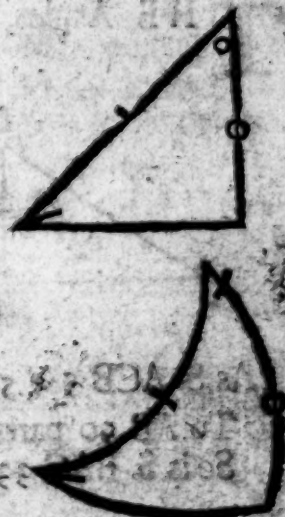
2 R. Ang. two Right-Angles.

Q. Square,

In Right-angled Plain Triangles, the Sides comprehending the Right-Angle are called the *Legs*; and the Side subtending (or opposite to) the Right-angle, is called the *Hypotenuse*.

In the Doctrine of Triangles; three Letters denote an Angle, as BAC signifies the Angle at A; ACB the Angle at C. Two Letters shew a Side, as Side AB, or AC.

In the Doctrine of Triangles, the given Sides or Angles are noted with a Dash, thus (*)



The required Sides or Angles with a Cypher, thus, (o)

In Right-angled Plain Triangles, there are seven Cases, and in Oblique Triangles five; For the Solution of which, these Four *Axioms* are sufficient.

AXIOM 1. Of Right-Angled Triangles.

In all Plain Right-angled Triangles, any of the Sides may be made Radius; and the other Sides will be Sines, Tangents or Secants: and what Proportion the Side put for Radius, hath to Radius, the same Proportion hath the other Sides, to the Sines, Tangents, and Secants by them represented.

AXIOM 2. Of Oblique Triangles.

In all Plain Triangles, the Sides are in such proportion one to another, as the Sines of their opposite Angles.

AXIOM 3.

In all Plain Triangles; As the Sum of two Sides is to their Difference; so is the Tangent of the half Sum of their two opposite Angles, to the Tang. of the Difference of either of them, above or under the half Sum

Plain Trigonometry.

AXIOM 4.

In all Plain *Triangles*; As the Base is in proportion to the Sum of the other Sides, so is the Difference of these Sides, to the Difference of the Segments of the Base.

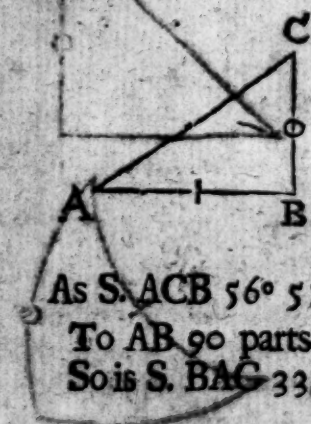
S E C T. II.

OF RIGHT-ANGLED PLAIN TRIANGLES.

Case I.

THE Angles, and one of the Legs given, to find the other Leg.

Example.



In the *Triangle* ABC,

There is given

BAC $33^{\circ} 45'$ } BC required.
AB, 90 parts. }

The Operation by the Logarithms.

As S. ACB $56^{\circ} 51'$	Log	9.91984
To AB 90 parts		1.95424
So is S. BAC $33^{\circ} 45'$		9.74474
		11.69898
To BC required, 60, 13 parts		1.77914

The General Rule for working Proportions by the Logarithms.

Add the Logarithms of the Second and Third Numbers together; From that Sum subtract the Logarithms of the first, and the Remainder is the Logarithm of the fourth Number sought, as is apparent by the precedent Operation.

Note, That the Work may be abbreviated in this and the following Cases: When Radius is not put in the Proportion; then take the *Complement* Arithmetical of the first Logarithm; and then adding the Logarithms of the second and third, and the *Complement* Arithmetical of the first into one Sum (from which bating Radius, or an Unite towards the left hand) the Remainder is the Logarithm of the fourth Number.

The

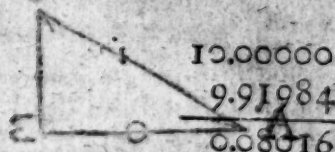
Plain Trigonometry.

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The Operation by the Compl. Arith.

Co. Ar.

As S. ACB $56^{\circ} 15'$ Log. ————— 0.08016
 To AB 90 parts ————— 1.95424
 So is S. BAC, $33^{\circ} 45'$ ————— 9.74474
 To AC required, 60, 13 parts ————— 11.77914
 The *Compl. Arith.* of a Log. is the Remainder thereof, being subtracted from Radius.
 So the *Compl. Arith.* of S. $59^{\circ} 15'$
 is 0.08016, as here appears :



But a readier way is hinted by Mr. Norwood, thus: By taking the *Compl.* or *Residue* of the first Figure towards the left-hand unto 9, and so of the rest, until you come to the last Figure towards the Right-hand thereof, set down the *Residue* to 10, thus, To take the *Compl. Arith.* of 9.91984. For 9 I write this *Residue* unto 9, which is 0; for 9, 0; for 1, 8; for 9, 0; for 8, 1; for 4, the *Compl.* to 10, which is 6. And so I have 0.08010, which is the *Compl. Arith.* of 9.91984.

How to work this and the following Cases by *Gunter's Scale*, shall be shewn in the Use of that Instrument.

Case II.

The Angles, and one of the Legs given, to find the *Hypotenuse*.

Example.

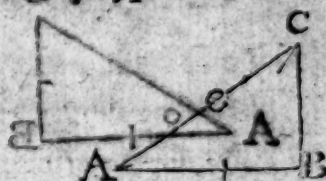
In a Triangle ACB,

There is given,

ACB $56^{\circ} 15'$

AB 90 parts

} AC required.



The Operation.

As S. ABC $56^{\circ} 15'$ Log. ————— 9.91984
 To AB 90 parts ————— 1.95424
 So is Radius ————— 10.00000
 To AC required, 2, parts ————— 2.03440

In the Operation of this Case there is no need to take the *Compl. Arith.* because Radius is one of the four Terms in Proportion; nor of adding the Logs. of the second and third together, according to the general Rule aforegoing; only subtract the former Figures of the first Log. from the second Log. And in subtracting the last Figure of the first Log. add to the corresponding Figure of the second Log. viz.

Say, 9 from 11, there remains 2; This Remainder 2.03440, gives the Log. of the fourth Number required. But

But if the Compl. Arith. of the Log. of the first Term be taken, the Labour of Subtraction may be saved.

Case III.

The Angles and *Hipotenuse* given, to find either of the Legs.

Example.

In the Triangle ABC,

There is given

ACB $56^{\circ} 15'$ } AB required.
AC 108 parts }

The Operation.



As Radius, ————— 10.00000

To AC 108 parts ————— 2.03342

So is S. ACB $56^{\circ} 15'$ ————— 9.91984

To AB required, $89 \frac{8}{10}$ parts ————— 11.95326

In this Operation, the second and third Log. being added together, the first, being Radius, is easily subtracted, by cutting off the last Figure towards the left-hand, as is evident in the Example.

Case IV.

The Legs given, to find the Angles.

Example.

In the Triangle ABC,

There is given

AB 90 } BAC required.
BC 60 }



The Operation.

As AB, 90 ————— 1.95424

To Radius ————— 10.00000

So is BC 60 ————— 1.77815

To \angle BAC required, $33^{\circ} 41'$ ————— 9.82391

This Operation is performed as the Example in the second Case foregoing.

Case V.

The *Hipotenuse*, and one of the Legs given, to find the Angles.

Example.

In the Triangle ABC,

There is given

AC 108 } ACB required.
AB 90 }



The

The Operation.

As AC 108 _____ 2.03342

To Radius _____ 10.00000

So is AB 90 _____ 1.95424

To S. ACB required, $56^{\circ} 26'$ _____ 9.92082

This is performed as the precedent Operation in the fourth Case.

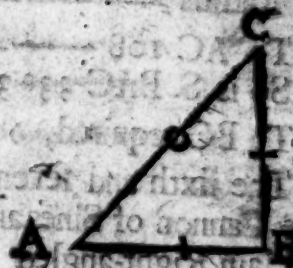
Case VI.

The Legs given, to find the Hypotenuse.

In the Triangle ABC

There is given,

AB 90 } AC required.
BC 60 }



This Case requires a double Operation.

1. By the 4th Case to find the Angles.
2. By the 2d Case to find the Hypotenuse.

The first Operation.

As AB, 90 _____ 1.95424

To Radius _____ 10.00000

So is BC 60 _____ 1.77815

To t. BAC, $33^{\circ} 41'$ _____ 9.82391

The second Operation.

As S. BAC $33^{\circ} 41'$ _____ 9.74398

To BC 60 _____ 1.77815

So is Radius _____ 10.00000

To AC required, 108 _____ 2.03417

Case VII.

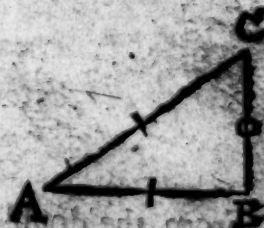
The Hypotenuse, and one of the Legs given, to find the other Leg.

Example.

In the Triangle ABC,

There is given,

AC 108 } BC required
AB 90 }



This Case likewise requires a double Operation.

1. By the 5th Case to find the Angles.
2. By the 1st or 3d Case to find the Leg required.

The

Plain Trigonometry.

The first Operation.

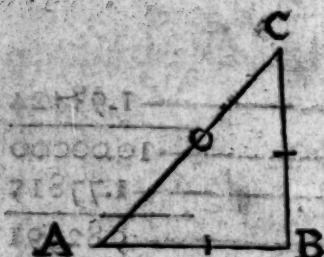
As AC 108	2.03342
To Radius	10.00000
So is AB 90	1.95424
To S. ACB $56^{\circ} 26'$	9.92082

The second Operation.

As Radius	10.00000
To AC 108	2.03342
So is S. BAC $33^{\circ} 34'$	9.74265
To BC required, 60	1.77607

The sixth and seventh Cases before-going, may be performed without the Cannon of Sines and Tangents, by the 46 Prop. 1. *Euclid. viz.* That in Plain Right-angled Triangle, the square of the *Hypotenuse* is equal to the Sum of the *Squares* of the two Legs.

Example of the Sixth Case.



In the Triangle ABC

There is given,

AB 90

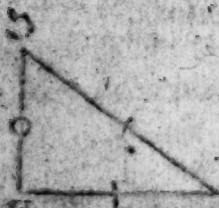
BC 60

AC required.

Square the given Legs severally, add their *Squares* together, the Square Root of that Sum is the *Hypotenuse* required.

The Operation.

AB 90	BC 60	the Square of AB 8100	
90		60 the Square of BC 3600	
00	00		11700
810	360		1
Square 8100	Square 3600		208



Otherwise by the Logarithms.

From the double Log. of a greater Leg subtract the Log. of the less, and to the absolute Number answering to the Difference of the Logs. add the less Leg; half the Sum of the Logs. of the said Sum and less Leg, is the Log. of the *Hypotenuse* required.

The

Plain Trigonometry:

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The Operation.

The greater Leg AB, 90 Log.	1.95424
The same again	1.95424
The double Log.	3.90848
The leis Leg BC 60 Log. subtr.	1.77815
The absolute Number 135	2.13033
The Sum 195 Log.	2.29003
Leis Leg BC 60 Log.	1.77815
Sum	4.06818
The Hypotenuse AC 108 $\frac{1}{2}$ Sum	2.03409

Example of the Sixth Case.

In the Triangle ABC,
There is given

AC 108 } BC required.
AB 90



From the Square of the Hypotenuse, subtract the Square of the given Leg, the Square Root of the Remainder is the Leg required.

The Operation.

AC 108	AB 90	the Square of AC 11664
108	90	the Square of AB 8100
864		Remainder 3564
1080	810	25
Squ. 11664	Square 8100	109 1064
		981
		183

Otherwise by the Logarithms.

Half the Sum of the Logs. of the Sum, and of the Difference of the Hypotenuse and given Leg, is the Log. of the Leg required.

The Operation.

The Hypotenuse AC 108	
The given Leg AB 90	
The Sum 198	Log. 2.29666
The Diff. 18	Log. 1.25527
	Sum 3.55193
The Leg BC 59 required, $\frac{1}{2}$ Sum	1.77596

E

SECT.

Plain Trigonometry.

S E C T. III. Of Oblique-angled Plain Triangles.

Case I.

THE Angles, and one of the Sides given, to find one of the other Sides.



Example.

In the Triangle ABC

There is given,

BAC $33^{\circ} 45'$ ABC $45^{\circ} 00'$

AC 40 parts

BC required.

The Operation of this and the following Case, depends upon the second *Axiom* aforegoing.

The Operation.

As S. ABC $45^{\circ} 00'$

To Side AC 40

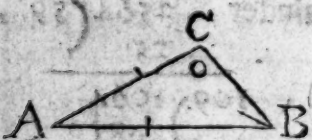
So is S. BAC $33^{\circ} 45'$

To Side BC required, 31

After the same manner you might find the Side AB if it were required.

Case II.

Two Sides, and an Angle opposite to one of them, being given, to find the other opposite Angle.



Example.

In the Triangle ABC;

There is given

ABC, $45^{\circ} 00'$

AB 100

AC 80

ACB required,

being Obtuse.

1. In this case, If the given Angle be Obtuse, the Angle required is Acute.

2. If the given Angle be Acute, and opposite to the greater of the given Sides, the required Angle is Acute.

3. If the given Angle be Acute and opposite to the least of the given Sides; it's doubtful whether the Angle sought be Acute or Obtuse, and ought to be determined before the Operation; as In this Example.

The Operation.

As Side AC 80

To S. ABC $45^{\circ} 00'$

So is Side AB 100

To S. ACB required. $117^{\circ} 54'$

Co. Ar.

8.09691

9.84948

2.00000

19.94639

This

Plain Trigonometry.

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This Operation produces the Log. Sine of $62^{\circ} 6'$ for the Angle sought; but because it is Obtuse, you must take its Complement to 180° . viz, $117^{\circ} 54'$.

Case III.

Two Sides, and their contained Angles given, to find the other Angles.

Example.

In the Triangle ABC,
There is given,

AB 25

AC 20

ABC $33^{\circ} 45'$

} ACB and ABC required.



The Operation of this Case depends upon the third Axiom.

The Operation.

The Side AB 25

The Side AC 20

BAC $33^{\circ} 45'$

The Sum of the Sides 45

Sum 146 15

Their Difference 05

+ Sum $73^{\circ} 07'$ of the unknown Angles

Co. Ar.

As the Sum of the Sides AB and AC 45 Log. 8.34679

To their Difference 05 Log. 0.69897

So is t. $\frac{1}{2}$ Sum of the opposite Angles $73^{\circ} 07'$ Log. 10.51783

To t. of their half Difference 20 06 Log. 9.56359

The half Difference added to the half Sum, gives the greater Angle; and subtracted leaves the less.

The $\frac{1}{2}$ Sum of the Angles $73^{\circ} 07'$

The $\frac{1}{2}$ Difference 20 06

Added, gives ACB

Subtracted, ABC

Case IV.

Two Sides, and their contained Angle given, to find the third Side.

Plain Trigonometry.

Example.

In the Triangle ABC,

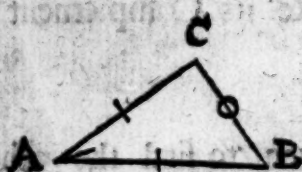
There is given

AB 335

AC 271

BAC $14^{\circ} 40'$

BC required.



This Case requires a double Operation.

1. By the 3d Case to find the Angles.
2. By the 1st Case to find the Side required.

To first Operation.

As the Sum of the Sides AB and AC 606	Log.	7.21753
To their difference 64		1.80618
So is $t \frac{1}{2}$ Sum Angles $82^{\circ} 40'$		10.89044
To $t \frac{1}{2}$ their Difference 291 22		9.91415
By which you will find the Angle ABC to be $43^{\circ} 18'$		

The second Operation.

As S. ABC $43^{\circ} 18'$	Log	0.16279
To Side AC 271		2.43297
So is S. BAC $14^{\circ} 40'$		2.40345
To Side BC required, 100		2.00021

Case V.

Three Sides given to find an Angle.

Example.

In the Triangle ABC,

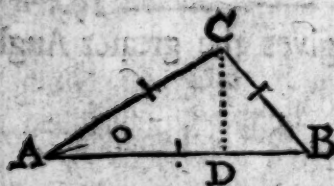
There is given

AB 64

AC 47

BC 34

BAC required.



The Resolution of this Case depends upon the 4th Axiom, reducing the Oblique-Angled Triangle into two Right-angled Triangles, by letting fall the Perpendicular CD upon the Base or greater side AB, and requires a double Operation.

The Base is that side upon which the Perpendicular falls.

1. To find the Segment of the Base AD.
2. To find (by the 5th Case of Rectangulars) the Angles required.

The

Of Spherical Triangles.

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The first Operation.

Co. Ar.

AC 47	As the Base AB	64	Log. 8.19382
BB 34	To the Sum of the Sides AC and BC	81	1.90848
Sum 81	So is the Difference of the Sides AC & BC	13	1.11394
Diff. 13	To the Differ. of the Segments of the Base	16	1.21624
	The Base is	64	
	The Difference of the Segments	16	

Sum 80

Half Sum 40, is AD the greater Segment of the Base, because adjacent to the greater side AC.

The second Operation.

In the Triangle ACD, Right-angled at D,

There is given AD and AC, to find CAD.

As AC, 47	Log. 1.67209
To Radius	10.00000
So is AD, 40	1.60206
To fc. CAD $31^{\circ} 40'$	9.92997

CHAP. IV.

The Doctrine of Spherical TRIANGLES:

SECT. I. Containing the Affections of Spherical Triangles, and their Axioms.

1. **A** Spherical Triangle is that which is described on the Surface of the Sphere.

2. The Sides of a Spherical Triangle, are the Arches of three great Circles of the Sphere mutually intersecting each other.

3. Spherical Angles are measured by the Arch of a great Circle, intercepted between the sides containing the Angle, the Pole of that Circle being the Angular Point.

4. Those are said to be great Circles which bisect the Sphere.

5. Those

5. Those Circles which cut each other at Right-angles, pass through the Poles of each other, and the contrary.

6. In every *Spherical Triangle*, each side is less than a *Semi-Circle*.

7. In every *Spherical Triangle*, any two sides together are greater than the third.

8. The sum of the sides of a *Spherical Triangle* is less than two *Semi-circles*.

9. If two sides of a *Spherical Triangle* be equal to a *Semi-circle*, the two Angles at the Base shall be equal to two Right Angles; if they be less than a *Semi-circle*, the two Angles shall be less; but if greater than a *Semi-circle*, the two Angles shall be greater than two Right Angles.

10. The sum of the three Angles of a *Spherical Triangle*, are greater than two Right-angles, and less than six.

11. Two Angles of any *Spherical Triangle*, are greater than the Difference between the third Angle and a *Semi-circle*. Therefore,

12. Any side being continued, the Exterior Angle is less than the two Interior opposite ones.

13. In any *Spherical Triangle*, the Difference of the Sum of two Angles and a whole Circle, is greater than the Difference of the third Angle and a *Semi-circle*.

14. In any *Spherical Triangle*, one side being produced, if the other two sides be equal to a *Semi-circle*, the outward Angle shall be equal to the inward opposite Angle upon the side produced: If they be less than a *Semi-circle*, the outward Angle shall be greater than the inward opposite Angle, if they be greater than a *Semi-circle*, the outward Angle shall be less than the inward opposite Angle.

15. A *Spherical Triangle* is either Right, or Oblique-angled.

16. A Right-angled *Spherical Triangle*, is that which hath one Right Angle at the least.

17. The Legs of a Right-angled *Spherical Triangle*, are of the same Affection with their opposite Angles.

18. In a Right-angled *Spherical Triangle*, if either Leg be a Quadrant the *Hypotenuse* shall be also a Quadrant; but if both the Legs be of the same Affection, (that is, be both greater, or both less than a Quadrant) the *Hypotenuse* is less than a Quadrant, or if of different Affections, then greater, and the contrary.

19. In a Right-angled *Spherical Triangle*, if either of the Angles at the *Hypotenuse* be a Right Angle, the *Hypotenuse* shall be a Quadrant; but if both shall be of the same Affection, it shall be less; if of different, it shall be greater, and the contrary.

20. In a *Right-angled Spherical Triangle*, the Sum of the *Oblique-Angles* are less than three *Right-Angles*.

21. An *Oblique Spherical Triangle* is either *Acute* or *Obtuse*.

22. An *Acute-angled Spherical Triangle* hath all its *Angles Acute*.

23. An *Obtuse-angled Spherical Triangle* hath all its *Angles* either *Obtuse* or *Mixt*, viz. some *Acute* and some *Obtuse*.

24. In any *Spherical Triangle* whose *Angles* are all *Acute*, each *Side* is less than a *Quadrant*.

In *Spherical Triangles* there are 28 Cases, 16 in *Rectangular*, and 12 in *Oblique-Angular*. The 16 Cases of *Rectangular* are resolved by these two *Axioms* following.

AXIOM 1.

In all *Spherical Rectangular Triangles*, having the same *Acute Angle* at the *Base*, the *Sines* of the *Hypotenusa's* are proportional to the *Sines* of their *Perpendiculars*.

AXIOM 2.

In all *Spherical Rectangular Triangles*, having the same *Acute Angle* at the *Base*; the *Sines* of the *Bases*, and the *Tangents* of the *Perpendiculars* are proportional.

That all the Cases of a *Right-angled Spherical Triangle* may be resolved by these two *Axioms*.

The several parts of the *Spherical Triangle* proposed, must sometimes be continued to *Quadrants*, that so the *Angles* may be turned into *Sides*, the *Hypotenusa's* into *Bases* and *Perpendiculars*, and the contrary. By which means the *Proportions*, as to the *Parts* of the *Triangle* given, instead of *Sines* do sometimes fall in *Co-sines*, and sometimes in *Co-tangents* instead of *Tangents*. Such *Parts* as do change their *Proportion*, are noted with their *Complements*, viz. the *Hypotenuse*, and both the *Oblique Angles*, but the *Sides* containing the *Right Angle* do not so change.

These are called the five *Circular Parts* of a *Triangle*, amongst which the *Right-Angle* is not reckoned, and therefore the two *Sides* which do contain it, are supposed to be joined together.

Each of these *Circular Parts* may by supposition be made the middle Part, and then the two *Circular Parts*, which are next to that middle Part, are the *Extreams* of the *Conjunct*; the other remote from the Part assumed, are the *Extreams Disjunct*.

As in the *Triangle ABC*, if *Comp. AC* be made the middle Part *Comp. A* and *Comp. C* are the *Extreams Conjunct*, and the *Sides AB* and *BC* are the *Extreams Disjunct*; and so of the rest, as in the *Table* following.



Of Spherical Triangles.

<i>Mid. Part.</i>	<i>Extr. Conj.</i>	<i>Extr. Disj.</i>
<i>Leg. A B</i>	<i>Comp. A</i> <i>Leg. BC</i>	<i>Comp. AC</i> <i>Comp. C</i>
<i>Comp. A</i>	<i>Comp. AC</i> <i>Lag. A B</i>	<i>Comp. C</i> <i>Leg. BC</i>
<i>Comp. AC</i>	<i>Comp. A</i> <i>Comp. C</i>	<i>Leg. A B</i> <i>Leg. BC</i>
<i>Comp. C</i>	<i>Comp. AC</i> <i>Leg. BC</i>	<i>Comp. A</i> <i>Leg. A B</i>
<i>Leg. BC</i>	<i>Comp. C</i> <i>Leg. AB</i>	<i>Comp. A</i> <i>Comp. AC</i>

The Parts of a Right-angled Spherical Triangle being thus distinguished into 5 Circular Parts, for the more ease in resolving all Spherical Triangles, observe this Catholick and Universal Proportion, invented by the Lord Napier.

The Sine of the Middle Part and Radius, are reciprocally proportional to the Tangents of the Extrems Conjunct, and the Co-fines of the Extrems Disjunct.

That is; As Radius, to the Tangent of one of the Extrems Conjunct; so is the Tangent of the other Extream Conjunct, to the Sine of the Middle-part.

And also, As Radius, to the Tangent of one of the Extrems Disjunct; so is the Co-sine of the other Extream Disjunct, to the Sine of the Middle-part.

Therefore if the Middle-part be sought, the Radius must be in the first place; if either of the Extrems, the other Extream must be in the first place.

Only note, that if the Middle-part, or either of the Extrems Conjunct, be noted with this Complement in the Circular Parts of the Triangle instead of the Sine or Tangent, you must use the Co-sine or Co-Tangent.

If either of the Extrems Disjunct be noted by its Complement in the Circular part of the Triangle, instead of the Co-sine you must use the Sine of such Extream Disjunct.

That the Directions may be the better understood, there is in the Table following the Circular Parts of a Triangle under their respective Titles, whether they be taken for the Middle-part, or for the Extrems, whether Conjunct or Disjunct; and unto those Parts there is prefixed the

Sine

Of Spherical Triangles.

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Sine and *Co-sine*, the *Tangent* or *Co-tangent*, as it ought to be by the Catholick Proportion.

<i>Mid. Part.</i>	<i>Extr. Conj.</i>	<i>Extr. Disj.</i>
<i>Sine. A B</i>	<i>Co-tang. A</i> <i>Tang. BC</i>	<i>Sin e. AC</i> <i>Sine. C</i>
<i>Co-sine. A</i>	<i>Co-tang. AC</i> <i>Tang. A B</i>	<i>Sine. C</i> <i>Co-sine. BC</i>
<i>Co-sine AC</i>	<i>Co-tang. A</i> <i>Co-tang. C</i>	<i>Co-sine. A B</i> <i>Co-sine. BC</i>
<i>Co-sine. C</i>	<i>Cotang. AC</i> <i>Tang. BC</i>	<i>Sine. A</i> <i>Co-sine. A B</i>
<i>Sine. BC</i>	<i>Co-tang. C</i> <i>Tang. AB</i>	<i>Sine. A</i> <i>Sine. AC</i>

AXIOM 3.

In all Spherical Triangles, the Sines of the Sides are in direct proportion to the Sines of their opposite Angles, and the contrary.

AXIOM 4.

In all Oblique angled Spherical Triangles, in which two sides are less than a Semi-circle:

As the Sine of half the Sum of two sides,

To the Sine of half their Difference;

So is the Co-tangent of half the contained Angle,

To the Tangent of half the Difference of the opposite Angles,

And, As the Co-sine of half the Sum of the Sides,

To the Co-sine of half their Difference;

So is the Co-tangent of half the contained Angle.

To the Tangent of half the Sum of the opposite Angles.

AXIOM 5.

In all Oblique-angled Spherical Triangles, in which two Angles are less than two Right-angles:

As the Sine of half the Sum of two Angles.

To the Sine of half their Difference;

So is the Tangent of half the interjacent Side,

To the Tangent of half the Difference of the opposite Sides.

And, As the Co-sine of half the Sum of the Angles.

To the Co-sine of half their Difference;

F

So

So is the Tangent of half the interjacent side,
To the Tangent of half the sum of the opposite sides.

AXIOM 6.

As the Rectangle of the Sines of the containing Sides,
To the Square of Radius;

So is the Rectangle of the Sines of half the sum of the three Sides,
and of the Difference of the opposite side therefrom.

To the Square of the Co-sine of half the Angle sought,

This being premised, the several Cases shall be set down, with their Analogies, and resolved by the Logarithms.

First, Of Right-angled Triangles.

Then, Of Oblique.

SECT. II. Of Right-angled Spherical Triangles.

Case I.

A Leg, and an Angle opposite thereto, being given to find the other Leg, if it be known, whether the *Hypotenuse*, or other Angle, be greater or lesser than a Quadrant.



Example.

In the Triangle ABC,

There is given

BAC $23^{\circ} 30'$ } AB required.
BC, 17 43 }

The Operation.

As Radius	_____	Log. 10.00000
To tc. BAC $23^{\circ} 30'$	_____	10.36170
So is t. BC 17 43	_____	9.50442
To f. AB required, $47^{\circ} 17'$	_____	19.86612

Case II. A Leg and an adjacent Angle giving, to find the other Leg.

Example.

In the Triangle ABC,

There is given,

BAC $23^{\circ} 30'$ } BC required.
AB 47 10 }



The

Of Spherical Triangles.

35

The Operation.

As $\text{tc. BAC } 23^{\circ} 30'$ ————— $\text{Log. } 10.36170$
 To Radius ————— 10.00000
 So is $\text{S. AB } 47^{\circ} 19'$ ————— 9.86635
 To $\text{t. BC required, } 17^{\circ} 43'$ ————— 9.50465

Case III. The Legs given to find an Angle.

Example.

In the Triangle ABC,

There is given,

$\text{AB } 47^{\circ} 19'$
 $\text{BC } 17.43$ } BAC required.



The Operation.

As $\text{t. BC, } 17^{\circ} 43'$ ————— $\text{Log. } 9.50442$
 To Radius ————— 10.00000
 So is $\text{S. AB } 47^{\circ} 19'$ ————— 9.86635
 To $\text{tc. BAC required, } 23^{\circ} 30'$ ————— 10.36193

Case IV. The Hypotenuse and a Leg given to find the contained Angle.

Example.

In the Triangle ABC,

There is given,

$\text{AC } 49^{\circ} 48'$
 $\text{BC } 17.43$ } ACB required.



The Operation.

As Radius ————— $\text{Log. } 10.00000$
 To $\text{tc. AC } 49^{\circ} 48'$ ————— 9.92689
 So is $\text{t. BC } 17^{\circ} 43'$ ————— 9.50442
 To $\text{fc. ACB required, } 74.21$ ————— 19.43131

Case V. A Leg and the adjacent Angle given to find the Hypotenuse.

Example. In the Triangle ABC,

There is given

$\text{BAC } 23^{\circ} 30'$
 $\text{AB } 47.19$ } AC required.



The Operation.

As $\text{t. AB } 47^{\circ} 19'$ ————— $\text{Log. } 10.03516$
 To Radius ————— 10.00000
 So is $\text{fc. BAC } 23^{\circ} 30'$ ————— 9.96240
 To $\text{tc. AC required, } 49^{\circ} 47'$ ————— 9.92724

Case VI. The Hypotenuse and an Angle given, to find the Leg adjacent to the given Angle.

F 2

Ex-

Of Spherical Triangles.

Example. In the Triangle ABC

There is given,

ACB $74^{\circ} 19'$ } BC required.
AC $49^{\circ} 48'$



The Operation.

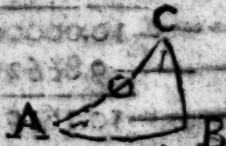
As tc. AC $49^{\circ} 48'$	_____	Log. 9.92689
To Radius	_____	10.00000
So is sc. ACB $74^{\circ} 19'$	_____	9.43188
To t. BC required, $17^{\circ} 44'$	_____	9.50499

Case VII. The Oblique Angles given to find the Hypotenuse.

Example. In a Triangle ABC

There is given,

ACB $74^{\circ} 19'$ } AC required.
BAC $23^{\circ} 30'$



The Operation.

As Radius	_____	Log. 10.00000
To tc. ACB $74^{\circ} 19'$	_____	9.44836
So is tc. BAC $23^{\circ} 30'$	_____	10.36170
To sc. AC required, $49^{\circ} 47'$	_____	9.81006

Case VIII. The Hypotenuse and one of the Angles given, to find the other Angle.

Example. In the Triangle ABC

There is given,

ACB $74^{\circ} 19'$ } BAC required.
AC $49^{\circ} 48'$



The Operation.

As tc. ACB $74^{\circ} 19'$	_____	Log. 9.44836
To Radius	_____	10.00000
So is sc. AC $49^{\circ} 48'$	_____	9.80987
To tc. BAC, required, $23^{\circ} 31'$	_____	10.36151

Case IX. The Hypotenuse and an Angle given, to find the Leg opposite to the given Angle.

Ex

Example.

In the Triangle ABC

There is given,

$$\left. \begin{array}{l} \text{BAC } 23^{\circ} 30' \\ \text{BC } 49 \text{ } 48 \end{array} \right\} \text{BC required.}$$

The Operation.



As Radius	_____	Log.	10.00000
To f. BAC $23^{\circ} 30'$	_____		9.60070
So is f. AC $49^{\circ} 48'$	_____		9.88298
To f. BC required, $17^{\circ} 43'$	_____		9.48332

Case X. A Leg and an Angle opposite thereto, being given, to find the *Hypotenuse*; if it be known, whether it or the other Leg, or unknown Angle, be greater or less than a Quadrant.

Example.

In the Triangle ABC

There is given,

$$\left. \begin{array}{l} \text{BAC } 23^{\circ} 30' \\ \text{BC } 17 \text{ } 43 \end{array} \right\} \text{AC required.}$$

The Operation.



As f. BAC $23^{\circ} 30'$	_____	Log.	9.60070
To Radius	_____		10.00000
So is f. BC $17^{\circ} 43'$	_____		9.48332
To f. AC required, $49^{\circ} 48'$	_____		9.88262

Case XI. The *Hypotenuse* and a Leg given, to find the Angle opposite to the given Leg.

Example.

In the Triangle ABC

There is given,

$$\left. \begin{array}{l} \text{AC } 49^{\circ} 48' \\ \text{BC } 17 \text{ } 43 \end{array} \right\} \text{BAC required.}$$

The Operation.



As f. AC $49^{\circ} 48'$	_____	Log.	9.88298
To Radius	_____		10.00000
So is f. BC $17^{\circ} 43'$	_____		9.48332
To f. BAC required, $23^{\circ} 28'$	_____		9.60034

Case XII. A Leg, and an Angle adjacent thereunto being given, to find the other Angle.

Ex.

Of Spherical Triangles.



Example. In the Triangle ABC

There is given,

BC $17^{\circ} 43'$ } BAC required.
ACB $74^{\circ} 19'$ }

The Operation.

As Radius	-----	Log.	10.00000
To f. ACB $74^{\circ} 19'$	-----		9.98352
So is f. BC $17^{\circ} 43'$	-----		9.97890
To f. BAC required, $23^{\circ} 30'$	-----		9.96242

Case XIII. A Leg and an Angle opposite thereto, being given, to find the other Angle; If it be known whether it, the other Leg, or the *Hypotenuse*, be greater or less than a Quadrant.



Example. In the Triangle ABC,

There is given,

BAC $23^{\circ} 30'$ } ACB required.
BC $17^{\circ} 43'$ }

The Operation.

As f. BC $17^{\circ} 43'$	-----	Log.	9.97890
To Radius	-----		10.00000
So is f. BAC $23^{\circ} 30'$	-----		9.96240
To f. ACB required, $74^{\circ} 19'$	-----		9.98350

Case XIV. The Oblique-angles given, to find either Leg.



Example. In the Triangle ABC,

There is given,

ACB $74^{\circ} 19'$ } BC required.
BAC $23^{\circ} 30'$ }

The Operation.

As f. ACB $74^{\circ} 19'$	-----	Log.	9.98352
To Radius	-----		10.00000
So is f. BAC $23^{\circ} 30'$	-----		9.96240
To f. BC required $17^{\circ} 43'$	-----		9.97888

Case XV. The Legs given, to find the *Hypotenuse*.



Example. In the Triangle ABC,

There is given,

AB $47^{\circ} 19'$ } AC required.
BC $17^{\circ} 43'$ }

The

Of Spherical Triangles.

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The Operation.

As Radius	-----	Log. 10.00000
To sc. AB $47^{\circ} 19'$	-----	9.83119
So is sc. BC $17^{\circ} 43'$	-----	9.97899
To sc. AC required, $49^{\circ} 47'$	-----	9.81018

Case XVI. The *Hypotenuse* and a Leg given, to find the other Leg.

Example. In the Triangle ABC,

There is given,
 AC $49^{\circ} 48'$
 BC $47^{\circ} 43'$ } AB required.



The Operation.

As sc. BC $17^{\circ} 43'$	-----	Log. 9.97890
To Radius	-----	10.00000
So is sc. AC $49^{\circ} 48'$	-----	9.80987
To sc. AB required, $47^{\circ} 21'$	-----	9.83097

SECT. III. Oblique-Angled Spherical Triangles.

Case I.

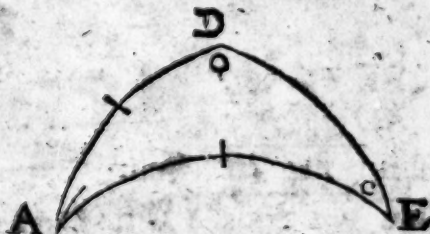
TWO Sides, and an *Angle* opposite to one of them, being given; to find the other opposite *Angle*; if it be known, whether the *Angle* ought be greater or less than a *Right Angle*.

Example.

In the Triangle ADE,

There is given,

AE $69^{\circ} 47'$
 DE $38^{\circ} 28'$ } ADE required
 DAE $37^{\circ} 03'$ } being Obtuse.



The Operation.

As sc. DE $38^{\circ} 28'$	-----	Log. 9.20617
To sc. DAE $37^{\circ} 03'$	-----	9.77996
So is sc. AE $69^{\circ} 47'$	-----	9.97228
To sc. ADE required, $114^{\circ} 39'$	-----	9.95851

Co. Ar.

Case

Of Spherical Triangles.

Case II. Two Angles, and a Side opposite to one of them, being given, to find the other opposite Side; if it be known, whether it be greater or less than a Quadrant.

Example.



In the Triangle ADE,
There is given
ADE $114^{\circ} 38'$ } ED required
EAD $45^{\circ} 00'$ } being less than
A'E $69^{\circ} 47'$ } a Quadrant.

The Operation.

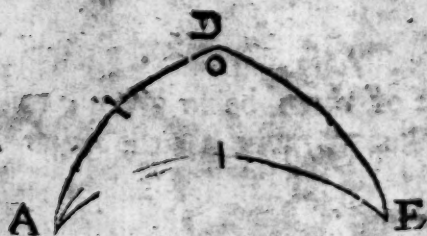
Co. Ar.

As f. ADE $114^{\circ} 38'$ _____ Log. 0.04144
To f. AE $69^{\circ} 47'$ _____ 9.97238
So is f. EAD $45^{\circ} 00'$ _____ 9.84948
To f. ED required, $46^{\circ} 53'$ _____ 9.86330

The Resolution of this and the former Case depends upon the third Axiom.

Case III. Two Sides, and their contained Angles being given, to find the other Angles.

Example.



In the Triangle ADE,
There is given,
DAE $37^{\circ} 03'$ } ADE }
AE $69^{\circ} 47'$ } and } required.
AD $46^{\circ} 53'$ } AED }

The Operation.

AE $69^{\circ} 47'$
AD $46^{\circ} 53'$
Sum, $116^{\circ} 40'$ Sum; $58^{\circ} 20'$
Diff. $22^{\circ} 54'$ Diff. $11^{\circ} 27'$
DAE $37^{\circ} 03'$ half thereof is $18^{\circ} 31'$

Co. Ar.

As f. $\frac{1}{2}$ Z cr. AE and AD $58^{\circ} 20'$ _____ Log. 0.07001
To f. $\frac{1}{2}$ X cr. _____ 9.29779
So is tc. DAE _____ 10.47506
To t. $\frac{1}{2}$ X \angle s D and E _____ 9.84286

As

As $\frac{1}{2}$ c. $\frac{1}{2}$ Z cr ^a . AE and AD	58 20	Log. 0.27986
To $\frac{1}{2}$ c. $\frac{1}{2}$ X cr ^a .	11 27	9.99127
So is tc. $\frac{1}{2}$ DAE	18 31	10.47506
To t. $\frac{1}{2}$ Z Ls D and E	79 49	10.74619
$\frac{1}{2}$ Z Ls D and E	79 49	
$\frac{1}{2}$ X Ls	34 51	
Sum,	114 40	ADE } required.
Rem.	44 58	

Having by the fourth *Axiom* found the half Sum, and half Difference of the Angles ; if to that half Sum you add the half Difference, the Total is the greater Angle ; and if from the half Sum, you subtract the half Difference, the Remainder is the lesser Angle sought.

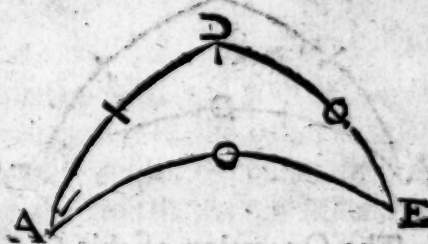
Note ;] If the Sum of the two containing Sides exceed a Semi-Circle, then subtract each side severally from 180, and proceed with those Complements as with the Sides given in the Example foregoing. The Operation produces the Complements of the Angles sought to a Semi-circle.

Case IV. Two Angles, and the interjacent Side being given, to find the other Sides.

Example.

In the Triangle ADE,
There is given,

DAE	26 23	} AE } and } DE }	required.
ADE	137 55		
AD	81 50		



The Operation.

ADE	137 55
DAE	26 23
Sum	164 18
Diff.	111 32
AD	81 50

$\frac{1}{2}$ Sum,	82 09
$\frac{1}{2}$ Diff.	55 46
half thereof	40 55

As f. $\frac{1}{2}$ Z Ls A and D	82 09	Co. Ar.
To f. $\frac{1}{2}$ X Ls	55 46	Log. 0.00409
So is t. $\frac{1}{2}$ AD	40 55	9.91738
To t. $\frac{1}{2}$ X cr ^a . AE & DE	35 52	9.93789
		19.85936

G

As

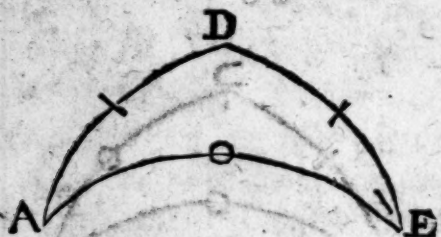
	°	'	Co.	Ar.
As $\text{fc. } \frac{1}{2} Z \text{ } \angle s \text{ } A \text{ and } D$	82	09	Log.	0.86461
To $\text{fc. } \frac{1}{2} X \text{ } \angle s$	55	46		9.75017
So is $t. \frac{1}{2} AD$	40	55		9.93789
To $t. \frac{1}{2} ZAE \text{ and } DE$	74	21		10.55267
$\frac{1}{2} Z \text{ cr. } AE \text{ and } DE$	74	21		
$\frac{1}{2} X \text{ cr.}$	35	52		

Sum, 110 13 AE } required.
 Rem. 38 29 DE }

This Case is wrought by the fifth *Axiom*, and the half Sum of the Sides added to the half Difference, gives a greater Side; and the half Difference subtracted, leaves the less.

Note;] If the Sum of the given Angles exceed 180° , subtract each Angle from 180° , and proceed with Residues, the Operation will produce each Sides Compl. to a Semi-circle.

Case V. Two Sides, and an Angle opposite to one of them, being given, to find the third Side; if it be known, whether the other opposite Angle, of the required Side, be greater or less than a Quadrant.



Example. In the Triangle ADE
 There is given,

AD 46 53 } And AE required,
 DE 38 28 } being less than a
 AED 45 00 } Quadrant.

The Operation of this Case depends upon the 3^d and 5th *Axiom*.

First, By the third *Axiom* find the Angle opposite to the other given Side.

Secondly, Having two sides, and their opposite Angles, you may find the third Side by the former part of the fifth *Axiom* inverted.

	°	'	The Operation	Co.	Ar.
As $\text{f. } AD$	46	53		Log.	0.13670
To $\text{f. } AED$	45	00			9.84948
So is $\text{f. } DE$	38	28			9.79383
To $\text{f. } DAE$	37	03			10.978001
AED	45	00			
DAE	37	03			
Sum.	82	03	$\frac{1}{2}$ Sum,	41°	01
Diff.	07	57	$\frac{1}{2}$ Diff.	03	58
AD	46	53			
DE	38	28			
Diff.	08	25	$\frac{1}{2}$ Diff.	04	12

Of Spherical Triangles.

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Co. Ar.

As f. $\frac{1}{2}$ X	∠s A and E	03 58	Log	1.16004
To f. $\frac{1}{2}$ Z	∠s	41 01		9.81709
So is t. $\frac{1}{2}$ X	cr. AD & DE	04 12		8.86598
To t. $\frac{1}{2}$ AE	required	34 52		19.84303

34 52

34 52

AE 69 44 required.

Case VI. Two Angles and a Side opposite to one of them, being given, to find the third Angle; if it be known, whether the opposite Side, or Angle required, be greater or less than a Quadrant.

Example.

In the Triangle ADE,

There is given,

DAE 37° 03' } ADE required, be-
AED 45 00 } ing Obtuse.
ED 38 28 }



The Resolution of this Case depends upon the third and fourth *Axioms*.

First, By the third *Axiom* find the Side opposite to the other Angle.

Secondly, Having the two Angles, and their opposite Sides, the third Angle may be found by the former part of the fourth *Axiom* inverted.

		The Operation.	Co. Ar.
As f. DAE	37 03		Log. 0.22004
To f. DE	38 28		9.79383
So is f. AED	45 00		9.84948
To f. AD	46 53		19.86335
AD	46 53		
DE	38 28		

Sum, 85 21 $\frac{1}{2}$ Sum, 42° 40'

Diff. 08 25 $\frac{1}{2}$ Diff. 04 12

AED 45 00

DAE 37 03

Diff. 07 57 $\frac{1}{2}$ Diff. 03 58

G 2

Co.

Co.

	Co. Ar
As f. $\frac{1}{2}$ X cr ^a . AD and DE 04 12 —————	Log. 1.13527
To f. $\frac{1}{2}$ Z cr ^a . —————	9.83106
So is t. $\frac{1}{2}$ X Ls A and E 03 58 —————	8.84120
To tc. $\frac{1}{2}$ AD required, —57 19 —————	19.80733
57 19	

114 38 required.

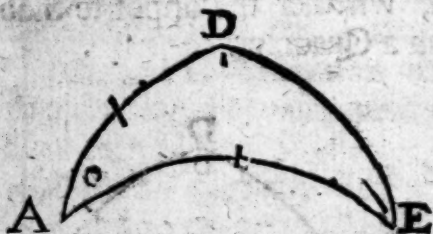
Case VII. Two Sides, and an *Angle* opposite to one of them, being given, to find the contained *Angle*; if it be known, whether the other opposite *Angle*, or the *Angle* required be Acute or Obtuse.

Example.

In the Triangle ADE

There is given,

AED 45° 00'	} DAE required, being Acute.
AE 110 13	
AD 81 50	



This *Case* is wrought by the help of the third and fourth *Axioms*.
First, by the third *Axiom* to find the other opposite *Angle*.
Secondly, by the fourth *Axiom*, to find the contained *Angle*.

The Operation.

	Co. Ar.
As f. AD ——— 81 50 —————	Log. 0.00443
To f. AED 45 00 —————	9.84948
So is f. AE 110 13 —————	9.97238
To f. ADE 137 55 required —————	19.82629
ADE 137 55	
AED 45 00	
Diff. 92 55 $\frac{1}{2}$ Sum, 46° 27'	
AE 110 13	
AD 81 50	
Sum, 192 03 $\frac{1}{2}$ Sum, 96 01	
Diff. 28 23 $\frac{1}{2}$ Diff. 14 11	

	Co. Ar.
As f. $\frac{1}{2}$ X cr ^a AE and AD 14 11 —————	Log. 0.61079
To f. $\frac{1}{2}$ Z cr ^a —————	9.99760
So is t. $\frac{1}{2}$ X Ls D and E 46 27 —————	10.02199
To tc. $\frac{1}{2}$ DAE required, 13 11 —————	10.63038
13 11	

DAE 26 22 required.

Case

Of Spherical Triangles.

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Case. VIII. Two Angles, and a Side opposite to one of them, being given, to find the interjacent Side; if it be known, whether the other opposite Side, or Side sought, be greater or lesser than a Quadrant.

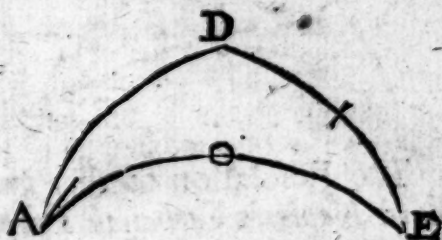
Example.

In the Triangle ADE,

There is given,

AED $45^{\circ} 00'$
DAE $37^{\circ} 03'$
DE $48^{\circ} 28'$

} AE required, being
} less than a Quadrant



This Case is resolved by the third and fifth *Axioms*.

First, By the third *Axiom*, to find the other opposite Side.

Secondly, By the fifth *Axiom*, to find the interjacent Side.

The Operation.

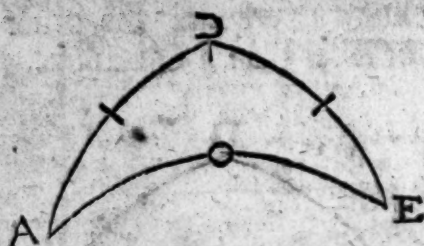
Co. Ar.

As f. DAE	37 03	Log.	0.22004
To f. DE	38 28		9.79383
So is f. AED	45 00		9.84948
To f. AD	46 53		9.86335
AED	$45^{\circ} 00'$		
DAE	$37^{\circ} 03'$		
Sum	82 03	$\frac{1}{2}$ Sum,	$41^{\circ} 01'$
$\frac{1}{2}$ Diff	07 57	$\frac{1}{2}$ Diff.	$03^{\circ} 58'$
AD	46 53		
DE	38 28		
Diff.	08 25	$\frac{1}{2}$ Diff.	$04^{\circ} 12'$

As f. $\frac{1}{2}$ X Ls A and E	03 58	Log.	1.16005
To f. $\frac{1}{2}$ Z Ls	41 01		9.81709
So is t. $\frac{1}{2}$ X cr. AD and DE	04 12		8.86590
To t. $\frac{1}{2}$ AE required	34 52		9.84304
	34 52		
	34 52		
	69 44	required.	

Case IX. Two Sides, and their contained Angle being given, to find the third Side.

Ex.



Example.

In the Triangle ADE

There is given,

ADE	137° 55'	} AE required.
AD	81 50	
DE	38 28	

The Resolution of this and the following Case is deduced from the Lord Napier's *Catholick Proposition* (the Oblique Triangle by a supposed Perpendicular being reduced into two Rectangulars) by the Ingenious Mr. Collins, in his *Sector on a Quadrant*, whom in this I shall imitate.

The Operation.

As Radius	-----	Log. 10.00000
To sc. ADE the contained Angle 137° 55'	-----	9.87050
So is t. DE the lesser Side	38 28 -----	9.90009
To t. of a fourth Arch,	30 31 -----	19.77059

If the contained Angle be less than 90°, subtract the fourth Arch from the greater Side; but if it be greater than 90°, from its Complement to 180°, the Remainder is the Residual Arch.

As sc. of the fourth Arch	30° 31' -----	Log. 0.06476
To sc. of the Residual	67 39 -----	9.58008
So is sc. of the lesser Side DE	38 28 -----	9.89374
To sc. of the Side required, AE	110 13 -----	19.53858

Case X. Two Angles, and the interjacent Side being given, to find the third Angle.

Example.

In the Triangle ADE

There is given.

ADE	114 39	} AED required.
DAE	37 03	
AD	46 53	



The

The Operation.

As Radius ————— Log. 10.00000

To sc. AD the interjacent Side, 46 53 ————— 9.83473

So is t. DAE the lesser Angle, 37 03 ————— 9.87790

To t. of the fourth Arch ——— 27 17 ————— 19.71263

If the interjacent Side be more than a Quadrant, subtract the fourth Arch from the greater Angle, if less, from the said Angle's Complement to 180°, the Remainder is the Residual Arch.

o 1

As sc. fourth Arch ——— 27 17 ————— Log. 0.05122

To sc. Residual Arch — 38 04 ————— 9.89614

So is sc. DAE the lesser Angl. 37 03 ————— 9.90206

To sc. AED the Ang. required, 45 00 ————— 19.84942

In this and the foregoing Case, the Affection of the required Side or Angle may be determined by the Residual Arch.

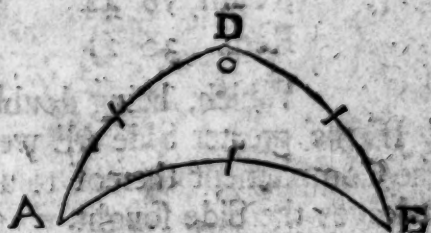
For if the contained Angle, or interjacent Side be less than a Quadrant, and the Residual Arch more; or when the contained Angle, or interjacent Side is greater than a Quadrant, and the Residual Arch less, the Side or Angle required is greater than 90°, in all other Cases less.

Case XI. Three Sides given, to find an Angle.

Example.

In the Triangle ADE
there is given,

AE 110 13 }
AD 81 50 } ADE required.
DE 38 28 }



The Resolution of this Case depends upon the sixth *Axiom*; and for the more speedy Operation take this brief Direction.

Add the three Sides together, and from their half Sum subtract the Side opposite to the Angle required.

Then to the Compl. Arithmetical of the Logarithm Sines of the containing Sides, add the Logarithm Sines of the half Sum and Remainder, Half the total of these four Logarithms is the Sine Complement of half the Angle required.

The

Of Spherical Triangles.

The Operation.

AD 81 50 } The containing } S.

DE 38 28 } Sides. } S.

AE 110 13 $\frac{1}{2}$ Sum, 115° 15' S.

Sum, 230 31 Rem. 05 02 S.

 $\frac{1}{2}$ Sum, 115 15

Remain. 05 02

fc. 68. 57

Which, being doubled, produces ADE 137° 55' required.

Case XII. Three Angles given, to find a Side.

Example.

In the Triangle ADE,

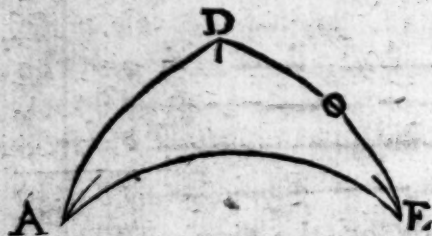
There is given,

ADE 137 55

AED 45 00

DAE 26 23

} DE required.



This Case is likewise performed by the 6th Axiom, the Angles being converted into Sides, and the Sides into Angles, by taking the Comp. of the greatest Angle to a Semi-circle.

Compl. ADE 42 05 } The adjacent } S.

AED 45 00 } Angles. } S.

DAE 26 23 $\frac{1}{2}$ Sum, 56° 44' S.

Sum, 113 28 Rem. 30 21 S.

 $\frac{1}{2}$ Sum, 56 44

Rem. 30 21

fc. 19 15

Which, being doubled, gives DE 38° 30' required.

If the greater Side AE were required, the Operation would produce, the Complement thereof to a Semi-circle; which subtracted from 180° it leaves the Side sought.

Co. Ar. 0.00443

Co. Ar. 0.20617

9.95639

8.94317

Sum, 19.11016

 $\frac{1}{2}$ Sum, 9.55508

Co. Ar. 0.17379

Co. Ar. 0.15052

9.92227

9.70353

Sum, 19.95011

 $\frac{1}{2}$ Sum. 9.97505

CHAP. V.

The Doctrine of Plain Triangles applied in PROBLEMS of Plain Sailing.

SECT. I.

The Application of Right-angled Triangles in Plain Sailing.

Although the Ground and Projection of the Plain Chart be erroneous, yet seeing it is more facile to the Learner, and may serve as an Introduction to what is more difficult, it shall not be here omitted.

PROB. I. The Course and Distance given, to find the Difference of Latitude and Departure.

Example. A Ship sailing N. E. by N. 372 Minutes.

I demand her Difference of Latitude and Departure.

Plate I. Fig. 1.

In the Triangle ABC,

AC represents the Distance sailed.

AB the Diff. of Latitude.

BC the Departure.

BAC the Angle of the Course from the Meridian.

ACB the Compl. of the Course.

The Operation. For the Difference of Latitude.

As Radius	_____	Log. 10.00000
To the Distance sailed	_____ 372 ¹ _____	-2.57054
So is sc. of the Course,	_____ 33° 45' _____	-9.91985
To the Diff. Latitude	_____ 309 _____	-12.49039

For the Departure.

As Radius	_____	Log. 10.00000
To the Distance sailed	_____ 372 ¹ _____	-2.57054
So is S. Course,	_____ 33° 45' _____	-9.74474
To the Departure	_____ 206 _____	-12.31528

PROB. II. The Course and Diff. Latitude being given, to find the Distance and Departure.

H

Example.

Plain Sailing.

Example. A Ship sailing N. W. by N. until her Difference of Latitude be 309', I demand her Distance and Departure.

Plate 1. Fig. 2.

The Operation. For the Distance.

As sc. of the Course	33° 45'	Log.	9.91985
To the' Diff. Latitude	309		2.48996
So is Radius			10.00000
To the distance sailed	371		2.57011

For the Departure.

Co. Ar.

As sc. Course	33° 45'	Log.	0.08015
To the diff. Latitude	309		2.48996
So is f. Course	33 45		9.74474
To the Departure	206		2.31485

PROB. III. The Course and Departure given, to find the distance and difference of Latitude.

Example. A Ship Sailing S. E. by S. until her departure be 206', I demand the distance and difference of Latitude.

Plate 1. Fig. 3.

The Operation. For the Distance.

As f. Course	33° 45'	Log.	9.74474
To the Departure	206		2.31387
So is Radius			10.00000
To the Distance	370		2.56913

For the Diff. of Latitude.

Co. Ar.

As f. Course	33° 45'	Log.	0.25526
To the Departure	206		2.31387
So is sc. Course	33 45		9.91985
To Diff. Lat	308		2.48898

PROB. IV. The distance and difference of Latitude given, to find the Course and Departure.

Example. A Ship sails between the North and the East 372', until her diff. of Latit. be 309'; I demand the Course and Departure.

Plate 1. Fig. 4.

The

Plain Sailing.

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The Operation. For the Course.

As the distance sailed, 372' ————— Log. 2.57054
 To Radius ————— 10.00000
 So is the Diff. Lat. 309 ————— 2.48996
 To the sc. Course 33° 50' ————— 9.91942

For the Departure.

As Radius ————— Log. 10.00000
 To the Distance ————— 372' ————— 2.57054
 So is the f. Course, 33° 50' ————— 9.74568
 To the Departure ————— 207' ————— 2.31622

PROB. V. The Distance and Departure given, to find the Course and Difference of Latitude.

Example. A Ship sails between the South and the West 372', until her departure be 206; I demand the Course and Diff. of Latitude.

Plate I. Fig. 5.

The Operation. For the Course.

As the Distance ————— 372' ————— Log. 2.57054
 To Radius ————— 10.00000
 So is the departure 206 ————— 2.31387
 To the S. Course 33° 37' ————— 9.74333

For the Diff. Latitude.

As Radius ————— Log. 10.00000
 To the distance ————— 372' ————— 2.57054
 So is sc. of the Course, 33° 37' ————— 9.92052
 To the diff. Latitude, ————— 309 ————— 12.49106

PROBLEM VI. The difference of Latitude, and departure given, to find the Course and distance.

Example. A Ship sailing between the South and West, until her differ. Latitude by 309 min. and her departure 206 min. I demand the Course and Distance.

Plate I. Fig. 6.

Plain Sailing.

The Operation. For the Course.

As the differ. Latitude 309 min. ————— Log. 2.48996
 To Radius ————— 10.00000
 So is the departure 206 min. ————— 2.31387
 To t. Course $33^{\circ} 41'$ ————— 9.82391

For the Distance.

As f. Course ————— $33^{\circ} 41'$ ————— Log. 9.74398
 To the Departure ————— 206 ————— 2.21387
 So is Radius ————— 10.00000
 To the distance ————— 371 ————— 2.56989

SECT. II. The Doctrine of Oblique Triangles applied in Problems of Plain Sailing.

PROB. I.

TWO Ships sail from the same Port, the one sails ENE. 40 min. the other E. by S. so far, until she find the first Ship bear N. W. by W. I demand the second Ship's Distance from the Port, and the Distance between the two Ships. Plate I. Fig. 7.

In the Triangle ADE,

A represents the Port.

AD the ENE. Course, and AE the E. by S. Course.

The Operation.

To find the second Ship's Distance from the Port.

Co. Ar.

As S. AED ————— 22 30 ————— Log. 0.41716
 To AD ————— 40 ————— 1.60206
 So is S. ADE ————— 123 45 ————— 9.91985
 To AE ————— 86 ————— 11.93907

To find the Distance between the Ships.

Co. Ar.

As S. AED ————— 22 30 ————— Log. 0.41716
 To AD ————— 40 ————— 1.60206
 So is S. DAE ————— 33 45 ————— 9.74474
 To DE ————— 58 ————— 11.76396

PROB.

P R O B. II. Suppose there are two Ports that lie East and West one from another; one Ship sails from the Westermost Port N. E. 41° , the other Sails from the Eastermost Port 80° , and meets with the first Ship: I demand the Course steer'd by the second Ship, and the Distance between the two Ports.

Plate 1. Fig. 8.

Let A represent the Westermost.

E the Eastermost.

AD the Course and Distance of the first Ship.

D the Place where the Ships meet.

To find the second Ship's Course.

The Operation.

Co. Ar.

As DE	80'	Log.	8.09691
To f. DAE	$45^\circ 00'$		9.84948
So is AD	41		1.61278
To f. AED	$21^\circ 14'$		2.955917

The Course is N. $68^\circ 46'$ W. or W.N.W. a little Westerly.

To find the Distance between the two Ships.

Co. Ar.

As f. DAE	$45^\circ 00'$	Log.	0.15052
To ED	80		1.90309
So is f. ADE	$113^\circ 46'$		9.96151
To AE	103		2.01512

P R O B. III. Suppose two Ship's set sail from a certain Road, the one sails S. by E. 20 min. the other S.S.W. 25 min. I demand their Bearing and Distance from each other.

Plate 1. Fig. 9.

In the Triangle ADE.

A represents the Road.

AD the first Ship's Course and Distance.

AE the second Ship's Course and Distance.

The Operation. To find the Bearings.

AE 25	$180^\circ 00'$
AD 20	DAE 33 45
Sum 45	146 15, Z/s ADE and AED.
Diff. 05	73 07, $\frac{1}{2}$ Sum.

As

As Z cr. AE and AD	45	Co. Ar.	Log. 8.34679
To their Differ.	05		0.89897
So it t. $\frac{1}{2}$ Z Ls D and E	73° 07'		10.51783
To t. their Difference	20 06		19.56359
$\frac{1}{2}$ Z Ls 73° 07'			
$\frac{1}{2}$ X Ls 20 06			
Sum, 93 13 ADE			
Diff. 53 01 AED			

The Bearings of the Ships are N. E. 75° 31', and S. W. 75° 31', or E.N.E. $\frac{1}{4}$ E. and W.S.W. $\frac{1}{4}$ W. *ferè*.

To find their Distance.

As f. AED	53° 01'	Co. Ar.	Log. 0.09756
To AD	20		1.30103
So is f. DAE	33 45		9.74474
To DE	13 $\frac{1}{2}$		11.64333

PROB. IV. A Ship sails from a certain Port S.S.E. 68 min. and then 72 min. more Easterly, but is forced back by foul Weather 82 min. to the Port from whence she set sail; I demand what Course she steered from the second Place to the third, and how she sailed back to the first Port.

Plate 1. Fig. 10.

Let A represent the Port,

E the second Place

D the third Place.

The Operation.

To find the Course from the second Place to the third.

AD 82

AE 68

Sum, 150

Diff. 14

As DE the Base	72	Co. Ar.	Log. 8.14267
To Z cr. AE and AD	150		2.17609
So is their Difference	14		1.14613
To a Segment of the Base. 29			11.46489

DE

DE ——— 72 ¹	DE ——— 72
Segment 29	Segment 29
Diff. ——— 43	Sum ——— 101
$\frac{1}{2}$ Diff. ——— 21 $\frac{1}{2}$, or 21 $\frac{1}{2}$ $\frac{1}{2}$ EB.	$\frac{1}{2}$ Sum. 50 $\frac{1}{2}$ DB 50 $\frac{1}{2}$
As AE ——— 68 ¹	Log 1.83251
To Radius ———	10.00000
So is EB 21 $\frac{1}{2}$ $\frac{1}{2}$	1.33244
To sc. AEB, or AED. 71° 34'	9.49993
The Course from the second Place to the third, is N.E. 49° 04', or N. E. $\frac{1}{2}$ E. <i>ferè</i> .	

To find the Course back to the Port.

	Co. Ar.
As AD 82 min. ———	Log. 8.08619
To f. AED, 71° 34'	9.97712
So is AE 68 min. ———	1.83251
To f. ADE 51° 53'	19.89582
The Course to the Port is N. W. 79° 03', or W. by N. a little <i>Westerly</i> .	

CHAP. VI.

The Doctrine of Plain Right-angled Triangles applied in PROBLEMS of Mercator's Sailing.

THE true Sea Chart, commonly called *Mercator's Chart* (which is the useful Invention of our Country-Man Mr. *Edward Wright*, altho' this *Stranger* hath got the Name thereof) performs the like Conclusions, and almost in the same manner for ease, and yet most exactly; because all Places may be laid down upon this Chart with the same truth as upon the Globe, both as to their Latitude and Longitude, Bearing and Distance from each other.

PROBLEM I.

To find the Meridional Difference of Latitude, or the Difference of Latitude in Meridional Parts.

First, If one Place be under the Equinoctial, and the other in North or South Latitude, the Meridional Parts (in the Table of Meridional Parts) answering to the Degrees and Minutes of the Place's Latitude, is the Meridional diff. of Latitude.

Example.

Example.

One Place in Latitude $37^{\circ} 27'$ North, the other under the Equinoctial : I demand the Difference of Latitude in Meridional Parts.

Lat. $37^{\circ} 27'$ ————— 2426

2426 is the Meridional diff. Latitude.

Secondly, If two Places be both in North or both in South Latitude, Subtract the Meridional Parts of the less Latitude from those of the greater, the Remainder is the Meridional diff. Lat.

Example 1.

One Place in the Latitude $37^{\circ} 20'$ N.

The other in the Latitude $17^{\circ} 10'$ N.

The Meridional diff. Latitude

M. Pts.

2418

1046

1372

Example 2.

One Place in the Latitude $45^{\circ} 56'$ S.

The other in the Latitude $29^{\circ} 17'$ S.

The Meridional diff. Latitude,

M. Pts.

3110

1839

1271

Thirdly, If of the two Places the one have North Latitude, the other South, add the Meridional Parts of each Latitude together, the Sum is the Difference of Latitude in Meridional Parts.

Example.

One Place in the Latitude $42^{\circ} 17'$ S.

The other in the Latitude $27^{\circ} 19'$ N.

The Meridional diff. Latitude,

M. Pts.

2805

1705

4510

P R O B. II.

Both Latitudes, and the difference of Longitude between any two Places being given, to find the Course and Distance.

Example.

Admit the *Lizard* in the Latitude 50° North, and *Barbadoes* in the Latitude $13^{\circ} 12'$ North, the diff. of Longitude $52^{\circ} 57'$ West ; I demand the Course and Distance.

In the Right-angled Triangle $A b c$,

$A b$ represents the proper Difference of Latitude,

$b c$ the Departure,

$A c$ the Distance sailed,

$b A c$ the Course,

$A c b$ the Compl. of the Course.

In the Right-angled Triangle A B C,

A B represents the Meridional diff. Latitude

B C the difference of Longitude,

B A C the Angle of the Course

A C B the Compl. of the Course.

The Difference of Longitude reduced to Minutes, makes 2177 min.

To find the Meridional Difference of Latitude.

	<i>M. Pts.</i>
One Place in the Latitude $50^{\circ} 00'$ N.	3475
The other in the Latitude $13^{\circ} 12'$ N.	799
The Meridional diff. Latitude	2676

The Operation. For the Course.

As Meridional Difference Lat. 2676 min.	Log. 3.42749
To Radius	10.00000
So is the differ. Longitude 3177 min.	3.50202
To t. Course $49^{\circ} 53'$	10.07453
The Course is S. W. $\frac{1}{2}$ W.	

For the Distance.

Lat. $50^{\circ} 00'$	
Lat. $13^{\circ} 12'$	
Proper Diff. Lat. 36 48, which is 2208 min.	
As sc. Course $49^{\circ} 53'$	Log. 9.80912
To proper Diff. Lat. 2208	3.34400
So is Radius	10.00000
To the Distance — 3426	3.53488

PROB. III. Both Latitudes and the Course given, to find the distance and difference of Longitude.

Example. A Ship sails from the North, until she be in the Lat. $13^{\circ} 12'$ North, her Course S. W. $50^{\circ} 57'$, or S. W. $\frac{1}{2}$ W. somewhat more Westerly; I demand the Distance, and Difference of Longitude.

The proper difference of Latitude is 2208 min.

The Meridional Difference of Latitude is 2676.

Mercator's Sailing.

The Operation. For the Distance.

As sc. Course	50° 57'	Log. 9.79934
To the Diff. of Latitude	2208	3.34400
So is Radius		10.00000
To the Distance	3504	3.54466

For the Difference of Longitude.

As Radius		Log. 10.00000
To the Merid. Diff. Lat. 2676'		3.42749
So is t. Course,	50° 57'	10.09086
To the differ. of Long. 3298		13.51835

PROB. IV. Both Latitudes and the Distance given, to find the Course and Difference of Longitude.

Example. A Ship sails from the Lat. 50° North, 3505', until she be in the Latitude 13° 12' North, ; I demand the Course and Difference of Longitude.

The Meridional Difference of Latitude is 2676 min.

The proper difference of Latitude is 2208 min.

The Operation. For the Course.

As the Distance	3505'	Log. 3.54469
To Radius		10.00000
So is the difference of Lat. 2208		3.34400
To sc. Course	50° 57'	9.79931

For the Difference of Longitude.

As Radius		Log. 10.00000
To the Merid. Diff. Lat. 2676'		3.42749
So is t. Course	50° 57'	10.09086
To the differ. of Longitude 3298		3.51835

PROB. V. One Latitude, the Course and Difference of Longitude being given, to find the other Latitude, and the Distance.

Example. A Ship sails S. 50° 57' W. or S. W. $\frac{1}{2}$ W. somewhat more Westerly, from the Latitude 50° North, until the Difference of Longitude be 3297' ; I demand the other Latitude and Distance.

The

Mercator's Sailing.

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The Operation. For the other Latitude..

As t. Course ————— $50^{\circ} 57'$ ————— Log. 10.09086
 To the difference of Longit. 3297 ————— 3.51812
 So is Radius ————— 10.00000
 To the Merid. Diff. Lat. — 2674 ————— 3.42726
M pts.

The Meridional Parts answering to Latit. 50° North, are — 3475
 From which subtract — 2674
 There remains — 801

Against which, in the Table of Meridional Parts, is the Latitude of $13^{\circ} 14'$, which is the Latitude of the Place, North.

For the Distance.

The proper Difference of Latitude is 2206 min.

As sc. Course ————— $50^{\circ} 57'$ ————— Log. 9.79934
 To the difference of Latitude 2206 ————— 3.34360
 So is Radius ————— 10.00000
 To the Distance ————— 3501 ————— 3.54426

PROB. VI. One Latitude, the Course and Distance given, to find the other Latitude and Difference of Longitude.

Example. A Ship being in the Latitude 50° North, sails S. W. $50^{\circ} 57'$, or S. W. $\frac{1}{2}$ W. and somewhat more Westerly 3505; I demand the other Latitude, and Difference of Longitude.

The Operation. For the Difference of Latitude.

As Radius' ————— Log. 10.00000
 To the Distance — 3505' ————— 3.54469
 So is sc. Course — — $50^{\circ} 57'$ ————— 9.79934
 To the Diff. Latitude — 2208 ————— 3.34403

The other Latitude 13 deg. 12 min. North.

The Meridional Diff. Latitude is 2676 min.

For the Difference of Longitude.

As Radius ————— Log. 10.00000
 To the Meridional Diff. Lat. 2676' ————— 3.42749
 So is t. Course — — $50^{\circ} 57'$ ————— 10.09086
 To the Diff. of Longitude — 3298 ————— 3.51835

PROB. VII. Two Places both in one Parallel or Latitude, and their diff. of Longitude being given, to find the Distance between them.

Example. Suppose two Places both in the Parallel or Latitude of 50 deg. and their difference of Longitude 70 deg. I demand the Distance between them.

The Operation.

The Difference of Longitude in Minutes is 4200.

As Radius	10.00000
To diff. Longitude 4200 min.	3.62325
So is sc. Latitude 50 deg.	9.80807
To the Distance 2700 min.	3.43132

PROB. VIII. Two Places both in one Latitude, and their Distance given, to find their Difference of Longitude.

Example. Suppose two Places both in the Latitude 50 deg. and the Distance between 2700 min.

I demand the difference of Longitude.

The Operation.

As sc. Latitude 50 deg.	Log. 9.80807
To the Distance 2700 min.	3.43136
So is Radius	10.00000
To the diff. Longitude 4200 min.	3.62329

PROB. IX. Two Places situated both in one Parallel of Latitude, their Distance and Difference of Longitude being given, to find the Parallel of Latitude.

Example.

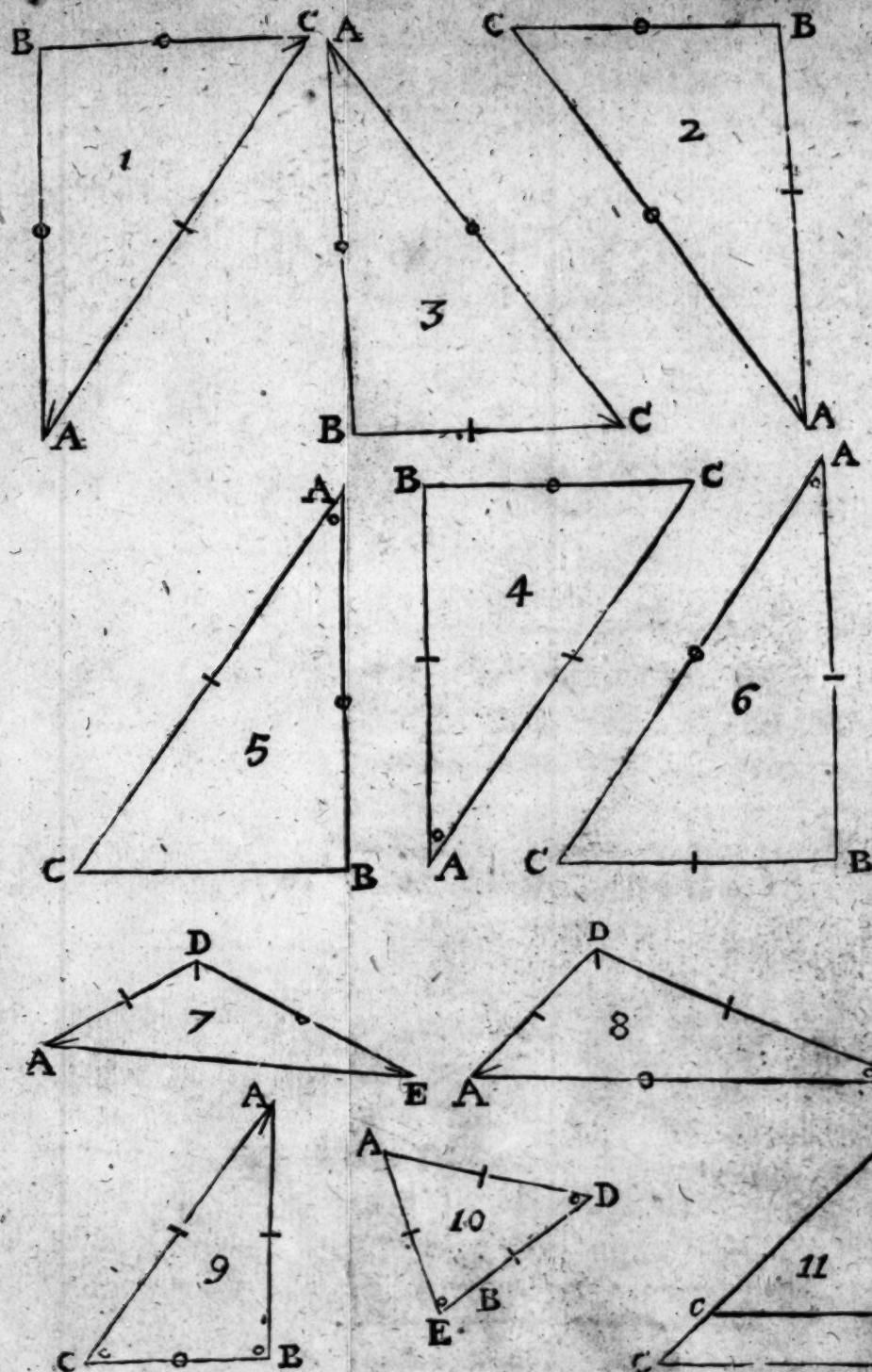
A Ship failing due West 2700 minutes, until

her Diff. Longitude be 4200 minutes;

I demand what Latitude the Ship fails in.

The Operation.

As diff. Longitude 4200 min.	Log. 3.62325
To Radius	10.00000
So is the Distance 2700 min.	3.43136
To sc. Latitude 50 deg.	9.80811



C H A P. VII.

The Doctrine of Spherical Triangles applied in PROBLEMS
of Great Circle Sailing.

Although it be hardly possible for a Ship exactly to trace out the Arch of a Great Circle, yet it may be of advantage to keep conveniently near it, especially in a Parallel (or East and West) Course.

P R O B. I.

Two places differing only in Longitude.

Example. A Ship being in the Latitude 50° North, is bound to a Port in the same Parallel, whose Difference of Longitude Westerly is 47° ; I demand the Angles of Position, the Distance in the Arch of a Great Circle, by what Latitude and Longitudes the Arch shall pass, likewise the Course and Distance from Place to Place, according to *Mercator*.

Let A represent the first Place,
E the second.

Plate 2. Fig. 12.

The Operation.

To find the Angles of Position, BAD and BED.

The Oblique-angled-Triangle ADE is reduced into two equal Right-angled Triangles ABD and EBD, the Sides and Angles being equal, therefore in either of them there is given the *Hypotenuse*. and the Angle at D, to find the Angle at A or E.

In the Triangle ABD.

As tc. ADB	$23^{\circ} 30'$	Log.	10.36170
To Radius			10.00000
So is sc. AD	$40^{\circ} 00'$		9.88425
To tc. BAD	$71^{\circ} 35'$		9.52255

2. To

Great Circle Sailing.

2. To find the Distance AE.
In the Triangle ABD.

As Radius	_____	Log. 10.00000
To \angle DA	40° 00'	6.80807
So is \angle ADB	23 30	9.60070
To \angle AB	14 51	9.40877
AB 14 51 being doubled, produces		
AE 29 42, or 1782 min.		

3. To find the Latitudes by which the Arch shall pass at every five Degrees of Longitude from A; representing the first Port.

First, You must find the greatest Latitude by which the Arch passes, DB.

In the Triangle ABD.

As \angle AD	40° 00'	Log. 10.07619
To Radius	_____	10.00000
So is \angle ADB	23 30	9.96240
To \angle BD	37 35	9.88621

The Compl. of BD (to 90°) 42° 25' is the greatest.

Secondly. To find the Latitude by which the Arch passes at every five Degrees of Longitude from A, you must resolve the several Right-angled Triangles, BDa, BDc, BDe, &c.

Subtracting five deg. from ADB	23 30
There remains	aDB 18 30
Subtracting five deg. from	18 30
Remains	BDc 13 30

And so for the rest, as follows in the Table.

a D B	18 30	In the Triangle aBD
B D c	13 30	
B D e	08 30	
B D f	03 30	
B D g	01 30	
B D h	06 30	
B D i	11 30	To find by what Latitude the Point (a) passes.
B D k	16 30	
B D l	21 30	

As Radius	_____	Log. 10.00000
To \angle BD	37° 35'	10.11371
So is \angle aDB	18 30	9.97696
To \angle Da	39 04	10.09067

The Complement of D a 50 deg. 56 min. North, is the Latitude of the Point (a).

After

After the same manner are found the Latitudes for the Points c, e, &c. in the subsequent Table.

	Long.	Lat.
A	00° 00'	50° 00'
a	05 00	50 56
c	10 00	51 38
e	15 00	52 06
f	20 00	52 22
g	25 00	52 24
h	30 00	52 14
i	35 00	51 51
k	40 00	51 14
l	45 00	50 24
E	47 00	50 00

Thirdly, Having the Latitudes and Longitudes by which the Arch passes, you may find the Course and Distance from Place to Place, by *Mercator*.

So to find the Course and Distance Aa, There is given both *Latitudes* 50 deg. North, and 50 deg. 56 min. North.

And the difference of Longitude, 5 degrees West.

The Meridional Difference of Latitude is 87 minutes.

For the Course.

As Merid. diff. Lat.	87	Log. 1.93952
To Radius		10.00000
So is the diff. of Long.	300	2.47712
To t. Course	73° 49'	10.53760

For the Distance.

As sc. Course	73° 49'	Log. 9.44515
To the diff. of Lat.	56	1.74819
So is Radius		10.00000
To the Distance		2.30304

After the same manner you will find the Courses and Distances ac, ce, &c. as they follow in the Table.

Places.	Courses.	Distances
From A to a	N W 73° 49'	200
From a to c	N W 77 13	189
From c to e	N W 81 28	188
From e to f	N W 85 02	184
From f to g	N W 19 22	180
From g to h	S W 86 45	179
From h to i	S W 82 58	187
From i to k	S W 78 41	188
From k to l	S W 75 14	196
From l to E	S W 72 51	081

But

But in regard most of the Courses afore-found are so near the West you may sail W. N. W. $917'$, until you are in the Latitude $55^{\circ} 51'$ North; and then W. S. W. 917 min. further, you will arrive at your Port. By this means you will alter your Latitude almost 6 deg. and the distance is but 52 more than that of a Great Circle, and not above 22 min. more than the Parallel or West Distance.

PROB. II. Two Places differing both in Latitude and Longitude.

Example. Suppose the two Places to be, one in Latitude 36° North, the other in the Latitude 50° North, the Difference of Longitude between them 68° Easterly. I demand the Angles of Position, the Distance in the Arch, the Latitudes and Longitudes by which the Arch passes, and the Course and Distance from Place to Place, through those Latitudes and Longitudes, according to the true Chart.

Let A represent the first place, in the Lat. 36° :

E the second, in the Lat. 50° .

Plate 11. Fig. 13.

The Operation.

First, To find the Angles of Position.

In the Triangle ADE.

AD	$54^{\circ} 00'$	ADE	$68^{\circ} 00'$
DE	$40^{\circ} 00'$	$\frac{1}{2}$ ADE	$34^{\circ} 00'$
Sum,	$94^{\circ} 00'$	$\frac{1}{2}$ Sum,	$47^{\circ} 00'$
Diff.	$14^{\circ} 00'$	$\frac{1}{2}$ Diff.	$07^{\circ} 00'$

Co. Ar

As f. $\frac{1}{2}$ Z cr ¹ AD and DE	$47^{\circ} 00'$	Log.	0.13587
To f. $\frac{1}{2}$ 12 X cr ¹ .	$07^{\circ} 00'$		9.68589
So is tc. $\frac{1}{2}$ ADE	$34^{\circ} 00'$		10.17101
To t. $\frac{1}{2}$ X Ls A and E	$13^{\circ} 52'$		19.39277

Co. Ar

As fc. $\frac{1}{2}$ Z cr ¹ . AD and AE	$47^{\circ} 00'$	Log.	0.16622
To fc. $\frac{1}{2}$ X cr ¹ .	$07^{\circ} 00'$		9.99673
So is tc. $\frac{1}{2}$ ADE	$34^{\circ} 00'$		10.17101
To t. $\frac{1}{2}$ Z Ls A and E	$65^{\circ} 08'$		10.33398
$\frac{1}{2}$ Z Ls $65^{\circ} 08'$			
$\frac{1}{2}$ X Ls $13^{\circ} 52'$			
Sum,	$79^{\circ} 00'$	AED } The Angles of Position.	
Diff.	$51^{\circ} 16'$		
		DAE }	

Second.

Great Circle Sailing.

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Secondly, To find the Distance.
In the Triangle ADE.

	Co.	Ar.
As f. AED —————	79 00	Log. 0.00805
To f. AD —————	54 00	9.90796
So is S. ADE —————	68 00	9.96716
To f. AE —————	49 50	9.88317

The Distance is 49 deg. 50 min. which reduced into minutes makes 2990 minutes.

Thirdly, To find the Latitudes and Longitudes by which the Arch passes.

First, Find the greatest Latitude by which the Arch passes.

In the Right-angled Triangle ABD.

As Radius	_____	Log.	10.00000
To f. AD	_____ 54° 00'		9.90796
So is f. DAB	_____ 51 16		9.89213
To f. DB	_____ 39 07		9.80009

DB is 39 deg. 07 min. whose Compl. 50 deg. 53 min. is the greatest Latit.

Secondly, To find the Vertical Angles ADB, and BDE.

In the Right-angled Triangle ABD.

As tc. BAD —————	51° 16'	Log. 9.90423
To Radius —————		10.00000
So is fc. AD —————	54 00	9.76922
To tc. ADB —————	53 46	9.86499
From — ADE 68° 00'		
Subtract ADB 53 46		
Remains BDE 14 14		

Thirdly, To find the Latitudes by which the Arch passes at every five Degrees Longitude from A, you must resolve the several Right-angled Triangles BDa, BDb, BDc, &c.

Subtracting five deg. from ADB 43° 46'	
There remains ADb 48 46'	
Subtracting five deg. from 48 46	
Remains hDB 43 46	

So of the rest in the following Table.

BDa 48 46	BDb 13 46
BDb 43 46	BDi 08 46
BDc 38 46	BDk 03 46
BDd 33 46	BDl 01 14
BDe 28 46	BDm 06 14
BDf 23 46	BDn 11 14
BDg 18 46	

K

In

Great Circle Sailing.

In the Triangle aDB , to find by what Latitude
the Arch passes at the Point a .

As t. DB	$39^{\circ} 07'$	Log. 9.91018
To Radius		10.00000
So is sc. aDB	$48 \ 46$	9.81897
To tc. aD	$50 \ 59$	9.90879

Whose Compl. $39^{\circ} 01'$ is the Latitude at a .

After the same manner are found the Latitudes of several Points
 b, c, d, e , &c. as in the subsequent Table.

	Latitude.		Long.
A	36°	$00'$	$00'$
a	39	01	05
b	41	36	10
c	43	47	15
d	45	37	20
e	47	09	25
f	48	22	30
g	49	20	35
h	50	33	40
i	50	30	45
k	50	49	50
l	05	03	55
m	50	43	60
n	50	20	65
E	50	00	68

Fourthly, Having thus the Latitudes and
Longitudes of the Arch, you may find
the Courses and Distances from Place to
Place, according to *Mercator*.

So to find the Course and Distance

$A a$.

Both Latitudes are 36 deg. and 39
deg. 01 min.

The difference of Longitude 5 deg.

The proper difference of Latitude 181
min.

The Merid. difference of Latitude 228
min.

For the Course.

As Merid. differ. Latit. 228 min.	Log. 2.35793
To Radius	10.00000
So is the differ. of Longitude 300 min.	2.47712
To t. Course $52^{\circ} 45'$	10.11919

For the Distance.

As sc. Course $52^{\circ} 45'$	Log. 9.78197
To diff. Lat. 181	2.25768
So is Radius	10.00000
To the distance 299	2.47571

After

After the same manner you may find the Courses and Distances *a b* *b c*, *c d*, &c. as they follow in the Table.

Places.	Courses.	Distances.
		min.
From <i>A</i> to <i>a</i>	N E 52 45	299
From <i>a</i> to <i>b</i>	N E 55 54	176
From <i>b</i> to <i>c</i>	N E 59 10	255
From <i>c</i> to <i>d</i>	N E 62 40	239
From <i>d</i> to <i>e</i>	N E 66 05	226
From <i>e</i> to <i>f</i>	N E 70 01	212
From <i>f</i> to <i>g</i>	N E 73 39	202
From <i>g</i> to <i>h</i>	N E 77 35	199
From <i>h</i> to <i>i</i>	N E 81 05	193
From <i>i</i> to <i>k</i>	N E 85 14	192
From <i>k</i> to <i>l</i>	N E 89 02	177
From <i>l</i> to <i>m</i>	S E 87 19	192
From <i>m</i> to <i>n</i>	S E 83 09	193
From <i>n</i> to <i>D</i>	S E 80 13	117

CHAP. VIII.

The Doctrine of the Sphere: Containing sundry Astronomical Problems useful in the Art of Navigation.

SECT. I

Astronomical Definitions.

THE Poles of the World are two fixed Points in the Heavens diametrically opposite to one another, the one visible in our Hemisphere, called the North or *Arctic Pole*, noted with the Letter P.

Plate 2. Fig. 14.

The other not seen of us, being in the lower Hemisphere, called the South or *Antarctic Pole*, noted with S.

The *Axis of the World* is an imaginary Line drawn from Pole to Pole, about which the *Diurnal Motion* is performed from East to West.

The *Meridians* are great Circles concurring and intersecting one to another in the Poles of the World; as PES, and P c S.

The *Equinoctial*, or *Equator*; is a Great Circle 90 deg. distant from the Poles of the World; cutting the *Meridians* at Right-Angles, and dividing the World into two Parts, called the North and South Hemispheres; as E $\hat{=}$ Q.

The *Ecliptick* is a Great Circle, crossing the *Equinoctial* in the two opposite Points *Aries* and *Libra*, and making an Angle therewith (called its *Obliquity*) or 23 deg. 30 min. represented by $\odot \hat{=}$ w.

The Circle is divided into 12 Signs, each containing 30 deg. whose Names and Characters follow.

<i>Aries</i>	γ	Which are Northern Signs.	<i>Libra</i>	$\hat{=}$	These are Southern Signs.
<i>Taurus</i>	δ		<i>Scorpio</i>	m	
<i>Gemini</i>	II		<i>Sagittarius</i>	f	
<i>Cancer</i>	\odot		<i>Capricornus</i>	w	
<i>Leo</i>	U		<i>Aquarius</i>	$\hat{=}$	
<i>Virgo</i>	η		<i>Pisces</i>	x	

The *Zodiack* is a Zone or Girdle, having eight degrees of Latitude on either side of the *Ecliptick*, in which space the Planets make their Revolutions. 'Tis divided and distinguished by the twelve Signs.

The *Colures* are two *Meridians*, dividing the *Equinoctial* and the *Ecliptick* into four equal parts; one of these passes by the *Equinoctial* Points, *Aries* and *Libra*, and is called the *Equinoctial Colure*, as P $\hat{=}$ S.

The other by the beginning of *Cancer* and *Capricorn*, called the *Solstitial Colure*, P \odot , S w.

The Poles of the *Ecliptick* are two Points, 23° 30' distant from the Poles of the World, as I and K.

The *Tropicks* are two small Circles, parallel to the *Equinoctial*, and distant therefrom 23° 30', limiting the Sun's greatest Declination.

The *Northern Tropick* passes by the beginning of *Cancer*, and is called the *Tropick of Cancer*, as \odot a D.

The *Southern Tropick* passes by the beginning of *Capricorn*, and is called the *Tropick of Capricorn*; as A b w.

The *Polar Circle* are two small Circles parallel to the *Equinoctial*, and distant therefrom 66 deg. 30 min. and from the Poles of the World, 23 deg. 30 min.

That which is adjacent to the North Pole, is called the *Arctic Circle* as G d I.

And

And the other the *Antarctick Circle*, as K d M.

The *Zenith* and *Nadir* are two Points diametrically opposite.

The *Zenith* is the *Vertical Point*, or the Point right over our Heads, as Z.

The *Nadir* is directly opposite thereto, as N.

The *Azimuth* or *Vertical Circles*, are great Circles of the Sphere, concurring and intersecting each other in the *Zenith* and *Nadir*; as Z f N.

The *Horizon* is a great Circle 90 deg. distant from the *Zenith* and *Nadir*, cutting all *Azimuths* at Right-Angles, and dividing the World into two equal parts, the *Upper* and visible *Hemisphere*, and the *Lower* and invisible: This Circle is represented by H \perp R.

The *Meridian* of a Place, is that *Meridian* which passes by the *Zenith* and *Nadir* of the Place, as PZSN.

The *Almicanthers*, or *Parallels of Altitude*, are small Circles, parallel to the *Horizon*, imagined to pass through every Degree and Minute of the *Meridian*, between the *Zenith* and *Horizon*; as BaF.

Parallels of Latitude or *Declination*, are small Circles, parallel to the *Equinoctial*: They are called *Parallels of Declination*, in respect of the Sun or Stars in the Heavens; and *Parallels of Latitude*, in respect to any Place upon the Earth.

The *Latitude of a Place*, is the Height of the Pole above the *Horizon*, or the Distance between the *Zenith* and the *Equinoctial*.

The *Latitude of a Star*, is the Arch of a Circle contained between the Center of a Star, and the *Ecliptick* Line; this Circle making Right-Angles with the *Ecliptick*, and counted either Northward or Southward, according to the situation of the Star.

Longitude on the Earth is measured by an Arch of the *Equinoctial*, contained between the primary *Meridian* (or *Meridian* of that Place where Longitude is assigned to begin) and the *Meridian* of any other Place counted always Easterly.

The *Longitude* of a Star is that Part of the *Ecliptick* which is contained between the Star's Place in the *Ecliptick*, and the beginning of *Aries*, counting them according to the Succession of the Signs.

Altitude of the Sun or Stars, is the Arch of an *Azimuth* contained betwixt the Center of the Sun or Star, and the *Horizon*.

Ascension is the rising of any Star, or any part of the *Equinoctial* above the *Horizon*, and *Descension* is the setting thereof.

Right-Ascension is the Number of Degrees and Minutes of the *Equinoctial*, (counted from the beginning of *Aries*) which cometh to the *Meridian* with the Sun or Star, or with any portion of the *Ecliptick*.

Oblique Ascension is an Arch of the *Equinoctial* between the beginning of

of *Aries*, and that part of the *Equinoctial* that riseth with the Center of a Star, or with any portion of the *Ecliptick*, in an *Oblique Sphere*.

Oblique Descension is that part of the *Equinoctial*, which sets therewith.

Ascensional Difference is an Arch of the *Equinoctial*, being the Difference between the *Right* and *Oblique Ascension*.

The *Amplitude* of the Sun or Star, is the Distance of the rising or setting thereof, from the East or West Point of the *Horizon*.

The *Parallax* is the Difference between the true and apparent Place of the Sun or Star; so the true Place in respect of Altitude is in the Line ACE, or ADG, the Sun or Star being at C or D. *Plate 3. Fig. 15.*

And the apparent Place in the Line BCF, or BDH.

So the Angles of *Parallax* are ACB, or ECF; and ADB, or GDH.

In this Scheme, ABK represents a Quadrant on the Earth's Superficies.

A the Center of the Earth. B any Point of the Earth's Surface.

Refraction of the Stars, observed by Tycho.		
Alt.	Refract.	
0°	30	30"
1	21	30
2	15	30
3	12	30
4	11	00
5	10	00
6	9	00
7	8	15
8	6	45
9	6	00
10	5	30
11	5	00
12	4	30
13	4	00
14	3	30
15	3	00
16	2	30
17	2	00
18	1	15
19	0	30
20	0	00

The *Refraction* is caused by the *Atmosphere*, or Vapourous Thickness of the Air near the Earth's Superficies, whereby the Sun and Stars seem always to rise sooner, and set latter than really they do.

In the Latitude of 55 degrees, and thereabouts, it is allowed to be as follows in the Table, although it varies by the Weather.

And in the more Northren Parts it hath been observed to be greater.

The Use whereof is this;

Suppose the Altitude observed were 10 degrees; the Correspondent Refraction is 5 min. 30 seconds, which subtracted from 10 deg. the Remainder 9 deg. 54 min. 30 seconds, is the true Altitude.

S E C T.

SECT. II. Astronomical Problems.

PROBLEM I.

THE Sun's Place in the *Ecliptick*, and greatest Declination being given, to find his present Declination.

Example 1. The Sun's Place being in 36 degrees 41 minutes of *Taurus*, and his greatest Declination, or the Angle of the *Ecliptick* with the *Equinoctial*, 23 degrees 30 minutes; to find his present Declination.

Plate 3. Fig. 16.

In the Right-angle Spherical Triangle γBC , there is given γC the *Hypotenuse* 56 degrees 41 minutes, the Sun's distance from *Aries*, and the Angle $B \gamma C$, the greatest Declination (by the 9th Case) to find the opposite Leg, BC , the Sun's present Declination.

Therefore the Proportion and Operation is;

As Radius ————— Log. 10.00000

To $f. B \gamma C$ 23° 30', the Sun's greatest declinat. ————— 9.60070

So is $f. \gamma C$ 56 41, the Sun's distance from γ ————— 9.92202

To $f. BC$ — 19 28, the present Declination N ————— 19.52272

Note; That the Sun's distance is always accounted from the nearest of the *Equinoctial* Points *Aries* or *Libra*: Therefore if the Sun be in the Northern Signs, *Aries*, *Taurus*, or *Gemini*; or in the Southern Signs, *Capricornus*, *Aquarius*, or *Pisces*, his distance is computed from *Aries*.

But if his Place be in the Northern Signs, *Cancer*, *Leo*, or *Virgo*, or in the Southern Signs, *Libra*, *Scorpio*, or *Sagittarius*, 'tis reckoned from *Libra*.

If the Sun be in the Northern Signs, his Declination is *Northerly*; if the Southern Signs, *Southerly*.

Example 2. The Sun's Place is 22° 12' of *Aquarius*, his greatest Declination (as before) 23° 30'; to find his present Declination.

Plate 3. Fig. 16.

The Sun's Distance from *Aries*, is 37 deg. 48 min.

The Operation. In the Right-angled Triangle γDF .

As Radius ————— Log. 10.00000

To $f. D \gamma F$ 23° 30', the greatest Declination ————— 9.60070

So is $f. \gamma F$ — 37 48, the Distance from *Aries* ————— 9.78739

To $f. DF$ — 14. 08, the present Declination S ————— 19.38809

Your

The Doctrine of the Sphere.

You may find the Sun's Place by the Tables in *Astronomia Carolina*.
PROB. II. The Sun's Place given, to find his Right Ascension.

Note 3. The Sun's greatest Declination is concluded by Mr. *Street*, in his *Carolina Tables*, to be $23^{\circ} 30'$, therefore it is always given.

Example 1. The Sun's Place is $26^{\circ} 41'$ of *Taurus*;

To find the Right-Ascension.

Plate 3. Fig. 16.

In the Right-angled Triangle γBC , there is given the Hypotenuse γC $56^{\circ} 41'$ the Sun's Place from *Aries*.

The Angle $B \gamma C$, $23^{\circ} 30'$ the greatest Declination, (by the 6th Case) to find the adjacent Leg γB , the Right-Ascension.

The Operation.

As Radius	_____	Log.	10.00000
To t. γC $56^{\circ} 41'$ the Sun's Long. from γ	_____		10.18224
So is $\text{fc } B \gamma C$ $23^{\circ} 30'$, the greatest Declination,	_____		9.96240
To t. γB $54^{\circ} 22'$, the Right-Ascen. from γ	_____		10.14464

Example 2. The Sun's Place is $22^{\circ} 12'$ of *Aquarius*,

To find the Right-Ascension.

Plate 3. Fig. 16.

The Operation.

In the Right-angled Triangle γDF .

As Radius	_____	Log.	10.00000
To t. γF $37^{\circ} 48'$, the Sun's Long. from γ	_____		9.88928
So is $\text{fc } D \gamma F$ $23^{\circ} 30'$, the greatest Declination	_____		9.96231
To t. γD $35^{\circ} 25'$, the Right-Ascension from the	_____		
next Equinoctial Point			19.85199

This Proportion finds the Right-Ascension from the nearest Equinoctial Point, as you account the Longitude in the Operation. But the Right-Ascension is to be reckoned from *Aries*, according to the Succession of the Signs.

Therefore in this last *Example*, the Complement of $35^{\circ} 25'$ to 360 , which is $324^{\circ} 35'$, is the Right-Ascension sought.

P.R.O.B. III. The Sun's Declination given, to find his Place or Longitude from *Aries*.

Example 1. The Sun's Declination is $19^{\circ} 30'$ North encreasing.

To find his Place.

Plate 3. Fig. 16.

The Doctrine of the Sphere.

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In the Right-angled Triangle γ B C.

There is given the Leg BC 19 d. 30 m. the Sun's present Declination.
The opposite Angle B γ C. 23 deg. 30 min. the greatest Declination.
And the *Hypotenuse* γ C required (by the tenth Case) being the Sun's Distance from *Aries* or *Libra*.

The Operation.

As f. B γ C — 23° 30', the greatest Declination — Log. 9.60070
To Radius ————— 10.00000
So is f. B C 19 30, the present Declination ————— 9.52349
To f. γ C 56 50 ————— 9.92279
Which 56 50 reduced into Signs, is 1°. 36° 50',
or 26 50 of *Taurus*.

If the Sun's Declination be North, and encreasing, this Proportion finds the Sun's Distance from *Aries*; if decreasing, from *Libra*; in the Northern Signs.

If the Sun's Declination be South, and encreasing, from *Libra*; if decreasing, from *Aries*, among the Southern Signs.

Example 2. The Sun's Declination is 14° 10' South decreasing.

To find the Longitude from *Aries*.

Plate 3. Fig. 16.

The Operation. In the Triangle γ D F.

As f. D γ F 23° 30', the greatest Declination ————— 9.60070.
To Radius ————— 10.00000
So is f. D F 14 10, the present Declination ————— 9.38871
To f. γ F 37 52, the distance from *Aries* ————— 9.78801
The Compl. of 37 deg. 52 min. to 360 deg. is 322 deg. 08 min.
Which reduced into Signs, 10° 22° 8', or 22° 8' of *Aquarius*.

P R O B. IV. The Sun's Declination given, to find the Right-Ascension.

Example 1. The Sun's Declin. is 19 d. 30 m. North encreasing.

To find his Right-Ascension.

Plate 3. Fig. 16.

In the Right-angled Triangle γ B C,

There is given the Leg BC 19° 30', the Sun's present Declination.

And the opposite Angle B γ C 23° 30', the greatest Declination.

(by the 1st Case) to find the Leg γ B, the Right-Ascension.

As Radius ————— 10.00000
To tc. B γ C 23° 30', the greatest Declination ————— 10.36170
So is t. BC 19 30, the present Declination ————— 9.54915
To f. γ B — 54 32, the Right Ascension, from γ — 19.91085

The same Caution which was given for the right accounting the Sun's Place in the third Problem, serves for the Right-Ascension; only

as that was given in Signs, Degrees and Minutes, this must be given in Degrees and Minutes from *Aries*.

Example 2. The Sun's Declin. is 14d. 10m. South decreasing.

To find the Right-Ascension.

Plate 3. Fig. 16.

The Operation.

In the Right-angled Triangle γ DF.

As Radius ————— Log. 10.00000

To tc. D γ F ——— 23° 30', the Sun's greatest Declinat. ——— 10.36170

So is t. DF ——— 14. 10, the present Declination ——— 9.40212

To f. γ F ——— 35. 29, the Right-Ascension ——— 19.76382

The Complement of 35 deg. 29 min. to 360 deg. is 224. deg. 31 min.
the Right-Ascension from *Aries*.

P R O B. V. The Latitude of a Place, and the Sun's Declination being given, to find the Ascensional Difference.

Example. In the Latitude 51 deg. 32 min. the Sun's Declination being 20 deg. 12 min. to find the Ascensional Difference.

In the Right-angled Triangle abc.

Plate 3. Fig. 17.

There is given the Leg bc 20 deg. 12 min. the Sun's Declination and the opposite Angle bac 38 deg. 28 min. the Compl. of the Latitude, or the Angle between the Equinoctial and Horizon (by the first Case) to find the other Leg ab, the Ascensional Difference.

The Operation.

As Radius ————— Log. 10.00000

To tc. bac 38° 28' the Compl. of the Lat. ——— 10.09991

So is t. bc—20. 12, the Declination ——— 9.56576

To f. ab ——— 27. 35, the Ascensional Difference ——— 19.66567

P R O B. VI. To find the Oblique Ascension or Descension.

First, Find the *Ascensional Difference* by the fifth Problem, and the *Right-Ascension* by the fourth Problem.

Secondly, If the Sun's Declination be Northerly, the *Ascensional Difference* subtracted from the *Right Ascension* leaves the *Oblique Ascension*; and added to the *Right Ascension*, gives the *Oblique Descension*.

Thirdly, If the Sun's Declination be Southerly, the *Ascensional Difference* added to the *Right Ascension*, gives the *Oblique Ascension*; and subtracted therefrom, leaves the *Oblique Descension*.

Note;] If the *Right Ascension* be less than the *Ascensional Difference*, add 360 deg. to the *Right Ascension*; and then subtract it therefrom; or if the Sum of the *Right Ascension* and *Ascensional Difference*, exceeds

ceeds 360 deg. reject 360 deg. the Remainder is the *Oblique Ascension* or *Descension* required.

P R O B. VII. To find the Time of the *Sun's Rising* or *Setting*; and consequently the length of the Day or Night.

First, Find the *Ascensional Difference* by the fifth Problem, which reduced into hours and minutes of Time, by allowing for every 15 deg. one hour, and for every degree less than 15, 4 min. of Time, and for every 15 min. one minute of Time.

Secondly, If the *Sun's Declination* be Northerly, the *Ascensional Difference* added to six hours, gives the Time of *Sun-setting*.

And subtracted therefrom, leaves the Time of *Sun-rising*.

On the contray, If the *Sun's Declination* be Southerly, the *Ascensional Difference* add to six hours, gives the the time of *Sun-rising*, and subtracted therefrom, the Time of *Sun-setting*.

Thirdly, If you double the Time of *Sun-setting*, it gives you the Length of the Day: And the Time of *Sun-rise* doubled, the Length of the Night.

Example 1. In the Latitude 51 deg. 32 min. North, the *Sun's Declination* 20 deg. 12 min. North.

And the *Ascensional Difference* by the fifth Problem is 27 degrees 35 minutes, which reduced into Time, makes 1 hour 50 minutes.

	ho. min.
Therefore the Time of <i>Sun-setting</i> is	7 50

The Time of <i>Sun-rising</i>	4 10
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The Length of the Day	15 40
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The Length of the Night	8 20
-------------------------	------

Example 2. In the Latitude 51 deg. 32 min. the *Declination* 20 deg. 12 min. South.

And the *Ascensional Difference* is 27 deg. 35 min. which makes, (as before) 1 hour 50 minutes of Time.

The Time of <i>Sun-rising</i>	7 50
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The Time of <i>Sun-setting</i>	4 10
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The Length of the Day	8 20
-----------------------	------

The Length of the Night	15 40
-------------------------	-------

P R O B. VIII. The Latitude of a Place, and the *Sun's Declination* being given, to find the *Sun's Amplitude*.

Example. In the Latitude 51 deg. 32 min. the *Sun's Declination* being 20 deg. 12 min. to find the *Amplitude*.

In the Right-angled Triangle *abc*, there is given the Leg *bc* 20 deg. 12 min.

12 min. and the opposite Angle bac, 38 deg. 28 min. (by the tenth Case) to find the *Hypotenuse* ac, the *Amplitude*. Plate 3. Fig. 17.

The Operation.

As f. bac 38° 28' the Compl. of the Lat. ————— 9.79383
 To Radius ————— 10.00000
 So is f. bc 20 12, the Declination ————— 9.53819
 To f. ac 33 43, the *Amplitude* ————— 97.4436

If the Sun's Declination be Northerly, the *Amplitude* is to the Northward of the East or West; if the Declination be Southerly, to the Southward.

PROB. IX. The Latitude of a Place, and the Sun's Declination being given, to find what time the Sun shall be due East or West.

Example. In the Latitude 15 deg. 32 min. North. the Sun's Declination 20 deg. 12 min. North.

To find what time the Sun shall be due East or West:

In the Right-angled Triangle ade, there is given the Leg de 20 deg. 12 min. and the opposite Angle dae, 51 deg. 32 min. (by the first Case) to find the Leg ae, the Time from fix. Plate 3. Fig. 17.

The Operation.

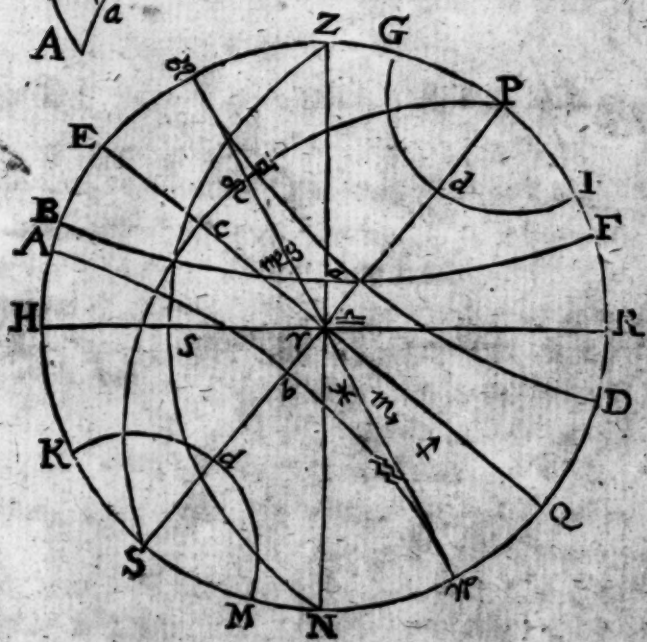
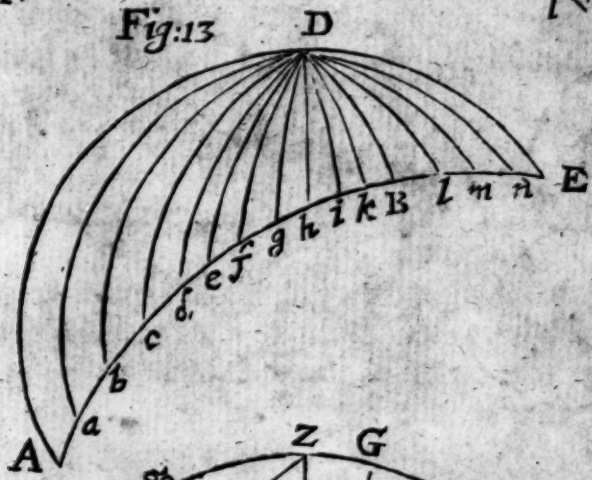
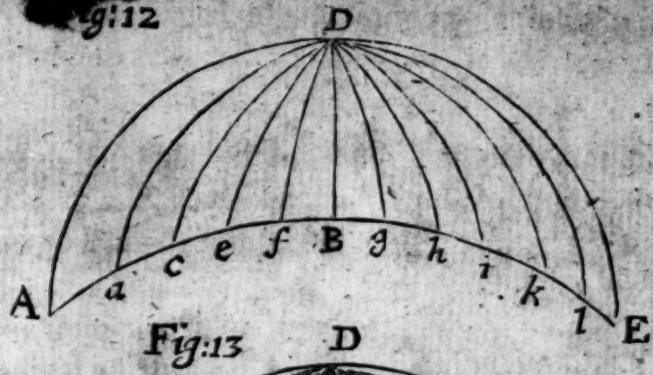
As Radius ————— Log. 10.00000
 To tc. dae 51° 32', the Latitude ————— 9.90009
 So is t. de 20 12, the Declination ————— 9.56576
 To f. ae —16 59, the distance from fix ————— 19.46585

Which being reduced into Time, makes one hour eight minutes *ferè*, which added to fix hours, gives 7 hours and 8 minutes, at which time the Sun comes to the East; and subtracted from fix hours, leaves four hours 52 minutes, the time of his being in the *West Azimuth*, or *Prime Vertical*.

PROB. X. The Latitude of the Place, and the Sun's Declination being given, to find the Sun's Latitude, being in the East or West *Azimuth*, or *Prime Vertical*.

Example. In the Latitude 51 deg. 32 min. North, the Declination 20 degrees 12 minutes North, to find the Sun's Altitude, being due East or West.

In the Right-angled Triangle ade, there is given the Leg de 20. 12, and the opposite Angle dae 51 deg. 32 min. (by the tenth Case) to find the *Hypotenuse* ad. Plate 3. Fig. 17.



The Operation.

As f. dae $51^{\circ} 32'$ the Latitude ————— 9.89374

To Radius ————— 10.00000

So is f. de 20 $12'$ the Declination ————— 9.53819

To f. ad 26 $10'$, the Alt. in the *Prime Vertical* ————— 9.64445

PROB. XI. The Latitude of a Place, and the Sun's Declination being given, to find the Sun's Altitude at Six of the Clock.

Example. In the Latitude 51° deg. $32'$ min. North, the Declination 23° deg. $30'$ min. North, to find the Sun's Altitude at fix.

In the Right-angled Triangle abc, there is given the *Hypotenuse* ac, 23° deg. $30'$ min. and the Angle bac, 51° deg. $32'$ min. (by the ninth Case) to find the opposite Leg. bc. Plate 3. Fig. 18.

The Operation.

As Radius ————— Log. 10.00000

To f. ac. $23^{\circ} 30'$ the Declination ————— 9.60070

So is f. bac $51^{\circ} 32'$, the Latitude ————— 9.89374

To f. bc $18^{\circ} 11'$, the Altitude at fix ————— 9.49444

PROB. XII. The Latitude of a Place, and the Sun's Declination, being given, to find the *Azimuth* at fix.

Example. In the Latitude 51° deg. $32'$ min. North, the Declination 23° deg. $30'$ min. North, to find the Sun's *Azimuth* at fix of the Clock.

In the Right-angled Triangle abc, there is given the *Hypotenuse*, ac, 23° deg. $30'$ min. and the Angle bac, 51° deg. $32'$ min. (by the sixth Case) to find the adjacent Leg. ab.

The Operation.

As Radius ————— Log. 10.00000

To t. ac $23^{\circ} 30'$ the Declination ————— 9.63830

So is f. bac $51^{\circ} 32'$, the Latitude ————— 9.79383

To t. ab $15^{\circ} 08'$, the *Azimuth* from the East ————— 9.43213

PROB. XIII. The Latitude of the Place, the Sun's Altitude and Declination being given, to find his *Azimuth*.

Example 1. In the Latitude 51° deg. $32'$ min. North, the Declination 23° deg. $30'$ min. North, the Altitude 49° deg. $40'$ min. To find the Sun's *Azimuth*.

In the Oblique angled Triangle DPZ, there is given the three Sides, ZP $38^{\circ} 28'$, the Compl. of the Latit. PD $66^{\circ} 30'$, the Compl. of the Declination, or the Sun's Distance from the elevated Pole, and DZ $40^{\circ} 26'$, the Compl. of the Altitude, (by the 11th Case) to find the Angle DZP, the Sun's *Azimuth* from the North. Plate 3. Fig. 18.

The

Operation.

The \angle ZD	40° 20'	Sine	_____	Co.	Ar.	0.18894
Legs \angle ZP	38 28	Sine	_____	Co.	Ar.	0.20614
The Base DP	66 30	Sum	72° 39'	Sine Log.	_____	9.97978
Sum	145 18	Rem.	06 00	Sine	_____	9.02992
$\frac{1}{2}$ Sum	72 39	_____	_____	Sum,	_____	19.40481
Rem.	06 09	fc.	59 44	_____	$\frac{1}{2}$ Sum,	9.60240
Which doubled,	_____	59 44	_____	produces	_____	_____
The Sun's Azimuth	119 28	_____	_____	from the North.	_____	_____

Example 2. In the Lat. $31^{\circ} 52'$ North, the Sun's Declin. is $15^{\circ} 16'$ South, and his Altitude $19^{\circ} 37'$; To find his Azimuth from the North.

Plate 4. Fig. 19.

Operation.

In the Triangle DPZ,						
There is given PZ $38^{\circ} 28'$						
DZ $70^{\circ} 23'$, DP $105^{\circ} 16'$, and DZP required.						
The \angle ZD	70° 23'	Sine	_____	Co.	Ar.	0.02597
Legs \angle ZP	38 28	Sine	_____	Co.	Ar.	2.20617
The Base DP	105 16	Sum	107° 03'	Sine Log.	_____	9.98048
Sum	214 07	Rem.	01 47	Sine	_____	8.49304
$\frac{1}{2}$ Sum	107 03	_____	_____	Sum	_____	18.70566
Rem	01 47	fc.	76 59	_____	$\frac{1}{2}$ Sum,	9.35283
Which doubled,	_____	76 59	_____	produces	_____	_____
The Sun's Azimuth	153 58	_____	_____	from the North.	_____	_____

Example 3. In the Lat. $51^{\circ} 32'$ South, the Sun's Declin. $23^{\circ} 30'$ South, and his Altitude $49^{\circ} 40'$; To find his Azimuth from the South.

In the Triangle DPZ, P must represent the South Pole; then there is given PZ 38 deg. 28 min. the Compl. of the Latit. DZ 40 d. 20 min. the Compl. of the Altitude; PD 66 deg. 30 min. the Compl. of the Declination, or the Sun's Distance from the elevated (or South) Pole; to find PZD, the Sun's Azimuth from the South. Plate 3. Fig. 18.

The Operation is the same with the first *Example*; only as the Azimuth there was accounted from the North, this finds it from the South part of the Horizon, which is 119 deg. 28 min.

Example 4. In the Lat. 51 deg. 32 min. South, the Sun's Declination is 15 deg. 16 min. North, and the Altitude 19. deg. 37 min. to find his Azimuth from the South. Plate 4. Fig. 19.

In the Triangle DPZ, P represents the South Pole, as in the former *Example*. Then

Then there is given PZ 38 deg. 28 min. DZ 70 deg. 23 min. PD 105 deg. 16 min. and DPZ required.

The Operation is the same with the second *Example*, only the *Azimuth* found is to be accounted from the South, which will be found 153 deg. 58 min.

PROB. XIV. The Latitude of the Place, the Sun's Declination and Altitude being given, to find the Hour of the Day.

Example 1. In the Latit. $51^{\circ} 32'$ North, the Sun's Declin. is $23^{\circ} 30'$ North, and his Altitude $49^{\circ} 40'$, to find the Hour from Noon.

In the Triangle DPZ, there is given PZ 38 deg. 28 min. DZ 40 deg. 20 min. DP 66 deg. 30 min. and DPZ the hour from Noon required.

Plate 3. Fig. 18.

The Operation.

The \angle DP	$66^{\circ} 30'$ Sine	Co. Ar. 0.03760
Legs \angle PZ	$38^{\circ} 28'$ Sine	Co. Ar. 0.20617
The Base DZ	$40^{\circ} 20'$ Sum $72^{\circ} 39'$	Sine Log. 9.97978
Sum	145 18 Rem. 32 13	Sine 9.72683
$\frac{1}{2}$ Sum	72 39	Sum 19.95038
Rem.	32 13 Sc. 19 11	$\frac{1}{2}$ Sum 9.97519

The Double of 19 deg. 11 min. is 38 deg. 22 min. which being reduced into Time, gives 2 hours 33 min. from Noon; so that the hour of the day is either 2 hours 33 min. Afternoon, or 9 hours 27 min. before Noon.

Example 2. In the Latit. $51^{\circ} 32'$ North, the Sun's Declin. $15^{\circ} 16'$ South, and his Altit. $19^{\circ} 37'$, to find the Hour P. M. or Afternoon.

In the Triangle PDZ, there is given the three Sides PZ $38^{\circ} 28'$, DZ $70^{\circ} 23'$, PD $105^{\circ} 16'$, and DPZ required.

Plate 4. Fig. 19.

The Operation.

The \angle PD	$105^{\circ} 16'$ Sine	Co. Ar. 0.01560
Legs \angle PZ	$38^{\circ} 28'$ Sine	Co. Ar. 0.20167
The Base DZ	$70^{\circ} 23'$ Sum $107^{\circ} 03'$	Log. 9.98048
Sum	214 07 Rem. 36 40	9.77609
$\frac{1}{2}$ Sum	107 03	19.97834
Rem.	36 40 Sc. 12 44	9.98917

Which doubled, produces 25 deg. 28 min. and that reduced into Time, makes 1 hour 42 min. *ferè*.

PROB. XV. The Latitude of a Place, the Sun's Declination, and the Hour of the Day given, to find the Sun's Altitude.

Example.

Example. In the Lat. 51 deg. 32 min. North, the Sun's Declination is 23 deg. 30 min. North; the Hour, 1 hour 53 min. Afternoon.

To find the Sun's Altitude.

1 Hour 53 Minutes reduced, makes 28 degrees 15 minutes.

In the Triangle DPZ, there is given the two Sides, PZ 38 deg. 28 min. DP 66 deg. 30 min. and the contained Angle DPZ 28 deg. 15 min. and the third Side DZ required.

Plate 3. Fig. 18.

The Operation.

As Radius	_____	Log.	10.00000
To sc. DPZ	28° 15' the contained Angle	_____	9.94492
So is t. PZ	38 28 the lesser Side	_____	9.90009
To t. _____	34 59 a fourth Arch	_____	19.84501
	From the other Side PD	_____	66° 30'
	Subtract the fourth Arch	_____	34 59
	The Remainder is the Residual Arch 31 31		

			Ca. Ar.
As sc. _____	34 59 the fourth Arch	_____	0.08655
To sc. _____	31 31 the Residual Arch	_____	9.93069
So is sc. PZ	38 28 the lesser Side	_____	9.89374
To sc. DZ	35 27 the side sought	_____	19.91098
Whose Compl. 54 degrees 33 minutes is the Altitude required.			

P.R.O.B. XVI. The Latitude of a Place, the Sun's Declination, and the hour given, to find the Sun's Azimuth.

Example. In the Latitude 51 degrees 32 min. North, the Sun's Declination is 15 degrees 16 minutes South, and the hour, 10 hours 18 Minutes in the Morning; to find the Sun's Azimuth.

The Time from Noon is 1 hour, 42 minutes.

Which reduced, is 25 degrees 30 minutes

In the Triangle DPZ, there is given the two Sides PZ 38 degrees 28 minutes, PD 105 degrees 16 minutes, and the contained Angle DPZ 25 degrees 30 minutes; to find one of the opposite Angles, viz. PZD.

Plate 4, Fig. 19.

The Operation.

PD	105	16		
PZ	38	28		
Sum	143	44	Sum	71° 32'
Diff	66	48	Diff.	33 24
			DPZ	25° 30'
			the half	12 45

Ca. Ar.

As $f \frac{1}{2}$ Z cr' DP and PZ	71	52	Co. Ar.
To $f \frac{1}{2}$ X cr'	33	24	0.02212
So is tc. $\frac{1}{2}$ DPZ	12	45	9.74074
To t. $\frac{1}{2}$ X Ls PDZ and PZD	68	39	10.64536

Co. Ar.

As $fc. \frac{1}{2}$ Z cr' DP and PZ	71	52	0.50692
To $fc. \frac{1}{2}$ X cr'	33	24	9.92161
So is tc. $\frac{1}{2}$ DZP	12	45	0.64536
To t. $\frac{1}{2}$ Z Ls PDZ and PZD	85	10	11.07389

$\frac{1}{2}$ Z Ls 85° 10'
 $\frac{1}{2}$ X Ls 68 39

Sum 153 40 DZP required.

Which is the Sun's *Azimuth* from the North.

PROB. XVII. The Latitude of a Place, the Sun's *Altitude*, and *Azimuth* given to find the Hour.

Example. In the Latitude 51 degrees 32 minutes, the Sun's *Altitude* 49 degrees 40 minutes, his *Azimuth* 119 degrees 44 minutes from the North; to find the Hour Afternoon.

In the Triangle DPZ, there is given the two Sides DZ 40 deg. 20 min. PZ 38 deg. 28 min. and the contained Angle DZP, 219 deg. 44 min. and the opposite Angle DPZ required. *Plate 3. Fig. 18.*

The Operation.

DZ 40 20
PZ 38 28

Sum 78 48½ Sum 39° 24½ DZP 119° 44'

Diff. 01 52½ Diff. 00 56 the half 59 52 Co. Ar.

As $f \frac{1}{2}$ Z cr' DZ and PZ	39° 24'	0.19741
To $f \frac{1}{2}$ X cr'	00 56	8.21189
So is tc. DZP	59 52	9.76377
To t. $\frac{1}{2}$ X Ls PDZ and DPZ	00 51	18.97307

Co. Ar.

As $fc. \frac{1}{2}$ Z cr' DZ and PZ	39	24	0.11197
To $fc. \frac{1}{2}$ X cr'	00	56	9.99994
So is tc. DZP	59	52	9.76377
To t. $\frac{1}{2}$ Z Ls PDZ and DPZ	36	54	19.87568

$\frac{1}{2}$ Z Ls 36° 54'
 $\frac{1}{2}$ X Ls 00 51

Sum 37 45 DPZ required.

M

Note.

Note; DPZ is the greater Angle, because opposite to the greater Side DZ; 37 deg. 45 min. reduced, makes the Time 2 hours 31 min. Afternoon.

PROB. XVIII. The Latitude and Longitude of a fixed Star being given, to find the *Right Ascension* and *Declination*.

Example. The Longitude of *Castor* is 15 deg. 33 min. of *Cancer*, and his Latitude 10 deg. 02 min. North, to find his *Right Ascension* and *Declination*.

In the Oblique Triangle DIP, there is given two Sides, IP 23 deg. 30 min. the distance between the Pole of the *Equinoctial*, and the Pole of the *Ecliptick*; ID 79 deg. 58 min. the Complement of the Latitude; and the contained Angle DIP 15 deg. 33 min. the Longitude from *Cancer*: To find one of the opposite Angles DPI, the Complement to 180 deg. of the *Right Ascension* from *Cancer*; and the third Side DP, the Complement of *Declination*.

The Operation. For the *Right Ascension*.

ID	79° 58'				
IP	23 30				
Sum	103 28	Sum	5 14		
Diff	56 28	Rem	28 14		
As f. $\frac{1}{2}$ Z cr. ID and IP	51 44				
To f. $\frac{1}{2}$ X cr.	26 14				9.64548
So is tc. $\frac{1}{2}$ DIP	07 46				9.686521
To t. $\frac{1}{2}$ X Ls DPI and IDP	76 22				10.61571
As fc. $\frac{1}{2}$ Z cr. ID and IP	51 44				Co. Ar. 10.20808
To fc. $\frac{1}{2}$ X cr.	26 14				9.95279
So is tc. $\frac{1}{2}$ DIP	07 46				X 10.86521
To t. $\frac{1}{2}$ Z Ls DPI and IDP	84 37				11.02608
$\frac{1}{2}$ Z Ls 84° 37'					
$\frac{1}{2}$ X Ls 79 22					
Sum	160 59	DPI			

Whose Complement to 180 degrees is 19 degrees 1 minute, the *Right Ascension* from *Cancer*; the *Right Ascension* of *Cancer* is 90 degrees; and therefore the *Right Ascension* from *Aries* is 19 degrees 1 minute.

Fig: 16

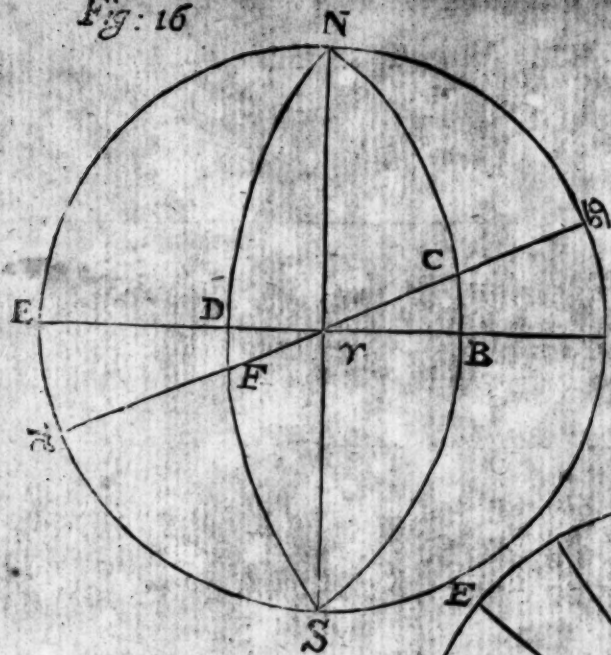


Fig: 15

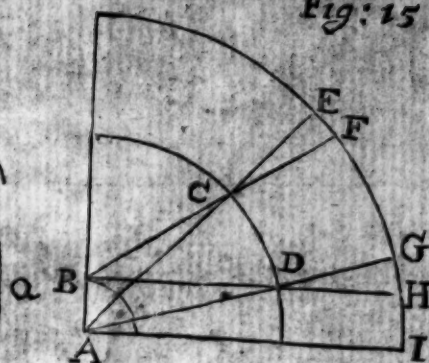


Fig: 17

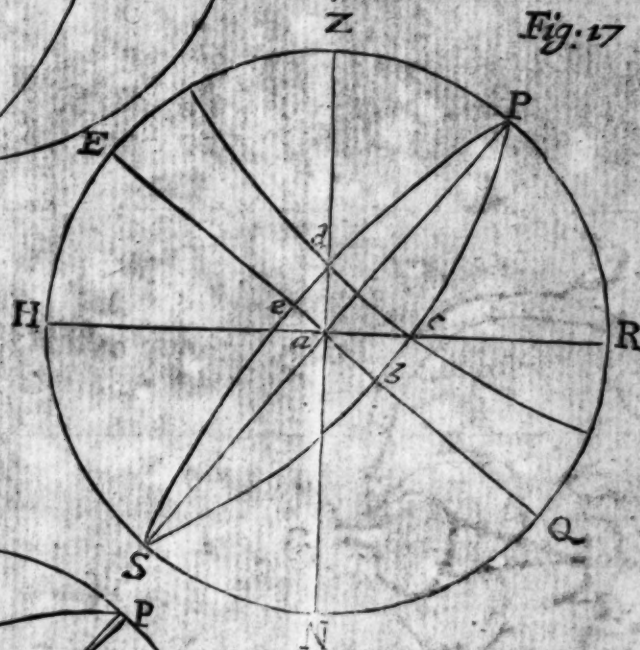
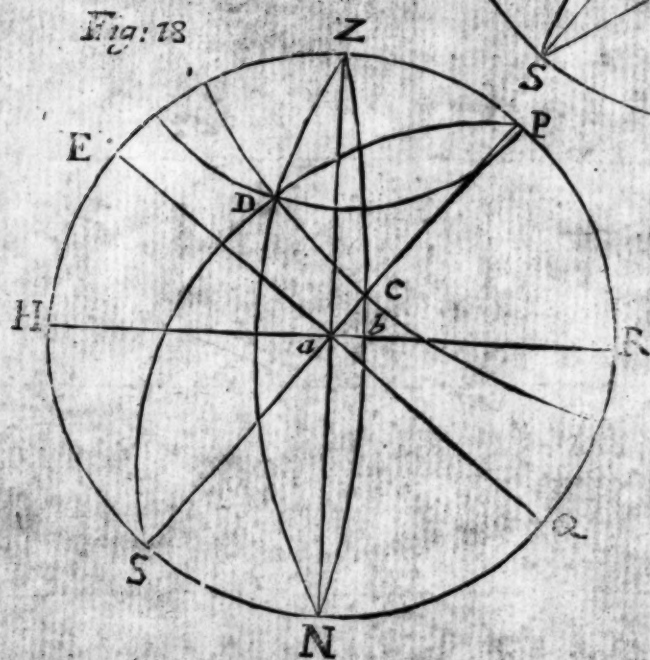


Fig: 18



The Doctrine of the Sphere.

83

For the Declination.

As f. DPI	160	59	the Compl. of the Right-Ascension	0.48700
To f. DI	79	58	the Complement of the Latitude	9.99331
So is f. DIP	15	33	the Longitude from Cancer	9.2826
To f. DP	54	6	the Complement of the Declination	9.90857
Whose Compl. 35° 54'			is the Declination Northernly	

PROB. XIX. The Right-Ascension and Declination of a fixed Star being given, to find the Longitude and Latitude thereof.

Example. The Right-Ascension of *Castor* is 18° 15', and his Declination 32° 32' North; to find his Longitude and Latitude.

In the Triangle IDP, there is given the two Sides, IP 23° 30'; PD 57° 28', and the contained Angle DPI 161° 45', to find the opposite Angle DIP, and the third Side DI.

Fig. 20.

The Operation. To find the Longitude.

PD	57	28		
IP	23	30		
Sum	80	58	Sum 40° 29'	DPI 161° 45'
Diff.	33	58	Diff. 16° 59'	DECLIN 32° 32'

As f. $\frac{1}{2}$ Z cr. PD and IP	40	29		Co. Ar. 0.18760
To f. $\frac{1}{2}$ X cr.	16	59		9.46552
So is tc. $\frac{1}{2}$ DPI	80	52		9.28621
To t. $\frac{1}{2}$ X Ls DIP and IPD	04	08		28.85933

As f. $\frac{1}{2}$ Z cr. PD and IP	40	29		Co. Ar. 0.11885
To f. $\frac{1}{2}$ X cr.	16	59		9.98063
So is tc. $\frac{1}{2}$ DPI	80	52		9.26621
To t. $\frac{1}{2}$ Z Ls DIP and IDP	11	25		29.30569

$\frac{1}{2}$ Z Ls 11° 25'

$\frac{1}{2}$ X Ls 04° 08'

Sum 15 33 DIP the Longitude from Cancer.

To find the Latitude.

As DIP	15	33	the Longitude from Cancer	0.57174
To f. DP	57	28	the Complement of Declination	9.92587
So is f. DPI	161	45	the Compl. of the Right-Ascension	9.49577
To f. DI	80	01	the Complement of Latitude	9.99238

M 2

PROB.

PROB. XX. The distance of a Planet, Comet, or New-Star, from two known fixed Stars being given, to find the unknown Star's Longitude and Latitude.

Example: The unknown Star's distance from the Swan's Beak is 49 degrees 05 minutes, and from Perseus's Side 88 degrees 57 minutes, to find the Longitude and Latitude thereof.

Long. $\left. \begin{array}{l} \text{Of the Swan's Beak, } 26^{\circ} 39' \\ \text{Of Perseus's Side, } 82^{\circ} 12' \end{array} \right\} \text{Lat. } \left\{ \begin{array}{l} 49^{\circ} 02' \text{ N.} \\ 40^{\circ} 05' \text{ N.} \end{array} \right.$

1. In the Triangle ADI there is given two Sides, AI 40 deg. 58 min. the Compl. Lat. of the Swan's Beak, DI 59 deg. 55 min. the Compl. Lat. of Perseus's Side, the contained Angle AID 120 deg. 33 min. the difference of Longitude between the two Stars, and the Angle DAI, and the Side AD required.

Plate 4. Fig. 21.

The Operation.

			Co. Ar.
As f. $\frac{1}{2}$ Z cr. AI and DI	50	26	0.11301
To f. $\frac{1}{2}$ X cr.	09	28	9.21610
So is tc. $\frac{1}{2}$ L AID	60	16	9.75676
To t. $\frac{1}{2}$ X Ls DAI and ADI	06	56	19.08587
			Co. Ar.
As f. $\frac{1}{2}$ Z cr. AI and DI	50	26	0.19588
To f. $\frac{1}{2}$ X cr.	09	28	9.99404
So is tc. $\frac{1}{2}$ AID	60	16	9.75676
To t. $\frac{1}{2}$ Z Ls DAI and ADI	41	29	19.94668
The Angle DAI is 48	25		
			Co. Ar.
As f. DAI	48	25	0.12610
To f. DI	59	55	9.93716
So is AID	120	33	9.93510
To f. AD	85	02	19.99636

2. In the Triangle ADB there is given three Sides, AD 85 deg. 02 min. the distance between two known Stars, AB 46 deg. 05 min. the unknown Stars distance from the Swan's Beak, BD 88 deg. 57 min. the distance from Perseus's Side, and the Angle DAB required.

Plate 4. Fig. 21.

The Operation.

AD	85	02	Sine	Co. Ar.	0.00163
AB	49	05	Sine	Co. Ar.	0.12167
AD	-88	57	$\frac{1}{2}$ Sum	111° 32'	Sine 9.96858
Sum	223	04	Rem.	22 35	Sine 9.58436
$\frac{1}{2}$ Sum	-111	32			Sum 19.67624
Rem.	22	35	Sc.	-46 28 $\frac{1}{2}$	Sum 9.83812

Which being doubled, makes $92^{\circ} 56'$, the Angle DAB required.

Which being added to the Angle DAI, the Sum is the Angle BAI
141 deg. 21 min.

3. In the Triangle ABI there is given the two Sides, AI 40 deg. 58 min. AB 49 deg. 05 min. the contained Angle BAI, 141 deg. 21 min. and the Angle AIB, the difference of Longitude between the unknown Star and the *Swan's Beak*, and the Side BI, the Compl. of the unknown Star's Latitude required.

Plate 4. Fig. 21.

The Operation.

As f. $\frac{1}{2}$ Z cr. AI and AB	45	01	Co. Ar.	0.15039
To f. $\frac{1}{2}$ X cr.	04	02		8.84897
So is tc. $\frac{1}{2}$ BAI	70	40		9.54512
To t. $\frac{1}{2}$ X \angle s ABI and AIB	02	00		18.54448

Co. Ar.

As fc. $\frac{1}{2}$ Z cr. AI and AB	45	01	Co. Ar.	0.15064
To fc. $\frac{1}{2}$ X cr.	04	03		9.99891
So is tc. $\frac{1}{2}$ BAI	70	40		9.54512
To t. $\frac{1}{2}$ Z \angle s ABI and AIB	52	20		19.69467

The Angle AIB is 28 deg. 20 min. which added to the Longitude of the *Swan's Beak* \approx 26 deg. 39 min. makes the unknown Stars Longitude to be \approx 24 deg. 59 min.

Co. Ar.

As f. AIB	28° 20'	Co. Ar.	0.32367
To f. AB	49 05		9.87833
So is f. BAI	141 21		9.79557
To f. BI	38 57		19.99757

Whose Compl. to 90 deg. that is 6 deg. 03 min. is the unknown Stars Latitude Northerly.

P R O B. XXI. The *Meridian Altitude* of an unknown Star or Planet, and the Distance from a known fixed Star being given; to find the unknown Star's Latitude and Longitude.

Example

Example. In the Latitude 51 deg. 32 min. North, the Meridian Altitude of an unknown Star is 30 deg. 36 min. and his Distance from the Star in *Cepheus's* Girdle is 84 deg. 32 min. to find his Longit. and Latit.

The Meridian Altitude of the Star being given, his Declination is also given.

For the Meridian Altitude subtracted from the Complement of the Latitude 38 deg. 28 min. there remains 7 deg. 52 min. the Declination South.

First, Therefore in the Triangle AOP, there is given the three Sides, OP 20 deg. 52 min. the unknown Star's Distance from the North Pole, AP 97 deg. 52 min. the known Star's Distance therefrom, AO 84 deg. 32 min. the Distance between the two Stars, and the Angle APO required, being the Difference of Right-Ascension between the two Stars. Plate 5. Fig. 22.

The Operation.

OP	20° 52'	Sine	_____	-Co. Ar.	0.44831
AP	97 52	Sine	_____	-Co. Ar.	0.00411
$\frac{1}{2}$ Sum	101 38	Sine	_____		-9.99098
Rem.	97 06		_____		-9.46841
				Sum	19.91181
Sc.	25 23		_____		Sum 9.95590

Which doubled is 50 deg. 46 min. the Angled APO.

The Right-Ascension of *Cepheus's* Girdle is 321 deg. 02 min. to which adding 50 deg. 46 min. (the unknown Star being to the Eastward of the known Star) produceth the Right-Ascension of the unknown Star 11 deg. 48 min.

Secondly, Then having the unknown Star's Right-Ascension and Declination, you may find his Longitude and Latitude by *Problem 19*.

PROB. XXII. Having the Latit. of the Place, the Sun's Right-Ascension, and the Alt. of a known fixed Star; to find the Hour of the Night.

Example. In the Latitude 51 deg. 32 min. the Sun's Right Ascension being 228 deg. 45 min. and the Altitude of *Aldebaran* 38 deg. 58 min. to the Eastward of the Meridian; to find the hour of the Night.

The Right-Ascension of *Aldebaran* is 64 deg. 10 min. and his Declination 15 deg. 46 min.

In the Triangle APZ, there is given the three Sides PZ 38 deg. 28 min. the Compl. of the Latitude; AZ 51 deg. 02 min. the Compl. of the Star's Altitude; AP 74 deg. 14 min. the Complement of his Declination; to find the Angle APZ, the difference of Right-Ascension between the *Medium Cæli* and *Aldebaran*. Plate 5. Fig. 23.

The

The Operation.

AP	Sine	74° 14'	_____	Co. Ar.	0.01666
PZ	Sine	38 28	_____	Co. Ar.	0.20617
Sum	Sine	81 52	_____		9.99561
Rem.	Sine	30 50	_____		9.70973
				Sum,	19.92817
Sc.		22 59	_____		9.96408

Which doubled, produces 45 deg. 58 min.

This subtracted from the Right Ascension of *Aldebaran*; leaves 18 degrees 12 minutes, the Right Ascension of the *Mid-Heaven*. Add 360 deg. to 18 deg. 12 min. and from the Sum subtract the Sun's Right Ascension 228 deg. 45 min. the Remainder 149 deg. 27 min. reduced into time, makes 9 hours 57 minutes, 48 seconds, the hour of the Night sought.

P R O B. XXIII. Two unequal Altitudes of the Sun taken in one day, with the Time between the Observations, and the Sun's *Declination* being given; to find the Latitude of the Place of Observation.

Example. The Two Altitudes are 43 degrees 06 minutes, and 56 degrees 34 minutes, the Time between the Observations is 2 hours, and the Sun's *Declination* 20 degrees 14 minutes North; to find the Latitude of the Place Northerly.

In the Right-angled Triangle ABP, there is given the *Hypotenuse* AP 69 degrees, 46 minutes, the Complement of the *Declination*, the Angle APB 15 degrees, half the Time between the Observations, and the opposite Leg AB required.

Plate 5. Fig. 24.

The Operation.

As Radius	_____	10.00000
To f. APB 15° 00'	_____	9.41300
So is f. AP 69 46	_____	9.97734
To f. AB 14 03	_____	19.38934

Which being doubled, gives AE 28 degrees 06 minutes.

Secondly, In the Oblique-angled Triangle APE, there is given the two Sides AE 28 degrees 06 minutes, EP 69 degrees 46 minutes, the opposite Angle APE 30 degrees 00 minutes, and the other opposite Angle EAP required.

Plate 5. Fig. 24.

The Operation.

As f. AE	28° 06'	_____	Co. Ar.	0.32697
To f. APE	30 00	_____		9.69897
So is f. EP	69 46	_____		9.97234
To f. EAP	84 54	_____		9.99828

Thirdly,

Thirdly, In the Oblique-angled Triangle AZE, there is given the three Sides, AZ 33 deg. 26 min. the Complement of the greater Altitude, EZ 46 degrees 54 minutes, the Complement of the lesser AE 28 degrees 06 minutes, and the Angle EAZ required.

Plate 5. Fig. 24.

The Operation.

AZ	Sine	33 ^d 26'	_____	Co. Ar.	0.25888
AE	Sine	28 06	_____	Co. Ar.	0.32697
	Sine Sum,	54 13	_____	Log.	9.90915
	Rem. Sine	07 19	_____		9.10501
				Sum,	19.60001
				± Sum,	9.80000

Sc. 50 52

Which doubled, produces EAZ 101 deg. 44 min. from which subtracting EAP 84 deg. 54 min. there remains PAZ 16 deg. 50 min.

Fourthly, In the Oblique-angled Triangle APZ, there is given the two Sides AP 69 deg. 46 min. AZ 33 deg. 26 min. the contained Angle PAZ 16 deg. 50 min. and the third Side PZ required.

Plate 5. Fig. 24.

The Operation.

As Radius	_____	_____	10.00000
To sc. PAZ	16 ^d 15'	_____	9.98098
So is t. AZ	33 26	_____	9.81968
To t. of a 4th Arch	32 17	_____	19.80066
			Co. Ar.
As sc. of the 4th Arch	32 ^d 17'	_____	0.07293
To sc. of the Residual	37 29	_____	9.89956
So is sc. AZ	33 26	_____	9.92144
To sc. PZ	38 26	_____	19.99393
Whose Compl.	51 34	is the Latit. Northerly.	

PROB. XXIV. Two unequal Altitudes of the Sun, and the Difference of their Correspondent Azimuths taken in one Day, and the Sun's Declination being given; to find the Latitude of the Place of Observation.

Example. The first Altitude is 43 deg. 6 min. and the second Altitude 56 deg. 34 min. the Difference of Azimuths 39 degrees 16 minutes, and the Sun's Declination is 20 degrees 14 minutes North; to find the Latitude of the Place Northerly.

First. In the Oblique-angled Triangle AEZ, there is given the two Sides AZ 33 degrees 26 minutes, EZ 46 degrees 54 minutes, the contained

tained Angle AZE 39 degree 16 minutes, the difference of the Azimuths; and the Angle EAZ, and the third Side AE required.

Plate 5. Fig. 24.

The Operation.

As f. $\frac{1}{2}$ Z cr ^a AZ and EZ	400	101	0.19043
To f. $\frac{1}{2}$ X cr ^a	06	44	9.05911
So is tc. $\frac{1}{2}$ AZE	19	38	10.44765
To t. $\frac{1}{2}$ X Ls EAZ and AEZ	27	00	19.70719

Co. Ar.

As f. $\frac{1}{2}$ Z cr ^a AZ and EZ	400	101	0.11681
To f. $\frac{1}{2}$ X cr ^a	06	44	9.99699
So is tc. $\frac{1}{2}$ AZE	19	38	10.44765
To t. $\frac{1}{2}$ Z Ls EAZ and AEZ	74	39	10.56145

The Angle EAZ is 101. 39.

Co. Ar.

As f. EAZ	101	39	0.00904
To f. EZ	46	54	9.86342
So is AZE	39	16	9.80136
To f. AE	28	09	19.67382

Secondly ; In the Right-angled Triangle ABP, there is given the Hypotenuse AP 69 deg. 46 min. the Leg. AB 14 deg. 04 min, the half of AE, and the adjacent Angle BAP required.

Plate 5. Fig. 24.

The Operation.

As Radius			10.00000
To tc. AP 69° 46'			9.566654
So is t. AB 14 04			9.39892
To fc. BAP 84 42			18.96546

From the Angle EAZ 101 deg. 39 min. subtract the Angle EAP 84 deg. 42 min. there remains the Angle PAZ, 16 deg 57 min.

Thirdly, In the Oblique-angled Triangle PAZ, there is given the two Sides AP 69° 46', AZ 33° 26', the contained Angle PAZ 16° 57', and the third Side PZ required.

Plate 5. Fig. 24.

The Operation.

As Radius			Log. 10.00000
To fc. PAZ	16° 57'		9.98071
So is t. AZ	33 26		9.81968
To t. of a fourth Arch	32 16		19.80039

N

Co. Ar.

			Co.	Ar.
As sc. of the fourth Arch	32	16		0.07285
To sc. of the Residual	37	30		9.89947
So is sc. AZ	33	26		9.92144
To sc. PZ	38	28		19.89376
Whose Compl.	51	32	is the Latitude North.	

SECT. III. Containing the general Astronomical Theories.

The Ptolomaick System.

THE Ptolomaick System is that which was by Ptolomy invented, and supposeth the Earth to be fixed as the Centre of the World, and that all the Celestial Bodies move round the same in their Diurnal and Annual Revolutions.

The World is supposed to be divided principally into two parts, Elementary and Celestial.

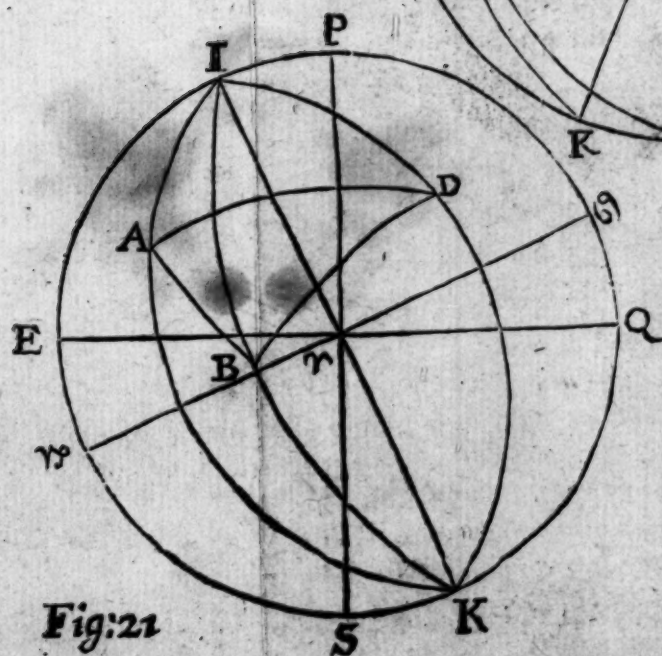
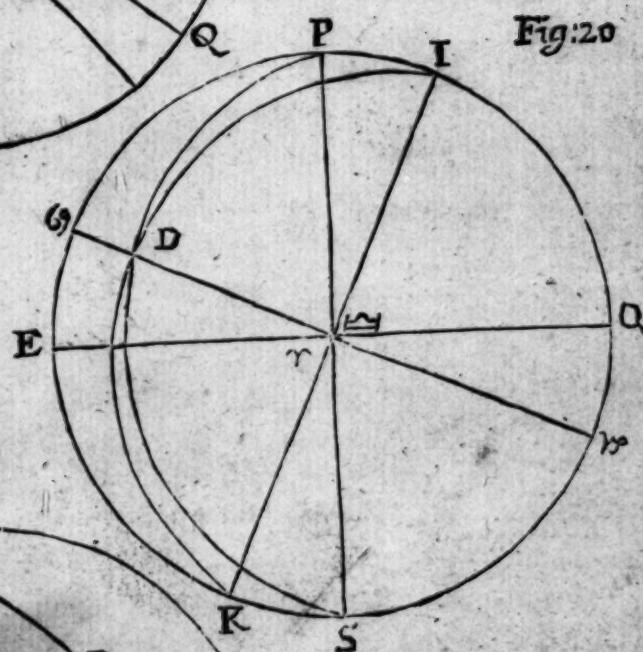
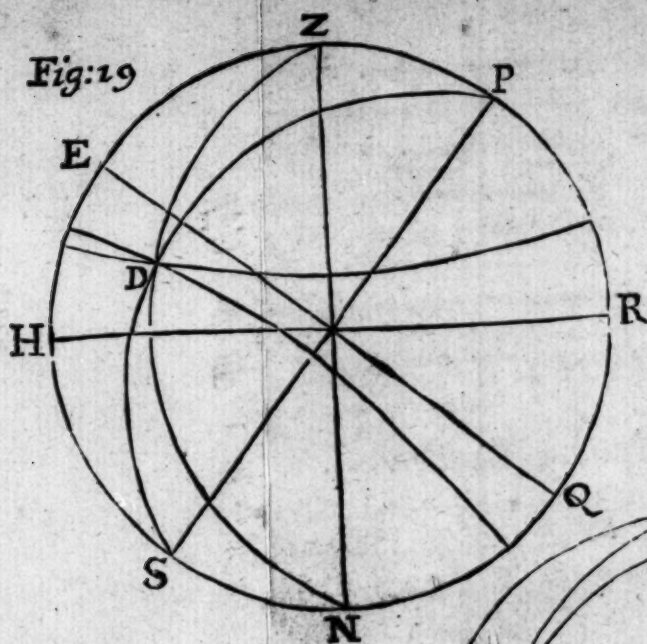
The Elementary admits of four Divisions.

The first is the *Earth*.

The second is the *Water*; both which make one entire Body or Globe whereon we dwell.

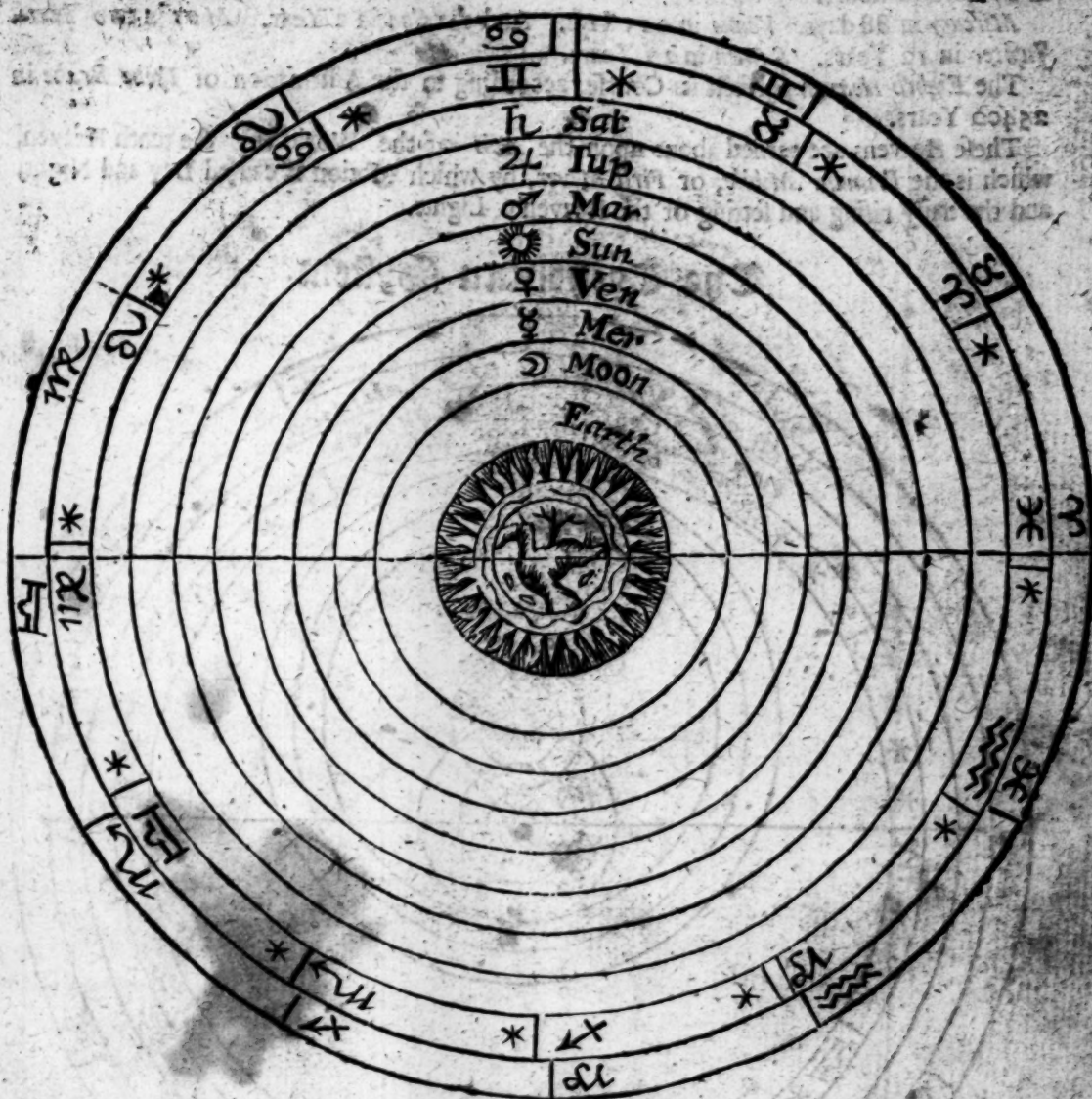
The Third is the *Air*, encompassing the *Earth*.

And the fourth is *Fire*, which according to the Opinion of antient Philosophers, is contained in that space between the *Air* and the Sphere of the Moon; as you may see in the following Figure.



The Planetary Systems.

The Figure of the Ptolomaick System.



10

These four Elements are subject to a continual Change and Alteration one into another, according to the Proverb, *Omnia Sublunaria mutabilia*.

The Cœlestial Part is that which is without these Elementary Parts, void of all Changes, and is by the Ancient Astronomers divided into ten Parts, or Heavens.

The first of which, next to the Region of Fire, is the Heaven, or Orb of the Moon.

The second of Mercury. The third of Venus. The fourth of the Sun. The fifth of Mars. The sixth of Jupiter. The seventh of Saturn. The eighth of the Fixed Stars. The ninth is called the *Crystalline Heaven*. The tenth the *Primum Mobile*.

The Planetary Systems.

The Magnitude of these Heavens is known by the Courses which those great Bodies within them make round the Poles of the *Zodiack*.

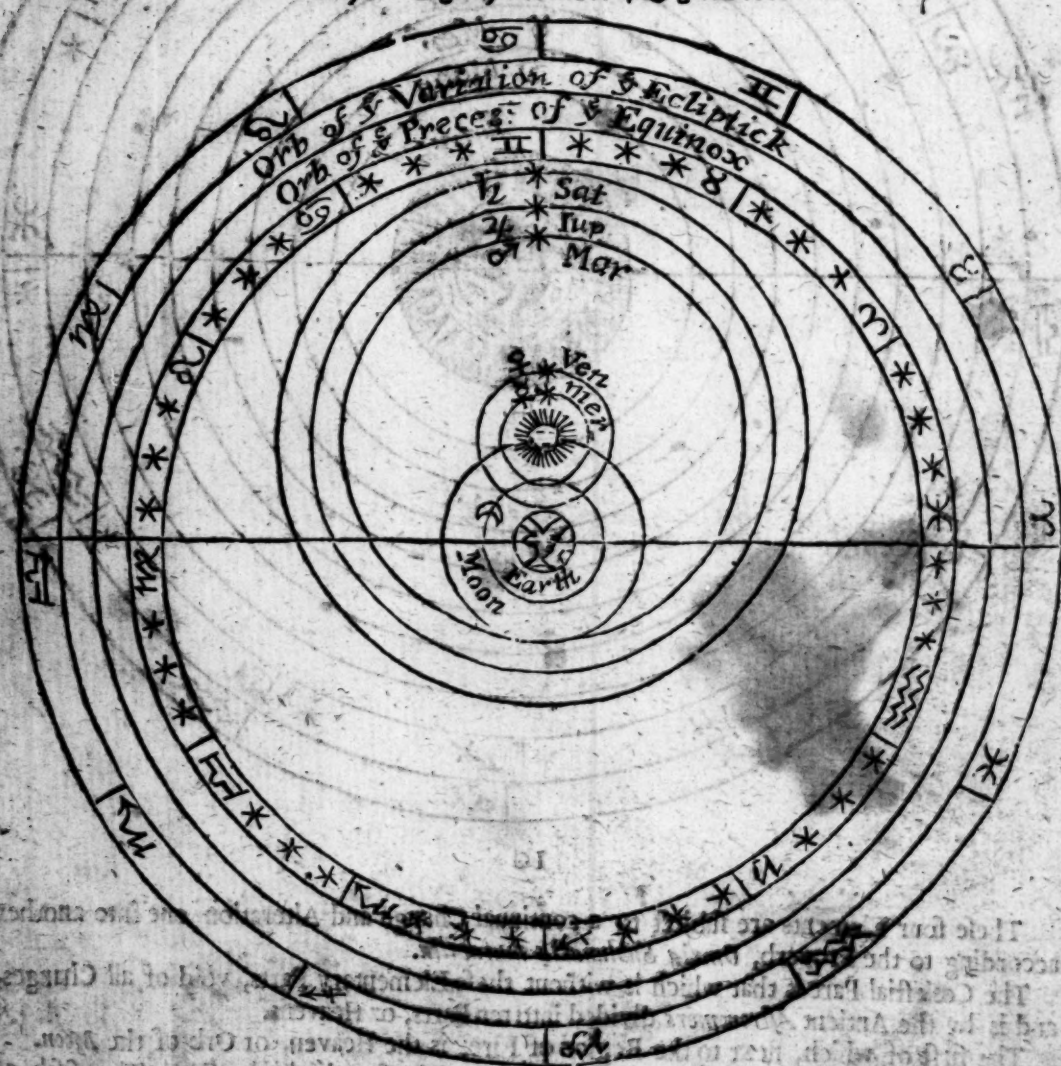
The *Moon* runs ~~round~~ through the Heavens, by her own natural Course, from West to East, in 27 days, 8 hours.

Mercury in 88 days. *Venus* in 225 days. And the *Sun* in a Year. *Mars* in two Years. *Jupiter* in 12 Years. *Saturn* in 30 Years.

The *Eighth Heaven* perfects its Course, according to the Affirmation of *Tycho Brahe* in 25400 Years.

These Heavens are turned about upon the *Axis* of the World by the tenth Heaven, which is the *Primum Mobile*, or *First Mover*, by which Motion is caused Day and Night, and the daily rising and setting of the Heavenly Lights.

The Tychoonian System.



This Hypothesis derives its Name from the Author thereof, *Tycho Brahe*, a Nobleman of *Denmark*, the most famous *Astronomical* Observer in the World

Fig:22

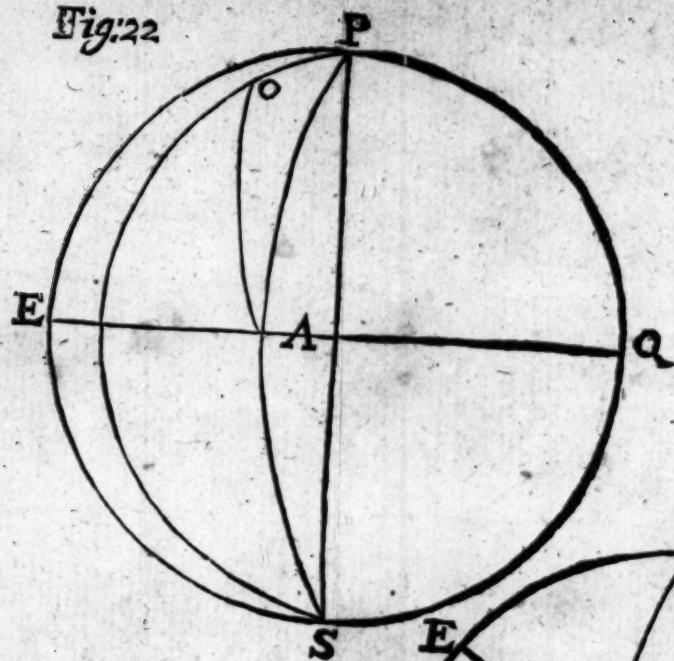


Plate V.

Fig:23

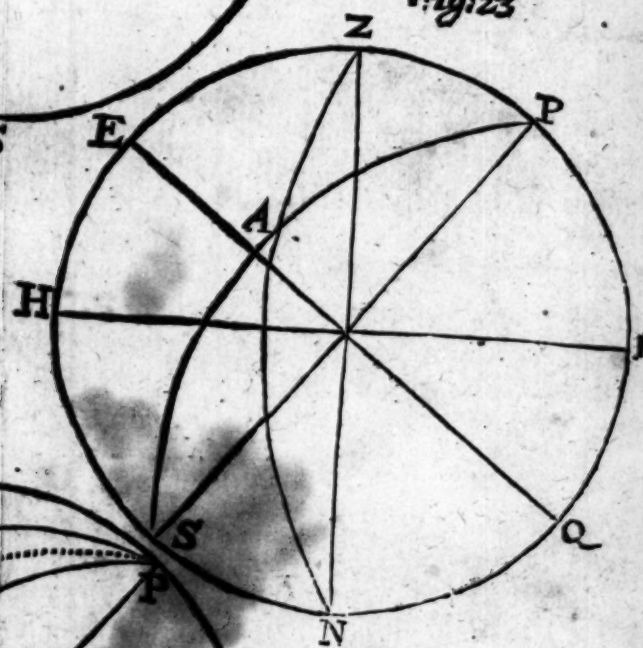
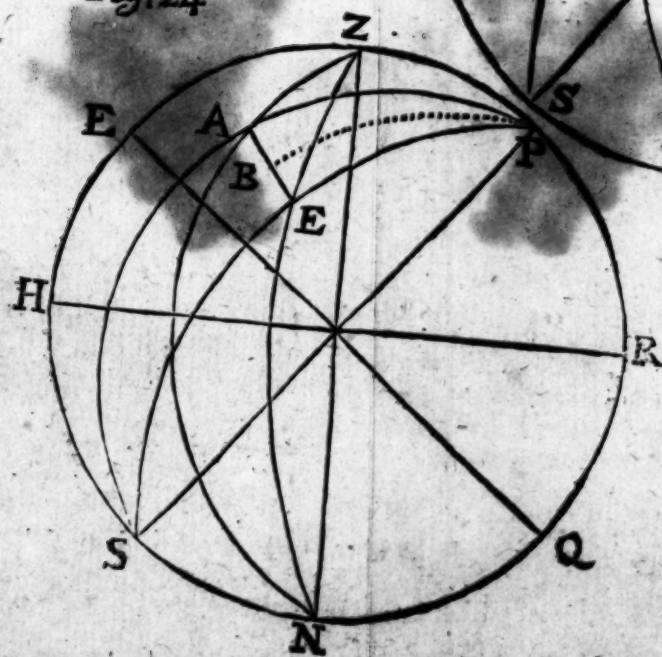
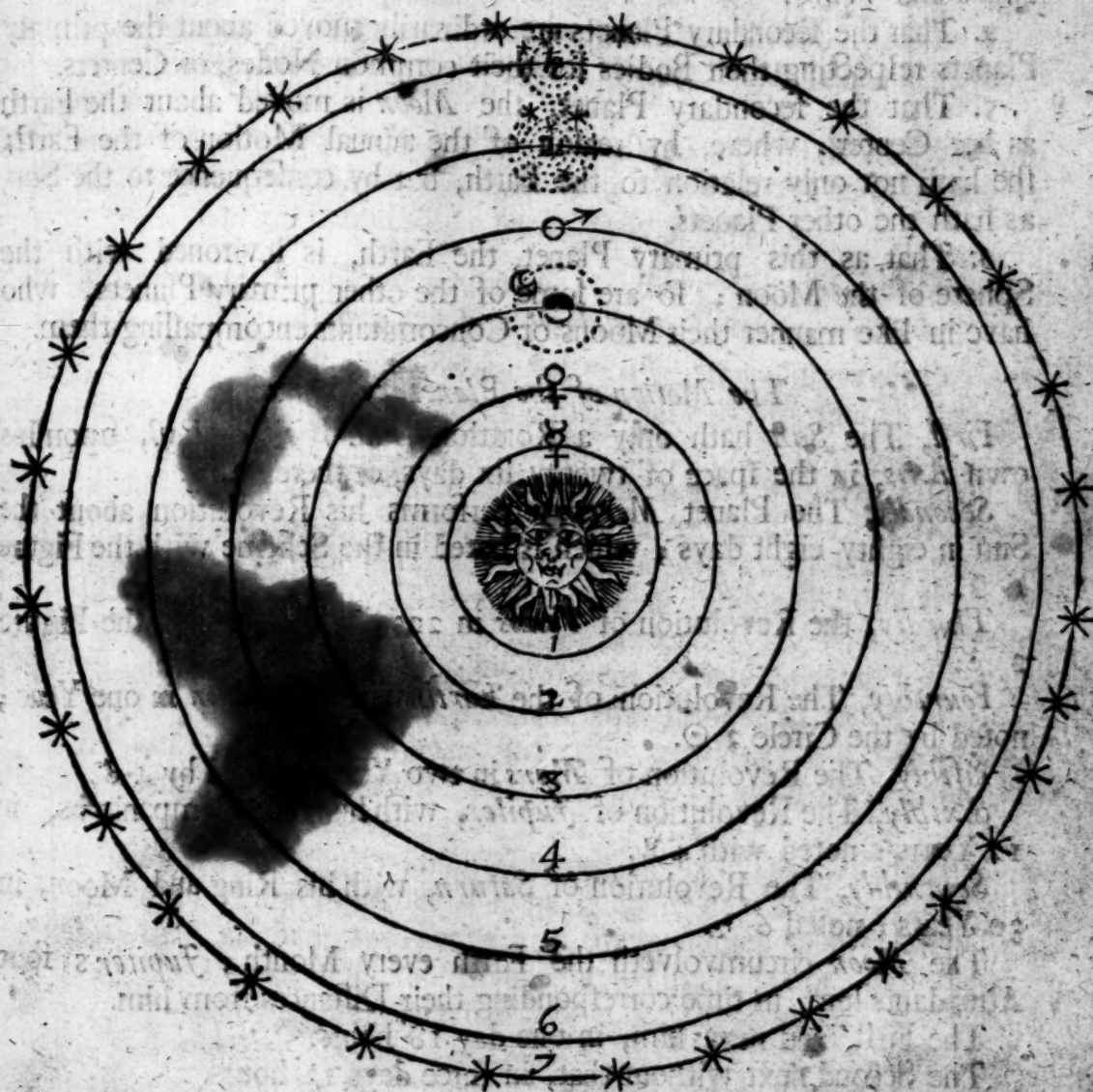


Fig:24



in his Days ; who by his own Observations did rectify the Places of most of the *Fixed Stars*, which appeared in that *Horizon* wherein he lived. This famous Man, according to his present apprehension, framed this *Hypothesis* of the Heavenly Motions, wherein he suppoeth, that *Venus*, *Mercury*, *Mars*, *Jupiter*, *Saturn*, in their Motion, respect the *Sun* as their Centre ; and the *Sun* and *Moon* the *Earth* ; and that *Saturn*, in opposition to the *Sun*, is nearer to the *Earth* than *Venus* in *Apogee*, and that *Mars* in *Opposition* is nearer the *Earth* than the *Sun* it self ; as may appear in the said *Hypothesis*.

The Copernican System.



This *Hypothesis* was first invented by *Pythagoras*, and revived by *Copernicus*, a famous *Astronomer* of *Germany*, who lived in the Year 1500, who supposes, 1

1. That

1. That the Sun is placed in the Midst of the World, in or about the Center of the Sphere of the fixed Stars, and hath no Circular motion, but Cential only.

2. The primary Planets are each of them in their proper Systems moved about the Sun, and accomplish their Periodical Revolutions most exactly in their determinate and appointed times.

3. That the Earth is one of the Planets, and with her annual Motion about the Sun, describeth her Orb in the middle between the Orbs of *Mars* and *Venus*.

4. That the secondary Planets are ordinarily moved about the primary Planets respecting their Bodies for their common Nodes, or Centers.

5. That the secondary Planet, the *Moon* is moved about the Earth as her Center; where, by reason of the annual Motion of the Earth, she hath not only relation to the Earth, but by consequence to the Sun, as hath the other Planets.

6. That as this primary Planet, the Earth, is invironed with the Sphere of the Moon; so are some of the other primary Planets, who have in like manner their Moons or Concomitants encompassing them.

The Motion of the Planetary System.

First, The Sun hath only a Rotation from West or East, upon his own *Axis*, in the space of twenty six days, or thereabouts.

Secondly, The Planet *Mercury* performs his Revolution about the Sun in eighty eight days; which is noted in the Scheme with the Figure 1 8.

Thirdly, the Revolution of *Venus* in 225 days, noted by the Figure 2 8.

Fourthly, The Revolution of the Earth with the Moon in one Year; noted by the Circle 3 0.

Fifthly, The Revolution of *Mars* in two Years, noted by 4 8.

Sixthly, The Revolution of *Jupiter*, with his four Companions, in 12 Years; noted with 4 4.

Seventhly, The Revolution of *Saturn*, with his Ring and Moon, in 30 Years; noted 6 4.

The *Moon* circumvolveth the Earth every Month; *Jupiter's* four Attendants him, in time corresponding their Distances from him.

The First, and next him, in one day 18 hours.

The Second next without that, in three days 13 hours.

The Third in 7 days 4 hours.

And the Fourth and outmost, in 16 days 8 hours.

Saturn's

Saturn's Moon moves about him in 16 days; and all from *West* to *East*, according to their Revolutions about the *Sun*.

Saturn, *Jupiter*, *Mars*, the *Earth*, *Venus*, and *Mercury* (whose Revolutions respect the *Sun* only) are called *Primary Planets*.

The rest (that move again) about *Saturn*, *Jupiter*, and the *Earth*, *Secondary Planets*.

The *Earth* hath a Revolution upon her *Equinoctial* Poles in 24 hours, from *West* to *East*.

The *Secondary Planets* are all of them much less in Magnitude than their *Primary*; and all the *Planets* together much less than the *Sun*, from whom they all receive their Light, Virtue, and Principal Power of Motion.

Far without the *Planetary System* are placed all the *Fixed Stars*, in several Distances, but all unto us incommensurable. The *Parallax* of the *Earth's* Orb being insensible in any of their Places.

A Description of the Golden Number, Cycle of the Sun, Roman Indiction, Epact, and Leap-Year.

THE *Golden Number*, or *Prime*, is a Circular Revolution of 19 Years, in which Term of Years it hath been antiently supposed, that the *Sun* and *Moon* do make all the variety of Aspects one to another.

The *Cycle of the Sun* maketh its Revolution in 28 Years, because in that time all the variety of the *Dominical Letters* and *Leap-Years* are expired, and the 29th Year the Cycle doth begin again; which number is to find out the *Dominical Letter* for any Year past, present, or to come.

The *Roman Indiction* consisteth of 15 Years, and is set down in the Charters and Writings of the *Protonotaries of the Pope of Rome*; for once in 15 Years the Nations were to pay Tribute to the *Romans*.

The *Epact* is a number never exceeding 30 days; it is the 11 days and six hours, which added to the *Lunar Year*, being 354 days, do make it equal to the *Solar Year*, which is 365 days.

The *Leap-Year* is every fourth Year, which hath one day more in it than a common Year; this day is made up in four Years, by the odd six hours that are over and above 365 days, which day is added after the 24th of *February*: So that in the *Leap-Year* *February* hath twenty nine days. And here note, that the *Prime* and *Dominical Letters*, and the *Cycle of the Sun*, change the first of *January*; and the *Epact* the first of *March*; and the *Roman Indiction* the first of *September*.

Memorial Verses on the Ecclesiastical and Civil Kalendar, &c.
By Mr. T. S.

To know if it be Leap-Year.

*Divide the Year by 4 ; What's left shall be,
For Leap Year 0, for past, 1, 2. or 3.*

HERE you may omit the Hundreds of the Year of our Lord, and divide the Residue by 4.

For Example.

Anno 1707, omitting the Hundreds, I divide the Residue, which is 7 ; by 4, and there remains 3, which shews, it is the third after Leap-Year

To find the Dominical Letter.

*Divide the Year its 4th, and 4 by 7 ;
What's left subtract from 7 ; the Letter's given.
A 1. B 2. C 3. D 4. E 5. F 6. G 7.*

Example.

Of the Year of Christ	_____	1707
The 4th part (omitting Fraction) is	_____	426
To both which I add the Number	_____	4
The Sum is	_____	2137

Which divided by 7, there is left 2 ; which subtracted from 7 there rests 5 ; which shew the Dominical Letter for the Year 1706, is the 5th in order of the Alphabet; that is E.

But the Leap Year hath two Dominical Letters ; the later found by this Rule serveth for St. *Matthias's* day to the Year's end ; and for finding *Easter*, the former (next following in order from A to G, and beginning again at A) serveth for *New-Year's-Day* unto St. *Matthias*.

For the Golden Number, Cycle of the Sun, and Indiction.

*When 1, 9, 3, 10th Year hath added been
Divide by 19, 28, 15.*

Example.

To 1707 I add 1, the Sum 1708 I divide by 19, and there remains 17, which is the Golden Number for the Year 1707.

Again, to 1707 I add 9, and the Sum 1716 I divide by 28, the Residue 8 is the Cycle of the Sun Anno 1707.

Lastly,

Lastly, To 1708 I add 3, the Sum 1712 divided by 15, the Remainder 2, which shews it is the second Year of the Indiction for the Year 1709.

The Prime or Golden Number being given, to find the Epact.

Divide by 3, for each one left add 10 ;
30 reject : the Prime makes Epact then.

Example.

Anno 1707, the Golden Number 17, I divide by 3, and there is left 2 : therefore ten times 2, which is 20, added to 17, the Sum is 37, out of which subtract 30, and there will remain 7, the Epact for the Year 1707.

By the nineteen Epacts, to find the Day of Easter-Limit from the beginning of March, inclusively.

The Epacts take from 47 ; but two,
The greatest take from 77 ; 'twill do.

Example.

Anno 1707, the Epact being 7, I subtract it from 47, and the Residue 40 is Easter-Limit, Anno 1707, that is April the 9th, reckoned from the beginning of March Inclusively.

But when the Epact is 28 or 29, it must be subtracted from 77, that so the Limit may remain. And the next following Sunday after the Limit is always Easter-Day.

Easter Limit, and the Dominical Letter being given, To find Easter-Day.

The Letter more by 4 from Limit take ;
What's left from nearest Sevens, shall Easter make.

Or thus ; Take the number of the given Letter more by 4 from the given Limit and the Residue from the nearest greater Sum, of Sevens ; the last Remainder added to the Limit ; the Sum, or its excess above 31, is Easter-Day, in March or April.

Example Anno 1707, the Dominical Letter is E, which is the fifth Letter in order, which more by 4 is 9 ; which taken from the Limit 40, the Residue is 31 ; this take from the nearest greater Sum of Sevens, which is 35, and there remains 4, which being added to the Limit 40, the Sum 44, therefore the 13th of April, is Easter-Day 1707.

For the Days of the Month on which the Sun entreteth the twelve Signs.

*Twice 9, twice 10, four 12's, 11 ;
Then 10, then 9, then 8, or 7.*

Anno 1700. ☉ in.

γ.	δ.	ι.	ϛ.	ϙ.	π.	μ.	Ϟ.	ζ.	ν.	ξ.	κ.
Mar.	Apr.	May.	June	July,	Aug.	Sep.	Oct.	Nov.	Dec.	Jan.	Feb.
9.	9.	10.	10.	12.	12.	12.	12.	11.	10.	9.	8.

For the Degree of the Sun's Place on any Day.

From the day of the Month on which the Sun's Place is required, if you may, or else from the Sum of that and 30, subtract the day of his entrance into the Sign of that Month, the Remainder will be the degree of his Place in that or the next preceding Sign.

For the Age of the Moon, or Day of her Change.

Janus 0, 2, 1, 2, 3, 4, 5, 6 ;

8, 8, 10, 10, these to the Epact fix :

The Sum (bate 30) to the Month-day add,

Or take from 30 ; Age or Change is had.

Or thus ; Add to the Epact in

Jan.	Feb.	Mar.	Apr.	May.	Jun.	Jul.	Aug.	Sept.	Oct.	Nov.	Dec.
0.	2.	1.	2.	3.	4.	5.	6.	8.	8.	10.	10.

The Sum, if it be less than 30, or else the excess above 30, added to the day of the given Month (rejecting 30 if need be) gives the Age of the Moon that day ; but subtracted from 30, leaves the day of the Change in or from the beginning of that Month.

For the day of the Full Moon, add or subtract 15 to or from the day of the Change.

Example.

1. For the Age of the Moon, Anno 1707, May 29, the Number for the Month 3, added to the Epact 7, makes 10 ; which added to 29, (rejecting 30 from the Sum) gives 9, the Age of the Moon required.

2. For the day of the Change or (New-Moon) in May 1707, the Epact 7, with the Month 3, makes 10, as before ; which subtracted from 30, the Residue 20, is the day of the New-Moon in May 1707.

3. From which 15 being subtracted, leaves 5, the day of Full-Moon in May 1707.

To find the Day of the New Moon, and the Entrance of the Sun into the Signs, for Time past, or to come.

312, 131, —————
Past, add; to come, subtract for Moon and Sun.

Or thus, For every 312 Years past, add 1 day to the time of the New-Moon found above; for 312 Years to come, subtract 1 day.

Likewise for 131 Years past, a day is to be added to the former account of the Sun's Entrance; and for 131 Years to come, subtracted.

To find the Distance of the Sun from the Nodes of the Moon perpetually in all Lunations; Remember,

Year 17 hundred, Node, Sign 4, Degree
27, 3, 800, 43.

1. Take the Interval between the given Time, and 1700 compleat in Years and Days, allowing 12 Months to the Year, and 30 days to a Month, and the account will suffice for this Work.

2. Multiply the Years of the Interval by 43, and divide the Product by 800, the Residue multiply by 9; then take the half of this Product, and distinguish the last Figure from the rest by a Point. So have you the degrees, and 10th part of a degree, answerable to the years of Interval. Also multiply the days the of Interval by 43, and divide by 800; this Quotient shews the degrees, and the Remainder divided by 80, the 10th part of a degree of the Motion for the days of Interval. Then collect the former and latter degrees and tenths into one Sum, and reduce it into Signs, Degrees, and Tenths.

3. For time afore 1700 compleat, add the Signs, Degrees and Tenths thus found, to 4°, 27', 3 tenths, but for Time after 1700 compleat, subtract them from 4°, 27', 3 tenths, and the Sum or Remainder shall be for the place of ☊, adding 1 degree for the tenths, if they exceed 5, else rejecting them.

Always in Additions omit Cycles, (to wit, 12°, or 360°) but in Subtractions add one Cycle, if need be, to the Number from which you are to subtract.

Next by the common Rule for 1700, without any Correction for time past or to come, find the Sign and Degree of the Sun's Place, and subtract the last found place of ☊ from it; the Residue is the distance of ☉ from ☊ required.

The Limits of Eclipses of the Sun and Moon, in degrees from

8 or 8

*Within 16 the Sun, and 10 the Moon,
Suffer Eclipse; above 18, 12, none.*

*To find the Length of the Days and Nights in the Latitude
52 deg. for ever.*

To 15, 1; 1, 16; 1, 2, 6, 3;

1, 2; 3, 4 hours; 4 and half agree.

To the given distances of the Sun from the next Equinoctial Points the answerable hours are these; to 15° , 1 hour; to 1 Sign, 2 hours; to 1 Sign 16° , 3 hour; to 2 Signs 6° , 4 hours; and to 3 Signs, 4 hours and a half; which hours added to 12, the Sum is from the Vernal Equinox to the Autumnal, the just length of the day; but from the Autumnal to the Vernal, the length of the Night in those distances.

And for all other intermediate Distances of \odot from the Equinoctial Points, the Proportion is, As $15, 16$, or 20° to $60'$; or as 20 to $30'$; So are the degrees of the excess of the intermediate Distances above 0° , 15° , 1° , 16° , or 2° , 61° , and not exceeding 2° , 26° to the minutes of the length of the day or night, above 12, 13, 14, 15 or 16 hours. Always allowing 4 degrees or days afore and after the Ingress into ϵ and γ , for Solstices.

The length of the day and night taken together is 24 hours, from which if the one be subtracted, there will remain the other; And,

Half the Length of the $\left\{ \begin{array}{l} \text{Night,} \\ \text{Day,} \end{array} \right\}$ is the time of $\left\{ \begin{array}{l} \text{Sun-rising.} \\ \text{Sun-setting.} \end{array} \right\}$

*To find the Hour of the Moon's coming to South, and High-Water
at London.*

*The Moon's Age multiply by 4; Divide
By 5 for Southing; Add 3 for the Tide.*

But when the Age of the Moon exceeds 15 days, you may reject 15; As in this Example.

Anno 1710, the Moon being 27 days old, out of which reject 15, the Remainder is 12, which being multiplied by 4 makes 48, which divide by 5, the Quotient is 9, and 3 in the Remainder: which shews that the Moon cometh to South at 9 of the Clock, and three times 12 minutes past, which is 36 minutes, (and here note that for every Unit in the Remainder, you must reckon so many times 12; which must be added to the hour found in the Quotient, as in the Example foregoing) to which I add 3 hours, and the Sum is 12 hours 36 min, the time of Full Sea at London.

But

But it is here to be noted, that by manifest Experience it is found, that when the Moon is in either of the Quarters, then the Tides do not hold out their full time, but it is High-water sooner then is found by the Rule; which may partly be occasioned by the weakness of the Tide at such a time, and the length of the River. For by the foregoing Rule you may find, that when the Moon is 7 days old, the time of High-water will be at 9 of the Clock, when upon true Observation it will be found to be an hour sooner; and therefore to know the true time of High-water, you must subtract some minutes from the Time found by the precedent Rule, according to the Age of the Moon, as you may plainly see in the annexed Table.

The Moon's Age H. M.				Subtract.	
1	14	16	29		
2	13	17	28		
3	12	18	27		
4	11	19	26		
5	10	20	25		
6	9	21	24		
7	8	22	23		

Example. The Moon being 7 days old, it is high Tide (by the Rule) at London, at 9 of the Clock; then in this Table look for the Figure 7 which is in the first Column, and right against it in the two last Columns, under the Title of Hour and Minute, you will find one Hour which must be subtracted from the Hour, found by the Rule, and the Remainder is 8, the true Time of High-water.

A Table shewing the time of the Moon's coming to South, any day of her Age.

Moon's Age.		Moon's Southing.		
Days.		H.	M.	
1	16	0	48	The Use of the Table to find the Time of the Moon's coming to South. The first and second Columns shew the Days of the Moon's Age, in the third and fourth, the Hour and Minute of the Moon's coming to South.
2	17	1	36	
3	18	2	24	<i>Example.</i> The Moon being 10 days old, I would know at what time the Moon will be South. I find 10 under the Title of the Moon's Age, in the first Column; and right against it, in the third and fourth Columns, you may have 8 hours 00; which sheweth that the Moon being 10 days old, cometh to South at 8 of the Clock, and no Minutes; unto which if you add the time of flowing at Full and Change, the Sum will be the time of Full-Sea at the same Place. As here at London, the time of Flowing at Full and Change is at 3 of the Clock, which you are to add to the Moon's Southing, and the Sum is 11, which is the time of High-water when the Moon is 10 days old.
4	19	3	12	
5	20	4	00	The
6	21	4	48	
7	22	5	36	
8	23	6	24	
9	24	7	12	
10	25	8	00	
11	26	8	48	
12	27	9	36	
13	28	10	24	
14	29	11	12	
15	30	12	00	

To find the Hour of the Night by the shadow of the Moon upon a Sun-Dial.

First, Find her coming to South, as before ; then see how many hours and minutes the shadow wants of the hour of 12 ; which hours and minutes take from the hour and minute of the Moon's coming to South ; and the Remainder is the hour of the Night ; but if the shadow be past the hour of 12, then you must add so many hours and minutes as the shadow is past 12, to the hour and minutes of the Moon's coming to South, and that will be the hour of the Night.

Example. On the 5th of Decemb. 1706, I find the Moon to be 11 days old, and therefore she comes to the South at 48^h after 8 of the Clock ; and suppose the same Night you look upon a Sun-Dial, and should find the shadow to fall upon half an hour past 1, which is an hour and a half past the Line of 12 ; which 1^h. 30^m. must be added to 8^h. 48^m. the Moon's Southing, shews it is 18^m. past 10 of the Clock.

Again, Suppose the same Night the shadow had fallen upon half an hour past 11 ; which wants half an hour of 12 ; which is to be subtracted from 8^h. 48^m. the Moon's Southing, and the Remainder will be 18^m. after 8 of the Clock.

CHAP. IX.

Of the MARINER'S COMPASS.

Of the *Variation* of the *Compass*, and the probable *Causes* thereof. Some *Observations* to find the *Variation*. The *Description* and *Use* of the *Azimuth Compass*. Of the *Universal Ring-Dial*.

SECT. I. *Of the Original Discovery, and Invention of the Mariner's Compass, and the Excellency thereof.*

THIS most useful Instrument, call'd the *Mariner's Compass*, is justly ranked among the greatest Wonders that this World affords ; and deserves well to be understood by all that are Students and Practitioners in the Art of Navigation. For without the help thereof, it were impossible to trace out the unbeaten Paths of the Ocean, for the procuring Trade and Traffick beyond the Seas, to remove parts of the World ; whereby the glorious Gospel hath been transmitted into the most dark Corners of the Earth.

As to the Original Inventor hereof, Modern Historians do somewhat vary ; some attribute the Invention thereof to one *John Goia* (or *Flavia Goia*, as others stile him) of *Amalphi* in *Campania*, in the Kingdom of *Naples*,

Naples, who only accommodated the *Superfices* thereof with 8 Points, that is four Cardinal, and four Collateral; and so left the Improvement of this Invention to be attempted by Posterity. Others do entitle the Invention thereof to the People of *China*. Dr. *Gilbert*, in his Book *De Magnete*, asserts, that *Paulus Venetus* transported it first into *Italy*, in the Year 1260, having learned it from the *Chineses*. And *Ludi Verio-mannus* affirms, that when he was in the *East-Indies*, about the Year 1500, he saw a Pilot of a Ship direct his Course by a Compass, fashioned and framed as those which now are commonly used.

And Mr. *Barlow*, in his Book, Entituled, *The Navigator's Supply*, Anno 1597, relating a Story of two *East-Indians*, that he had personal Conference with (one of them was of *Mamila* in the Isle of *Lazon*, the other of *Miaco* of *Japan*) who declared, that instead of our Compass, they use a Magnetical Needle of six Inches, and longer, upon a Pin, in a Dish of white *China-Earth* filled with Water, in the bottom whereof they have two cross Lines for the principal Winds, the rest of the Divisions being left to the Skill of their Pilots. Also he there relates, that the *Portuguese*, in their first Discoveries of the *East-Indies*, got a Pilot of *Malinde*; that brought them from thence in 33 days within the sight of *Calecut*; by which it appears that then they had the Use of the Compass.

But let the Invention be attributed to whom it will, 'tis manifestly known to have received its absolute Perfection in these Parts of the World: But more particularly, the compleating of this Invention is due to the People of *Antwerp* and *Bruges*, and also to our own Nation, by annexing to the Compass twenty four subordinate Winds or Points; and also on the Limb thereof 360 Degrees, which are numbred from North and South, towards the East and West, with 10, 20, 30, &c. So that it appeareth, that every Point containeth 11° 15'. Upon the North Point there is a *Flower-de-luce*, to distinguish it from the rest of the Points.

Before the Invention of this rare Instrument, Men were directed in their Voyages by certain Stars they took notice of, especially the *Pleia-des* or *Seven Stars*: by *Charle's Wain*, and the two Stars in the Tail of of the *Little Bear*, which were therefore called *Lead-Stars*. Also Travellers in the Desarts of *Arabia*, and those of *Tartaria*, were guided by some fixed Stars in the Night-time, to steer their Courses in those pathless, disorder'd, and unhospitable ways. So Seamen were directed by the like Heavenly Guides, in the untractable Wilderiness of Waters, and unbeaten Paths of the Ocean, before this excellent Artifice was discovered. But if the Sky happen to be sullied with Mists, and the Stars

Stars to be muffled with Clouds, then the most experienced Mariners was at a loss, and was constrained to come to an Anchor, or to lie by, to wait the Appearance of his Cœlestial Directors. And if you consult *Pliny*, he will tell you of the Inhabitants of *Taprobana*, now called *Sumatra*, because they could not behold the *Pole-Star* to sail by, carried certain Birds to Sea, which they often did let fly : and as those Birds by natural Instinct applied their flight always to Land, so the Mariners directed their Course after them.

To these and the like Difficulties were Men exposed before the Invention of this Marvellous Instrument ; And by it Posterity is secured with a noble Remedy against this grand Inconvenience ; and a Method discovered, as by an immediate Messenger from Heaven, to steer an infallible Course in the most gloomy Nights, and tumultuous Seas ; and by the Providence of the Almighty be safely conducted to the desired Port.

Yet this Instrument is not so absolutely perfect (by that acquired Virtue it receives from the Load-stone) but that it requires some Improvements, because it doth not conform it self to the true Meridian in all places, but varies, in some Places more, in some less, from the direct Position of the true North, and South. This Variation of the Compass augments the Mariner's Care, and ought to be constantly observed in all Voyages, the neglect of which may expose them to many Dangers.

A Discourse of the Variation, and of the probable Conjectures of the natural Cause thereof, is handled in that which follows, I thought it necessary (for Method-sake) to subjoyn the Figure of the *Mariner's Compass*.

the Equinoctial, and Parallels; then take a small Magnetical Needle on a Pin, and if you apply this Needle to this Equinoctial of the said Stone, the Needle will lie parallel to the Axis thereof; and if you move it towards either Pole, the Needle will immediately incline towards the said Pole, according as you move it, until you come to the Pole; then will one Part of the Needle point directly to the very Pole of the Stone.

But if this Spherical Magnet shall have a part of it excavated, then if you move the Needle about the Stone, as before, so soon as it shall draw near to the Limb of this Excavation, it will in its course of moving suddenly alter, and incline to one of the Solid Sides, not at all respecting the aforesaid Poles. And this Deflection may explain the *Variation of the Needle*; and the greater will this *Variation* be, the nearer it approacheth to the Poles; For whereas before the Excavation, each side being alike potent, the Needle inclined according to its natural Position; but meeting with this Accident, the Excavation, it will convert it self to the more solid Side, rejecting the imperfect and defective; and so much the more powerfully, by how much the defective part hath lost of its magnetical and vigorous Substance.

And as it is with this little, so likewise may it be with the greater Magnet, the Earth, whose solid magnetical Parts are great Continents; the defective and excavated, the deep and vast Channel of the Sea. And therefore the Cause of *Variation* may be the Inequality of the Earth, variously disposed, and differently mixed with the Sea; and all the different Emission of its Strength and Magnetical Vigour, from the more eminent and gibbose, and from the more hallow and excavated Parts thereof. So the Needle naturally endeavours to conform unto the Meridian, being also detracted that way, where the greater and more powerful Parts of the Earth are situated.

To this may be added, That the *Variation* proceedeth not only from some eminent Terrestrial Knobs or Excrescencies, which appear like so many Wens upon the face of the Earth; as also from many magnetical Veins of the Earth collaterally respecting the Needle; but likewise from the different Accumulation of the Earth, disposed unto the Poles, lying under the Sea and Waters, which affect the Needle with a greater or lesser *Variation*, according to the Vigour or Impotency of the *subterraneous Lines*, or the entire or broken body of the *magnetical Fabrick* under it; as is observable from several Load-stones placed at the bottom of any Water: for a Needle upon the Surface, will variously conform it self according to the *Vigour or Imbecility* of the Load-stones under it.

Observations of the Variation.

The Globe of the Earth is known to be very uneven, and unequally mixed with many Materials, differing from the Magnetical Quality, having great and stony Mountains, large Vallies, deep Seas, long and high Continents and Promontories, with mighty scattered Rocks of Load-stones, of Iron Mines, and other Magnetical Matters.

This *Variation* of the *Compass* was formerly supposed to remain the same, but now 'tis known to vary in all Places. To illustrate this Truth, I shall here insert some Observations of the *Variation* of the *Compass*, near the City of *London*, for an hundred Years last past.

Mr. Burroughs his Observation of the Variation made at Lime-House, Octob. 16. 1580.

Before Noon.		After-noon.		Variation.	
<i>Sun's Alt.</i>	<i>Mag. Azi.</i>	<i>Sun's Alt.</i>	<i>Mag. Azi.</i>		
Gr. min.	Gr. min.	Gr. min.	Gr. min.	Gr. min.	
17 00	52 35	17 00	30 00	11 17	Mean Variation 11° 17' from the North Eastward.
18 00	50 08	18 00	27 45	11 11	
19 00	47 30	19 00	24 30	11 30	
20 00	45 00	20 00	22 15	11 22	
21 00	42 15	21 00	19 30	11 22	
22 00	38 00	22 00	15 30	11 15	
23 00	34 40	23 00	12 00	11 20	
24 00	29 35	24 00	07 00	11 17	
25 00	22 36	25 00	00 28	11 04	

Observations of the Variation.

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*Mr. Gunter's Observation, made at Lime House,
June 13, Anno 1622. Afternoon.*

<i>Sun's Alt.</i>	<i>Mag. Azim.</i>	<i>Sun's. Azim.</i>	<i>Variation.</i>	
Gr. min.	Gr. min.	Gr. min.	Gr. min.	
19 00	82 02	75 52	06 10	Variation, 56 55' East- ward.
18 05	80 50	74 44	06 06	
17 34	80 00	74 06	05 54	
17 00	79 15	73 20	05 55	
16 18	78 12	72 32	05 40	
16 00	77 50	72 10	05 40	
15 10	71 02	64 49	06 13	
19 52	70 12	64 25	05 47	

In this Interval of the Observations made by Mr. Burroughs and Mr Gunter in 42 Years, the evident Diminution hath been 5 degrees.

*Mr. Gillibrand's Observations made at Deptford
Anno 1634. June 12. Before Noon.*

<i>Alt. Sol. Vera.</i>	<i>Azim. Mag.</i>	<i>Azim. Sol.</i>	<i>Variation.</i>
Gr. min.	Gr. min.	Gr. min.	Gr. min.
44 45	106 00	110 06	04 06
46 30	109 00	113 10	04 10
48 31	113 00	117 01	04 01
50 54	118 00	122 03	04 03

Observations of the Variation.

In the Afternoon the same Day.

<i>Alt. Sol. Vera.</i>	<i>Azim. Mag.</i>	<i>Azim. Sol.</i>	<i>Variation.</i>
Gr. min.	Gr. min.	Gr. min.	Gr. min.
44 37	114 00	109 53	04 07
40 48	108 00	103 50	04 10
38 46	105 00	100 48	04 12
36 43	102 00	097 56	04 04
34 32	099 00	095 00	04 00
32 10	096 00	091 55	04 05

The mean of which Observation is $04^{\circ} 06'$ Eastward.

Observations Made by Mr. Gillibrand at Paul's Gray in Kent.
July 4: 1634. Afternoon.

<i>Vera. Alt. Sol.</i>	<i>Azimi. Mag.</i>	<i>Azim. Sol.</i>	<i>Variation.</i>
Gr. min.	Gr. min.	Gr. min.	Gr. min.
40 55	111 30	107 30	04 00
40 01	110 00	106 05	03 55
39 41	109 30	105 34	03 56
38 42	108 00	104 05	03 55
35 32	103 30	99 32	03 58
34 49	102 30	98 32	03 58
33 41	101 00	97 00	04 00
32 57	100 00	96 02	03 58
32 09	99 00	94 58	04 02
31 25	98 00	94 00	04 00
30 39	97 00	93 01	03 59
29 29	95 30	91 31	03 59
27 51	93 30	89 28	04 02

The mean Variation is $4^{\circ} 01'$ Eastward.

So that here also may be noted, that the Diminution of the Variation in 45 Years (from the time of Mr. Burrough's Observations) is more than 7 degrees. Ob-

Observations of the Variation.

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Observations made by *John Seller*, at the *Hermitage* near *London*, with a Quadrant of 6 Foot Radius for the Altitude; and an Instrument of 2 Foot Radius for the Azimuth taken, in the Year 1666. Lat. 51 deg. 32 min.

June the 4th, 1666. in the Forenoon.

Sun's Altit.	Sun's Azim.	Mag. Azim.	Variation
o i	o i	o i	o i
26 00	84 36	85 00	00 24
27 30	86 26	87 00	00 34

June the 13th, 1666. in the Afternoon.

08 24	62 31	62 00	00 31
08 09	61 51	61 30	00 21
07 38	61 29	60 45	00 44
07 07	60 47	60 00	00 47

June the 14th, 1666. in the Forenoon.

29 30	88 30	89 30	00 50
31 20	91 30	91 30	00 27

The mean of these Observations is 34 Minutes Welterly.

May the 28th, 1670. in the Afternoon, taken by the Worshipsful Sir Nicholas Miller, at his House in Battersey.

24 30	83 34	81 40	1 54
20 30	78 44	76 35	2 09
17 03	74 32	72 18	2 14
15 42½	72 54	70 40	2 14
13 36½	70 18	68 10	2 08
11 11	67 14	65 15	1 59
10 11	75 58	63 45	2 13

The mean Variation is 02° 06' Welterly.

Mr.

Mr. Bond's Theory of the Motion of the Variation for time to come.

Years.	Variation West.	Years.	Variation West.
	Gr. M.		Gr. M.
1689	5 39	1703	7 36
1690	5 39	1704	7 45
1691	5 48	1705	7 53
1692	5 57	1706	8 01
1693	6 06	1707	8 09
1694	6 16	1708	8 17
1695	6 25	1709	8 25
1696	6 34	1710	8 33
1697	6 43	1711	8 41
1698	6 52	1712	8 49
1699	7 01	1713	8 56
1700	7 10	1714	9 04
1701	7 19	1715	9 11
1702	7 28	1716	9 17

SECT. III. The Description and the Use of Azimuth Compass.

THIS Compass doth derive its Name from its Use, being principally to find the *Magnetical-Azimuth* of the Sun, and is in several respects like unto another Compass, only with such necessary things added, as are most convenient for that purpose.

Upon the round Box, wherein are the Fly and Needle, is fastened a broad Circle of Brads, the one half of the Limb thereof is divided into 90 degrees numbered from the middle of the said Divisions both ways, with 10, 20, 30, &c. unto 45 degrees; which degrees are also subdivided into Minutes by *Diagonal Lines*, and by certain *Excentrick Circles* intersecting one another; for these degrees are drawn from the opposite part of the Limb whereon the Index moveth, cutting those degrees. On this Index is erected a Sight, which for conveniency is to fall down with a Hinge, and so set up upon occasion; and from the top of this Sight, down to the middle of the Index is fastned a Thread or Lute-string, to shew the shadow of the Sun upon a Line that is on the middle of the said Index.

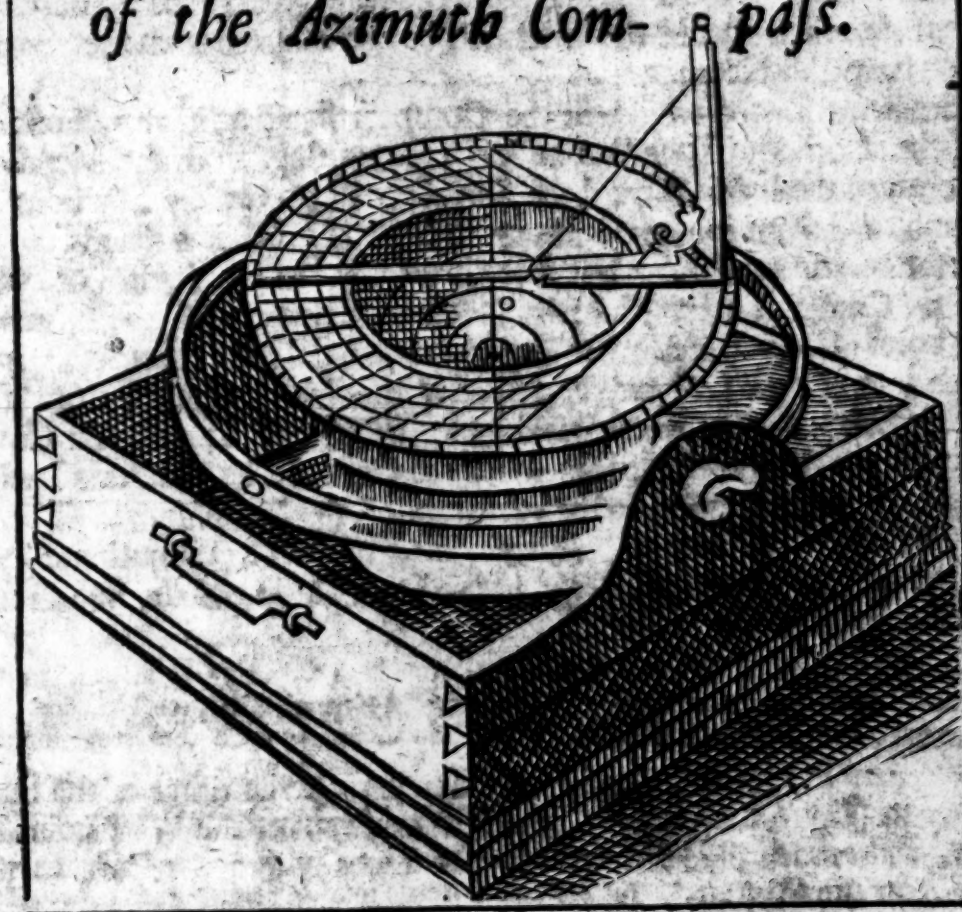
And by this means of placing the Index upon the Circumference, the degrees come to be as large as they would be, if it be again moved upon the Center; the Truth hereof is evidently demonstrated in the Third Book of *Euclid*, Prob. 20.

This broad Circle is crossed at Right-Angles, with two Strings, and commonly from the Terminations of these Strings are drawn four small black Lines on the Inside of the Box, for rectifying the Instrument in time of Observation, by the four Lines that are also drawn at Right-Angles, on the Superficies of the Fly.

This Compass being thus fitted, is hung in strong Brads Rings, and those also fastned into a square Wainscot Box, fit for that purpose; which you may more plainly perceive in this following Figure.

The

The figure
of the Azimuth Com- pass.



The Use of the Azimuth- Compass.

First, You must rectify the Brass Limb on the Edg of the Box (by the Needle and Fly within the Box) according as the nature of the Observation doth require. For if the Observation be in the Forenoon, then you must put the Center of the Index upon the West Point of the Chard or Fly within the Box; and so, that the Four Lines on the Edg of the Chard, and the Four Lines by the inside of the Box, do always concur.

The Instrument being thus rectify'd, turn the Index towards the Sun, until the shadow of the *Hypotenusal Thread* fall directly into the very slit of the Sight that is on the Index, and also upon a Line that is in the middle of the Index; that at the same time will the inner Edge of the Index cut the degree and minutes of the Sun's Magnetical Azimuth from the East to the Northward or Southward.

As for Instance: Suppose the Instrument be rectify'd, as before is shewr; for an Observation in the Forenoon, and that the Index should cut ten
Q degrees.

114 The Description of the Azimuth Compass.

degrees upon the Limb to the Northward of the East, then is the Azimuth of the Sun 80 degrees from the North, or else 100 degrees from the South. So likewise if the Index had cut 10 degrees to the Southwards of the East, then would the Azimuth be 80 degrees from the South, and 100 from the North.

And here also observe, that the Compass standing in this Position, and if the Azimuth of the Sun be less than 45 deg. from the Meridian, and you turn the Index toward the Sun, it will go off the Divisions on the Limb, and there can be no use made thereof as it now stands.

Therefore you must turn the Instrument just one Quadrant, or quarter of the Compass, *viz.* Place the Center of the Index on the North or South Point of the Chard, according to the Sun's Position from you, and then the Edg thereof will cut the degree of the Sun's Azimuth from the North or South. That which is said as to the Use of the Azimuth Compass, when the Sun is on the East-side; the like is to be understood with the same reason when he is on the West-side of the Meridian.

And also Note, That the Observations of the Sun's Azimuth are best when the Sun is near the Horizon, because the Motion of the Sun in his Altitude is more easily observ'd.

To take an Amplitude by the Azimuth-Compass.

If the Amplitude be taken in the Morning, at the rising of the Sun, then you must turn the Center of the Index right over the West point of the Fly, and rectify the Instrument by the Lines within the Box, to the Lines on the Fly.

Then looking through the Sight, turn the Index towards the Sun, until you cut the Body of the Sun with the Thread; at the same time will the Edg of the Index shew the degree of the Sun's Magnetical Amplitude, upon the Limb of the Instrument, from the East, either Northerly or Southerly.

But if you take the Amplitude in the Afternoon, at the setting of the Sun, then you must turn the Index over the East Point of the Fly, and proceed as before.

Having found the Magnetical Azimuth or Amplitude by the Compass, find the Sun's Azimuth by *Problem 13. Chap. 8.* and the Sun's Amplitude by *Problem 8. Chap. 8.*

Then find the Difference between the Sun's Azimuth or Amplitude, and the Magnetical Azimuth or Amplitude, by subtracting the one from the other; this Difference is the Variation of the Compass. And to know whether the Variation be Easterly or Westerly, observe these following Rules.

Rules

Rules for casting the Variation.

I. By the Observation of the Azimuth.

In the Forenoon. 1. If the Angle of the Sun's Azimuth (by Calculation) from the North, be greater than the Magnetical Azimuth (by Observation) then is the Variation Easterly.

2. If the Angle of the Sun's Azimuth from the North be less than the Magnetical, then is the Variation Westerly.

In the Afternoon. 3. If the Sun's Azimuth from the North be greater than the Magnetical, then is the Variation Westerly.

4. If the Sun's Azimuth from the North be less than the Magnetical, then is the Variation Easterly.

Example 1. Suppose on the 4th of June 1690, In the Forenoon, I set the Sun with my Azimuth Compass, and find his Magnetical Azimuth to be $90^{\circ} 48'$ from the North, at the same time the Sun's Azimuth, by Calculation, is $84^{\circ} 20'$ from the North part of the Meridian.

The difference of these Azimuths (which is the Variation) is $06^{\circ} 18'$; I demand which way the Compass varies?

Ans. Westerly; because that Observation being made in the Forenoon, and I find the Sun's true Azimuth from the North to be less than the Magnetical, according to the second Rule foregoing.

Example 2. Admit that in the Afternoon, at the same time that I find the Sun's Azimuth to be $102^{\circ} 00'$, I find his Magnetical to be $96^{\circ} 00'$ from the North.

The difference is $06^{\circ} 00'$; I demand which way the Compass varies?

Ans. Westerly; because the Observation being made in the Afternoon, I find the Sun's Azimuth from the North to be greater than the Magnetical, according to the third Rule.

Note. These four Rules for casting the Variation, by Observation of the Sun's Azimuth, are the same in South as in North Latitude, the Sun's Declination being either Northerly or Southerly.

II. By the Observation of the Amplitude.

At Sun-rising. 1. If the Sun's Amplitude be nearer to the North than the Magnetical, then is the Variation Westerly.

2. If the Sun's Amplitude be farther from the North than the Magnetical, then is the Variation Easterly.

At Sun-setting. 3. If the Sun's Amplitude be nearer to the North than the Magnetical, then is the Variation Easterly.

4. If the Sun's Amplitude be farther from the North than the Magnetical, then is the Variation Westerly.

Example. Admit that by the Azimuth-Compass, at Sun-setting, I find the Magnetical Amplitude to be 19 deg. 00 min. and the Sun's Amplitude to be 24 deg. 00 min. from the West Northerly; I demand which way the Compass varies?

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Ans. Easterly : because by an Observation at Sun-setting, the Sun's Amplitude is nearer to the North than the Magnetical, according to the third Rule.

Having by the former Rules found the Quantity and Quality of the Variation, it yet remains there be some Directions for rectifying the Course.

The manner that I shall here set down is perform'd by a Compass-Chard, having Degrees on the Limb, and a pair of Compasses; which tho' it be mechanical, yet it's facile and demonstrative, and in my Opinion exact enough for Nautical Uses; however, any one may use the Pen if he please.

But before we deliver the Rule for Operation, it will not be amiss for plainness sake, to give these Cautions.

1. That when a Man directly beholds the North part of the Horizon, the East is on the Right-Hand, and the West on the Left; and therefore when the North-point of the Compass (and consequently all the other Points) vary from the true North or Meridian to the Eastward, then the Variation is reckon'd to the Right-Hand; and for the same Reason, if the Variation be Westerly, it's accounted to the Left.

2. That in the use of the Compass-Chard, you must always observe, that you place the Course, or Point on which you steer, right from you.

The Rule. Take the quantity of the Variation in degrees, from the Limb of the Chard, between the Compasses (the Chard lying before you as is directed) placing one Foot in the Rhomb or Course; if the Variation be Easterly, turn the other Foot towards the Right Hand; but if Westerly, to the Left: The Number of Degrees in which the Point of the Compass stays, shews the true Course from the North or South, either Easterly or Westerly, the Quantity and Quality of the Variation being allow'd.

As for Example. 1. Let the Magnetical Rhomb, or Point of the Compass be North-East, and the Variation 10 degrees Easterly; I demand the true Rhomb?

The Chard lying as is directed, take the extent of the Degrees between the Compasses, and place it from the N. E. toward the Right Hand, because the Variation is Easterly, that shews the true Course to be N. E. 55 degrees, or N. E. by E. a little Easterly.

2. Let the Course by the Compass be West and by South, (*i.e.*) S.W. 78 deg. 45 min. and the Variation 10 deg. Easterly, as before, I demand the true Rhomb?

Take the extent of 10 degrees between your Compasses, and place it from W. by S. towards the Right Hand; it shews the true Rhomb to be S.W. 88 deg. 45 min. or almost West.

3. Let the Magnetical Rhomb be West, and the Variation 10 degrees Easterly, I demand the true Course?

Take

Take the extent of 10 degrees, as before, set it off from the West towards the Right-hand, it gives the true Rhomb N. W. 80 deg. 00 min. or almost West by North.

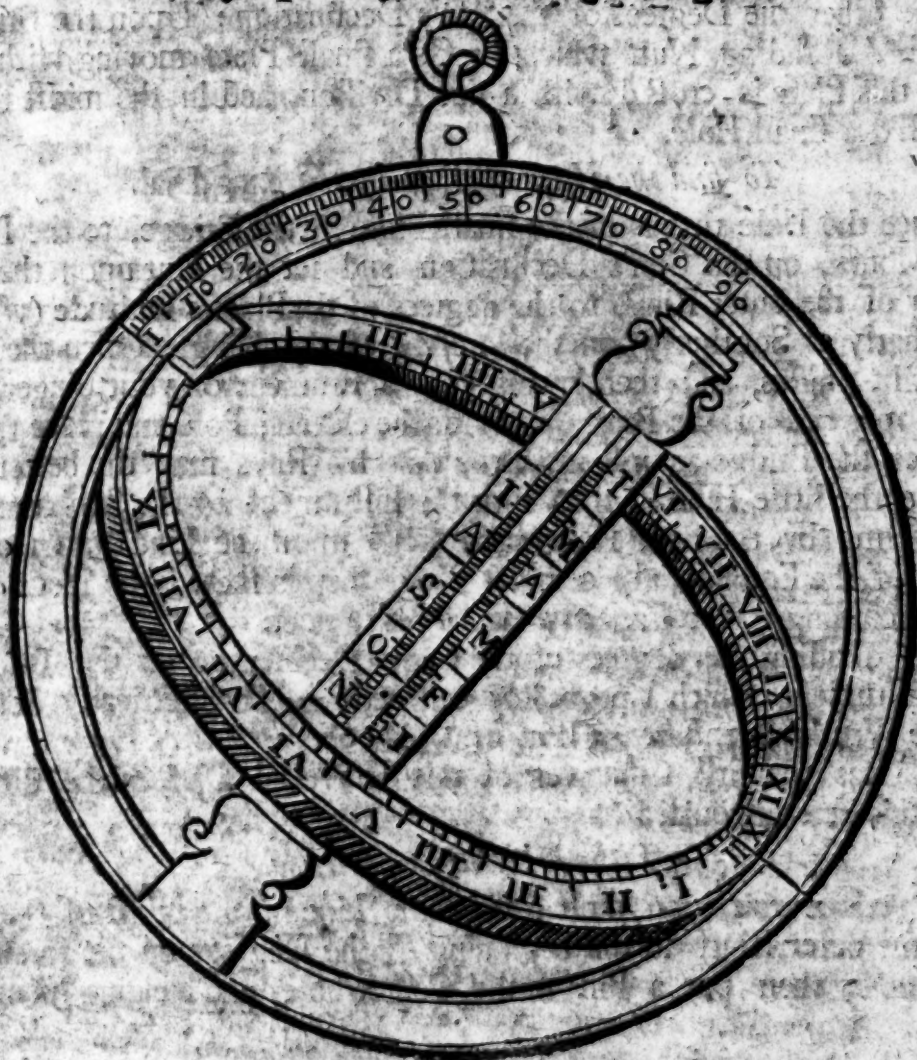
4. Let the Magnetical Rhomb be N. N. W. the Variation 10 deg. Westerly, I demand the true Rhomb?

Take the extent of 10 degrees, place it from N. N. W. towards the Left-hand, because the Variation is Westerly, it gives the true Rhomb N. N. W. 32 deg. 30 min. or almost N. W. by N.

5. Let the Course by the Compass be West, the Variation 10 deg. Westerly, I demand the true Course?

Take the quantity of the Variation 10 deg. place it from the West towards the Left-hand, which shews the true Rhomb to be S. 80 deg. W. or almost W. by S.

The Description of the Universal Ring-Dial.



This

THIS Instrument consists chiefly of two Rings, closely sitting within each other, and a Bridge, and is made either of Brass or Silver.

The outermost Ring represents the Meridian of the Place, and on the fore-side has one of its upper Quadrants divided into 90 degrees: likewise on the back-side a Semi-circle is divided into the like Number of degrees from the Hole or Center in the Circumference. On the Convexity of this Ring is fitted a Nut with a Wire-ring to it, having a small Line drawn in the middle of it, to move to any of the degrees on the fore-side.

The inner Ring (when they are open at Right-angles) represents the Equinoctial Circle, on the inside of which is drawn a Line in the very midst, and thereon are divided the Hours into Halves and Quarters, and are number'd with their proper Figures on the upper side of this Ring.

The Bridge represents the Axis of the World, in the middle whereof there is cut a long slit, upon one side are plac'd the Days of the Month, on the other the Degrees of the Sun's Declination: Upon the Bridge is contriv'd a sliding Nut, which directs a small Plate moving within the slit; this Plate is cross'd with a fine Division, and in the midst thereof is drill'd a small Hole.

To find the Hour of Day by the Ring-Dial.

Place the Hole that is on the small Plate on the Bridge, to the Day of the Month, on the Sun's Declination, and set the Nut upon the Convexity of the outer Ring, to the degrees of the Place's Latitude (whether Northerly or Southerly) on the fore-side of the Ring: Open the Rings to Right-Angles, and then having your Instrument on your Finger, turn the upper-end of the Bridge towards the elevated Pole, and place the flat side of the Bridge against the Sun, that his Rays may the better transpierce the little Hole; then turn the Instrument to the Sun, until the Sun-beams (by the little Hole) fall exactly upon the Line drawn on the inside of the Equinoctial, or inner Ring, then is shewn the Hour of the Day according to the Capacity of the Instrument.

The dividing the degrees of the Sun's Declination on the Bridge of this Instrument (which I proposely omitted) is Geometrically describ'd by the Worthy Mr. *Edward Wright*, in his *Corrections of Errors*, who, I think, was the first Contriver of this Universal Dial, altho' differing from this here discoursed of.

To find the Sun's Altitude.

To perform this, you must first set the Line in the midst of the Nut, upon the outer Ring, to the beginning of the Degrees on the fore-side of the same; then put a Pin in the Center-hole, and hanging your Dial upon

upon your Finger, turn the Edg of the outer Ring towards the Sun, so as the Shadow of the Pin may fall upon the Divisions on the back-side; the Degrees cut by the Shadow in the Sun's Altitude.

Note, If you use the Ring-Dial in South Latitude, you must place the Hole in the sliding Plate on the Bridge, to the Sun's Declination, using the South-Declination instead of the North, and the contrary.

CHAP. X. *Containing the Use of the Cross-Staff, and Quadrant : Likewise how to find the Latitude of a Place by the Meridian Altitude and Declination of the Sun : And the Use of the Nocturnal.*

The Figure of the Cross-Staff, and the Manner of the Observation.



THIS Instrument is of some Antiquity in Navigation, and is commonly used at Sea to take the Altitude of the Sun or Stars, which it performs with sufficient exactness, especially if it be less than 60 degrees; but if it exceed 60, it is not so certain, by reason of the length of the Cross, and the smallness of the Graduations on the Staff.

The Staff is made straight, four-square, and commonly of Box or Pear-tree, and graduated on the Sides with degrees or minutes.

The Crosses, usually four, are commonly made of the same Wood with the Staff, of a convenient breadth, and of length proportional to the Graduations, fitted to slide evenly upon the Staff, without jogging.

On one side of the Staff, the Graduations being about three degrees, and proceeding towards the Center or Eye-end, increase by every 10 minutes to 10 degrees; and this side is call'd the Ten-side; sometimes the breadth of the Thirty-Cross supplies the place of the Ten-Cross.

On

The Use of the Cross-Staff.

On another side of the Staff, the Divisions begin at about three 10° , and increase upwards to 30° ; this is call'd the Thirty-side.

On another side of the Graduations, begin about 20° ; and increase towards the end of the Staff to 60° ; this is nam'd the Sixty-side.

The remaining and fourth Side hath the Divisions beginning at 30° , and increasing upwards to 90° , from thence it is nam'd the Ninety-side, and his Cross (the longest) the Ninety-Cross.

Sometimes the several sides of the Staff are numbred likewise with their Complements to 20° in small Figures, viz. at 90° stands 00, against 80° 10° , at 70° stands 20, and so of the rest.

The Use of this is to take the Complement of the Altitude, or Zenith-distance from the Staff, without Subtraction.

A Table of the Lengths and Half Lengths of the Crosses, shewing the Measure of each Cross by the Graduation on the Staff, proving whether they be rightly made or not.

Crosses.		Whole Length of the Crosses		Half Length of the Crosses	
		Degrees.	Minutes.	Degrees.	Minutes.
10	From 10 30 60 90	08	48	02	12
30		19	47	23	52
60		30	00	40	13
90		36	52	53	07

An Example of the Sixty-Cross.

The length of the Sixty-Cross, if rightly made, must reach from 60° to $30^{\circ} 00'$; and his half Length to $40^{\circ} 13'$.

There are two ways principally for the graduating the Cross-Staff, one by Geometrical Projection, the other by Arithmetical Calculation.

I will give you an Example of the latter, by which you may divide any Staff, or at least be able to examine one that is already graduated.

Example of the Sixty-Cross.

Suppose the Length of the Sixty-Cross to be $10 \frac{1}{2}$ Inches, and the half Length $5 \frac{1}{2}$ Inches; I desire to know the distance of $45^{\circ} 30'$ from the Center of the Staff proportional to this Length of the Cross. Take half of $45^{\circ} 30'$, that is $22^{\circ} 45'$.

The Proportion is,

As the Tangent of $22^{\circ} 45'$	9.62256
Is to half the Length of the Cross. $5 \frac{1}{2}$ Inches,	0.70757
So is the Radius	10.00000
To the distance required. 12. 16. Inches,	1.08501

This

This gives the distance from the Center of the Staff, to the Division, representing $45^{\circ} 30'$ to be 12. 16 (or $\frac{1}{16}$) Inches.

But if you do propose to graduate a Staff, the more ready and expediate way is to divide the half length of the Cross into 100 or 1000 equal parts, and taking only the Tangent Complement of half the Angle requir'd, out of a Canon of Natural Tangents, gives the Distance requir'd.

Example. Suppose, as before, the half length of the Sixty-Cross to be $\frac{1}{16}$ Inches, and it is requir'd to know the Distance from the Center to $45^{\circ} 30'$?

The half-length of the Cross being divided into 100 equal Parts, or into as many as conveniency admits of the rest (supputated by Estimation) look into the Tables of Natural Tangents, for the Tangent Complement $22^{\circ} 45'$, (the half of $45^{\circ} 30'$) and you will find 238472; then cutting off two Figures towards the Right-hand, the Remainder 2384 shews the Number of equal Parts (whereof the Half-Cross contains 1000) which must be taken, to set off the Distance from the Center to $45^{\circ} 30'$, that is twice the half-length of the Cross, and 384 Parts more.

The like you may perform for any other Degree, to every tenth or fifth Minute, or less, according as the Staff will admit of the Divisions; and as you see in the Example of this Cross, so the like may be perform'd for any Cross of what length soever.

The Use of the Cross-Staff.

To take a forward Observation of the Sun's Meridian-Altitude at Sea.

When you do intend to take the Meridian-Altitude at Sea (in order to the obtaining of the Place's Latitude) it is convenient that you be preparing yourself for your Observation some competent time before Noon; and consider what the Sun's greatest Altitude may be that Day, accordingly to use those Crosses that may be most fit for your purpose.

As suppose the Meridian-Altitude for that Day be judg'd to be 20° , then use the Thirty-side of the Staff, and the Thirty-Cross; If you think it will be 30° , or more, then take the Sixty-Cross.

There is another Requisite fit to be understood before you proceed to Observation; and that is, how to place your Fore-Staff to your Eye, to prevent an Error mention'd by Mr. Wright, in his *Correction of Errors*; to avoid which, take these few Hints.

First, Place the Center of the Staff at A, to the out-side of the Corner of your Eye, as near your Eye as conveniently you can, without hindring your Sight, letting the End rest upon your Eye-bone, respecting as it were the Eye's Center, and cause the visual Rays to concur with the middle Parallels drawn on each side of the Cross-Staff, and then is your Staff rightly plac'd for Observation: But because this is somewhat

difficult plainly to be describ'd, and perhaps that which is already said may not be so obvious to the Reader as I could wish it. I will therefore give an easy Illustration, which may be verify'd by Experience.

Having first of all satisfy'd your self in the truth of the Divisions on the Staff, and likewise of the exact Length, and Half-length of your Crosses, then put on the Sixty-Cross, and place it to 30° on his proper Side, and also slip on your Ninety-cross, parallel with the former, and put that to 30° likewise, on his peculiar Graduations; then bring the End of the Staff to the Corner of your Eye (as is directed) and remove it so that you see each End of the two Crosses at once exactly to concur and agree with the visual Lines proceeding from your Eye; that is the place of your Staff in time of Observation, and may easily be found by frequent Trial.

Having thus prepar'd for your Observation, and acquainted your self with the Holding of your Instrument, being upon the Deck, turn your Face towards the Sun, and place your Staff to your Eye, holding the Cross upright, look at the upper-end of your Cross at C for the Sun, and at the lower at B for the Horizon: But if the Sea obscure the Horizon from your Sight, then remove the Cross a little further from your Eye, if on the contrary, your Sight do not extend so low as the Horizon, but the Sky only appears in the stead thereof, then move the Cross a little nearer your Eye, until by the upper part thereof you see the Center of the Sun, and by the lower Horizon, exactly at the same time; then look upon the proper side of the Staff (for the Cross you use) the Sun's present Altitude be cut by the same; and this if it were for one single Observation either of the Sun or any Star, were sufficient.

But the Sun's greatest Altitude being that you are to take, you must therefore wait (making your Observation as your Judgment shall direct you) until the Sun be upon the Meridian, still sliding the Cross nearer your Eye as the Sun rises, until you perceive it to be at the highest; for so soon as the Sun is to the Westward of the Meridian, and falling, if you make Observation again, you will find the Sea to obscure the Horizon from your Sight, and then in no Case remove your Cross, but let it remain fix'd, and finish your Observation for that Season.

Then cast your Eye upon that Side of the Staff belonging to the Cross you use, the Degrees and Minutes cut thereby, and number'd with larger Figures, (decreasing always from the Center of the Staff) gives the Sun's Meridional Altitude, and the small Figures underneath, the Complement of the Altitude, or the Zenith Distance.

In observing forward by the Cross-Staff, 'tis usual to have a peice of Red-Glass to defend the Sight from the Lustre of the Sun in time of Observation.

[It would, in my Opinion, be better to have the Glass fitted in a piece of Brass, and so to be put upon the end of any of the Crosses, as occasion requires. Thus much for a forward Observation.]

After the same manner you must observe the Altitude of the Stars.

To make a backward Observation of the Sun's Altitude by the Cross-Staff.

These Observations are frequent at Sea, especially with the *Hollanders*; and to perform this, you must have a Horizon-Vane, the inner-side of which fits upon the Center of your Staff, or else a sliding one according to the *Dutch Fashion*.

Likewise there is a Shoe of Brass to fit on the End of any of the Crosses, whose Use is the same with the Horizon-Vane in the Quadrant.

Having a Staff thus fitted, place the Horizon-Vane upon the Center or Eye-end of your Staff, and put on a Cross fittest for your purpose; fix the Brass-Shoe at the lower End thereof, then turn your Back to the Sun, and looking thro' the Sight (made by the Brass Shoe) on the end of your Vane, elevate or depress the end of your Staff, until the shadow made by the upper-end of the Cross, fall upon the upper-part of the sight in the Horizon-Vane; then look through that sight for the Horizon: But if the Sea obscure the Horizon from your sight, then remove your Cross a little nearer to the Horizon-Vane; but if on the contrary your sight doth not extend so low as the Horizon, but the Sky only appears instead thereof, then remove the Cross further from the Horizon-Vane, till you see the shadow fall upon its due place, and perceive the Horizon exactly at the same time, then have you the Sun's present Altitude.

If you observe for the Latitude, you must reiterate your Observation as before; and when you perceive the Sun to be past the Meridian, desist, and concluding your Observation, account your Degrees and Minutes, either of the Altitude, or its Complement, as is before shewn.

To use the Staff in a backward Observation, after the *Dutch Fashion*, there must be a Horizon-Vane fitted to slide evenly upon the Staff, and then all the variety from the former manner of Observation will be this:

Place any of your Crosses that you intend to use upon the Center of the Staff turning the Nut inward, then slide on your Horizon-Vane with the Nut inward, and fix on the Brass Shoe to the lower-end of your Cross; then proceed with your Observation, removing your Horizon-Vane, as before you did the Cross, and the Degrees and Minutes cut by the Edge of the Horizon-Vane, upon the side peculiar to the Cross you use, is the Sun's Altitude, or Complement thereof, as you reckon it in the greater or lesser Figures.

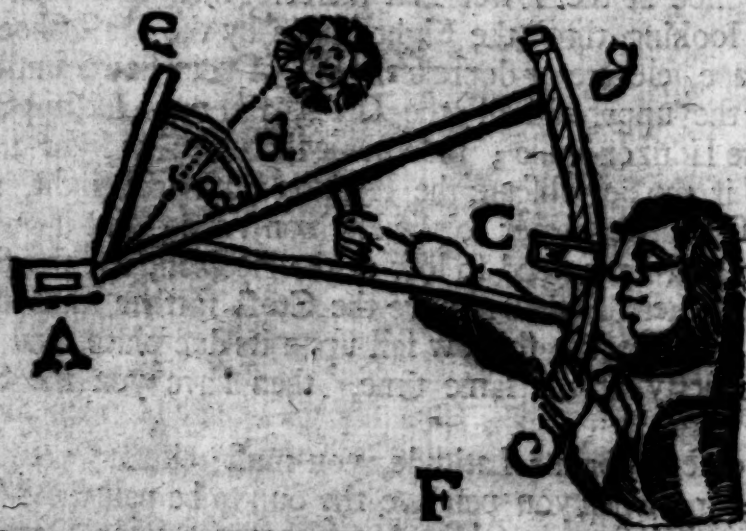
Sect. II. *The Description and Use of the QUADRANT.*

THIS *Quadrant* is of a very commodious Form and Contrivance, being at present the best approv'd, and most general Instrument that is in use, for observing the Sun's Meridian Altitude at Sea.

The Parts of this Instrument are principally Three Vanes, and Two Arches, which Arches together contain 90 Degrees, and give it therefore the Denomination of a *Quadrant*.

This Instrument is said to be first contriv'd by Captain *Davis*, (that was employ'd in Queen *Elizabeth's* time to discover the North-West Passage) and therefore call'd *Davis's Quadrant*, and by the *French*, the *English Quadrant*.

The Figure of the Quadrant, and Manner of Observation.



Of the Three Vanes; That which in time of Observation respects the Horizon, in this annex'd Figure represented by A, is call'd the Horizon-Vane; that which gives the Shadow, noted by B, is nam'd the Shadow and Horizon, distinguish'd with C, is called the Sight-Vane.

Of the Arches. The lesser noted with *d e*, is nam'd the Sixty-Arch, because it usually contains but 60°; it is of a small Radius (advise'dly so contriv'd) for the more apt placing of the Vane B thereon, that the Shadow thereof falling upon the Horizon-Vane A, at this short distance, might become the stronger, and the more perspicuous to the Eye of the Observer.

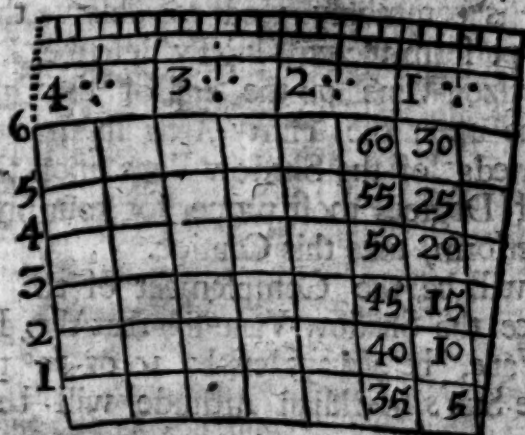
This Arch is commonly divided but to every Degree, and numbred from the upper-end of the Arch downwards to the Line of Partition, (which is a Line drawn on the middle of the upper Leg of the Quadrant, between

between the Two Arches) with 5, 10, 15, &c. And this is the Complement of the Altitude. Sometimes this Arch is figur'd with the Altitude from the Line of Partition upwards towards the higher end of the Arch, with 5, 10, 15, &c. to 60; but this is not frequently used.

The greater Arch, here denoted by the Letters *fg*, is call'd the Thirty-Arch; this Arch is of a large Radius, the better to be divided and subdivided into Degrees and Minutes, the Limb whereof is of a competent breadth; and thereon are usually describ'd several Concentrick Circles, intersected with Diagonal Lines, for the more facile and exact dividing the Degrees into every 5th, or every 2d Minute; and hereby the Subdivisions are conspicuous, and may readily be computed by the Observer.

But because possibly this manner of Division may not be understood by every One that has occasion for this Instrument, for their sakes therefore I have annex'd this following Figure.

The Figure of part of the Arch.



The foregoing Figure is part of the Limb of this Arch, as 'tis usually drawn upon the Limb of the Quadrant, each Degree being subdivided into 5 Minutes: upon the Plane of this Arch are describ'd 6 Concentrick Circles, and are noted with the Figures 1, 2, 3, 4, 5, 6. And in the Limits of each degree are drawn 2 Diagonals, intersecting these Circles; and those Diagonals divide each Degree into 2 parts, viz, into 30 Minutes; and the Concentrick Circles subdivide each of these Diagonals, representing 30 Minutes into 6 other Parts, being 5 Minutes a-piece: Therefore the 1st Intersection at 5, is 5 Minutes; the 2d at 10, is 10 Minutes; the 3d at 15, is 15 Minutes; the 4th at 20, is 20 Minutes; the 5th at 25, is 25 Minutes; the 6th at 30, is 30 Minutes: The 1st again at 35, is 35 Minutes; the 2d at 40, is 40 Minutes; at 45, is 45 Minutes; at 50, is 50 Minutes; at 55, is 55 Minutes, and at 60, 60 Minutes, or 1 Degree. And the like is to be understood of the rest, always as they ascend, increasing 5 Minutes.

And

And take this for a General Rule: First count how many concentrick Circles there are, which are 6 or 10, and are to be computed as is here shewn, and noted by the Figures at the end of this Scheme; then see how many Diagonal Lines are drawn within the extent of each Degree, which are 2 or 3; then multiply the Number of concentrick Circles, by the Number of Diagonals in 1 Degree, and by the Product divide 60, (the Minutes in a Degree) the Quotient shall give you the Number of Minutes that each intersection increases by, and is more than the precedent. As suppose the concentrick Circles to be 10, the Diagonals in each Degree 3; then multiply 10 by 3, the Product is 30, by which if you divide 60, the Quotient is 2, which shews that the intersections increase by 2 Minutes, the first representing 2 Min. and so 4, 6, 8 Minutes, &c. to 58 and 60 Min. or 1° ; and then 1° , 2° , 1° $4'$, 1° $6'$ &c. And the like is to be understood of the rest.

The Use of the Quadrant.

This Instrument is commonly used to observe the Sun's Meridian Altitude, which to perform we will briefly describe.

First, Put the Horizon-Vane on the end of the Quadrant on A, and then the Sight-Vane upon the Thirty-Arch in the precedent Figure; and lastly, the upper-edg of the Shadow-Vane upon the Sixty-Arch, to a certain Number of Degrees most proper for your present Observation; which readily to perform, take this Caution.

Consider what will be the Complement of the Meridian Altitude that Day, then place the Shadow-Vane so, that the Degrees cut by the upper-edg of the Vane, be always less by 10 or 15° then you judge the Complement of the Sun's Meridian Altitude will be that Day in the place of Observation.

For instance: Suppose that the greatest Altitude of the Sun for the time in the place of Observation, be estimated to be 45° , the Complement is 45° ; then place the Shadow-Vane at 30 or 35° deg. which are proper for your present Observation.

Having thus prepar'd your Instrument, and being ready upon the Deck, turn your Back towards the Sun, and holding the Quadrant as upright as you can, place the Sight-Vane to your Eye, and looking thro' the Sight, bring the Shadow of the upper-edge of the Shadow-Vane, to fall upon the upper-part of the Slit, or open Sight in the Horizon-Vane, and at the same time look thro' the said Slit for the Horizon; and if the Sea obscure the Horizon from your Sight, then slide your Sight-Vane a little lower down towards *f*; but if on the contrary, your Sight doth not extend so low as the Horizon; but if the Sky only presents itself to your Eye, then remove your Sight-vane a little higher towards *g*; then make Observation again, continuing to move your Sight-vane higher or lower according

according to these Directions, until looking thro' the Sight-Vane, the Shadow fall upon his due place, and that at the same time you exactly see the Horizon through the Sight in the Horizon-Vane, then have you the Sun's present Altitude. But it being the Meridian or the greatest Altitude that you are to observe, you must therefore continue to make Observation as often as you shall think fit, (but especially you are to tend your Observation, when you perceive the Sun almost upon the Meridian) until the Sun be to the Westward of the Meridian, and is lessening his Altitude; for then, if you make Observation, the Sky will be seen and not the Horizon; and in this Case you must not alter your Sight-Vane, but letting it stand, conclude your Observation for that Season: Then cast your Eye upon the Thirty-Arch, and see how many Degrees and Minute are cut by the Inside of the Sight-Vane, and thereto add the degrees at the upper-edg of your Shadow-Vane, the Sum is the Complement of the Altitude, or the Sun's Distance from the Zenith.

Note: The small Arch in some Quadrants contain 70 degrees, and the greater 20 degrees, whose Sum is 90. These Arches are numbred and divided like the former; and if that be well understood, this will not seem obscure, and therefore it is needless to say any more of this Alteration.

And here Note, That there is a late Contrivance with a small Convex-Glass to be let into the Shadow-Vane, which may be used when the Sun is hazy, and will not strike a clear shadow upon the Horizon-Vane; then this Glass will contract the Beams of the Sun, and reflect a small speck of Light upon a small black Line drawn on the Horizon-Vane, which respects the Center of the Sun. And further *Note,* That in those Observations made by the upper-edge of the Shadow-Vane it is proper to subtract 16 min. or somewhat less, from the Sun's Altitude, or add it to the Zenith Distance (for the Semi-diameter of the Sun), but in using the Glass you are not to make any such Allowance, because the Speck represents the Center of the Sun.

SECT. III. *Rules for finding the Latitude of the Place by Observation of the Sun's Meridian Altitude, or Zenith Distance, by help of the Table of the Sun's Declination.*

BECAUSE 'tis common to work the Observation of the Sun, taken by the Quadrant, and other Instruments now in use, by the Complement of the Meridian Altitude, or the Sun's Distance from the Zenith, I shall therefore give Rules, illustrated with Examples, for that purpose.

Rule 1. If the Sun comes to the Meridian in the South, and have South-Declination, subtract the Declination from the Complement of the Meridian Altitude, the Remainder is the Latitude of the Place of Observation Northerly: But if the Declination exceed the Zenith Distance, then subtract

subtract the Zenith Distance from the Declination, the Remainder is the Latitude Southerly.

Example 1. Admit you are at Sea, and the Sun being upon the Meridian in the South, is 37 deg. 30 min. distant from the Zenith, and at the same time hath 12 deg. 00 min. South Declination; I demand the Latitude of the Place.

The Operation.

Complement of the Meridian-Altitude	— 37° 30'
The Sun's Declination South, subtract	— 12 00
The Latitude of the Place	— 25 30 North.

Example 2. Admit (being at Sea) the Sun being on the South part of the Meridian, is 10 deg. distant from the Zenith, and the Declination 20 deg. 30 min. South: I demand the Latitude of the Place.

The Operation.

The Sun's Declination	— 20° 30'
The Distance from the Zenith, subtract	— 10 00
The Latitude	— 10 30 South.

Rule 2. If the Sun be upon the Meridian in the South, and hath North-Declination, then add the Declination to the Zenith-distance, the Sum is the Latitude Northerly.

Example. Admit a Ship at Sea, and the Sun on the South-part of the Meridian is 30 deg. 30 min. from the Zenith, and the Declination is 15 deg. 30 min. North; I demand the Latitude?

The Operation.

The Compl. of the Alt. or Zenith-dist. is	30° 30'
The Declination added	— 15 30
The Latitude	— 46 00 North.

Rule 3. If the Sun be on the Meridian in the North, and have North Declination, then subtract the Zenith-distance from the Declination, the Remainder is the Latitude Northerly: but if the Zenith-distance exceeds the Declination, then subtract the Declination therefrom, the Remainder is the Latitude Southerly.

Example 1. Suppose the Declination were 20 deg. North, and the Zenith-distance 12 deg. 30 min. the Sun being upon the Meridian in the North; I demand the Latitude?

The Operation.

The Sun's Declination North	— 20° 00'
The Zenith Distance subtracted	— 12 30
The Latitude of the Place	— 07 30 North.

Example 2. Suppose the Sun's Declination to be as before, 20 deg. North, and that being upon the Meridian to the Northwards, his Zenith Distance is 40 deg. 15 min. I demand the Latitude?

The Operation.

The Zenith distance of the Sun is	— 40° 15'
The Declination North subtract	— 20 00
The Latitude	— 20 15 South.

Rules for working of Observations.

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Rule 4. If the Sun be upon the Meridian in the North, and hath South Declination, then add the Declination to the Zenith Distance, the Sum is the Latitude Southerly.

Example. Admit the Sun's Declination were 16 deg. 45 min. South, and the Zenith Distance 29 deg. 45 min. I demand the Latitude.

	The Declination of the Sun South ————	16° 45'
The	The Zenith Distance add ————	29 45
Operation.	The Latitude ————	46 30 South.

Rule 5. If the Sun have no Declination, then the Complement of the Altitude is the Latitude of the Place; and if the Sun be on the Meridian in the South, your Latitude is Northerly; if in the North, Southerly. This needs no Example.

Rule 6. If the Sun be in the Zenith, *i. e.* 90 deg. above the Horizon, then the Declination either Northerly or Southerly, is the Latitude of the Place. This likewise needs no Illustration.

Rule 7. If you be within the Arctick, or Antartick Circles, and observe the Sun upon the Meridian under the Pole, then add the Sun's Declination to the Complement of the Altitude, and subtract the Sum from 180°, the Remainder is the Elevation of the Pole.

Note. If your Instrument wherewith you observe give only the Meridian Altitude, then subtract that Altitude from 90 deg. the Residue is the Zenith Distance, or Co-Altitude of the Sun; and the Operation is the same as the precedent Examples.

For the Stars.

What hath been here delivered in these Rules, concerning the Sun's being upon the Meridian, the same is to be understood of any Star whose Declination is known.

Admit you should observe the bright Star *Arcturus*, whose Declination is 20 deg. 58 min. North, when he is upon the Meridian in the South, and find his Altitude to be 65 deg. 25 min. the Compl. thereof 24 deg. 35 min. is the Zenith distance; then adding 20 deg. 58 min. to 24 deg. 35 min. the sum 45 deg. 33 min. the Latitude Northerly, according to the second Rule foregoing.

But if you observe by any of the Stars near the North-Pole, whose Polar-distance is set down in the Tables of Declination; and if they be on the Meridian under the Pole, add the Complement of the Declination, or Polar-distance, to the Meridian-Altitude found, the sum is the Latitude Northerly.

But, *Secondly*, if you observe any Star that is upon the Meridian in the North above the Pole, then from the Meridian-Altitude of that Star, subtract the Complement of the Declination, or Polar-distance, the Remainder is the Latitude Northerly: But if the Complement of the Star's

Declination cannot be subtracted from his Meridian-Altitude; subtract the Meridian-Altitude therefrom, the Remainder is the Latitude Southerly. The same may be understood of Stars near the South-Pole.

Here I thought it necessary to mention something of the *Crofters*, which are certain Stars that are of good use in the Southern Navigation; they are so called, because they do somewhat resemble the Form of a Cross, according to the annexed Figure.

The Figure of the Constellation called the Crofters.

The Head *A* of Declination from the South-Pole $34^{\circ} 45'$

The *Cock's Foot*, Declination from South-Pole $28^{\circ} 45'$.

The Star at *C*, call'd the *Cock's Foot*, or rather the *Cross-Foot*, whose Declination, according to the Observation of Mr. *Edmond Halley*, at *St. Hellena*, is $61^{\circ} 15'$ Southerly; and so the Compl. of the Declination or Polar-distance, is $28^{\circ} 45'$ min. By this Polar-distance, and the Meridian-Altitude of this Star, when he is either above or below the Pole, you may find the Latitude of the Place by the Rules of the Stars last mention'd. The Polar-distance of the Head of the Cross, is $34^{\circ} 45'$ min.

To know when these Stars are fit for Observation, hold up a Thread and Plummets; and when the Thread cuts the Star at *A* and that at *C* both at the same time, then they are upon the Meridian, and fit to be observed.

Sect. V. *The Description and Use of the Nocturnal.*

THIS Instrument consists of Three Parts:

First, The broadest and greatest, which we may call the unmoveable Part, which hath a handle to hold it by, in time of Observation.

Secondly, The first moveable, or middle Part.

Thirdly, The long Index, that is to turn to the Position of those Stars for which they are made, *viz.* the Guards of the *Little* or *Great-Bear*.

The fore-side of the first, or unmoveable Part, hath the Limb, or outward Circle divided into 12 Months, and each Month subdivided into its respective Days, and are counted towards the Left-hand, and mark'd with their Names, or the first Letter thereof, as *J* for *January*, *F* for *February*, *M* for *March*, &c. And upon some of them there are two other Circles, the outermost of which is divided into 24 equal Parts, or Hours; and the other into 29 Parts and a half, or Days of the Moon's Age; by which the Moon's Southing may be known; by Inspection, and thereby a Computation of the Tides.

The Use of the Nocturnal.

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Of these *Nocturnals* there are two sorts, one for the Guard of the *Little*, the other for the Guards of the *Great-Bear*, or *Charles's Wain*, commonly call'd the two *Pointers*. Now to know for which of these Constellations any *Nocturnal* is made, you may observe, that the *Nocturnals* that are for the Guards of the *Great-Bear*, have the 17th of *February* on the Top; and if it be for the Guard of the *Little-Bear*, then you will find the 21st of *April* there. The back-side of this Part is divided into the 32 Points of the Compass, which are to shew the bearing of Guards, thereby to know what Declination the North-Star hath upon any Point of the Compass.

The second and moveable Part hath a Tooth proceeding from it, with the edg continu'd in a right Line from the Center; which is to be turn'd to the Day of the Month at pleasure; and on the Superficies thereof is a Circle divided into 24 equal Parts or Hours; which when the said Tooth is set to the Day of the Month, and the Index turn'd to the Position of the Guards, the straight side of the Index will shew the Hour of the Night upon the said Circle.

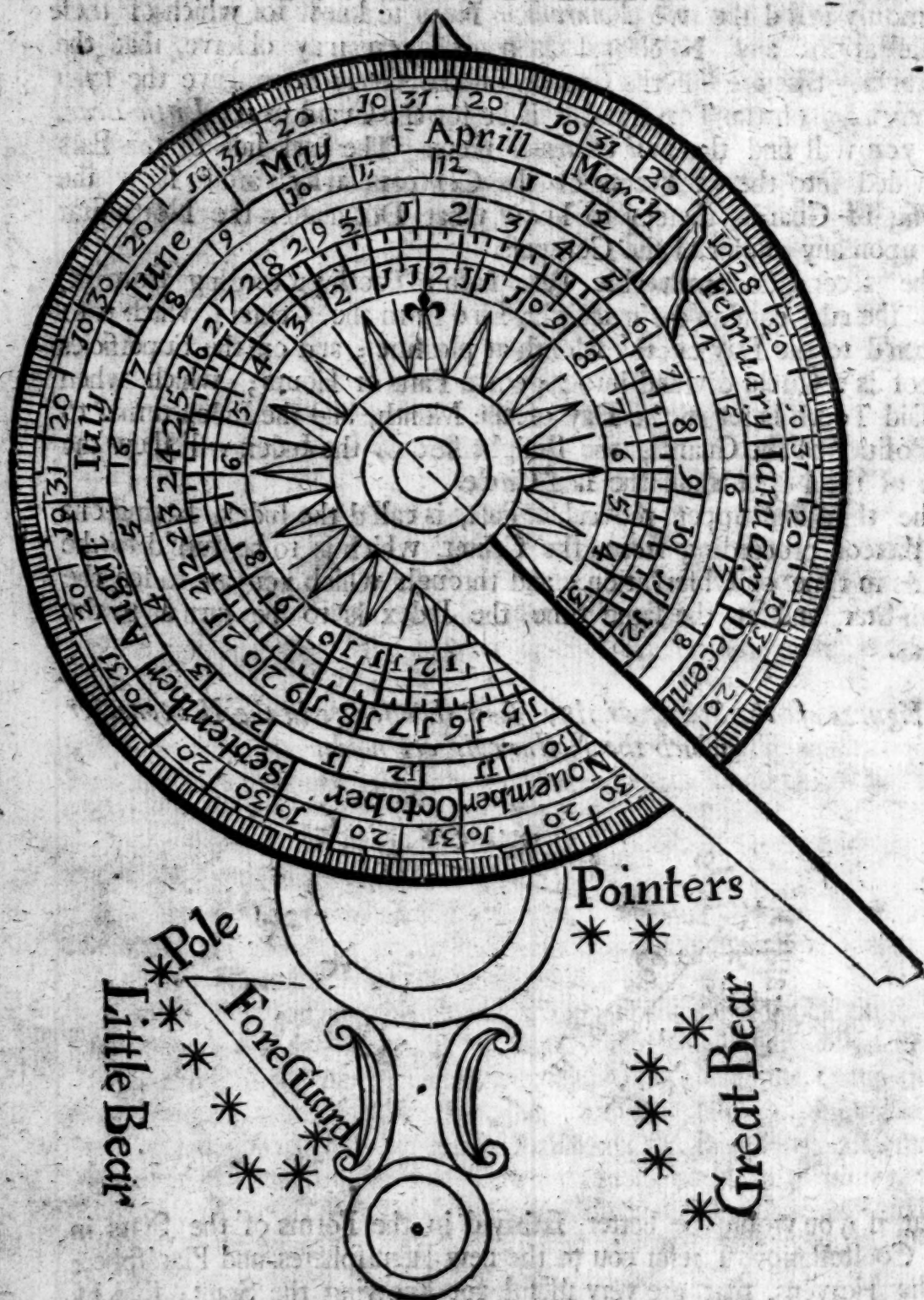
The third and upper moveable Part, is call'd the Index, having one side thereof proceeding from the Center, which is to be turn'd to the Guards in time of Observation; and through which you are to see the North-Star, and at the same time the Index is to be turn'd to the Guards.

The Figures of the Stars, as they shew themselves in the Heavens, for which the Nocturnals are made.



But if you would be better satisfy'd in the Forms of the Stars in each Constellation, I refer you to the new Hemispheres and Planisphere of the Heavens, that are very useful for knowing the Stars; sold by the Author.

The Figure of the Nocturnal.



Here followeth a Table for the Declination of the North Star, upon every Point of the Compass the Guards are upon, fitted for both sorts of Nocturnals.

If the former of the Guards be ascending from the North, or lower part of the Meridian.	Points of the Compass.	For the guard of the Little Bear.		If the after-Wheels, or two Pointers be ascend. from the North, or lower part of the Merid.	For the guards of the great Bear, or aftermost Wheels in Charle's Wain, called the two Pointers.	
		D. M.	The North Star is above the Pole.		D. M.	Above the Pole.
If the former of the Guards be descending from the South; or upper part of the Meridian.	North.	2	09	If the two Pointers be descending from the South, or upper part of the Meridian.	2	20
	N. by E.	1	52		2	20
	N. N. E.	1	29		2	35
	N. E. by N.	1	02		2	33
	North East.	0	35		2	26
	N. E. by E.	0	06		2	13
	E. North E.				1	55
	E. by N.	0	22		1	33
		0	52		1	07
	East.	1	18		0	38
	E. by S.	1	41		0	08
	E. S. E.	2	01		0	29
	S. E. by E.	2	16		0	28
	South East.	2	25		1	20
	S. E. by S.	2	30		1	44
	S. S. E.	2	29		2	04
	S. by E.	2	22		2	20
	South.				2	30
	S. by W.	1	55		2	35
	S. S. W.	1	34		2	33
	S. W. by S.	1	10		2	26
	South West.	0	43		2	13
	S. W. by W.	0	14		1	55
	W. S. W.	0	15		1	33
	W. by S.	0	44		1	07
	West.	1	11		0	38
	W. by N.	1	36		0	08
	W. N. W.	1	58			
	N. W. by W.	2	14		0	22
	North West.	2	25		0	52
	N. W. by N.	2	30		1	20
	N. N. W.	2	29		1	44
	N. by W.	2	22		2	04

The North Star is under the Pole.

Above the Pole.

The

The Manner of holding the Nocturnal in Time of Observation.

Take the Handle in your Hand, with the fore-side towards you, holding of it upright in your Hand, (which you may discern by the Tip that is on the very top of the Nocturnal) then looking through the Hole in the Center to the North-Star, you must turn the upper Edg of the Index (which cometh from the Center) to the Guards; this being understood, you may now proceed to the several Uses thereof.

To find the Hour of the Night by the North-Star, and the Guards either of the Little or Great-Bear, and upon what Point of the Compass they are.

To perform this, you must first set the Index of the second moveable Part to the Day of the Month, (then if it will not stay of it self, you must stay it with your Thumb) holding it as you are before directed; find the North Star through the Hole, and turn the Index to the Guards, and then upon the second moveable Part, the edg of the Index shall cut the Hour of the Night. At the same time you will find on the back-side what Point of the Compass the Guards are upon, so that you may know also what Distance the North-Star hath at that time, either above, or under the Pole.

To find the time of the Moon's coming to South any day of her Age, and also the Time of High-water that Day.

First, find the Moon's Age on the moveable Part, and right against it in the Circle of Hours, you will find the time of the Moon's Southing.

Suppose the Moon were eight days old, I demand the Time of her coming to South.

Therefore look for 8 on the Circle of her Age, and right against it you will find in the Hour-circle, almost half an hour past 6 of the Clock in the Evening (because that always between the Change and the Full she cometh to South in the Evening, but after the Full she cometh to the South in the Morning): So having found the Moon's Southing, if you add thereto the Hour of the flowing at any place, it will shew you the Time of High-water that Day.

Example. Suppose here at London, the Moon being 8 Days old, I find by the Nocturnal, that the Moon cometh to South at almost half an Hour past Six of the Clock; to which I add three Hours, the Time of High-water at the Full and Change, which makes Nine of the Clock and almost half an Hour past, the Time of High-water at London-Bridge, that Day of the Moon's Age.

And if those Numbers being added together should exceed 12, that 12 must be subtracted from it, and that will be the Time of Full-Sea.

As suppose the Moon should be 13 Days old, at which time I find by the Nocturnal that the Moon cometh to the South at 10 of the Clock,
and

and almost half an Hour, unto which if you add 3 it makes 13 Hours and a half; from which if you take 12, there remains 1 of the Clock, and almost half an Hour, the Time of High-water at London-Bridge, according to the common way of Computation.

And to know the Time of Full-Sea at any other Place, I refer you to the Tide-Tables.

Chap. XI. *Containing the Use of the Plain Scale, Gunter's Scale, Sinical Quadrant, Plain Chart, Mercator's Chart, of both Globes, and likewise the secret Properties of the Load-stone.*

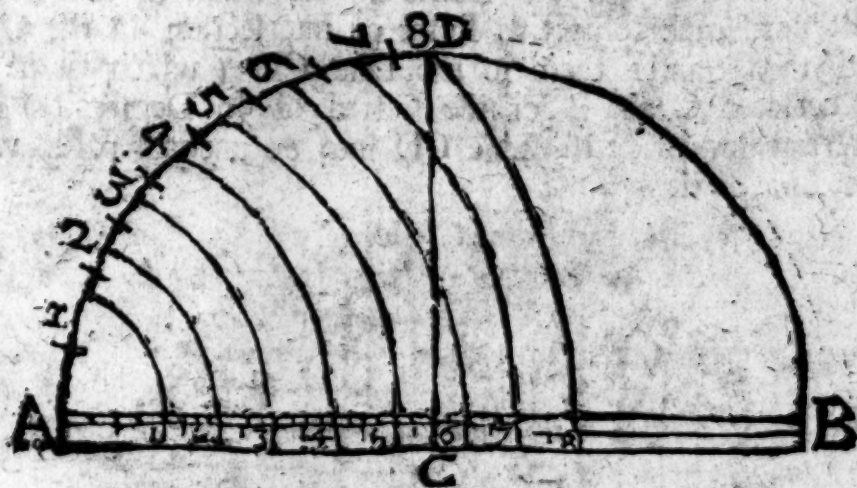
The Description and Use of the Plain-Scale.

THE Use of this Instrument is facile and delightful, and serves the Construction of Problems in *Navigation* and *Astronomy*.

The Lines on a *Plain-Scale* are usually a Line of equal Parts, Chords, Rhombs, and Longitude; but on this here described, are likewise a Line of Sines, Tangents, and Secants. Plate 6. Fig. 25.

We shall here insert the Projection of these Lines on the Scale.

The Line of Rhombs.



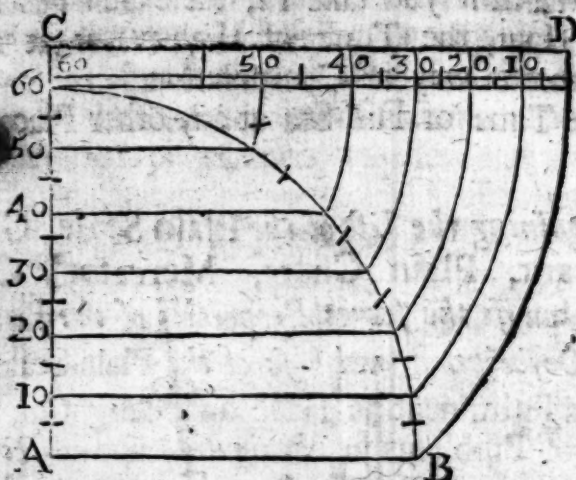
The Projection of the Line of Rhombs.

For the dividing of the Line of Rhombs, first draw the line ACB, and upon the Point C describe the Semi-circle ADB, and divide the Quadrant AD into 8 equal parts: which being done, set one foot of your Compasses in the Point A, and with the other foot extend to each of those Divisions, and transfer those Extents unto the line ACB, which will divide the said line into 8 unequal parts, which will be a line of Rhombs, and to number with 1, 2, 3, 4, &c. unto 8: And so the Halves and Quarter-points of the Compass are to be inserted.

The

The Line of Sines.

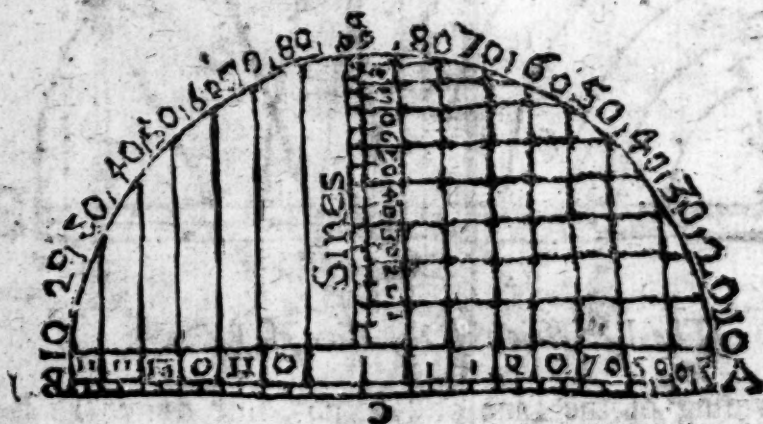
The Line of Longitude.



The Proportion of the Line of Longitude.

First, draw the Quadrant CAB, and divide the Side CA, into 60 equal Parts, then through each of those equal parts draw Lines parallel to the Side AB, until they touch the Quadrant CB; which being done, set one foot of your Compasses in the Point C, and extend the other foot unto each respective Point of Interfection in the Quadrant CB, and then tranfer them to the Line CD (which is to be the Distance between C and B, or the Chord of 90 Degrees;) so shall those Interfections divide the Line CD into 60 unequal parts, which is called the *Line of Longitude*.

The Line
of Sines.



The Projection of the Line of Sines is thus to be performed; First draw the Line ACB, and upon C draw the Semi-circle, and one of the Quadrants divide into 90 Degrees, as the Quadrant ADC; then draw a line through each tenth Degree of the Quadrant parallel to the line ACB, it will divide the line DC into 90 unequal parts, which will be a Line of Sines, to be numbred from C towards D, with 10, 20, 30, &c. unto 90.

The

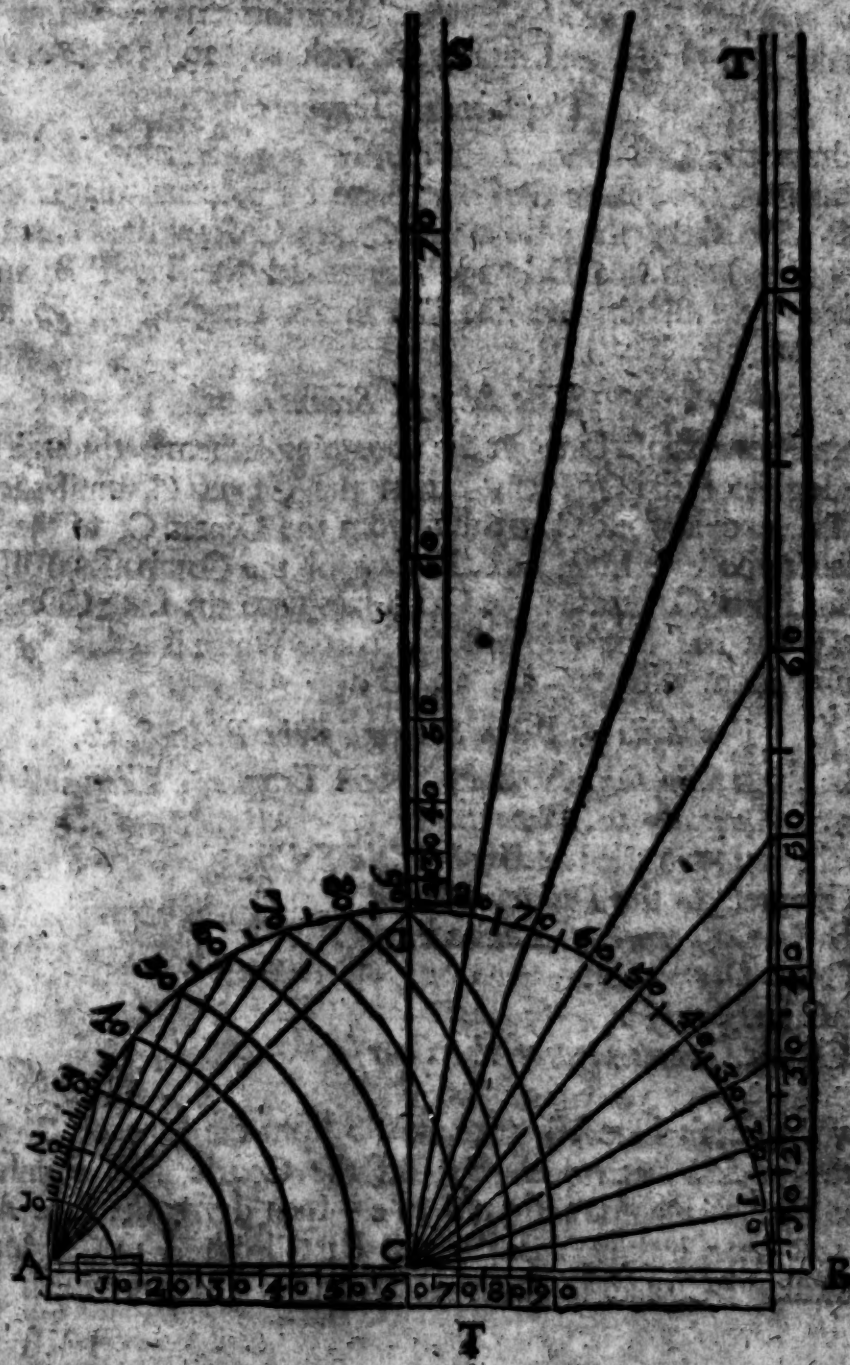
The Projection of the Line of Chords.

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The Lines of Versed Sines.

The Projection of the *Line of Versed Sines*, is thus to be affected: First, draw the line ACB, and upon C describe the Semi-circle ADB, which divide into 180 Degrees; then through each Deg. drawing Right Lines parallel to the Line DC, they will divide the Line AB into 180 unequal Parts, which will be a Line of Versed Sines, to be numbered with 10, 20, 30, 40, &c. unto 180.

The Line of Chords.



For the Projection and Division of the Line of Chords, you must first draw the Diameter ACB in the foregoing Scheme, and upon the Center C describe the Semi-circle ADB; which Semi-circle divide into two Quadrants by the point D, then divide the Quadrant DA into 90 equal Parts or Degrees; this being done, set one foot of your Compasses in the point A, and the other be extended to each degree of the Quadrant AD, which Extents transfer unto the line ACB, as you may see the Arches lead in the foregoing Figure. This Line so divided into 90 unequal divisions, is called a *Line of Chords*. After this manner you make it of what Radius you please, and number it with 10, 20, 30, &c.

The Line of Tangents.

First draw the Quadrant, as in the foregoing Scheme, and divide it into 90 degrees, and from the Point B erect a perpendicular Line, as the innermost Line TB; then from the Center C draw lines through each degree of the Quadrant CDB, until they touch the line TB, and those Intersections will divide the line TB into a Tangent, to be numbred with 10, 20, 30, &c.

The Line of Secants.

Having drawn those Lines in the foregoing Scheme, through each respective degree of the Quadrant, from the Center C, until they touch the line TB, extend your Compasses from the Center C, to the extremity of each respective Line, and the foot of the Compasses still remaining in the Point C, transfer the said Lines unto the Line CDS, so shall they divide the said line into unequal parts, which is a *Line of Secants*, and number them with 10, 20, 30, &c.

Problems of Plain Sailing by the Plain Scale.

PROB. I. *A Ship sails N. E. by E. 108 Leagues; I demand the Difference of Latitude and Departure.*

In the following *Problems of Plain Sailing.*

AC represents the *Distance sailed.*

AB the *Difference of Latitude.*

BC the *Departure.*

BAC the *Course.*

ACB the *Complement of the Course.*

Plate 6. Fig. 26.

Draw the occult Line AB, take off 60 from the Line of Chords, and sweep the prick'd Arch d e. Set off the Course five Points, taken from the Line of Rhombs, from d to e; then draw the Line AeC. and set off 108 Leag. by the Line of equal Parts from A to C; let fall the Perpendicular BC, and so finish the Triangle ABC, in which you will find

find the diff. Lat. A B 60 Leagues; the Departure BC 90 Leagues.

PROB. II. *A Ship sails N. E. by E. until her difference of Latitude be 60 Leagues; I demand the Distance and Departure?*

Plate 6. Fig. 26.

Draw AB of the given Length, and raise the Occult Perpendicular BC, set off the Course five Points, as in the former Problem. Draw AC until it meet with BC, and finish the Triangle; the distance is 108 leagues, and the Departure 90 leagues.

PROB. III. *A Ship sails N. E. by E. until her departure be 90 Leagues; I demand the distance and difference of Latitude?*

Plate 6. Fig. 27.

Draw the occult Line AB, and raise the Perpendicular BC of the given Length 90 Leagues; then upon the Point C sweep the Arch de with the Chord of 60°, and place the Complement of the Course three Points from d to e; then draw CeA until it met with AB, and finish the Triangle. The Distance is 108 Leagues, the difference of Latitude 60 Leagues.

PROB. IV. *A Ship sails between the North and the East 108 Leagues, until the Difference of Latitude be 60 Leagues; I demand the Course and Departure?*

Plate 6. Fig. 28.

Draw AB 60 leagues, and raise the occult Perpendicular BC, take off the Length of AC the Distance 108 Leagues, and placing one point of your Compasses at A, describe the Occult Arch cutting the Line BC at the point C, by which draw AC, and finish the Triangle; the Departure BC is 90 Leagues; with a Chord of 60° sweep the Arch de, which measured upon the Line of Rhombs, will be found five Points, the Course sought.

PROB. V. *A Ship sails between the North and the East 108 Leagues, until her Departure be 90 Leagues; I demand the Course and Difference of Latitude?*

Plate 6. Fig. 28.

Draw the occult Line AB, and raise the Perpendicular BC of the given Length 90 Leagues; take AC 108 Leagues, and setting one Point of the Compasses at C, describe the occult Arch, cutting the Line AB at A, by which draw AC, and finish the Triangle. The Course is found five points, measured as in the former Problem, the difference of Latitude 60 Leagues.

PROB. VI. *A Ship sails between the North and East, until the difference of Latitude be 60 Leagues, and the departure 90 Leagues; I demand the Course and Distance?* Plate 6. Fig. 28.

Draw AB 60 Leagues, raise the Perpendicular BC 90 Leagues, and by the Points A and C draw AC, and finish the Triangle. The Course is found 5 Points, as in the 4th Problem, the Distance 108 Leagues.

PROB. VII. *There are two Ports that bear S.W. by S. and N.E. by N. distance 40 Leagues; A Ship sails from the Northermost of them, first South, and then West by South, sometimes upon one of those Courses, sometimes upon the other, until she arrive at the Southermost Port; I demand how many Leagues she hath sail'd upon one Course, and how many upon the other?* Plate 6. Fig. 29.

Let A represent the Northermost Port, and E the Southermost, AE their distance, AD the distance sail'd upon the South Course DE, the distance upon the W. by S. Course.

Draw the Line AE 40 Leagues, being a N.E. by N. and S.W. by S. Line, describe the Arch fg, setting off three Points, and draw the occult Line AD, being a South Line; then sweep the Arch, hl, and set off four Points, drawing the occult Line DE, until it meet with AD, and so finish the Triangle ADE. The Distance sail'd South is 29 Leagues, and W. by S. is 22 Leagues.

PROB. VIII. *There are two Islands that bear East and West, and are distant 40 Leagues; A Ship sails from the Westermost N.E. by E. and then sailing 22 Leagues and a half farther, arrives at the Eastermost Port; I demand the Distance sail'd upon the first Course, and what was the second Course?* Plate 6. Fig. 29.

Let A represent the Westermost Port, E the Eastermost, D the Place where the Ship altered her Course, making the best of her way; AD the N.E. by E Course; DE the other Course unknown: Draw AE 40 Leagues, set off an Angle of three Points, and draw AD, the N.E. by E. Line occultly; take the distance 22 Leagues and a half, and placing one Point of your Compasses in the Point E, cross the Line AD in the Point D, draw DE, and finish the Triangle. The Distance upon the first Course is 29 leagues, the Angle at E is four Points, therefore the second Course S. E.

PROB. IX. *Two Ships sail from the same Island, the first sails N.W. by N. 22 leagues and a half, the second W. by N. 40 leagues, and arrive at their several Ports; I demand the Bearing and Distance of those Ports.*

Plate 6. Fig. 29.

E represents the Island, D the Northermost Port, A the Westermost.

Draw.

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Draw AE 40 leagues, and set off the Angle at E four Points, and draw DE 22 leagues and a half; then by the Points D and A draw AD, and finish the Triangle. The Angle at A is three Points, which shews the Bearing of the Ports to be E. N. E. and W. S. W. and the Distance AD almost 29 leagues.

PROB. X. *A Ship sails from a certain Port W. N. W. 22 Leagues and a half, and then more Southerly 29 Leagues and then she is forc'd back again to the Port from whence she came 40 Leagues; I demand her Course from the second Place to the third, and how she steer'd back again?*

Plate 6. Fig. 29.

E represents the first Port, D the Place where the Ship altered her Course, A the Place where she was driven back.

Draw the Line DE 22 Leagues and a half, take the Distance AD 29 Leagues placing your Compasses in D, describe the occult Arch at A, and take the distance A E 40 Leagues; describe another occult Arch from E crossing the former in the Point A; draw A E and A D, and finish the Triangle. The Arch mn is 9 Points, therefore the Course from the second Place to the third, is S. W. by S. and she steer'd back again to the first Port E. N. E.

Here follow some Problems of Mercator's Sailing, wrought two ways.

First, by the Plain Scale only, by taking the middle Latitude, which is not exactly true, but may serve as an Approximation in a single Course provided the Distance be but small, otherwise 'tis too gross.

The second way is by the Meridional Parts, which will be exact according to the Capacity of the Instrument.

The Use of the Plain Scale in Mercator's Sailing by the middle Latitude.

PROB. I. *A Ship being in the Latitude of 40° , sails a N. Westerly Course, until she come into the Latitude $45^{\circ} 30'$, the Difference of Longitude 90 Leagues; I demand the Course, Distance, and Departure?*

Plate 7. Fig. 30.

For the Solution thereof by the Plain Scale, first draw the Line ACB, and upon the Center C describe the Semi-circle ADB, and cross the Line ACB at Right-Angles with the Line ECD; then find the middle Latitude, by taking the Half-Sum of both Latitudes added together, which you will find to be $42^{\circ} 45'$, which middle Latitude set off from D to M and L both ways, and draw the Line ML; then set the Distance D F from B to G, then set off the Difference of Latitude 110 Leagues from B. to H, and from G to A, and upon the Point A erect

a Perpendicular, as A K, and from A set off the Difference of Longitude in Leagues, which is 90; from the Point K draw the Line K G, then from the Point H, erect an occult Perpendicular, as the Line H I; then laying a Ruler from the Point B to the Point E (where the Line B K doth cut the Line EC) and draw the Line B I; then upon the Point B describe the Occult Arch C n, which being measured on the Line of Chords, will be found to be 31° or two Points three Quarters, which is the Course required, N. N. W. three Quarters Westerly: and the Line B I is the Distance required, which being measured upon the Line of Leagues, will be found to be 129 Leagues, and the Departure H I 66 Leagues.

PROB. II. *A Ship being in the Latitude 40° North, sails N. N. W.; (or 7° Westerly) until she come into the Latitude of $45^{\circ} 30'$; I demand the Distance run, the Difference of Longitude, and the Departure?* Plate 7. Fig. 30.

In the Solution of this Problem by the Plain Scale, draw the Line A B, at any convenient Length, and upon C describe the Semi-circle ADB, and find the middle Latitude as before, and set it off from D to M and L, and draw the Line M L, and upon the Point B describe the obscure Arch C n, and set off the Course given, (which is 2 Points three quarters, or 31° and a quarter) from C to n, and set the distance CF from C to G, and from B set off the Difference of Latitude 110 Leagues, and the same Distance from G to A, and from the Points H and A erect the two perpendiculars H I and A K; then through the Point n, draw the Line B I, which being measured in the Scale of Leagues, will be found to be 129; then laying a Ruler from G to the Intersection of the Lines at F, draw the Line G K, and note where it intersecteth the Line A K, which is at K: So the Distance A K being measured upon the Scale of Leagues, will be found to be 90 Leagues, the Difference of Longitude sought, and H I the Departure 68 Leagues.

PROB. III. *A Ship being in the Latitude 40° North, sails between the North and the West, until she arrive to the Latitude $45^{\circ} 30'$, and that her Distance run be 129 Leagues; I demand the Course, Difference of Longitude, and Departure?* Plate 7. Fig. 30.

For the Solution of this Problem, first draw the Line A C B at any convenient length: and upon C describe the Semi-circle ADB, and set off the middle Latitude as before, and likewise the Distance CF from C to G, also the Difference of Latitude in Leagues from B to H, and from G to A; then erect the two Perpendiculars at H and A, then take the

the Distance between the Compasses, and set one foot of the Compasses in B, and extend the other Foot towards I, until it doth intersect the Perpendicular at H, in the Point I, and draw BI; then laying a Ruler upon the Point G, unto the Intersection of the Lines at E, draw the Line GK, and note where it doth intersect the Perpendicular at A, which will be at K; then the Distance KA being measured on the Scale of Leagues, will be found to be 90, the Difference of Longitude sought. Then for finding of the Course, with the Radius of your Scale, draw the obscure Arch Cn, and that being measured on the Line of Chords, will be found to be 31° , or two Points three Quarters, the Course required, which is N. N. W. three Quarters Westerly, and the Departure HI 66 Leagues.

PROB. IV. *A Ship being in the Latitude 40° North, sails N.N.W. $\frac{1}{4}$ or (7°) W. 129 Leagues; I demand the Latitude of the second Place, the Difference of Longitude and Departure? Plate 7. Fig. 30.*

For the Solution of this Problem, first Draw the Line BA of any convenient Length; then from one end thereof, as B, describe the occult Arch Cn, and set off 31° , or two Points three Quarters from C to n; then by the Point n draw the Line BI, the Distance 129 Leagues, and from the end thereof as at I, let fall the Perpendicular HI; then measure the Distance HB, which you will find to be 110 Leagues, or $50^{\circ} 30'$; the Latitude of the second Place is $45^{\circ} 30'$. Then having the two Latitudes find the middle Latitude, as is before directed; then upon the Line BA, and upon the Center C, describe the Semi-circle BDA, and drawing the Line DE from the Point D, set off the middle Latitude $42^{\circ} 45'$ both ways to M and L, and draw the Line ML; then take the distance DF in your Compasses, and set it off from B to G, and from H to A; then upon the Point A erect an occult Perpendicular at MK; then by the Point E, draw the Line GK, till it intersect the Perpendicular at K; then draw AK, which being measured in the Line of Leagues, will be found to be 90 Leagues, or $4^{\circ} 30'$, the Difference of Longitude, and HI the Departure 67 Leagues.

PROB. V. *A Ship being in the Latitude 40° , sails in that Parallel, until her Difference of Longitude be 6° ; I demand the Distance run;*

This Question is usually demonstrated among the Problems of Mercator's Sailing, by a Scheme drawn for that purpose, differing from that already described; but we shall here shew the way how to resolve this Problem by the Line of Longitude on the Plain-Scale.

It is to be understood, that according to the Globe, the Meridians do incline nearer together, until the concur and intersect each other in the Poles, so that hereby the degrees of Longitude are not 60 of the Equinoctial Minutes in any Parallel on the North or South Side of the Equinoctial; but the nearer to either of the Poles you approach, the more they decrease; so that in the Latitude of 60 deg. there are but 30 min. of the Equinoctial to one Degree of Longitude; and in the Latitude of 84 Degrees, there are but 6 Minutes, which doth shew the Errors of the *Plain Chart*: And therefore in sailing, it ought to be rectified according to the Globe, and to that end was this Line of Longitude contrived, which is thus to be used.

If you desire to know how many minutes there are in a Degree of Longitude in any Latitude, you must extend the Compasses from the Center in the Line of Chords, to the Degrees of the Latitude of the Place, and the same extent will reach from the Center at 60 on the Line of Longitude, to the number of Minutes answering to a Degree of Longitude in that Latitude.

Therefore for the Solution of the fifth Problem here proposed, extend your Compasses upon the Line of Chords, from the Center to the Latitude of the Place, which is 40° , and the same extent will reach from the Center at 60, in the Line of Longitude, to 46, which shews that 46 make a degree of Longitude in that Latitude, which 46 being multiplied by 6, the Degrees of Longitude gives 276', the Distance run which was required.

PROB. VI. *A Ship being in the Latitude of 40° , sails in that Parallel 276'; I demand her difference of Longitude?*

For the Solution of this Problem, find how many Minutes make a degree of Longitude in the Latitude of 40° , (as in the last Problem) which is 46; therefore if you divide 272 (the distance run) by 46 (the Miles in a degree of Longitude in that Latitude) the Quotient will be 60, the difference of Longitude required.

Another way to work Mercator's Sailing by the Plain-Scale, and the Meridional Parts.

PROB. I. *A Ship sails N. N. W. from the Latitude 40° North, to the Latitude $42^{\circ} 20'$ North; I demand the Distance sailed, the Departure, and difference of Longitude?* Plate 7. Fig. 31.

Having the two Latitudes 40° North, and $42^{\circ} 20'$ North, find the
Meridional

Meridional Difference of Latitude by the Table of *Meridional Parts*, which is 186' and subtracting the one Latitude from the other, the difference is 2° 20', or 140'.

To work this Problem, draw the Line *AbB*, then place 140 from *A* to *b*, and 186 from *A* to *B*; raise the two occult Perpendiculars, *bc* and *BC*, set off the Course two Points and draw the Line *AcC*, producing it until it cut both the Perpendiculars in the Points *c* and *C*, and so finish the two Triangles *Abc*, and *ABC*. The distance *Ac* is 152', the Departure *bc* 58, and the difference of Longitude *BC* 77'.

PROB. II. *A Ship sails from the Latitude 40° N. to the Latitude 42° 20' N. until her Difference of Longitude be 77° Westerly; I demand the Course, Distance, and Departure?* Plate 7. Fig. 31.

The Meridional Difference of Latitude is, as in the first Problem, 186', the proper Difference of Latitude 140'.

Draw *AB* 186', place 140' from *As* to *b*, raise the Perpendicular *BC* of his given length 77', and also the occult Perpendicular *bc*; by the Points *A* and *C* draw *AC*, and finish the two Triangles. The Course the Angle at *A* is two Points, or N.N.W. the Distance *Ac* 152', the Departure 58'.

PROB. III. *A Ship sails Westerly 152' from the Latitude of 40° North, to the Latitude 42° 20' North; I demand the Course, Departure, and Difference of Longitude?*

Plate 7. Fig. 31.

The Meridional Difference of Latitude is 186 Minutes, the proper Diff. Lat. 140 Minutes.

Draw *AB* 186', and *Ab* 140'; as before, and raise the two occult Perpendiculars *bc* and *BC*; take the Distance 152'; and placing one Point of your Compasses in the Point *A*, cross the occult Line *bc* in the Point *c*, and draw *A c*, producing it until it concur with *BC*, and finish the Triangles. The Course is two Points, or N.N.W. the Departure 58', the Difference of Longitude 77'.

PROB. IV. *A Ship sails N.N.W. 152', from the Latitude 40° North; I demand the Latitude, Departure, and Difference of Longitude?*

Plate 7. Fig. 31.

Draw the occult Line *AB*, and set off the Course two Points, and the Distance *Ac* 152', let fall the Perpendicular *bc*, and so finish the Triangle *A b c*. Then *Ab* will be found 140', or 2° 20', which makes the other Latitude 42° 20', by which you will find the Merid. Parts to be

186'. Place 186' from A to B, and raise the occult Perpendicular BC, until it meet with AC continued, and so finish the Triangle ABC. The Departure bc is 58 min. The difference of Longitude BC 77 min.

PROBLEMS of Great Circle Sailing.

PROB. I. Two Places both in one Latitude, the Difference of Longitude being given; to find by what Latitudes and Longitudes the Arch passes, and the Courses and Distances from Place to Place, in the Arch of a Great Circle.

Example. Suppose the Lizard and Penguin Island on New-found-Land, both in the Latitude 50° North, the Difference of Longitude between them 47° ; I demand by what Latitudes and Longitudes the Arch passes, and the Courses and Distances from Place to Place.

Plate 7, Fig. 32.

Draw the Line AE, and place the Tangent of 40° deg. the Complement of the Latitude from A to B; with 60° deg. of the Chords sweep the Arch DE, and set off 47° deg. the difference of the Longitude from E to D, and draw the Line AD, and place the Tangent 40° deg. the Complement of the Latitude from A to C; then draw the Lines BC upon the Arch DE, set off every 05° deg. from E to D, and draw the prick'd Lines Ab, Ac, Ad, &c. and where these Lines intersect BC, place the Letters b, c, d, f, g, &c. The distances, Ab, Ac, Ad, &c. being measur'd on the Line of Tangents, are Tangents Complement of the Latitude, as follow.

Compl.	Lar.	The Latitudes.	
Ab	39	Therefore the Lat. are,	51
Ae	$38\frac{1}{2}$		$51\frac{1}{2}$
Ad	38		52
Af	$37\frac{1}{2}$		$52\frac{1}{2}$
Ag	$37\frac{1}{4}$		$52\frac{1}{4}$
An	$37\frac{1}{4}$		$52\frac{1}{4}$
Ao	38		52
Au	$38\frac{1}{2}$		$51\frac{1}{2}$
Al	$39\frac{1}{2}$		$50\frac{1}{2}$

These are the Latitudes by which the Arch passes at every 5° deg. of Longitude, from B representing the Lizard, to C which represents the Island.

Having

Having these Latitudes and Longitudes, you may find the Course and Distance from Place to Place, according to *Mercator's Sailing*.

Ac is the Tangent Compl. of the greatest Latitude by which the Arch passes, $52^{\circ}\frac{1}{2}$.

So the Latitudes and Longitudes of the several Points, b, e, d, &c. are as follow; likewise the Courses and Distances from Place to Place.

D. Long.	Lat.	Places.	Courses.	Dist.
B 0°	50°			
b 5	51	From B to b	W.N.W. $\frac{1}{2}$ W.	208
e 10	51 $\frac{1}{2}$	b to e	W.N.W. $\frac{1}{2}$ W.	206
p 15	52	e to d	W.N.W. $\frac{1}{2}$ W.	206
f 20	52 $\frac{1}{2}$	d to f	W.N.W. $\frac{1}{2}$ W.	206
g 25	52 $\frac{1}{2}$	f to g	W.	182
n 30	52 $\frac{1}{2}$	g to n	W. by S. $\frac{1}{2}$ W.	154
o 35	42	n to o	W. by S. $\frac{1}{2}$ W.	154
u 40	51	o to u	W.S.W. $\frac{1}{2}$ W.	186
i 45	50 $\frac{1}{2}$	u to i	W.S.W. $\frac{1}{2}$ W.	186
C 47	50	i to C	W.S.W.	79

PROB. II. Two Places differing both in Latitude and Longitude, to find the Lat. and Long. by which the Arch passes, and the Courses and Distances from Place to Place.

Example. Suppose the two Places to be *Trinity-Harbour* in *Virginia*, in the Latitude 36° North, and the *Lizard* in the Latitude 50° North, the difference of Longitude between them 68 deg. I demand by what Latitudes and Longitudes the Arch passes, and likewise the Courses and Distances from Place to Place?

Plate 7. Fig. 33.

Draw the Line AF; place the Tangent of 40 deg. the Complement of the *Lizard's* Latitude, from A to C; which 60 deg. of the Chords describe the Arch EF, placing 68 deg. from F to E, drawing the Line AE;

AE; then place the Tangent 45 deg. the Complement of *Trinity Harbour's* Latitude from A to B, and draw BC, letting fall the Perpendicular Ad; then set off every 5 deg. from E towards F, (because we sail from B) draw the prickt Lines A₁, A₂, &c. the distance, A₁, A₂, A₃, &c. measured on the Line of Tangents, gives the Complements of the Latitudes by which the Arch passes at every 5° difference of Longitude from B, representing *Trinity-Harbour*, toward C, which is the *Lizard*.

The Distances A₁, A₂, A₃, are as follow, &c.

dist.	deg.		Long.	Lat.	
A1	51	Therefore the Latitudes and Longitudes by which the Arch passes are as follow.	B	00	36
A2	48		1	05	39
A3	46		2	10	41
A4	44		3	15	43
A5	43		4	20	45
			5	25	47
A 6	41		6	30	48
A 7	40		7	35	49
A 8	40		8	40	50
A 9	39		9	45	50
A10	39		10	50	50
			11	55	51
A11	39		12	60	50
A13	39		13	65	50
A	39		C	68	50

Having the Latitudes and Longitudes by which the Arch passes, you may find the Courses and Distances from Place to Place, by *Metcator's Sailing*, as is the Problem afore-going.

The Courses and Distances from Place to Place, wrought by Mercator, are as follow in the Table.

Places.	Courses.	Distances.
From B to 1	N.E. $\frac{1}{2}$ E.	303
From 1 to 2	N.E. by E.	271
From 2 to 3	N.E. by E. $\frac{1}{2}$ E.	264
From 3 to 4	N.E. by E. $\frac{1}{4}$ E.	247
From 4 to 5	E. N. E.	236
From 5 to 6	E. N. E. $\frac{1}{2}$ E.	226
From 6 to 7	E. N. $\frac{1}{2}$ E.	208
From 7 to 8	E. N. $\frac{1}{4}$ E.	187
From 8 to 9	E. by N. $\frac{1}{2}$ E.	200
From 9 to 10	E. by N. $\frac{1}{4}$ E.	154
From 10 to 11	E. by N. $\frac{1}{2}$ E.	154
From 11 to 12	E. by S. $\frac{1}{2}$ E.	154
From 12 to 13	E. by S. $\frac{1}{4}$ E.	200
From 13 to C	E. by S.	77

Astronomical Problems wrought by the Plain-Scale.

PROB. I. *The Sun's Place or Distance from the next Equinoctial Point, and the greatest Declination being given; to find the present Declination.*

Example. The Sun's place is 26 deg. $\frac{1}{4}$ of Taurus, that is, 56 deg. $\frac{1}{4}$ from the Equinoctial Point Aries; I demand his Declination?

Plate 8. Fig. 34.

With the Chord of 60 deg. describe the Semi-circle BDC, and raise the Perpendicular AD, and from the point C set off the greatest Declination 23 $\frac{1}{4}$ deg. from C to E, and draw the line AE, then for the Sun's Longitude set off the Sine 56 deg. $\frac{1}{4}$ upon the Line AE. from A to F; then from the Point F, take the nearest Distance FI to the Line AC, which measured on the Line of Sines, is 19 deg. $\frac{1}{2}$, or else through the Point F draw GH, parallel to BAC; then AG measured on the Sines, or CH on the Chords, gives 19 $\frac{1}{2}$ deg. the Sun's present Declination Northerly.

PROB. II. *The Sun's greatest and present Declination being given; to find his Place or Longitude.*

Example.

Example. The Sun's Declination is $19^{\circ} \frac{1}{2}$ North, increasing; the greatest Declination (as before) $23^{\circ} \frac{1}{4}$; I demand the Sun's true Place.

Plate 8. Fig. 34.

Draw BC, and describe the Semi-circle BDC, raise the Perpendicular AD, and draw the Line AE, as in the former Problem, place the Sun's Declination $19^{\circ} \frac{1}{2}$ from B and C to H and K; draw the Line HK, which intersects AE in the Point F; the distance AF is the Sine of $56^{\circ} \frac{1}{4}$ the Sun's distance from Aries; so that the Sun's Longitude is $26^{\circ} \frac{1}{4}$ of Taurus.

PROB. III. The Sun's Place and greatest Declination being given, to find his Right Ascension.

Example. The Sun's place is $26^{\circ} \frac{1}{4}$ of Taurus, the greatest Declination, as before; I demand his Right Ascension?

Plate 8. Fig. 34.

Describe the Semi-circle AD and AE, as before, place the Sine of $56^{\circ} \frac{1}{4}$, the Sun's distance from Aries; from A to F; through the Point F draw the Parallel HK; then is FG the Sine of the Right Ascension, GH being Radius, which you may Measure after this manner: Place the Distance HG from A to o; upon o as a Center, with the distance FG, describe the occult Arch at m; a Ruler laid from A until it touch the Arch will cut the Semi-circle BDC in the Point N; the Arch CN is the Measure of FG $44^{\circ} \frac{31}{60}$, the Right Ascension

PROB. IV. The Sun's Declination given, (the greatest Declination being known) to find the Right Ascension.

Example. The Sun's Declination is $19^{\circ} \frac{1}{2}$ North increasing; I demand the Right Ascension.

Plate 8. Fig. 34.

Describe the Semi-circle BDC, and draw the Line AD and AE as before; place the Declination $19^{\circ} \frac{1}{2}$ from B and C to H and K, drawing HK; FG being measur'd, as in the third Problem, gives the Right Ascension (as before) $54^{\circ} \frac{1}{2}$.

PROB. V. The Latitude of the Place, and the Sun's Declination being given, to find his Amplitude.

Example. In the Latitude $51^{\circ} \frac{1}{2}$ North, the Sun's Declination being $17^{\circ} \frac{1}{4}$ N. I demand the Sun's Amplitude?

Plate 8. Fig. 35

Draw BAC, and the Semi-circle BZC, the Perpendicular AZ; place the Latitude or Height of the Pole $51^{\circ} \frac{1}{2}$ from C to P, and draw AP; set off the Complement of the Latitude $38^{\circ} \frac{1}{2}$ from B to Q, and draw AQ the Equinoctial; place the Chord of the Declination $17^{\circ} \frac{1}{4}$ from Q to D, and the Sine thereof from A to G, and draw the Parallel of declination DF. AF measured on the Line of Sines is $29^{\circ} \frac{1}{4}$, the Amplitude required.

PROB.

PROB. VI. *The Latitude of the Place, and the Sun's Declination being given, to find the Ascensional Difference.*

Example. In the Latitude $51^{\circ} \frac{1}{4}$ North, the Sun's Declination $17^{\circ} \frac{1}{4}$ North; I demand the *Ascensional Difference*?

Plate 8. Fig. 35.

Describe the Semi-circle BZC, and draw the Line AZ, AP, AQ, and DF, as in the fifth Problem; FG is the Sine of the *Ascensional Difference*, to the Radius DG, which is thus measured: Place DG from A to o; upon o, as a Center, with the distance FG describe the Arch at E; a Ruler laid from A until it touch the Arch, gives the Point I; and BI $23^{\circ} \frac{1}{4}$ is the measure of the *Ascensional Difference*.

What the *Ascensional Difference* is, and the Use of it, may be seen Prob. 5, 6, and 7, Chap. 8.

PROB. VII. *The Latitude of the Place, and the Sun's Declination being given, to find when the Sun shall be due East or West.*

Example. In the Latitude $51^{\circ} \frac{1}{4}$ North, the Sun's Declination $17^{\circ} \frac{1}{4}$ North; I demand at what time he shall be due East or West?

Plate 8. Fig. 36.

Describe the Semi-circle BZC, and draw the Lines AZ, AP, AQ, and DO, as before; EO is the Sine of the time from 6, that the Sun is East or West to the Radius DO) to measure which, place DO from A to a; and upon the Center a, with the Distance EO describe the Arch at g; a Ruler from A, until it touch the Arch, gives the Point L, and BL $14^{\circ} \frac{1}{4}$ is the measure of EO, which reduced to time (Vid. Prob. 7. Chap. 8.) makes 59° ; which shews that the Sun is due East at 59° past 6 in the Morning, and due West at one minute past 5, or 59° min. before 6 at Night.

PROB. VIII. *The Latitude of the Place, and the Sun's Declination being given, to find the Altitude of the Sun, being due East or West.*

Example. In the Latitude 51° North, the Sun's Declination being $17^{\circ} \frac{1}{4}$ N. I demand the Sun's Altitude, being due East or West?

Plate 8. Fig. 36.

Describe the Semi-circles BZC, and draw the Lines AZ, AP, QA, and DO, as before. AE being measured on the Line of Sines, is 23° *ferè*, Sun's Altitude being due East or West.

PROB. IX. *The Latitude of a Place, and the Sun's Declination being given, to find the Sun's Altitude at six.*

Example. In the Latitude 51° North, the Sun's Declination being $17^{\circ} \frac{1}{4}$ N. I demand his Altitude at six?

Plate 8. Fig. 36.
Describe

The Use of the Plain Scale.

Describe the Semi-circle BZC, draw the Lines AZ, AQ and DO, and through the Point O draw the Line Lob, parallel to BC, BL or Ch, measur'd on the Chords, or AI on the Sines, gives $13^{\circ} \frac{1}{2}$, the Altitude of the Sun at Six.

PROB. X. *The Latitude of the Place, and the Sun's Declination being given, to find the Sun's Azimuth at Six.*

Example. In the Latitude 51° North; the Sun's Declination $17^{\circ} \frac{1}{2}$ North: I demand the Sun's Azimuth at Six? Plate 8. Fig. 26.

Describe the Semi-circle BZC, and draw the Line AZ, AP, AQ and DO, as before; draw Lob as in the Ninth Problem: IO is the Sine of the Sun's Azimuth to the Radius IL which is thus measured; Place IL from A to e, with the distance Io upon the Centre e; describe the occult Arch at d; a Ruler laid to touch the Arch, gives the Point b, and Cb measured is $11^{\circ} \frac{1}{2}$ the Azimuth from the East or West. So that the Sun is E. by N. at 6 in the Morning, and W. by N. at 6 at Night.

PROB. XI. *The Latitude of the Place, the Sun's Declination and Altitude given, to find the Sun's Azimuth.*

Example. In the Forenoon, in the Lat. 51° deg. $\frac{1}{2}$ North, the Sun's Declination is 20° deg. $\frac{1}{2}$ N. and his Altitude 43° deg. I demand his Azimuth?

Plate 8. Fig. 37.

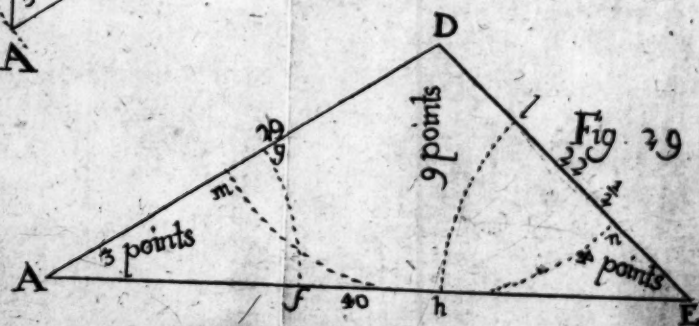
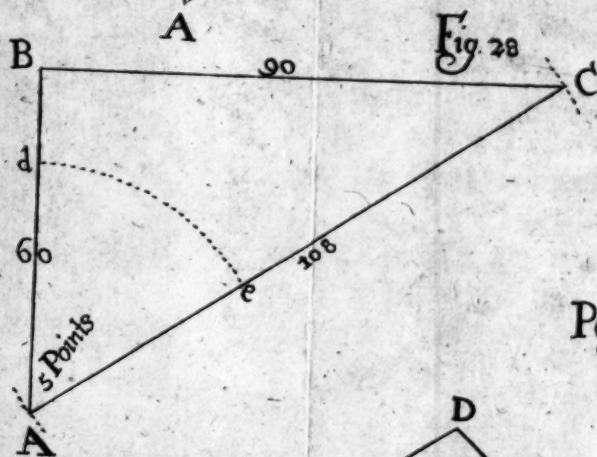
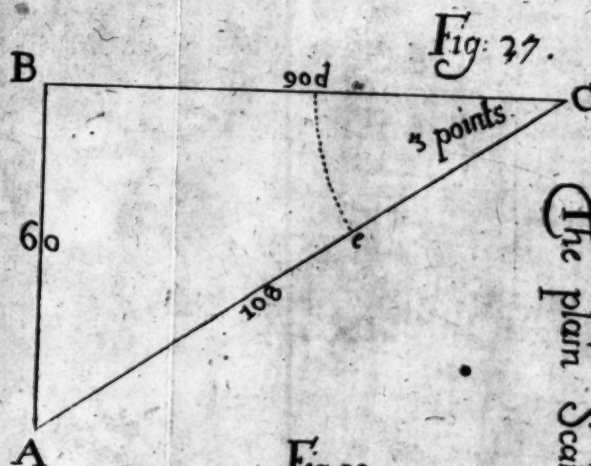
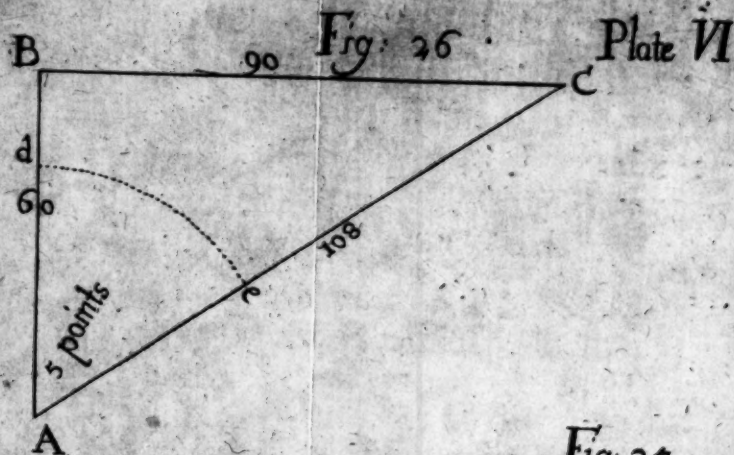
Describe the Semi-circle BZC, and draw the Lines AZ, AP, AQ and DF, the Parallel of Declination, as in the former Problems; place the Altitude 43° deg. from B and C to d and e, and draw the Parallel d e, which intersects the Parallel DF in the Point G, IG is the Sine of the Sun's Azimuth from the East towards the South, Id being the Radius; which to measure, place Id from A to c, and thereon with the distance IG describe the Arch at f; a Ruler laid from A to touch the Arch, gives the Point h, Bh 24° deg. $\frac{1}{2}$ is the Measure of IG, East Southerly. So that the Sun's Azimuth is S.E. 65° deg. $\frac{1}{2}$.

PROB. XII. *The Latitude of a Place, the Sun's Declination and Altitude being given, to find the Hour from Noon.*

Example. In the Afternoon, in the Latitude 51° deg. $\frac{1}{2}$ North, the Sun's declination is 20° deg. $\frac{1}{2}$, the Altitude 43° deg. I demand the Hour?

Plate 8. Fig. 37.

Describe the Semi-circle BZC, and draw the Lines AZ, AP, AQ, DF, and de, as in the 11th Problem; FG is the Sine of the Hour from Six, which to measure, place DF from A to u, and thereon with the distance FG sweep the Arch at K; a Ruler laid to touch the Arch, gives the Point o, and Co is the measure of FG 45° deg. which reduc'd into Time, gives three Hours, the time Afternoon.



The plain Scale.

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League	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Chord	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Longitud	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Sine & Sec	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Tangent	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Half tan	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Points	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Chords	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30

S E C T. II. *The Use of Gunter's Scale.*

I Shall not say any thing of the Description of the Scale, nor of the Projection of the Lines thereon, being the *Logarithms* of Numbers, Sines, Tangents, &c. placed upon a Scale. This is sufficiently Explain'd by Mr. Gunter, Mr. Wingate, and others.

To find a Whole Number in the Line of Numbers.

Among the figured Divisions, look for the first Figure of your Number ; then for the second Figure, count so many tenths from the long Divisions on towards the end of the Rule, as the Units in the second Figure amount to : Then for the third Figure, count from the last Tenth so many Centesims as the Figure hath Units ; and so likewise for the fourth Figure, count from the last Centesim so many Millions (or Thousands) as the same 4th Figure contains Units ; this done, that shall be the Point where the Number propounded is represented on the Line of Numbers.

The Number given being 12, to find the Point on the Line of Numbers that doth represent the same.

Therefore according to the Rule, 1 being the first Figure of this Number, I take the Division at the Figure 1 (in the middle of the Line) for the first Figure ; then the second Figure being 2, I count two tenths from that 1, and that is the Point representing 12, where commonly there is a small Brass Center, because it is often in use.

Suppose the Point representing 144 were required to be found upon the Line of Numbers.

For the first Figure in the Number being 1, I take (as before) the middle 1 ; then for the second Figure which is 4, I count 4 Tenths onwards, and from that Tenth I count 4 Centesims, or hundred parts further, and that is the Point representing 144.

To find the Point representing 1728, first (as before) for 1000 I take 1 in the middle of the Line ; secondly, for the second Figure being 7, I reckon seven Tenths onwards, and that is 700 ; thirdly, for the third Figure being 2, I reckon 2 Centesims from the 7 Tenths, which representeth 20 ; and then lastly, for 8 you may reasonably estimate 8 Millions, or thousand parts, from the last two Centesims, and that Point last found will be the Point representing the Number 1728.

To find a Fraction, or broken Number, on the Line of Numbers.

The Fractions that are to be found on the Line of Numbers, ought always to be Decimal Fractions. $\frac{1}{10}$, $\frac{1}{100}$, $\frac{1}{1000}$, (or ,1 ,01 001) either

ther Inches, Feet, Yards, Perches, or of any other Denomination ; all other Fractions must be reduc'd into Decimals ; and being thus consider'd, they are express'd as Whole Numbers upon the Line.

Note, If you call 1 at the beginning of the Line one tenth of any Integer, than 2 following must be two tenths, 3, three tenths, &c. and the 1 in the middle, one Integer ; 2, two Integers, &c. and the 10 at the end must be 10 Integers.

But if one at the beginning be one Integer, then one in the middle must be 10 Integers, and 10 at the farther end 100 Integers, and all the intermediate Figures, 20, 30, 40, 50, 60, 70, 80, 90, so many Integers ; and every longest Division between, as 21, 22, 23, 24, 25, 26, &c. single Integers ; and the shortest of those Divisions, tenths of those Integers ; and so in proportion, as $\frac{1}{10}$, 1, 10, 100, 1000, 100, 1000, 100, 1000, 10000, &c.

PROB. I. *Two Numbers being given, to find a third Geometrical Proportion, and to a third a fourth, and to a fourth a fifth, &c.*

Example. Let the two Numbers given be 2 and 4, unto which it is required to find a third Proportional, &c. Therefore for the performance hereof by the Line of Numbers, extend the Compasses from one of the Numbers given to the other ; this done, if you apply the same extent either upwards or downwards from either of the Numbers propounded, the moveable Point of the Compasses will fall upon the third Proportional required ; and so the same extent being applied the same way from the third, the moveable Point of the Compasses will fall upon the fourth Proportional, and from the fourth to a fifth, &c. and so to more, as you please ; for if you extend the Compasses from 2 to 4, and turn the Compasses upwards, with one Point resting on 4, the moveable Point will fall on 8, the third Proportional, and from 8 to 16, from 16 to 32, from 32 to 64, and so forward.

PROB. II. *One Number being given to be multiplied by another Number, to find the Product.*

To resolve this Question Arithmetically, whether by Natural or Artificial Numbers, the Proportion is ; As 1 to the Multiplicand, so is the Multiplier to the Product.

Example. Let the Multiplicand 8 be multiplied by 5 the Multiplier ; extend the Compasses on the Line of Numbers, from 1 to the Multiplicand ; the same extent being applied the same way from the Multiplier, will cause the moveable Point to fall on the Product ; for if you extend the Compasses from 1 to 8, the same extent the same way will reach from 5 to 40 : And so if you would now Multiply any
Number

Number by 8, as the Compasses now stand, it is but placing one Foot in any Number given, and the moveable Point will fall on the Product; as if you place one Foot in 9, the other will fall in 72, and so from 8 it will fall in 64, and from 7 to 56, and from 6 to 48: The extent of the Compasses may be taken from 10 at the further end of the Line, which you may call 1.

PROB. III. *One Number being given to be divided by another Number, to find the Quotient.*

For the Resolution of this Problem, the Proportion is thus: As the Divisor is to 1, so is the Dividend to the Quotient.

Example. Let 40 be the Dividend, and let the Divisor be 8: therefore extend the Compasses on the Line of Numbers from the Divisor 8 to 1; this done, the same extent the same way shall reach from the Dividend 40 to the Quotient which is 5.

Another Example, Let 750 be a Number given, to be divided by 25; therefore extend the Compasses downwards from 25 to 1, then applying that Extent the same way from 750, the moveable Point will fall upon 30, which is the Quotient required.

Now to know of how many Figures a Quotient ought to consist.

It will be necessary to observe how many times the Divisor may be written under the Dividend, according to the Rules of Division; for of so many Figures shall the Quotient be composed.

For Example: 12231 being given to be divided by 27, which said Number may be written, according to the Rules of Division, three times under the Dividend; therefore the Quotient shall consist of three Figures, and so of any other.

PROB. IV. *Three Numbers given, to find a fourth in a direct Proportion, as in the Rule of Three Direct.*

To resolve this Problem, the Proportion is thus: As the first Number given is to the second, so is the third Number to the fourth.

To perform this on the Line of Numbers, you must extend the Compasses from the first Number or Term given, to the second; which done that Extent being applied the same way from the third Term, will cause the moveable Point to fall on the fourth Term required.

Example, If the Circumference of a Circle whose Diameter is 7 Inches, be 22 Inches; what Circumference will a Circle have, whose Diameter is 14 Inches?

Therefore extend the Compasses in the Line of Numbers from 7 in the first part thereof, unto 14 in the second; this done, the same Extent

Fig: 32

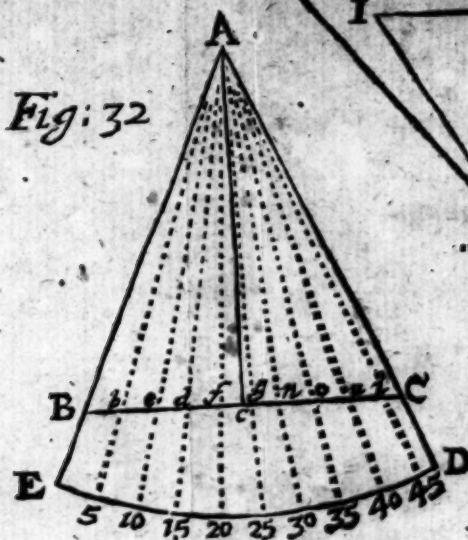


Fig: 30

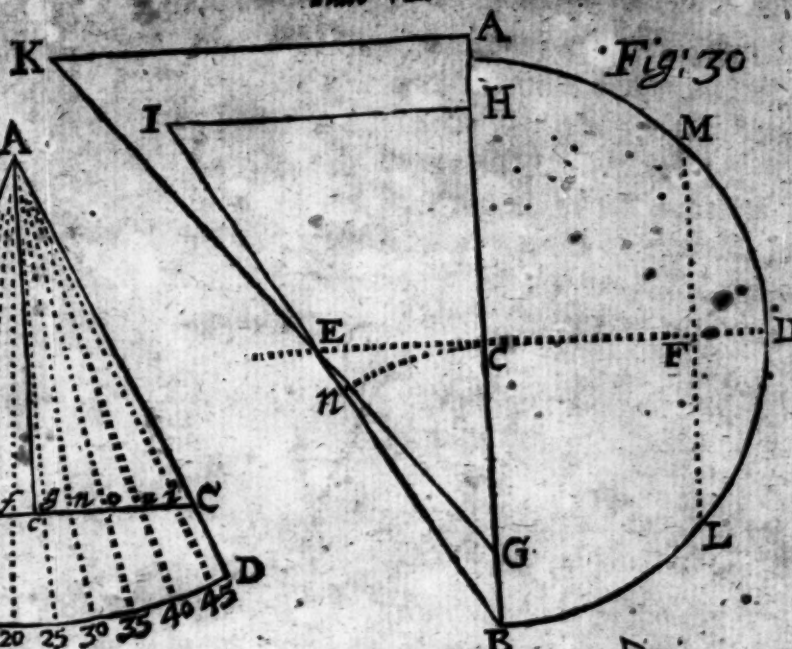


Fig: 31

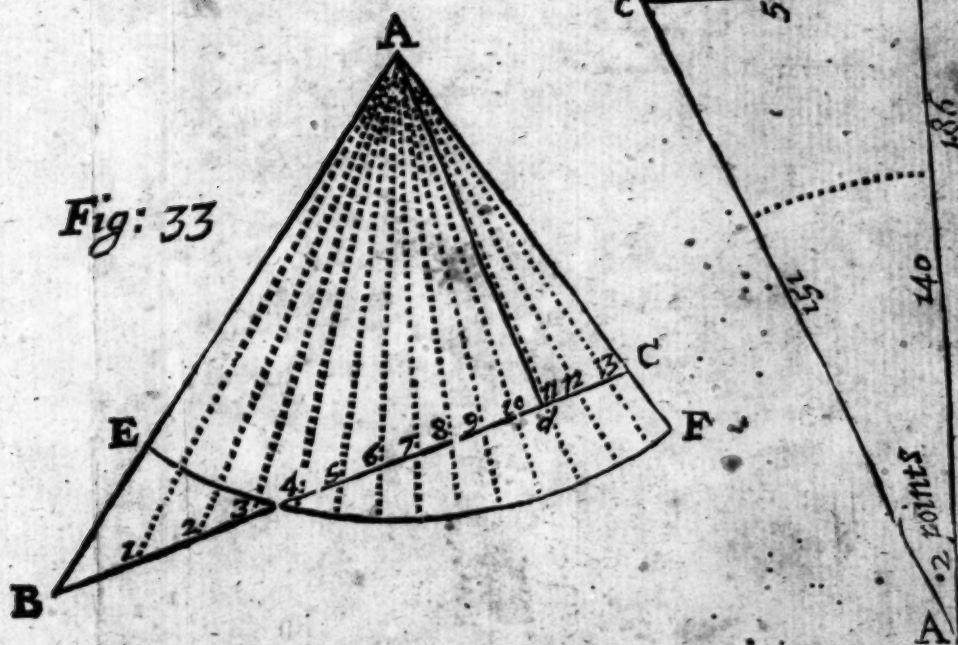
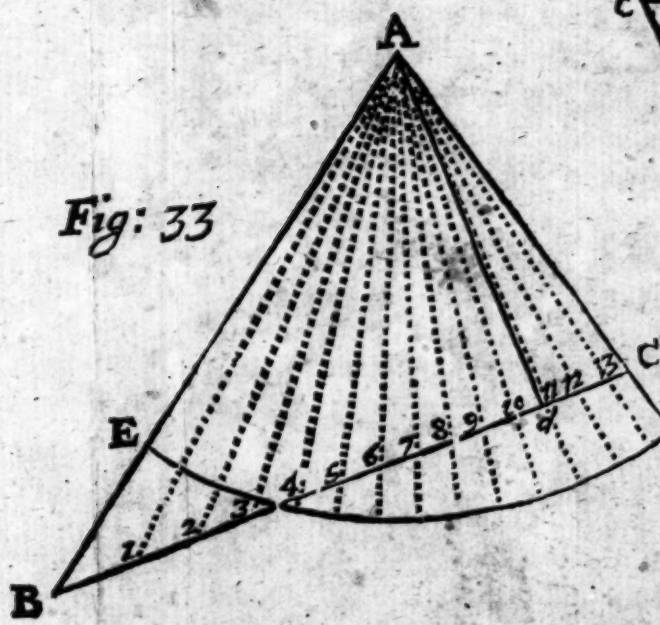


Fig: 33



But if the first and third Terms have the Denomination of Area's, or Contents, and the *Quæsitum* be a Line, then extend the Compasses upon the Line of Numbers, unto half the Distance between the first and third Term of the same Denomination, so the same Extent will reach from the second Term given to the fourth required.

Example 2. If the Diameter of a Circle, whose Area is 154 Inches, be 14 Inches, what Diameter will a Circle have, whose Area is 616 Inches?

Divide the Distance betwixt 154 and 616 into two equal parts, then set one Foot in 14, the other shall reach to 28, the Diameter required.

PROB. VII. *Three Numbers given, to find a 4th in a Triplicate Proportion.*

The Use of this Problem consisteth in the Proportion of Lines and Solids, & *contra*.

If therefore the first and third Terms have the Denomination of Lines, (as the Diameters of Spheres, or Sides of Solid Bodies) extend the Compasses upon the Line of Numbers, from the first Term to the third; this done, and that Extent applied three times the same way from the second Term, will cause the moveable Point to fall upon the fourth Term required.

Example 1. If an Iron Bullet, whose Diameter is 4 Inches, weigheth 9 Pounds, what is the Weight of another Iron Bullet whose Diameter is 8 Inches?

Therefore extend the Compasses on the Line of Numbers from 4 to 8; and that extent apply'd the same way three times from 9, the moveable Point will first fall upon 18, then from 18 to 36; and lastly, from 36 to 72, the Weight required.

But if two given Terms be Weight or Contents of Solids, and the Diameter of a Sphere, or Side of a Cube is sought, then divide the space between the two given Terms of the same Denomination into three parts, and that distance shall reach from the third to the fourth Proportional.

Example 2. If an Iron Bullet that weigheth 9 Pounds be 4 Inches Diameter, what Diameter shall the Shot of Iron be, whose Weight is 72?

Divide the space between 9 and 72 into three parts, and that third part shall reach from 4 to 8, the Diameter required.

PROB. VIII. *To find the Square Root of any Number under 100000.*

The Square Root of any Number is always the mean Proportional betwixt 1 and the Number propounded; but yet with this general Caution, *viz.* If the Figures of the Number be even, that is, 2, 4, 6, 8, 10, &c. then you must look for the Unit, or One, at the beginning of the Line of Numbers, and the Number given in the second part, and the

the Root in the first part ; or rather reckon 10 at the end to be the Unit, and then both Root and Square will fall backwards towards the middle in the second part of the Line ; but if they be odd, then the middle one will be best to be counted the Unit, and both Root and Square will be found from thenceforward towards 10 ; so that according to this Rule, the Square Root of 9 will be found to be 3 ; the Square Root of 64, will be 8 ; the Square Root of 144, will be 12 ; the Square Root 1444, to be 38 ; the Square Root of 57600, to be 240. And to know how many Figures any Root ought to consist of, put a prick over the first Figure, the third, the fifth, &c. beginning from the Right-hand, and as many pricks as are noted, so many Figures there must be in the Root.

PROB. IX. *To find the Cube Root of any Number under 1000000000 $\frac{1}{2}$.*

The Cube Root is always the first of two mean Proportionals, between 1 and the Number given, and therefore will be found by dividing the Space between them into three equal Parts. And to find how many Figures will be in this Root, you must prick over the first Figure, the fourth, seventh, beginning at the Right-hand ; and so many pricks as you find, so many Figures must be in the Root, which Root may be easily found, with these Cautions :

1. If the last prick fall on the last Figure towards the Left-hand, then the Unit is best placed at 1 in the middle of the Line, and then the Cube and Root will both fall forwards towards 10 at the end of the Line.

2. If the last prick fall on the last Figure but one towards the Left-Hand, you may place the Unit at 1 in the beginning of the Line, and the Cube in the second part of the Line, then will the Root be found in the first part of the Line.

If the last Prick fall on the last Figure but two, then place the Unit at 1 at the end of the Line, and then the Cube and Root will both fall backward, and be found the second part of the Line of Numbers.

These Notes being observed, the Cube Root of 1728, will be found to be 12 ; and the Cube Root of 17576, will be 26 ; and the Cube Root of 438976, will be found 76 ; and the Cube Root of 8120601, will be 201 ; the Cube Root of 11390625, will be 225.

P R O B. X. *How to work a Proportion in Sines alone ; or, three Sines being given, to find a fourth Proportional.*

Example. A Sine $22^{\circ} 45'$, to Sine $47^{\circ} 30'$; so is Sine $23^{\circ} 15'$, to a fourth Sine required. This

Fig 34

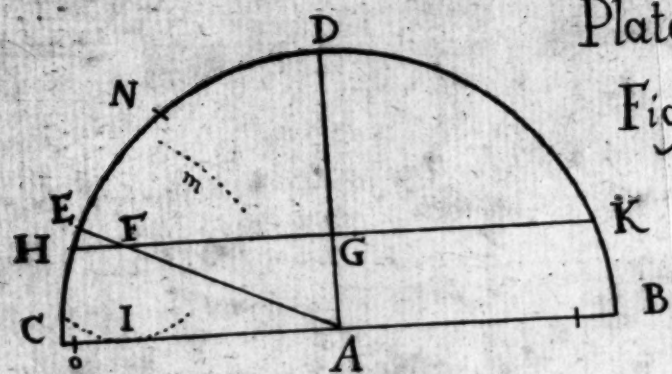


Fig 35

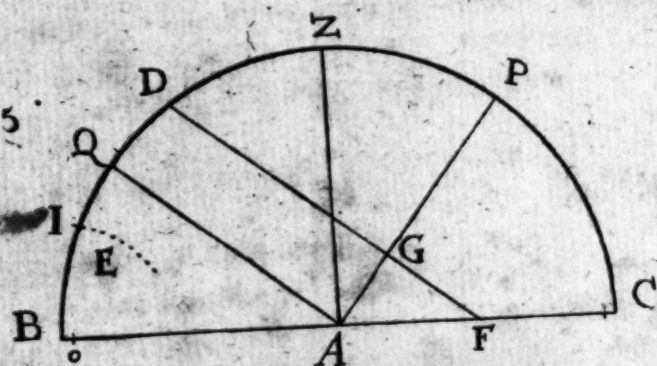


Fig 36

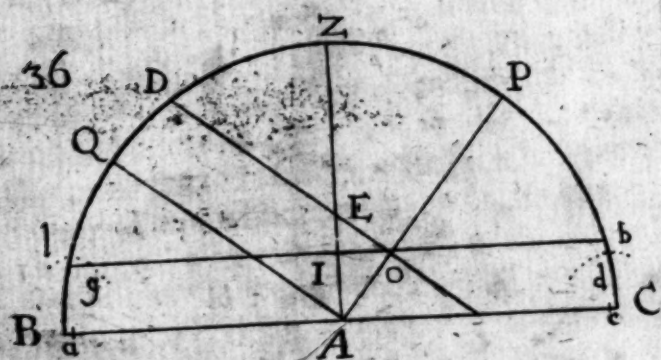
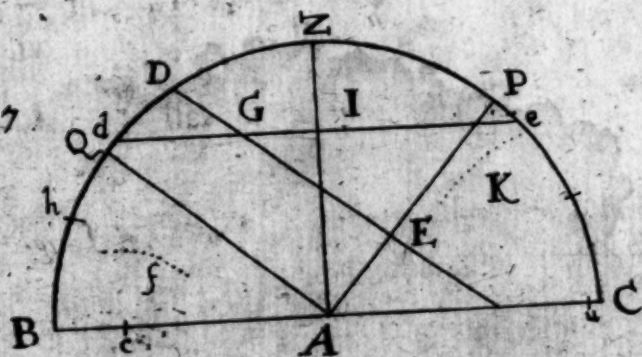


Fig 37



This Problem is wrought on the Line of Sines, as the fourth Problem is on the Line of Numbers. Take the Extent from the Sine $22^{\circ} 45'$ on the Line of Sines, to the Sine $47^{\circ} 30'$; the same Extent shall reach the same way, from the Sine of $23^{\circ} 15'$, to the Sine of $48^{\circ} 50'$, the fourth Sine required.

PROB. XI. *How to work a Proportion in Tangents alone; or, three Tangents being given, to find a fourth Proportional.*

Example. As Tangent $42^{\circ} 40'$ min. to Tangent $15^{\circ} 20'$ min. so is Tangent $39^{\circ} 8'$ min. to the fourth Tangent required.

This Problem is wrought on the Line of Tangents, as the former Problems on the Line of Sines.

Extend the Compasses on the Line of Tangents, from the Tangent $42^{\circ} 40'$ min. to the Tangent $15^{\circ} 20'$ min. the same Extent shall reach the same way, from the Tangent $39^{\circ} 8'$ min. to the Tangent $13^{\circ} 35'$ min. required.

Example. 2. As Tangent $14^{\circ} 58'$, to Tangent $39^{\circ} 15'$; so is Tangent $47^{\circ} 18'$, to a fourth Tangent required.

On the Line of Tangents, the Tangents above 45° , increase from 45° to 46° , 47° , to 50° , 60° , &c. backwards towards the beginning of the Line: Therefore in working this Proportion, the same Extent that reaches from $14^{\circ} 58'$, to $39^{\circ} 15'$, shall reach the contrary way from $47^{\circ} 18'$, to $73^{\circ} 10'$, the fourth Tangent required.

Example. 3. As Tangent $21^{\circ} 30'$, to Tangent $37^{\circ} 20'$; so is Tangent $42^{\circ} 40'$, to a fourth Tangent required.

The Extent from the Tangent $21^{\circ} 30'$ min. to the Tangent $37^{\circ} 20'$ min. if applied the same way, from Tangent $42^{\circ} 40'$ min. will fall beyond 45° at the end of the Line: Therefore to remedy this Inconveniency, having the distance between Tangent $21^{\circ} 30'$ min. and Tangent $37^{\circ} 20'$ min. place one Point of your Compasses in the Tangent 45° deg. and let the other Point fall backwards towards the beginning of the Line, and it will rest on the Tangent $27^{\circ} 20'$ min. This Point let remain fixed, and close the other Point which stands in 45° deg. to the Tangent $42^{\circ} 40'$ min. then keeping this distance, place one Point in Tangent 45° deg. the other will fall upon the Tangent $60^{\circ} 45'$ min. required.

PROB. XII. *How to Work a Proportion in Sines and Tangents together.*

Example. 1. As Sine $22^{\circ} 30'$, to Sine $37^{\circ} 10'$; So is Tangent $19^{\circ} 40'$, to a fourth Tangent required. The

The Extent on the Line of Sines from 22 deg. 30 min. to 27 deg. 10 min. shall reach on the Tangents from 19 deg. 40 min. to 22 deg. 25 min. required.

Example 2. *As Tang. Compl. $64^{\circ} 15'$, to Sine $56^{\circ} 45'$; so is the Radius to a Tangent required.*

Because there is a Tangent in the first place of the Proportion, and likewise a Tangent in the fourth, therefore this Proportion must be changed by putting Radius in the first Place: And instead of the Tang. Compl. in the first place, take Tangent 60 deg. 15 min. (if it had been a Tangent, you must have taken the Tang. Compl.) and then the Proportion will remain thus:

As Radius to Sine $56^{\circ} 45'$; so is Tangent $60^{\circ} 15'$ to the Tangent required.

The Extent from Radius, Sine 90° , to the Sine $56^{\circ} 45'$ on the Sines, shall reach from Tangent $60^{\circ} 15'$, to Tangent $55^{\circ} 40'$ required.

Example 3. *As Radius to Tangent Compl. $60^{\circ} 15'$; so is Tangent $55^{\circ} 40'$, to a Sine required.*

This Proportion must be chang'd, because there is Radius or Sine 90 deg. in the first Place, and a Sine required. Instead of the Tang. Compl. 60 deg. 15 min. take the Tangent 60 deg. 15 min. and put Radius in the third Place, and so the Proportion follows:

As Tangent 60 deg. 15 min. to Tangent 55 deg. 40 min. so is Radius to the Sine sought. Therefore the Extent from the Tangent 60 deg. 15 min. to Tang. 55 deg. 40 min. shall reach from Radius, or Sine 90 deg. to Sine 56 deg. 45 min. required.

PROB. XIII. *How to Work Numbers and Sines together.*

Example. *As 56 to 106; so is Sine $29^{\circ} 30'$ to a Sine required.*

Extend the Compasses on the Line of Numbers, from 56 to 106, the same Extent shall reach the same way on the Line of Sines from 29 deg. 30 min. to 68 deg. 30 min. required.

PROB. XIV. *How to Work by Numbers and Tangents together.*

Example. *As 202 to 52; so is Tangent $73^{\circ} 52'$ to Tangent required.*

The extent on the Line of Numbers, from 202 to 52, should reach the same way on the Line of Tangents from 73 deg. 52 min. to the Tangent required; but the Compasses so extended fall beyond the end of the Line, therefore this Defect must be remedy'd, as in the third Example, Problem XII. by placing the said Extent in Tangent 45 deg. and letting the other Point fall backwards in the Line, which being fixed, close the other Point to 73 deg. 52 min. and then placing your Compasses again in 45 deg. the moveable Point shall fall on 41 deg. 40 min. the Tangent required.

S E C T.

Sect. III. The Description and Use of the Sinical-Quadrant.

THIS Instrument is commonly made of Brass, Box, or Pear-Tree, being a Quadrant or fourth part of a Circle; the Limb thereof being divided into 90 equal Parts or Degrees, is numbred with 10, 20, 30, 40, &c. unto 90; and also divided into 8 equal parts, which are the Points of the Compass, and doth represent any of them according as the Nature of the Question requireth.

The two Sides thereof are commonly divided into 60 (or sometimes into 100) equal parts, and numbered from the Center with 10, 20, 30, &c.

Likewise there is an Index that moveth upon the Center of the Quadrant, and reacheth without the Limb, always divided with the same equal parts as the Sides, and numbered as before.

And from those equal parts on the Sides, are drawn Parallels throughout the whole Superficies of the Quadrant, crossing one another at Right-Angles.

And the Lines of Fives and Tens are commonly prick'd for Distinction sake; which said Lines and Parallels do represent the Sines and Sine Compl. of an Arch (divided into equal parts) [which I suppose is the reason why it is called a *Sinical-Quadrant*.]

But here note, that these Parallels that proceed from the side AB, (in the Figure of the *Sinical-Quadrant*) are for Distinction called *Sinical-Parallels*; and those Parallels that proceed from the side CD, are called *Co-Sinical Parallels*.

Now these Distinctions being observed, we shall proceed to the Use, in the Solution of several Problems in Navigation, and in working a Traverse at Sea, &c.

PROB. I. The Course and Distance being given, to find the Difference of Latitude and the Departure from the Meridian.

Course the fifth Rhomb, distance 45 Leagues.

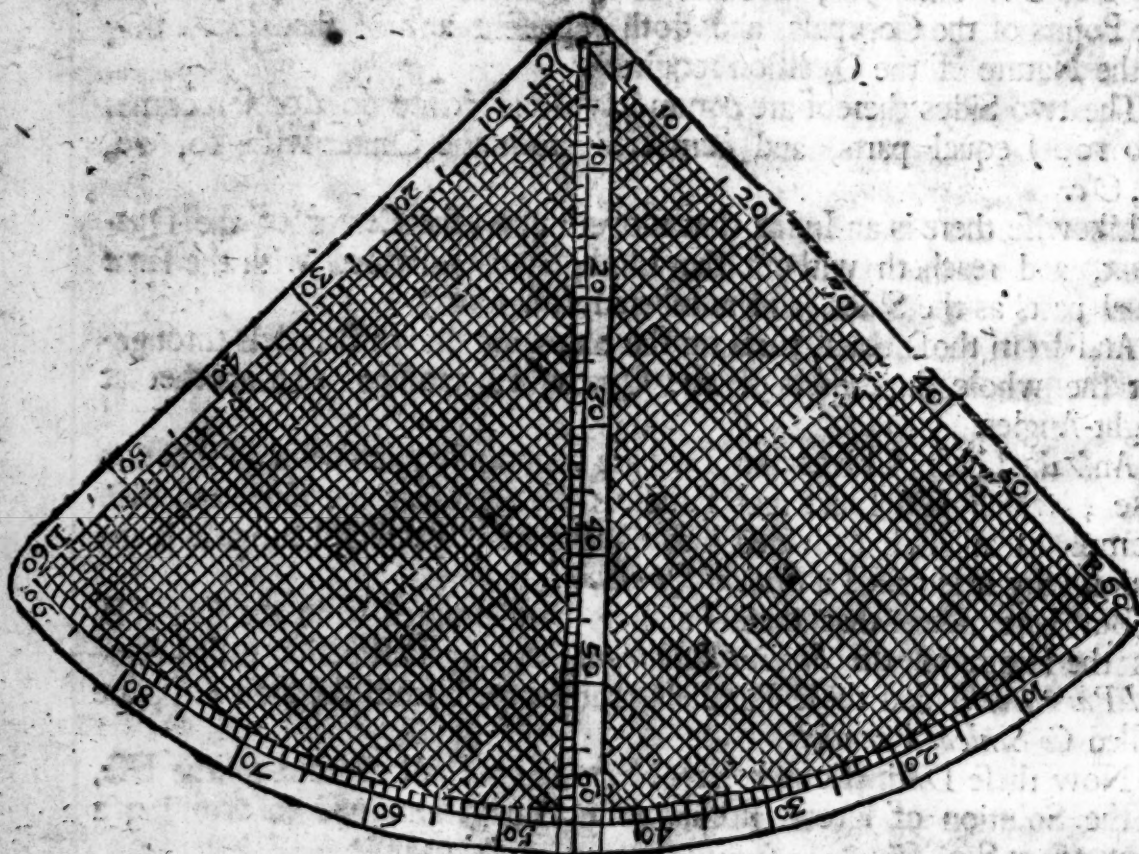
Therefore first put the Index to the fifth Rhomb, which being done, find the distance given thereon, which is 45 Leagues; and in the *Sinical-Parallels* you will find the Index to cut 25 Leagues, which is the difference of Latitude, and in the *Co-Sinical Parallels* it will cut 37 $\frac{1}{2}$ which is the departure.

PROB. II. The Course and Difference of Latitude being given, to find the Distance run, and the Departure from the Meridian.

Course the Fifth Rhomb, Difference of Latitude 37 $\frac{1}{2}$ Leagues.

Set the Index to the Course, and find the Difference of Latitude in

the *Sinical Parallels*, and where that doth intersect on the Index, is 45, which is the Distance required; and where it doth meet the *Co-Sinical-Parallels*, there is 25 Leagues, the Departure from the Meridian.



PROB. III. *The Course and Departure being given, to find the Distance, and Difference of Latitude.*

Course the fifth Rhomb, Departure $37\frac{1}{2}$ Leagues.

Set the Index to the Course found in the Limb, and in the *Co-Sinical-Parallels* find the Departure $37\frac{1}{2}$ (being numbred in the Margin;) and where it doth meet with the Index, it sheweth the Distance run to be 45 Leagues; and where the Index meeteth with the *Sinical-Parallels*, there you will find the Difference of Latitude to be 25 Leagues.

PROB. IV. *The Distance and Difference of Latitude being given, to find the Course and Departure.*

Distance 45, Difference of Latitude 25 Leagues.

First, Find the Distance run upon the Index, and then move the Index

dex until it doth Intersect the Difference of Latitude in the *Sinical Parallels*; and at this Position of the Index, look in the Limb, and there you will find the Course to be the fifth Rhomb which was required; and where the *Sinical Parallel* of 25 doth meet with the *Co-Sinical Parallel* under the edg of the Index, that will shew you the Departure from the Meridian $37 \frac{1}{2}$ Leagues on the Side CD.

PROB. V. *The Distance run, and Departure from the Meridian being given; to find the Course and Difference of Latitude.*

Distance 45 Leagues, Departure $37 \frac{1}{2}$ Leagues.

First, Find the Distance run on the Index, put that to the Departure in the *Co-Sinical Parallels*, and that Point shall cut in the *Sinical-Parallels* the Difference of Latitude 25 Leagues, and the Edg of the Index shall shew in the Limb the Course, which is the fifth Rhomb, which was required.

PROB. VI. *The Difference of Latitude, and Departure from the Meridian being given, to find the Course and Distance.*

Diff. of Lat. 25 Leagues, Departure $37 \frac{1}{2}$ Leagues.

First, Find the Difference of Latitude in the Margin of *Sinical-Parallels*, and also the Departure in the Margin of the *Co-Sinical Parallels*; and note where those Parallels meet each other, in that Point put the Index; then on the edg of the Index shall be cut 45 Leagues, the Distance, and on the Limb the edg of the Index will shew the fifth Rhomb which was required.

PROB. VII. *To know how many Leagues you must sail upon any Point of the Compass, to raise or depress a Degree of Latitude by the Sinical-Quadrant.*

To perform this, you may lay the Index upon the Point of the Compass, and see where the *Sinical Parallels* of 20 Leagues (which is one Degree in the Equinoctial) doth intersect the edg of the Index, there will be shewn the quantity of Leagues you must sail, to rise or depress the Pole upon any Point of the Compass.

As for Example, on the third Rhomb.

If you lay the Index on the third Rhomb, the *Sinical-Parallel* of 20 will shew 24 Leagues, which you must sail on that Point to raise or depress one Degree of Latitude, and that Point on the Index will shew in the *Sinical-Parallels*, the Departure from the Meridian to be 13 Leagues.

PROB. VIII. *Shewing the Use of the Sinical-Quadrant in working a Traverse at Sea.*

The *Sinical-Quadrant* is a plain and ready Instrument for this purpose, and is commonly employed for the working short Traverses at Sea. I'll give one Example of 24 hours run, in the manner as it is usually placed on the *Log-Board*, and how it may be taken off, and wrought by this Instrument.

Examp. Admit a Ship at Sea, and bound to the Northward, steers away her Course North-East, but then meeting with a contrary and shuffling Wind, she makes several Courses as is here under-expressed in this Table, after the Form of the *Log-Board*.

The Form of the Log-Board.					
H.	K.	HK	F.	C.	W.
2	4	0	0	N. E.	N. W.
4	3	1	0	E. N. E.	N. $\frac{1}{2}$ E.
6	3	0	0		
8	3	0	0		
10	3	1	0	E. $\frac{1}{2}$ N.	N. N. E.
12	4	0	0		
2	4	1	0		NE.
4	3	0	0	E. S. E. $\frac{1}{2}$ E.	
6	3	1	0		
8	4	0	0		
10	5	0	0	N. by W. $\frac{1}{2}$ W.	
12	4	1	0		

In this Table there are six Columns; the first distinguished with H, shews the Time, or Hours which these Courses and Distances are thus set down upon the *Log-Board*, that is, at 2 of the Clock, 4 of the Clock, 6 of the Clock, &c. the Log being commonly hove every two Hours.

The second, third, and fourth Columns shew the Knots, Half-Knots, and Fathoms, that the Ship runs upon any Course in the space of half a minute, measured by the *Log-line*.

The fifth Column contains the Course steered by the Compass, but the *Lee-way* that the Ship makes, is left to the Discretion of the Calculator, to be allow'd according to the Mould of the Ship, and the Sail she bears, and also having respect to the Wind and Sea at the same time.

The sixth Column shews on what Point of the Compass the Wind is, and manifesteth whether the Course be large or upon a Wind.

Thus.

To work a Traverse by the Sinical-Quadrant. 181

Thus much for the form of the Log-Board, and the manner of setting down the Courses and Distances thereon. Now somewhat briefly, how to take-off (as they call it) this account from the Log-Board, thereby to compute the Ship's true Course and Distance by the *Sinical-Quadrant*, or other Instrument, or Arithmetical Calculation.

'Tis usual for the Master, his Mates, and all others that are desirous to keep a Reckoning of the Ship's way, every Day at Noon, when the Ship is at Sea, to take an account of the several Runs upon the Log-Board for 24 hours last past, taking notice of the Wind, and other Accidents, allowing for every Knot and Half-Knot, so many Miles and half Miles run in one hour, and four times so many in a Watch or four hours: And because 'tis usual to heave the Log but twice in a Watch, or every two hours, and the Course set down accordingly; therefore the Knots and Half-Knots upon the Log-Board for each Course must be added together, and the Total doubled, gives the Number of Miles upon each respective Course: As for Instance, in this Example in the Table, under the Letters H, K, HK, &c. in the first Line, you shall find 4 knots N.E. which being doubled, give 8 Miles, the Distance upon that Course: But know for the more orderly working the 24 hours Run, it is convenient to frame a Table, after the form of this here annexed.

The Operation for these Traverses by the Sinical-Quadrant.

1. The Course is N.E. 8 Miles, the Wind large, therefore lay the Index upon the fourth Rhomb; or 45° from the Meridian, you shall find the Distance run 8 Miles upon the Index, to intersect at $5\frac{1}{2}$ in the *Sinical Parallels*, which is the Northing, and is to be placed in the N. Column, and to cut $5\frac{1}{2}$ in the *Co-Sinical-Parallels*, which is the Easting, to be placed in the E. Column; and the reason why the Difference of Latitude and Departure, now found by the *Sinical-Quadrant*, is set under the N. and E. Columns, is because the Course is between the North and East.

A Table of the Northing, Southing, Easting and Westing of those Courses found by the Sinical-Quadrant.					
Course.	Dist.	N.	S.	E.	W.
	Miles.	Miles.	Miles.	Miles.	Miles.
N.E.	08	$05\frac{1}{2}$		$05\frac{1}{2}$	
E. by N.	19	$03\frac{1}{2}$		$18\frac{1}{2}$	
E. $\frac{1}{2}$ S.	24		$2\frac{1}{2}$	24	
S. E. by E. $\frac{1}{2}$ E.	21		10	$18\frac{1}{2}$	
N. N. W. $\frac{1}{2}$ W.	19	17			09
Sum		26 $12\frac{1}{2}$	$12\frac{1}{4}$	$66\frac{1}{2}$ 09	09
Diff. of Lat.	No. 13	$\frac{1}{4}$		$57\frac{1}{2}$	E.

2. The

182 To work a Traverse by the Sinical-Quadrant:

2. The second Course is East by North 19 Miles upon a Wind, the Course steered is East-North-East the Ship lying within $5\frac{1}{2}$ Points of the Wind, and allowing one Point for Leeward-way, the true Course is, as before, E. by N. Therefore Place the Index to the seventh Point, or $78^{\circ}\frac{1}{4}$ from the Meridian, and by 19 Miles, the distance, there will be cut $3\frac{1}{2}$ Miles, in the *Sinical-Parallels*, which is the Northing and $18\frac{1}{2}$ Miles in the *Co-Sinical*, which is the Easting.

3. The Third Course is (allowing, as before, one Point for Leeward-way) East $\frac{1}{2}$ a Point Southerly, and the Distance 24 Miles; therefore lay the Index to $7\frac{1}{2}$ Points, or $84\text{ deg.}\frac{1}{2}$, and by 24 found on the Index shall be cut $2\frac{1}{2}$ in the *Sinical-Parallels*, which is the Southing, and 24 fere in the *Co-Sinical*, which is the Easting of this Course and Distance.

And what hath been said of these three Courses, the same is to be understood of the rest in the foregoing Table, giving the same Allowance as before, the Ship being still by a Wind.

Having thus therefore, according to these last Instances found the Northing and Southing, Easting, and Westing of these several Courses and Distances, and placed them in their proper Columns, sum up the Miles in those Columns, and orderly subscribe their Total, as in this Example.

The Sum of the North Column is 26 Miles, of the South Column $12\frac{1}{4}$; of the East, $66\frac{1}{2}$; and of the West, 9 Miles.

Then compare the North and South Columns together, and also the East, and West; and deduct the lesser from the greater, as in the foregoing Table; the Southing is to be subtracted from the Northing, and the Westing from the Easting; the Remainder Northerly $13\frac{3}{4}$ Miles, is the Difference of Latitude; the Residue under the East Column, $57\frac{1}{2}$ Miles, is the Departure to the Eastward of the Meridian.

And if the direct Course, and nearest Distance from the place where the Ship began this Traverse, to that where she now is supposed to be, were required, 'tis readily computed by the *Sinical Quadrant*. And, to perform this, find where $13\frac{3}{4}$ in the *Sinical-Parallels* intersect the *Co-Sinical-Parallel* of $57\frac{1}{2}$ and bring the Index to that Point, and by the Index in the Limb shall be shewn the Angle of the Course, $76\text{ deg.}\frac{1}{2}$ or 7 Points from the Meridian, viz. E. by N. and the Distance run found on the Index, will be 59 Miles.

And thus after the form of this first Example, you may find the Difference of Latitude and Departure from the Meridian of any 24 Hours Traverse, and likewise reduce it to one Course and Distance.

And what is here in particular applied to the *Sinical Quadrant*, the same is to be understood of the other Instruments, it being only a Repetition of the first Case, by the Course and Distance given, to find the

Diffe-

Difference of Latitude, and the Departure, which found, is orderly to be placed in a Table, as in the foregoing Example.

Having spoken somewhat of the Log-Board, and of the Use thereof, I think it not amiss here to say something of the Log-Line, and Half-Minute Glass.

An Advertisement concerning the Log-Line, and Half-Minute-Glass.

Seeing that the manner of keeping a Reckoning of the Ship's Way (by our *English Navigators*) is commonly by the Log-Line, and Half-Minute-Glass, there ought to be greater care had to the truth of them; but it hath been an antient Custom to measure seven fathom between Knot and Knot upon the Log-Line; which way of measuring hath been grounded upon a meer Conjecture, that five of our Feet make a Pace, and a thousand such Paces make a Mile, and sixty such Miles make a Degree, so that a Degree should contain 300000 of our Feet, and one Mile (or Minute) 5000 Feet; and because an half-Minute of Time is the 120th part of an Hour, the Log-line should answer to that Proportion, and be the 120th part of a Mile, which by this account is 41 $\frac{1}{3}$ Feet between each Knot on the Log-line.

But this Erroneous Computation hath been sufficiently refuted by Mr. Oughtred, Mr. Norwood, and others.

Mr. Oughtred in his *Circles of Proportion*, p. 153, doth there propose 66 $\frac{1}{4}$ Stature Miles to answer to one Degree upon the Earth, each containing 5280 Feet; so that according to this Computation, there is 349800 Feet in one Degree.

And Mr. Norwood, in his *Seaman's Practice*, doth declare, That (by a worthy and commendable Experiment of his) he found a Degree of the Circumference of the Earth and the Sea, to contain 367200 of our English Feet. But he further consenteth, That because the Ship's way is more than doth really appear by the Log-line, and because it is more safe to have the Reckoning to be somewhat before the Ship, together with the Evenness of Numbers to allow but 360000 Feet to be one Degree, and consequently 6000 English Feet to be one Minute, or the 60th part of a Degree (vulgarly called a Mile) which Number being divided by 120, giveth 50 Feet between Knot and Knot on the Log-Line; so that upon this ground, if a Ship runneth out one of those Knots in half a Minute, she runneth one Mile (or the sixth part of a Degree) in an hour, or one league and one Mile in a Watch, or 4 hours.

Likewise Mr. Picart has lately measured the length of one degree in France, and finds it to contain 365184 English Feet; nearly agreeing with Mr. Norwood. But notwithstanding these Experiments, (together

(together with the Consent and Approbation of other accomplished Mathematicians in their Books of *Navigation*) have sufficiently detected this Error, yet this Truth hath not had that Entertainment, as the Excellency thereof hath deserved, because Custom hath so long prevailed against Reason.

Mr. *Norwood*, in his fore-mentioned Book, hath assigned some Reasons why he supposeth this Error hath been so long received and tolerated; I shall forbear to mention them, referring you to the Book it self. But I shall assign one Reason more, which I have observed from Experience, which I hope, will in some measure help to prove the Truth of Mr. *Norwood*'s Experiment, and that the Log-line (as commonly divided) may be proved to be too short for true Measure: For I have observed, that if a Half-Minute-Glass be made of its due length, according to true Time, that then their Reckonings intollerably out-run the Ship, and they continually complain, that those Glasses are too long: But if they have a Glass that is 5 seconds shorter than true Time, they do reasonably well agree with the Log-line in their Reckonings; because one Error doth ballance another, *viz.* short measure, and short time. Yet notwithstanding this Concurrence and Affinity between this Log-line, and short Half-Minute-Glass, it is apparent that they are both Errors, and therefore to be rejected: For I suppose it would quickly appear, that if the Log-line where of its due length and measure, *i. e.* 50 Foot between each Knot, and the Half-Minute Glass of its due length, according to true Time, there would doubtless be a greater Harmony and Concurrence of Truth, and Navigation be of more certainty than it is.

So that now it doth plainly appear, by this above-mentioned Observation, that the Log-line, as commonly divided, is too short, according to Mr. *Norwood*'s Experiment, because the necessity of keeping a Concurrence in the Reckonings, is by a Glass that is too short by 5 seconds for the true Time of half a minute, or 30 seconds.

But here I shall give you a Rule, to prove whether a Half-Minute Glass be of true length or not; the way is generally approved to be very true, and what I have many times made Experience of, and can attest it by my own Knowledge. The Experiment is mentioned by Mr. *Philips*, in his *Advancement of Navigation*, and is thus to be performed.

An easy and exact Way to Measure a Half-Minute-Glass, or any small Portion of Time.

Take a Bullet of any weight whatsoever, and make fast a piece of Thread or Silk to it, being 38 $\frac{1}{2}$ Inches in length, from the Center of the Bullet unto the end of the Thread, where a Noose must be made

to hang it on a small Pin, which is to be fastned to any Place where the Bullet may swing freely.

This *Pendulum* being thus prepared, hang its Noose on a Pin, the Thread being exactly $38\frac{1}{2}$ Inches between the Center of Gravity, and the Center of Motion, each of the Swings of this Bullet (being either swift or slow) shall be a true second of Time, so that 60 of these Swings will be the true length of a Minute, and 30 the true length of half a Minute. So by this Ingenious Experiment you may know which of all your Half-Minutes is a true Glass: And if you have no Glass, you may measure any small Portion of Time by this Experiment; for half a second of Time is discovered every time the *Pendulum* doth pass the Perpendicular, that is supposed to fall from the Pin whereon the *Pendulum* doth hang.

But if it should be objected, That at Sea, when the Ship is thrown to and again by the Violence thereof, that then the *Vibrations* of the *Pendulum* may by that means be obstructed, and so the Swings to be uncertain.

A Remedy there is found against this Objection, by making the Thread 7 Inches shorter, and thereto make a small Knot, which Knot you are to hold between your Finger and Thumb, and then with the motion of your Hand, to cause the Bullet always to Ascend to an Angle of 60 Degrees (from the Perpendicular) and so shall each Swing be equivalent to those before; so that if a Ship be tossed by the Violence of the Sea, yet a Man may make shift to try this Experiment, and to measure a true Half-Minute of Time without the help of a Glass.

SECT. IV. *The Description and Use of the Plain Chart.*

IN the middle is a Center, upon which there is an occult Circle described, which is divided into 32 Parts or Points; by which are drawn several Lines quite thro' the Chart, representing the Rhombs or Points of the Compass, and upon these Lines are other Circles described and Rhomb-lines drawn, parallel to the former.

Then is the form of the Land portrayed upon it, and also a Scale of Leagues to measure the Distances of Places.

There is also a Meridian Line equally divided upon the Chart, which discovereth the Latitude of any Place. The several Uses follow.

1. *To find the Latitude of any Place upon the Chart.*

Take your Compasses, and set one foot in the Place required, and extend the other foot to the nearest Distance of an East and West Line, and note where the Line doth cut the Meridian-line, (that is divided

into Degrees) then set one foot where it intersects the Meridian line, and the other foot will reach upon the Meridian-Line, to the Latitude of the Place required.

2. To find the Distance of one Place from another.

If the Distance required be less than the length of the Scale, then take your Compasses, and set one foot in one of the Places, and the other foot in the other place, then with the Extent between your Compasses applied to your Scale of Leagues, will give the measure of the Distance of the two Places.

But if the Distance between the two Places be greater than the length of the Scale, then first extend your Compasses upon the Scale to the whole length thereof, and with that extent set one foot in one of the Places required, then direct the other foot towards the other Place by the help of a Scale, or Ruler, in a Right-line; and if the Distance be great, you must turn the Distance between the Compasses over twice, thrice, or oftner, until you come to the other place required, and if it falls out, that the last extent doth fall over the second place, you must then, from the last place where the Compasses stayed, draw in the other Point until it touch in the Place required, and measure that upon the Scale of Leagues. As suppose your Scale were an hundred Leagues; and if you turn your Compasses two or three times over, then is the Distance so many hundred Leagues, and that small Distance more, which being measured upon the Scale, it giveth the odd Leagues, and so consequently the Distance required.

3. To find upon what Point of the Compass one Place beareth from another.

If from the two Places propounded there be a Rhomb-line that lieth directly from Place to Place, then is there no more trouble in it but to look upon the small Compass upon the Chart, and see upon what Rhomb it is they bear one from another.

But in case a Rhomb-line doth not lie directly from one Place to the other, then extend your Compasses from the first Place in the nearest Distance to the next Rhomb-line, that you imagine in your Judgment lieth nearest a Parallel from Place to Place, and upon that Rhomb-line run your Compasses along, till the other Point (being at Right-Angles with it) doth reach the other Place, and that Rhomb-line is the true Point of bearing the one from the other.

4. To keep a Reckoning upon the Chart of a whole Voyage.

First, It is to be understood, that you are to keep a Reckoning of every

every day's Work, either by the Tables, or your *Sinical Quadrant*, (as you are before taught) or any other way necessary for such a purpose; and also to cast up all your Traverſes for one or more days: And then after you have ſo done, and brought it to the neareſt Truth you can, either by Obſervation, or otherwiſe, then you are to ſet off your Work upon your Chart, ſo that the Place where your Ship is, may appear to your Eye for the ſatisfaction of your Mind, and for the Information of your Judgment.

As ſuppoſe that you ſail from the *Lizard* South-Weſtwards; then from that very time you begin to keep your Reckoning of your ſeveral Courſes and Diſtances, until you have ſome convenient time to caſt up all your Work, to find the Difference of Latitude, and your Departure from the Meridian of the *Lizard*. The Difference of Latitude we will ſuppoſe to be 3° , and the Departure to be 50 Leagues, which 3° you muſt ſubtract from the Latitude of the *Lizard*, which we ſuppoſe to be $49^{\circ} 56'$ North; ſo that the Latitude that the Ship is now in, is $46^{\circ} 56'$, and 50 Leagues to the Weſtward.

Therefore to ſet the place of your Ship upon your Chart, you muſt uſe two pair of Plain-Compaſſes; with one pair take the Extent between the Latitude of $49^{\circ} 50'$ and $46^{\circ} 56'$, and ſet one Point of your Compaſſes in the *Lizard*, and extend the other Point towards the ſecond place, but ſo that your Compaſſes may ſtand parallel to a North and South Line, which may be eaſily found with the other pair of Compaſſes, by trying whether the Legs be equi-diſtant from the next North and South Line: This done, keep one foot of your Compaſſes in that Point, and with the other pair take the Departure 50 Leagues, from the Scale of Leagues; then interchange your Compaſſes, placing theſe laſt pair in the Point where the other pair ſtood; ſet this Departure 50 Leagues to the Weſtward, and ſo that your Compaſſes may ſtand parallel to an Eaſt and Weſt-Line, which you may try as is ſaid before. The ſecond Point thus found upon the Chart, is the place of the Ship (according to your Reckoning) which was required.

Sect. V. *The Uſe of the true Chart, commonly called Mercator's Chart.*

I Shall not here mention the Projection of this Chart, it being largely handled by the firſt Inventor, Mr. *Edward Wright*, in his *Correction of Errors in Navigation*, only here ſhew very briefly the ordinary and moſt neceſſary Uſes of this Excellent Chart.

1. *To find the Latitude of any Place in theſe Charts.*

This Operation upon theſe Charts is in all reſpects like that which

has already been delivered for the same purpose, in the Use of the plain Sea-Chart; for if you set one Point of your Compasses in the place whose Latitude is required, and open them in the shortest Distance to the next East and West Line, observing where it intersects the graduated Meridian, and then place one Point in that Intersection, turning your Compasses upwards or downwards, according as the place lies, from the East and West Line, and the moveable Point shall shew upon the said Meridian the Latitude of the Place required.

Suppose the Latitude of *Ushant* were required by this Chart.

If you take the nearest Extent to an East or West Line, and place that Distance from the Intersection on the graduated Meridian, as is before directed, you will find the Latitude of *Ushant* to be 48 Deg. 30 Min. Northerly.

2. To find the Longitude of a Place, and consequently the Difference of Longitude in Degrees, between any two Places situate upon the Chart.

To find the Longitude of any Place upon the Chart, set one Point of your Compasses in the said Place, and take the nearest Distance to the next North or South Line, and observe where this Line intersects the Equinoctial; and keeping the same Extent in your Compasses place one Point in the Intersection, and turning the Compasses the same way that the place, whose Longitude is sought, lies from the North and South Line, the moveable Point resting in the Equinoctial, will shew the Longitude required.

Suppose the Longitude of *Barbadoes* were required.

If you place the Point of your Compasses in the Island of *Barbadoes* in this Chart, and take the the shortest Extent to the next North and South Line, placing the same at the Intersection in the Equinoctial, as is directed, you will find the Longitude of *Barbadoes* to be in these Charts $60^{\circ} 30'$ from *London*. But the Longitude of Places being various, according to the Place from whence it begun, some reckoning it from *London*, some from *Teneriff*, &c. the chief Business will be to find the difference of Longitude between any two Places: which is thus to be performed.

When you have found the Longitude of the two Places, if they have the same Name, their difference, but if of contrary Names, their Sum is the Difference of Longitude between the two Places.

Suppose the two Places were the *Lizard*, in the Longitude $5^{\circ} 23' W.$ and *Barbadoes* in the Longitude $58^{\circ} 32' W.$ subtracting $5^{\circ} 23'$ from $58^{\circ} 32'$, the Remainder $53^{\circ} 9'$, is the Diff. Long.

Again

Again, Suppose the two Places were the *Lizard*, as before, and *St. Thomas's Isle* in the Longitude $8^{\circ} 20'$ E. Add $5^{\circ} 23'$ to $8^{\circ} 20'$ the Sum will be $13^{\circ} 43'$ the Difference of Longitude between the two given Places.

3. To know how one Place bears from another.

For the performance of this Problem, lay the Edge of a Ruler from one Place to another, and with a pair of Compasses try which of the Rhomb-lines the Edge of the Ruler is the nearest Parallel; which being found, that sheweth the Point of the Compass the two places bear one from another.

Suppose the bearing of *Barbadoes* from the *Lizard* were required.

Therefore lay the edge of the Ruler upon both Places, and you will find, that South West $\frac{1}{4}$ a Point Westerly, is the nearest Parallel thereto, which is the bearing of *Barbadoes* from the *Lizard*, and the opposite Point North East $\frac{1}{4}$ East, the bearing of the *Lizard* from *Barbadoes*.

4. To find the Distance of two Places upon Mercator's Chart.

If both Places be in one and the same Latitude, take with your Compasses the length of a degree of the Meridian at that Latitude, (taking half the degree above, and half beneath the Latitude) for so oft as you shall find that length between the two Places, so many times 20 Leagues are there betwixt them; but if the Distance be great, for Expedition, you may take five times the length of that degree, and counting it for 100 Leagues, proceed as before.

Suppose the Distance were required between the Point of *Ushant* and *Cape-bona-vista* in *New-found-land*.

The Distance taken as before about the Latitude of 49° , you will find it to be 560 Leagues.

But if two places have not the same Latitude, the Equinoctial not coming between them, subtract the lesser Latitude out of the greater, but if the Equinoctial cometh between them, add both Latitudes together, so have you the difference of Latitude between both Places.

Now if both places have the same Longitude, so many degrees as there are in the difference of Latitude, so many times 20 Leagues is the Distance.

But if the Places differ both in Latitude and Longitude, then look how many degrees the Difference of Latitude contains, so many degrees of the Equinoctial take between your Compasses; then lay a Ruler to both Places whose distance you seek, and observe where the Ruler crosses the Equinoctial, or some other East or West Line, (or Parallel

lel of Latitude) and leading one foot in the Equinoctial, or other Parallel, move forwards the other also Parallel-wise, keeping always that distance, till it cross the Rhomb of those two Places in such sort, that one foot resting by the Edg of the Ruler, the other carried about, may but only touch the Equinoctial, or other Parallel cut by the Edg of the Ruler; then take with your Compasses the Segment, or part of that Rhomb between that place and the crossing of the Equinoctial, or Parallel, which measure in the Equinoctial, and see how many degrees are contained betwixt them, so many times 20 Leagues is the distance of those two Places.

Or, if that Segment of the said Rhomb be greater than can well be taken with the Compasses, take the length of 5 Degrees of the Equinoctial between your Compasses, and look how oft you can find that length in the Segment of the Rhomb aforesaid, for so many hundred Leagues is the distance of those two Places.

If the Distance from the Lizard to Barbadoes were required, the difference of Latitude between those Places is $36^{\circ} 46'$; therefore take $36^{\circ} 46'$ from the Equinoctial, and laying a Ruler over both places, until it will cross some Parallel of Latitude; then keeping this distance of Degrees in your Compasses, apply one Point to the Edg of the Ruler, so that the other Point may but just touch the Parallel crossed by the Ruler; the Segment of the Rhomb between the Point where the Compasses stay, and the Intersection by the Ruler and Parallel of Latitude, measured by the degrees of the Equinoctial, gives the distance about 1140 Leagues, which was required.

There is nothing else that will be of any difficulty in the common Use of this Chart, if these brief Hints be understood.

SECT. VI. The Description and Use of the Globes.

OF Globes there are two sorts, one is *Terrestrial*, and the other *Celestial*.

The *Terrestrial* hath on the *Superficies* of the Body Pourtraied and Described the whole Form and Fashion of the Earth and Sea, with the Circles of the Sphere, as Colures, Equinoctial, Tropicks, &c.

The *Celestial Globe* hath on its Surface the Constellations of all the known Stars in the Heavens, placed in their Latitudes and Longitudes, Right Ascensions, and Declinations, drawn into several Images and Figures, according to the Fictions of the Antients, with the Circles of the Sphere, as is in the *Terrestrial Globe*.

Geogra-

Geographical Definitions necessary to be understood.

Defin. I. The Globe of the Earth is a Spherical Body, composed of Earth and Water, and is divided into Continents, Islands, and Seas.

II. A Continent is a great quantity of Land, not divided, nor separated by the Sea, wherein are many Kingdoms and Principalities; as Europe, Asia, and Africa, are one Continent, and America is another.

III. An Island is such a part of the Earth that is environed round with Water, as the Island of England and Scotland, and also Ireland, the Isle of Wight, Barbadoes, &c.

IV. A Peninsula is such a part of Land as is almost encompassed about with Water, and is only joined with the Land by an *Isthmus*; such is that great part of Land in America, called *Paruviana*, and *Alorea*, in the *Levant*.

V. An *Isthmus* is a narrow Neck of Land, which joineth the Peninsula to the Continent.

VI. A Promontory is some high Mountain, or great Cape of Land, that shooteth it self into the Sea; as *Cape Bon Esperance*, or *Cape de Verde* in Africa.

VII. The Ocean is a general Collection of the Waters, which environeth the Earth on every side.

VIII. The Sea is a part of the Ocean, to which we cannot come but thro' some Strait, as the *Mediterranean* and *Baltick* Sea.

IX. A Strait is a part of the Ocean, restrained within narrow Bounds, and opening a way to the Sea; as the Straights of *Gibraltar* that leadeth into the *Mediterranean*, and the Sound that leadeth into the *Baltick* Sea.

X. A Coast is a small narrow part of the Sea, or Rivers that go up but little way in the Land.

XI. A Bay is a great Inlet of the Land, as the Bay of *Biscay*, and the Bay of *Mexico*.

XII. A Gulph is a great Inlet of the Land, deeper than a Bay; such is the Gulph of *Venice*, and the Gulph of *Florida*.

XIII. A Climate is a certain space of Earth and Sea, that is included within the space of two Parallels; and of them there have been antiently accounted seven.

1. *Dia Meroës*. 2. *Dia Syonæ*. 3. *Dia Alexandria*. 4. *Dia Rhodæ*. 5. *Dia Rhomes*. 6. *Dia Bonisbonæ*. 7. *Dia Ripheæ*. But now there are 24 on each side of the Equator, ending where the longest Day is 24 Hours.

XIV. A Zone is a certain space of Earth contained between certain Circles of the Sphere, and are thus divided:

The Earth is divided into five Zones, viz. one Torrid or Burning Zone, two Temperate, and two Frozen Zones.

The

The *Torrid Zone* is that which is on each side the Equinoctial, bounded by the Tropicks of *Cancer* and *Capricorn*.

The two *Temperate Zones* are contained between each Tropick, and the Polar Circles.

The two *Frigid, or Frozen Zones*, are contained within each Polar Circle, and their respective Poles.

The *Globe* of the Earth is divided into four Parts, *Viz.*

EUROPE, } } AFRICA,
ASIA, } } AMERICA.

EUROPE is bounded from *Asia* by the *Mediterranean Seas*, on the East with the River *Tanais*, and on the West with the Western Ocean; and containeth these Provinces.

<i>Germany,</i>	<i>Spain,</i>	<i>Sweedland,</i>	<i>Hungary,</i>
<i>Italy,</i>	<i>Denmark,</i>	<i>Muscovy,</i>	<i>Slavony,</i>
<i>France,</i>	<i>Norway,</i>	<i>Poland,</i>	<i>Greece.</i>

The Principal Islands are,

<i>Great-Britain,</i>	<i>Candie</i>	<i>Sardinia.</i>	<i>Cyprus.</i>
<i>Ireland,</i>	<i>Sicily,</i>	<i>Corfica.</i>	

ASIA is bounded on the North with the Northern Ocean, and on the South with the Red-Sea; on the East with the East-Indian Ocean, and on the West with the Flood *Tanais*.

The Principal Regions are,

<i>Anatolia,</i>	<i>Armenia,</i>	<i>Assyria,</i>	<i>Persia,</i>	<i>China,</i>
<i>Syria,</i>	<i>Arabia,</i>	<i>Mesopotamia,</i>	<i>Mogul,</i>	<i>India, and the</i>
<i>Palestine</i>	<i>Georgia,</i>	<i>Chaldea,</i>	<i>Tartaria.</i>	<i>Islands thereof.</i>

AFRICA is bounded on the East with the Red-Sea, on the West with the *Atlantick Ocean*, on the South with the Southern Ocean, and on the North with the *Mediterranean Sea*.

The Provinces.

<i>Aegypt,</i>	<i>Barbary,</i>	<i>Aethiopia,</i>
<i>Abyssines,</i>	<i>Monomotapa,</i>	<i>Nubia.</i>

The Principal Islands are,

<i>Madagascar, or St. Laurence,</i>	<i>St. Thomas,</i>	<i>Cape de Verde,</i>
<i>The Canary Islands,</i>	<i>The Madera Islands,</i>	<i>Islands.</i>

AMERICA is bounded on the East with the *Atlantick Ocean*, on the West with the *Pacifick South Sea*, on the North without Bounds, and on the South with the *Magellanick Sea*.

It

The Divisions of the Earthly Globe.

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It consists of two, viz. North and South America.

The Provinces of North America are,

New France, New Jersey, Carolina,
New England, Maryland, Terra Florida,
Pensylvania, Virginia, Mexico, or New Spain.

The Chief Islands are,

Island, Hispaniola, Jamaica,
Greenland, Cuba, Barbadoes, and the rest of the Caribee
California, Porto Rico, Islands.

The Provinces of South America are,

Brazil, Chili, Amazonas, Magellanick Land,
Terra Firma, Peru, Paragua,

One Island, Terra del Fuego.

The Names of the Seas in several Parts of the World.

Mar del North, Narrow Sea, Mediterranean Sea, Mare Major, Mare
Pacificum, Mare Caspium, East-India Sea, Persian Sea, Red-Sea.

The Names and Number of the Stars of each Constellation on the Celestial
Globe.

Northern Constellations are 21, viz.

1 Ursa Major,	7	13 Serpens,	24
2 Ursa Minor,	27	14 Serpens,	18
3 Draco,	31	15 Sagitta,	5
4 Cepheus,	11	16 Aquila,	9
5 Bootes,	22	17 Aquinos,	7
6 Corona Borealis,	8	18 Delphinus,	10
7 Engonases, or Hercules,	29	19 Equuleus,	4
8 Lyra,	10	20 Pegasus,	20
9 Olor, or Cygnus,	17	21 Andromeda,	23
10 Cassiopeia,	13	22 Triangulum,	4
11 Perseus,	26	23 Coma Berenices,	14
12 Auriga,	14		

Zodiac Constellations, 12, viz.

1 Aries,	13	7 Libra,	8
2 Taurus,	23	8 Scorpio,	21
3 Gemini,	18	9 Sagittarius,	31
4 Cancer,	9	10 Capricornus,	28
5 Leo,	27	11 Aquarius,	42
6 Virgo,	26	12 Pisces,	34

C c

Southern

Southern Constellations. 27.

1 Cetus,	22	15 Piscis Austrinus,	11
2 Orion,	31	16 Grus,	13
3 Flumen Eridanus,	34	17 Phoenix,	15
4 Lepus,	12	18 Indus,	12
5 Canis Major,	18	19 Pavo,	20
6 Canis Minor, vel Canicula,	2	20 Apus avis Indica,	11
7 Argo Navis,	41	21 Apis Musca,	4
8 Hydra,	25	22 Camelion,	10
9 Crater,	7	23 Triangulum Auster,	5
10 Corvus,	7	24 Piscis volans,	7
11 Centaurus,	37	25 Dorado,	7
12 Fera, aut Lupus,	19	26 Toucan,	8
13 Ara,	7	27 Hydrus.	21
14 Corona Aust.	10		

The Globes are composed of these Parts :

- First, The Body, or Globe it self.
 Secondly, The Brazen-Meridian.
 Thirdly, The Quadrant of Altitude.
 Fourthly, The Hour-Circle and Index.
 Fifthly, The Wooden Frame in which it is put, called the Horizon.

The Globe doth represent the natural Situation and Position of the Earth and Heavens, and performs Problems of the Sphere, either in Astronomy or Geography.

1. The Brazen-Meridian is divided into 4 Parts, or Quadrants, each being divided into 90°, within this Meridian the Body of the Globe turneth upon the Axis, being two strong Wires.

2. The Hour-Circle is a flat Ring of Brass, fastned upon the North-part of the Meridian, and is divided into the 24 Hours of a Natural Day; and each of these Hours is subdivided into Halves and Quarters.

3. The Quadrant of Altitude is a long and thin Slip of Brass divided into 90°, and is to move up and down upon the Surface of the Globe to any Position required; and when placed in the Zenith, the Edg thereof representeth an Azimuth, and the Division shew the Almicanter, or Circles of Altitude.

4. The Horizon is a flat and round Frame of Wood, in which the Brazen-Meridian, and consequently the whole Globe doth move, being divided into a Kalender, shewing the Day of the Month, the Place of the Sun, the Rhombs, &c.

PROB. I. *How to set a Globe to the Latitude of a Place.*

Suppose you were to set the Globe to the Latitude of 52° North; the Globe being in the Frame, move the Meridian either higher or lower, until 52 doth cut the very Edg of the Horizon on the North-side thereof (the divided side of the Brazen-Meridian being towards you) then the Meridian of the Globe being turned North and South, by the help of a Magnetical Needle, it doth then represent the Natural Scituation of the Heaven or Earth upon the Celestial or Terrestrial Globe.

The Use of the Terrestrial Globe.

PROB. II. *To find the Latitude of any Place upon the Globe.*

First find the place required upon the Globe, then turn the Globe about until the place whose Latitude is required be just under the *Brazen-Meridian*, then note what Degree stands against it on the Meridian; that is the Latitude of the place which was required.

Example. Let it be required to find the Latitude of *Rome*: Turn the Body of the Globe about till *Rome* be just under the *Brass-Meridian*, and you will see 42 to be right against it, which is the Latitude of *Rome*.

PROB. III. *To find the Longitude of any Place upon the Globe.*

Turn the Body of the Globe about, till the place whose Longitude you require, comes under the Meridian: Then observe what Degree of the Equinoctial is cut by the *Brass-Meridian*, and the Number of those Degrees is the Longitude of a place you seek for.

Example. Let it be required to find the Longitude of *Rome*, as before: therefore bring *Rome* under the Meridian, which being done, the Meridian will cut the Equinoctial in $36^{\circ} \frac{1}{2}$, the Longitude required.

PROB. IV. *To find the distance of any two Places on the Globe.*

To perform this, lay the beginning of the *Deg.* on the *Quadr.* of *Altitude* upon one of the Places required, and note how many *Deg.* there are contained between them; which is the Distance between the said Places.

Example. Let it be required to find the Distance between *London* and *Rome*; therefore lay the *Quadrant* of *Altitude* from one Place to another, and you will find 12° to be intercepted between the aforesaid Places, which is the Distance between *London* and *Rome*.

PROB. V. *To find the Positions of Places one from Another.*

First set the Globe to the *Lat.* of one of the Places, and bring the same Place under the Meridian, and extend the *Quadr.* of *Altitude* being fixed over the first Place to the other Place, and the end of the *Quadr.* shall point out on the Horizon the Position that one Place hath from the other.

Ex. Let it be required to know the Position of *Rome*, from *London*; therefore bring *London* under the Meridian, and there fit the Quadr. of Altitude, and lay the edge thereof upon *Rome*, and the end of the Quadr. of Altitude will point to 53° , which is the Position of *Rome* from *London*.

The Use of the Celestial Globe.

PROB. VI. *The Day of the Month being given, to find what Sign and Degree the Sun is in.*

First find the day of the Month in the Kalendar, on the Horizon, and right against it you shall find the Sign and Degree in which the Sun is.

Example. Let it be required to find the Sun's Place on the fifth of *May*. You must find the fifth of *May* in the Kalendar, and right against it you will find 25° degrees in *Taurus*, which is the Sun's place that Day.

PROB. VII. *How to place the Index of the Hour-Circle for any Day in the Year.*

The place of the Sun found (as in the last Proposition) you must find that degree on the Ecliptick-line of the Globe, and bring that degree to the Brazen-Meridian; then staying the Globe there, turn about the Index of the Hour-Circle till it points just upon the upper-Line of XII in the Hour-Circle; which being done, the Hour-Circle is rectified for that Day.

PROB. VIII. *To find the Time of the Sun's Rising and Setting.*

The Hour-Circle being rectified, and the Globe set to the Latitude, then turn the Globe about till the degree in which the Sun is, cut the East-side of the Horizon; and then casting your Eye upon the Hour-Circle, the Index will shew you the Time of the Sun's Rising: and the Globe being turned about till the degree of the Sun cut the West-side of the Horizon, the Index will shew you the Time of the Sun's Setting.

Ex. Let it be required to find the Sun's Rising and Setting the fifth day of *May*, in the Lat. of *London*, the Sun being then in 25° of *Taurus*.

First, find the 25^{th} deg. of *Taurus* in the Ecliptick-line, which being turned to the East-part of the Horizon, you will find the Index point to a quarter after four of the Clock; the same point of the Ecliptick being turned to the West-part of the Horizon, you will find the Hour-Index point to 3 quarters past 7, the Time of Sun-setting.

Having the Time of the Sun's Rising and Setting, you may find the Length of the Day and Night; for the Time of the Sun's Rising being doubled, gives the Length of the Night, and the Time of Sun-setting doubled the Length of the Day.

Example. The fifth of *May*, the Sun riseth at 4 of the Clock and a quarter

quarter past, which being doubled, is 8 Hours and a half, the length of the Night; and the Sun-setting, which is at 7 a Clock, and three quarters, which being doubled, is $15\frac{1}{2}$ Hours, the Length of the Day.

PROB. IX. *To find the Sun's Amplitude.*

The Amplitude of the Sun is an Arch intercepted between the East or West-points, and that part of the Horizon where the Sun riseth or setteth.

The finding of the Amplitude differeth little from the last Proposition: For having brought the Degree of the Sun's Place to the Horizon, you count how many Degrees of the Horizon are intercepted between the East or West-point, and that part of the Horizon where the Sun either riseth or setteth.

Example. The fifth of May, I desire to know the Sun's Amplitude in the Latitude of London; therefore bring the place of the Sun that Day to the Horizon, and you find $31^{\circ}\frac{1}{2}$ intercepted between the Point of the Horizon, and the East-point, which is the Sun's Amplitude Northerly.

PROB. X. *How to find the Sun's Declination any Day of the Year.*

The Declination of the Sun is an Arch of the Meridian, intercepted between the Sun's Place and the Equinoctial; to find which you must bring the Degree in which the Sun is to the Brazen-Meridian, and there stay it, and count how many Degrees of the Meridian are contained between the Equinoctial and the Sun's Place, and that is the Declination.

Example. I would know what Declination the Sun hath the fifth of May, the Sun being 25° in Taurus, which being brought to the Meridian, you will find 90° intercepted between that Point and the Equinoctial on the Brazen-Meridian, which is the Declination required.

PROB. XI. *To find the Meridian Altitude of the Sun any Day of the Year.*

The Meridian-Altitude of the Sun is an Arch of the Meridian, intercepted between the Horizon, and the Degree in which the Sun is. To perform which, turn the Globe about till the Degree of the Sun be just under the Brass-Meridian: Then staying the Globe there, count how many Degrees are contained between the Place of the Sun under the Meridian and the Horizon; and that is the Meridian Altitude.

Example. On the fifth of May, it is required to find the Meridian Altitude of the Sun that Day in the Latitude of London; the Sun's Place in the Ecliptick is 25° Deg. in Taurus; therefore bring that Degree under the Brass-Meridian, and you will find 57° and a half to be intercepted upon the Brass-Meridian, between the Place of the Sun and the Horizon; that is the Meridian Altitude of the Sun that Day.

PROB. XII. *How to know what Altitude the Sun shall have any Hour of the Day, on any Day of the Year.*

Having found the Sun's Place, and rectified the Globe to the Latitude, and the Index of the Hour-Circle for the Day proposed, turn the Globe about

about till the Index of the Hour-Circle be just upon the Time when you would know the Altitude; then staying the Body of the Globe here, bring the Quadrant of Altitude, being scrued on to the Zenith, and lay it over the Sun's Place: Then the Number of the Degrees contained betwixt the Horizon and the Sun's Place, counted on the Quadrant of Altitude, is the Altitude of the Sun at that Hour.

Example. Let the Time given be the tenth Day of *April*, in the Latitude of *London*, at which time (by the sixth Proposition) I find that the Sun is in the beginning of *Taurus*, and I would know what Altitude the Sun will have at Nine of the Clock in the Morning: The Index of the Hour-Circle being rectified for that Day, turn the Body of the Globe about till the Index of the Hour-Circle lies just upon 9 of the Clock: Then staying the Globe there, lay the Quadrant of Altitude on the Sun's Place, and the Number of Degrees between the Horizon and the Sun's Place (counted upon the Quadrant of Altitude) is the Height of the Sun, which here I find to be 36° at that time, or at three in the Afternoon; for the Sun hath the same Altitude (nearly) at 9, 8, 7, 6, &c. in the Morning, as it hath 3, 4, 5, 6, &c. in the Evening.

PROB. XIII. *How to find the Hour of the Day by the Globe.*

This Proposition cannot be performed conveniently by the Globe only, but the Altitude of the Sun must be first taken by some Instrument, and then this is but the Converse of the former Proposition which it performs thus: The Globe being set to the Latitude, and the Index of the Hour-Circle rectified, turn the Globe about till the Degree of the Sun's Place meet with the Altitude, taken by the Instrument, upon the Quadrant of Altitude, and then will the Index on the Hour-Circle shew you the Hour of the Day.

PROB. XIV. *To find both the Right and Oblique Ascension, and Oblique Descension of the Sun.*

The Globe being set to your Latitude, bring the Degree of the Sun to the *Brazen-Meridian*, there staying it, see what Degree of the *Equinoctial* is cut by the said *Brazen-Meridian*, and that is the *Right-Ascension* of the Sun that Day. So the Sun being in the beginning of *Taurus*, his *Right-Ascension* will be found to be about 28° ; and bringing the Sun's Place to the East-part of the *Horizon*, in the Latitude of *London*, the *Horizon* will cut the *Equinoctial* in $13^{\circ} 4'$, which is the *Oblique-Ascension*, and bringing the Sun's Place to the West-part of the *Horizon*, the *Horizon* will cut the *Equinoctial* in 43° , the *Oblique Descension*.

PROB. XV. *To find the Meridian Altitude of a Star, or the Altitude of a Star at any time.*

To find the Meridian Altitude, let the Globe be set to your Latitude, and

and then turn the Body of the Globe about, till the Star be under the Brazen-Meridian, and then the Number of Degrees of the Meridian intercepted between the Star, and the North or South-part of the Horizon, according as the Star is situated, is the Meridian Altitude thereof.

Now to find the Altitude at any other Hour, turn about the Globe till the Index of the Hour-Circle be at the Hour you would know the Altitude of the Star (the Index of the Hour-Circle being first rectified to the Sun's Place) and then apply the Quadrant of Altitude to the Star, and the Degrees of the Quadrant cut by the Star, are the Altitude, at that Time.

PROB. XVI. *To know at any time of the Day or Night, what Stars be above the Horizon.*

This is no other, than to place the Globe in a true Position at that Time: Which is easily performed by turning the Globe (the Index first rectified to the Sun's Place) till the Hour-Index point to the Hour of the Day or Night; and staying the Globe there, you will see all the Stars that are above the Horizon at that time.

PROB. XVII. *How to know the Rising, Culminating, and Setting of any Fixed Star; also what part of the Horizon he riseth and setteth in.*

Having rectified the Index of the Hour-Circle, and placed the Globe according to the Latitude, then bring the Star, whose Rising, Culminating, or Setting you desire, to the East-side of the Horizon; then will the Index of the Hour-Circle shew you the Time of his Rising; then bring the same Star under the Brazen-Meridian, and there staying the Globe, the Index will shew you at what Hour the said Star Culminates, and comes to the Meridian. Lastly, bring the same Star to the Western-part of the Horizon, and then the Index of the Hour-Circle will shew you at what Hour the said Star setteth, and by the Horizon you may know the Amplitude, as of the Sun.

PROB. XVIII. *To find the Hour of the Night by the Globe.*

You must take the Altitude of some known Star by a Quadrant, or other Instrument, and then having rectified the Index of your Hour-Circle according to the Day of the Month, turn the Globe about till you make the Star agree with the Altitude upon the Quadr. of Altitude to the Eastward or Westward of the Meridian, according to the Star's Position; then the Index of the Hour-Circle will point out to you the Hour of the Night.

SECT. VII. *Shewing some secret Properties of the Loadstone.*

THE Nature and strange Properties of the Loadstone are such that the more they are known, the more they are justly to be admired, in their

their lively expressing the infinite Power and Goodness of God, who hath created so precious a Jewel for the profitable use of Man; and for the enlarging and setting forth of his own Glory, especially in that Assistance it affords to Man, in the Discovery of the whole Universe, which is the Work of his Hands, and his mighty Wonders in the deep Waters; the Properties not only serving for Maritime Affairs, but also in travelling by Land in vast and solitary Deserts; for moveable Sun-Dials in all Places of the World; for the more ready and exact Chorography of any Country, or true plotting of any ground, and for following of any Mineral Vein (void of Iron) under the Earth; and also for Coal-Mines, with several other necessary Uses; retaining in it self, as it were, the Mirror of Philosophy, manifested by its Sympathetical Coition, and Antipathetical Repulsion, with many other occult Operations very admirable to behold; two especially, that are treasured up in its dusky Entrails, one of Attraction, the other of Direction: It hath Substance, Virtue, and Operation, serving to many good Purposes; therefore this Stone of all others may be accounted the most precious, wherein the Majesty of Nature doth most appear; which admirable Treasure God hath vouchsafed to reveal unto the weak Knowledge of Man towards the end of the World, being so plain to the meanest Capacity, and that out of a base, contemptible Stone, as it seemeth to be, and yet filled with such excellent and wonderful Virtue, that all the Gems in the World have not the like.

Of the Name of the Stone, and of the Colour, and from whence it comes and how it was first found.

This Stone is called *Magnes*, used under the Promiscuous Appellation both by the *Greeks* and *Latins*; and, as *Lucretius* writeth, the Name is derived from the Country *Magnesia*,

*The Greeks do call it Magnes from the place,
For that the Magnets Land it doth imbrace.*

Plato saith some call it *Lapis Heracius*, from the Name of *Heraclea*, a City of *Lidia*, where it was first discovered, and upon the same account the Touchstone is called *Lapis Lidie*.

Theophrastus for the same reason calleth it *Herculeum*.

Nicander thinks the Stone so called, and so doth *Plini* from him, from one *Magnes* a Shepherd; for its reported that he found it by his Hob-nail'd Shoes, and Shepherd's Crook that stuck to it, when he fed his Flocks in *India*.

Others call it *Siderites*, from *σίδης*, which signifies *Iron*. By us it is called a *Loadstone*, alluding to the two Stars in the Tail of the Cœlestial Bear, which were antiently called Load-Stars, or Leading-Stars, and therefore this Stone bears that Appellation, which now performs the same Office.

This

A Table of the true time of High-water at Lond. Bridge, according to the Moon's Southing.

Moon South.		Tide London.		Moon South.		Tide London.		Moon South.		Tide London.		Moon South.		Tide London.	
H.	M.	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.
XII.	00	03	00	III.	00	05	15	VI.	00	07	30	IX.	00	11	15
	10	03	09		10	05	21		10	07	41		10	11	29
	20	03	18		20	05	27		20	07	52		20	11	43
	30	03	27		30	05	33		30	08	04		30	11	57
	40	03	36		40	05	40		40	08	14		40	12	10
	50	03	45		50	05	46		50	08	25		50	12	24
I.	00	04	54	IV.	00	05	52	VII.	00	08	36	X.	00	12	37
	10	04	02		10	05	59		10	08	48		10	12	50
	20	04	09		20	06	06		20	09	00		20	01	03
	30	04	16		30	06	13		30	09	13		30	01	16
	40	04	23		40	06	20		40	09	26		40	01	29
	50	04	30		50	06	28		50	09	39		50	01	42
II.	00	04	37	V.	00	06	36	VIII.	00	09	53	XI.	00	01	54
	10	04	44		10	06	44		10	10	06		10	02	03
	20	04	50		20	06	53		20	10	20		20	02	16
	30	04	57		30	07	02		30	10	33		30	02	27
	40	05	03		40	07	11		40	10	47		40	02	38
	50	05	09		50	07	20		50	11	01		50	02	49

The Description and Use of the following Table of Tides on the Sea-Coasts of Great-Britain, Ireland, Norway, Holland, Flanders, France, Biscay, &c. Shewing what Moon makes Full Sea in each of the Places, every Day of the Moon's Age, after the Full or Change.

First you are to understand, that in the first Column of the Table is the Age of the Moon after her Full and Change; and the second and third Columns shew the Hour and Minute of Full-Sea at each respective Place mentioned in the said Tables, and the fourth Column sheweth the Names of the said Places; and the fifth sheweth the Setting of the Tides upon the same Point of the Compass express'd in the Title. And also in the Title you have the Hour when the Moon cometh upon each Point of the Compass, at Full and Change. The Use of which Table shall be further illustrated by this following Example.

Suppose you would know what Moon makes Full-Sea at *Dartmouth* and *Torbay*, and at what Hour it cometh to such a Point of the Compass, and the time of High-Water any day of the Moon's Age. First, look for *Torbay* or *Dartmouth*, which you will find under the Title of *East by North*, and *West by South*, which doth shew, that at the Full and Change of the Moon she cometh on that Point of the Compass at 5 hour 15 minutes, and then it is Full-Sea in the forementioned Places. So likewise if it be demanded, what time it will be Full-Sea when the Moon is 6 days after Full or Change? Therefore look in the first Column for 6, and right against it, in the second and third Column, you will find 10 of the Clock, and 3 Minutes past, which is the time of Full-Sea in the forementioned Places, at that day of the Moon's Age.

The Tide-Table.

North and South.

D.	H.	M.	12 Hours, 00 Minutes.	Setting of the Tides upon the same Point.
0	12	00	In the Road of <i>Gibraltar</i> . On the Coast	From the Nis to Boleign.
1	12	48	of <i>Flanders</i> . At the North-foreland. At	
2	01	36	the <i>Futland Islands</i> . Before the <i>Hever</i> ,	From the Nis to Boleign.
3	02	24	<i>Eider</i> , and <i>Elve</i> , on the Coast of <i>Holland</i> .	
4	03	12	At <i>Dover Peer</i> , on <i>Beachy Shore</i> . At Or-	From the Nis to Boleign.
5	04	00	fordness; in the <i>Candado</i> ; before <i>Enchuy-</i>	
6	04	48	<i>sen</i> , <i>Horn</i> , and <i>Urck</i> , <i>Dunkirk</i> . Half-Tide	From the Nis to Boleign.
7	05	36	at <i>Newport</i> . Half-Tide at <i>Portsmouth</i> , and	
8	06	24	the <i>Island of Wight</i> . In the <i>Sleeve</i> , between	From the Nis to Boleign.
9	07	12	<i>Ushant</i> and <i>Silly</i> . At <i>Bolem</i> and <i>Graveling</i> .	
10	08	00	Before <i>Cherborough</i> , and the <i>Race of Blan-</i>	From the Nis to Boleign.
11	08	48	<i>quet</i> . At the <i>Shoe</i> , <i>Lee</i> , and <i>Kentish Knock</i> ,	
12	09	36	<i>pits</i> , and alongst the <i>Swin Port Desire</i> in	From the Nis to Boleign.
13	10	24	<i>South America</i> . From <i>Cape Cantin</i> to <i>Bo-</i>	
14	11	12	<i>jador</i> on the Coast of <i>Barbary</i> .	From the Nis to Boleign.
15	12	00		

North by East, and South by West.

D.	H.	M.	12 Hours, 45 Minutes.	Setting of the Tides upon the same Point.
0	12	45		From Boleign to the Same.
1	01	33	At <i>Guernsey</i> . At <i>Flushing</i> . Thwart	
2	02	21	of <i>Beachy</i> in the <i>Offing</i> . At <i>Winchelsea</i> .	From Staples to Boleign.
3	03	09	Within the <i>Maes</i> . Within <i>Terveer</i> . In	
4	03	57	the <i>Chamber of Rie</i> . West end of the	From Staples to Boleign.
5	04	45	<i>Nouer</i> . At <i>Rocheſter</i> , and <i>Malden</i> . At	
6	05	33	<i>Flushing</i> , <i>North-Caen</i> .	From Staples to Boleign.
7	06	21		
8	07	09		From Staples to Boleign.
9	07	57		
10	08	45		From Staples to Boleign.
11	09	33		
12	10	21		From Staples to Boleign.
13	11	09		
14	11	57		From Staples to Boleign.
15	12	45		

The Tide-Table.

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North North-East, and South South-West.

D	H.	M.		Setting of the Tides upon the same Point.
0	01	30	01 Hour, 30 Minutes.	
1	02	18	Before the Maes and Goree. Before	From Calice
2	03	06	Terveer. The Weilings. On the Coast of	to Boleign.
3	03	54	Zealand. Before the River of Thames.	
4	04	42	Before Yarmouth. In the Downs. Thwart	
5	05	30	of Donginess. From the West-end of	
6	06	18	Wight. Without Calace and Blackness	
7	07	06	In Bluet. At Bell-Isle, under Holy-Island,	
8	07	54	Tinmouth, Gravesend. At Corpus Christi	
9	08	42	Point. Before the Fen in the Channel.	
10	09	30	At Horn, Edam, and before Camfere. At	
11	10	18	Army, Ramkins and Camfere. At Ber-	
12	11	06	wick. On the Coast of Finmark. From	
13	11	54	the Straits Mouth to Cape Cantin on the	
14	12	42	Coast of Barbary.	
15	01	30		

North-East by North, and South-West by South.

D	H.	M.		Setting of the Tides upon the same Point.
0	02	15	02 Hours, 15 Minutes.	
1	03	03	Without Bluet. Before the Maes.	Between
2	03	51	Before the Weilings. St. Andrews. Dep-	Calace and
3	04	39	by. Without Fountnay.	Dover. From
4	05	27		Dunkirk to
5	06	15		Graveling.
6	07	03		From Staples
7	07	51		to Feram.
8	08	39		From Dart-
9	09	27		mouth to Ex-
10	10	15		mouth.
11	11	03		
12	11	51		
13	12	39		
14	01	27		
15	02	15		

The Tide-Table.

North-East and South-West.

D.H.M.	03 Hours, 00 Minutes.	Setting of the Tides upon the same Point.
00300	At London, Amsterdam, Dort, Rotterdam,	
10348	Zerickzee. Before Newcastle. In Robin-	
20436	Hood's Bay. Before the Tees and Hartle-	From Cape de
30524	pool. Without the Banks of Flanders. Be-	Hague to Alder-
40612	tween Calace and Dover. Before Conquet,	ney, through the
50700	the Pens, Groy, Armentiers, Use, Killiars,	Race of Alderney.
60748	Portbus. The River Bordeaux. The South	From Garnsey to
70836	Coast of Britain, Gascoin, and Poitou.	the Caskets.
80924	The Coast of Biscay, Galicia, Portugal and	From Milford
91012	Spain, North-cape, from the Race to the	to Ramsey.
101100	Polehead. Before the River of Nantz,	
111148	and before the Bay of Tinnmouth. Quarter	
121236	Tide at Flamborough-head; on the West	
130124	Coast of Ireland. At Buchaness, and Ork-	
140212	ness. In Shetland, and Fair-Isle. At the	
150300	Island Teneriff. At Cape Bona Esperanse.	

North-East by East, and South-West by West.

D.H.M.	03 Hours, 45 Minutes.	Setting of the Tides upon the same Point.
00345		
10433	Between Dover and Calace. At the	
20521	Maes. At Rouen, Silly. Before St. Mat-	From Struy-
30609	thews Point. At Brest. In the Sound.	hart to Deep.
40657	Between Ushant and the Main. Before	From the Lizard
50745	the Bass. At St. Matthews. Before Ro-	to the Start.
60833	chel. The River of Bourdeaux. Within	From Cape
70921	the Haven. On the Coast of Spain, Por-	Cleer unto
81009	tugal, Galicia. The South side of Bri-	Londay.
91057	tain, Gascoin, and the West Coast of	
101145	Ireland. At Hunclyfoot. Half-Tide at	
111233	Flamborough-head. Quarter-Tide between	
120121	it and Bridlington-Bay.	
130209		
140257		
150345		

The Tide-Table.

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East North-East, and West South-West.

D.	H.	M.		Setting of the Tides upon the same Point.
0	04	30	04 Hours, 30 Minutes.	
1	05	18	Before Humber, Flambrough, Scarbrough,	From Ostend to
2	06	06	Abberwarck. In Falmouth. In Mouse-	St. Cateline.
3	06	54	Hole. Sept. Isles. Without the Haven,	From Berchster
4	07	42	in the Broad Sound. Without the Fourn.	to Struyfart. The
5	08	30	All the South Coast of Ireland, as Kin-	Bree-sound, out
6	09	18	sale, Cork, Toughall, Waterford, and Cape	andin. From Cape
7	10	06	Cleer. In the Breesound and Vourd. The	Cleer to the Isle
8	10	54	Glests of Texel, Bloy, and St. Matthews.	of Salties. Between
9	11	42	At the Bay within Ushant. At Calace	Londy and the
10	12	30	in the Creek. Dungarvan. Baltimore.	Holms, unto Bri-
11	01	18	Within Mounts-Bay. In the Sea of Wales	stol. From Silly
12	02	06	and Severn.	to the Lands-end
13	02	54		of England. From
14	03	42		the Start to Portland
15	04	30		

East by North, and West by South.

D.	H.	M.		Setting of the Tides upon the same Point.
0	05	15	05 Hours, 15 Minutes.	
1	06	03	In Dartmouth and Plimouth, Foy and	From the Isle
2	06	51	Torbay, Falmouth, Milford, Ramsey. In	of Bass to the
3	07	39	Wales, thwart of Londey. Before Lin.	Fourn. From the
4	08	27	In all the Havens on the South Coast	Dorset to Cape
5	09	15	of Ireland, and in the Bay of Carnarven.	Cleer. From Silly
6	10	03	At the Mouth of Severn. Between Silly	to the Lizard.
7	10	51	and the Lizard. At the Spurn, Newcastle,	From Portland to
8	11	39	and Humber. At Moonless and Caldy.	Wight. From
9	12	27		Wight to Beachy.
10	01	15		
11	02	03		
12	02	51		
13	03	39		
14	04	27		
15	05	15		

The Tide-Table.

East and West.

D.	H.	M.		Setting of the Tides upon the same Point.
00	06	00	06 Hours, 00 Minutes.	
1	06	48	Before Broomen, Texel, and Hamburg.	From the
2	07	36	At Blackness, Wells, Hull, Concallo, St.	Caskets to
3	08	24	Malo's, St. Poul's in the Haven. With-	Berfleur.
4	09	12	out Silly in the Channel. Before Bour-	From the
5	10	00	deaux. Without Oshant. At Lin Half-	Land's-end
6	10	48	Tide, Weymouth, Looe, and the Holmes.	of England
7	11	36	At Bristol, Waterford, and Abermorick.	to the Liz-
8	12	24	At Archangel. At Quebec in Canada.	ard.
9	01	12	At the Mouth of the River Amazons	
10	02	00	in South America (if you add 15 min.	
11	02	48	more.)	
12	03	36		
13	04	24		
14	05	12		
15	06	00		

East by South, and West by North.

D.	H.	M.		Setting of the Tides upon the same Point.
0	06	45	06 Hours, 45 Minutes.	
1	07	33	Before St. Nicholas, and Podofemsk.	From the
2	08	21	In Russia. At Weymouth-Key, Bristol.	Isle de Bass,
3	09	09	Key. Between Foy and Falmouth in the	to Marwanen.
4	09	57	Channel. Foulness. At Garnsey Half-	
5	10	45	Tide. Before St. Nicholas and Podofem-	
6	11	33	sk in Russia.	
7	12	21		
8	01	09		
9	01	57		
10	02	45		
11	03	33		
12	04	21		
13	05	09		
14	05	57		
15	06	45		

The Tide Table.

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East South-East and West North-West.

D. H. M.
 0 07 30
 1 08 18
 2 09 06
 3 09 54
 4 10 42
 5 11 30
 6 12 18
 7 01 06
 8 01 54
 9 02 42
 10 03 30
 11 04 18
 12 05 06
 13 05 54
 14 06 42
 15 07 30

07 Hours, 30 Minutes.

Thwart of *Plimouth*, and of the *Stars*
 in the Channel. At the *Lizard* by the
 Land. Between *Maushole* and *Falmouth*.
 In the *Offing*. In the midst of the
 Channel. At *Kilduyn*. In the Road of
 the *Texel*. At the *Nes* by *Wieringhen*.
 At the Entrance of the *Emes*, or the
 River of *Emden*. Before the Coast
 of *Friezland* and and the *Fly*. *Milford*
Haven. At *Cape Cleer*. *Florida* in *Car-*
rolina.

Setting of the
 Tides upon the
 same Point.

From the
Island Bryack
 to *St. Maloes*.
 From *Berchfleu*
 to *Seyn-head*.

South-East by East, and North-West by West.

D. H. M.
 0 08 15
 1 09 03
 2 09 51
 3 10 39
 4 11 27
 5 12 15
 6 01 03
 7 01 51
 8 02 39
 9 03 27
 10 04 15
 11 05 03
 12 05 51
 13 06 39
 14 07 27
 15 08 15

08 Hours, 15 Minuts.

Thwart of the *Island Wight* in the
 Channel. Without the *Caskets* in the
 Channel. Between the *Wight* and *Bea-*
chy by the Shore. Without the *Fly*.
 To the Westwards of the *Foreland*. In
St. Magnes-Sound. *Tarmouth*. At *St.*
Helens. *Machael's-Castle*. *Dublin* and
Lambey. *Cape Seirrelione* in *Guinea*.

Setting of the
 Tides upon the
 same Point.

Behind
Guarnsey in the
Fair-Way.
 Without the
Seven-Islands.

South-East, and North-West.

D.	H.	M.		Setting of the Tides upon the same Point.
0	0	00	09 Hours, 00 Minutes.	
1	0	48	Between Guarnsey and the Caskets. At	In the Bay
2	1	36	the Race of Portland at the East-end	of Benuyt.
3	1	24	of Wight. Within the Seyn. Before	Between
4	1	12	Cromer, Winterton, and Yarmouth-Friz,	Morleaux and
5	0	00	and Wieringen Flat. On the Coast of	the Treacle
6	0	48	Friezland. Before the Eastern and Wes-	Pots.
7	0	36	tern Emes. Before the Fly and Schol-	
8	0	24	balgh. At Egmont, and Harlem off Basf.	
9	0	12	Before the Caskets and Guarnsey. At	
10	0	00	Orkney, Dunbar, and Kildny. At Fair-	
11	0	48	Isles, Seven-Clifts. At Home-head, and	
12	0	36	thwart of Plymouth and Dartmouth. Isle	
13	0	24	of Man, and Cateneffs. At the three	
14	0	12	Rivers in Canada.	
15	0	00		

South-East by South, and North-West by West.

D.	H.	M.		Setting of the Tides upon the same Point.
0	0	45	09 Hours, 45 Minutes.	
1	1	33	Thwart of Leystaff without the Banks.	Before Con-
2	1	21	The Needles, at the Isle of Wight. In	cala, and the
3	1	09	the Channel thwart of Wight. The Cas-	Island of St.
4	1	57	kets thwart of Garnsey in the Channel.	Michael.
5	0	45	At Dunnose, Terrou, Orfordness, and Al-	
6	0	33	brough. At Leystaff, and at Chamberness.	
7	0	21	At Cape Blanco in Africa.	
8	0	09		
9	0	57		
10	0	45		
11	0	33		
12	0	21		
13	0	09		
14	0	57		
15	0	45		

The Tide-Table.

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South South-East, and North North-West,

D.H.M.

10 Hour, 30 Minutes.

Setting of the
Tides upon the
same Point.

01030
11118
21206
31254
40142
50230
60318
70406
80454
90542
100630
110718
120806
130854
140942
151030

At St. Helens, and the Cows. At Orfordness, and Harwich without the Banks. In Yarmouth. And Leystaff-Road. Before the River of Thames. Between the Isle of Wight and the Main. At Bulleyn-deep, and Seyn-head. In the Fosse of Caen. At Strusaert, and all the Coast of Normandy and Picardy. Calice Road. In the Frish. At Leystaff, Quarter-Tide. Harwich, Dover, and the South Foreland. Between Orford and Orwel-Waves. In Chamberness-Road. In the Downs. At Senegal.

From Berch-
leur to Al-
bonga.

From Cape
Dorsey to the
Island Darden.

South by East, and North by West.

D.H.M.

11 Hours, 15 Minutes.

Setting of the
Tides upon the
same Point.

01115
11203
21251
30139
40227
50315
60403
70451
80539
90627
100715
110803
120851
130939
141027
151115

At Cows and Orfordness within the Sands, and Hampton, Portsmouth, and Dun-
nose. Before the Haven of Caen. Fair-
Isle Roads. Harwich within. Between the
Naze and Warhead of Lower. In the
Chamber and Gore-end. Between Cripple-
Sand and the Creyl. In the Frish and be-
fore Margate.

From St.
Matthew's-
Point to the
Bake-Ovens.

From Font-
ney to St.
Matthew's-
Point.

220 A Table of the Sun's Right Ascension.

Days.	Jan.		Febr.		March		April		May.		June.	
	☉ Right Ascen.		☉ Right Ascen.		☉ Right Ascen.		☉ Right Ascen.		☉ Right Ascen.		☉ Right Ascen.	
	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.
1	19	35	21	42	23	28	01	21	03	14	05	19
2	19	39	21	46	23	32	01	25	03	18	05	23
3	19	43	21	50	23	36	01	29	03	22	05	27
4	19	47	21	54	23	39	01	33	03	26	05	31
5	19	51	21	58	23	43	01	36	03	30	05	36
6	19	56	22	02	23	46	01	40	03	34	05	40
7	20	00	22	06	23	50	01	44	03	38	05	44
8	20	04	22	10	23	53	01	47	03	42	05	48
9	20	09	22	14	23	57	01	51	03	46	05	52
10	20	13	22	17	00	01	01	54	03	50	05	56
11	20	17	22	21	00	05	01	58	03	54	06	00
12	20	22	22	25	00	08	02	02	03	58	06	04
13	20	26	22	29	00	12	02	06	04	02	06	08
14	20	30	22	33	00	15	02	10	04	06	06	12
15	20	34	22	36	00	19	02	13	04	10	06	17
16	20	38	22	40	00	23	02	17	04	14	06	21
17	20	42	22	44	00	26	02	21	04	18	06	25
18	20	46	22	48	00	30	02	25	04	22	06	29
19	20	50	22	52	00	33	02	29	04	26	06	33
20	20	54	22	55	00	37	02	32	04	30	06	38
21	20	58	22	59	00	41	02	36	04	34	06	42
22	21	03	23	03	00	44	02	40	04	38	06	46
23	21	07	23	06	00	48	02	44	04	42	06	50
24	21	11	23	10	00	52	02	48	04	46	06	54
25	21	15	23	13	00	55	02	51	04	50	06	58
26	21	19	23	17	00	59	02	55	04	54	07	02
27	21	23	23	21	01	03	02	59	04	58	07	06
28	21	27	23	25	01	06	03	03	05	02	07	10
29	21	31			01	10	03	07	05	06	07	14
30	21	35			01	14	03	10	05	11	07	19
31	21	38			01	17			05	15		

A Table of the Sun's Right Ascension. 221

Days.	July. ☉ Right Ascen.		August. ☉ Right Ascen.		Septem. ☉ Right Ascen.		Octob. ☉ Right Ascen.		Novem. ☉ Right Ascen.		Decem. ☉ Right Ascen.	
	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.	H.	M.
1	07	23	09	25	11	19	13	08	15	07	17	15
2	07	27	09	29	11	23	13	12	15	11	17	20
3	07	31	09	33	11	26	13	15	15	15	17	25
4	07	35	09	37	11	30	13	19	15	19	17	29
5	07	39	09	40	11	33	13	22	15	22	17	34
6	07	43	09	44	11	37	13	26	15	27	17	38
7	07	47	09	48	11	41	13	30	15	31	17	42
8	07	51	09	51	11	44	13	34	15	36	17	47
9	07	55	09	55	11	48	13	38	15	40	17	51
10	07	59	09	58	11	51	13	41	15	45	17	56
11	08	03	10	02	11	55	13	45	15	49	18	00
12	08	07	10	06	11	59	13	49	15	53	18	05
13	08	11	10	10	12	02	13	53	15	58	18	09
14	08	15	10	14	12	06	13	57	16	02	18	14
15	08	19	10	17	12	09	14	00	16	07	18	19
16	08	23	10	21	12	13	14	04	16	11	18	24
17	08	27	10	25	12	17	14	08	16	15	18	28
18	08	31	10	28	12	20	14	12	16	19	18	33
19	08	35	10	32	12	24	14	16	16	23	18	37
20	08	39	10	35	12	27	14	20	16	28	18	41
21	08	43	10	39	12	31	14	24	16	32	18	45
22	08	47	10	43	12	35	14	28	16	36	18	49
23	08	51	10	46	12	38	14	32	16	40	18	54
24	08	55	10	50	12	42	14	36	16	44	18	58
25	08	58	10	53	12	45	14	39	16	49	19	03
26	09	02	10	57	12	49	14	43	16	53	19	07
27	09	06	11	01	12	53	14	47	16	57	19	11
28	09	10	11	04	12	57	14	51	17	02	19	16
29	09	14	11	08	13	01	14	55	17	06	19	20
30	09	17	11	11	13	04	14	59	17	11	19	25
31	09	21	11	15	—	—	15	03	—	—	19	30

A Table of the Fixed Stars.

A Table of Right Ascension and Declination of some of the most Notable Fixed Stars.

Stars Names.	Magnit.	Right Ascens.		Declination.		N. or S. I. N.
		H.	M.	D.	M.	
P ole Star —————	02	03	32	87	33	N
The Upper of the two foremost of the Square in the Little Bear —————	02	14	51	75	36	N
The Upper of the two foremost of the Square in the Great Bear —————	02	10	43	63	32	N
The Lower of the two foremost of the Square in the Great Bear —————	02	10	41	58	08	N
The Lower of the two latter of the Square of the Great Bear —————	02	11	36	55	33	N
The Upper of the two latter in the Square of the Great Bear —————	02	11	59	58	51	N
Last but two in the Great Bear's Tail —————	02	12	40	57	47	N
Last but one in the same —————	02	13	10	56	41	N
Last in the same —————	02	13	34	51	00	N
The Dragon's Tail —————	02	13	59	65	56	N
Arcturus —————	01	14	01	20	58	N
Brightest in the Crown —————	02	15	21	27	51	N
Brightest in the Harp —————	01	18	26	38	30	N
Swan's Tail —————	02	20	30	44	05	N
Perseus Right Side —————	02	02	57	48	36	N
Goat or Capella —————	01	04	52	45	37	N
Auriga's Right Shoulder —————	02	05	44	44	56	N
Brightest in the Serpent's Neck —————	02	15	28	07	30	N
Brightest between the Eagle's Shoulders —————	02	19	35	68	03	N
First in Pegasus Wing, or Marchab —————	02	22	48	13	28	N
Beginning of Pegasus Leg —————	02	22	48	26	18	N
End of Pegasus Wing —————	02	23	57	13	22	N
Andromeda's Head —————	02	23	52	27	18	N
Southermost in Andromeda's Girdle —————	02	00	51	33	55	N
Andromeda's Southermost Foot —————	02	01	44	40	44	N
The Bull's Eye, or Aldebrand —————	01	04	17	15	48	N
End of the Bull's Horn —————	02	05	06	28	21	N
Castor —————	02	07	14	32	33	N
Pollox —————	02	07	25	28	46	N
Bright Foot of Gemini —————	02	06	19	16	38	N
Brightest in the Lion's Neck —————	02	10	02	21	29	N
Lion's Heart —————	01	09	51	13	33	N
Lion's Tail —————	01	11	32	16	25	N
Virgins Spike —————	01	13	08	09	31	S
Southermost Scale of Libra —————	02	14	33	14	37	S

A Table of the Fixed Stars.

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Stars Names.	Magnit.	Right Ascens. H. M.	Decla- nation. D. M.	N or S I S
Northernmost Scale of <i>Libra</i> _____	02	14 59	08 07	S
<i>Scorpion's</i> Forehead _____	02	15 46	18 51	S
<i>Scorpion's</i> Heart _____	01	16 10	25 37	S
<i>Samabani</i> _____	01	22 39	31 17	S
<i>Whale's</i> Jaw _____	02	02 45	02 48	N
<i>Orion's</i> Right Shoulder _____	02	05 38	07 18	N
<i>Orion's</i> Left Shoulder _____	02	05 08	06 01	N
First in <i>Orion's</i> Belt _____	02	05 15	00 35	S
Middle of <i>Orion's</i> Belt _____	02	05 20	01 25	S
Last in <i>Orion's</i> Belt _____	02	05 24	02 09	S
<i>Orion's</i> Left Foot, or <i>Regel</i> _____	01	04 59	08 37	S
Mouth of the Great Dog or <i>Syrius</i> _____	01	06 31	16 14	S
Right Forefoot of the Great Dog _____	02	06 09	17 49	S
Little Dog's Thigh _____	02	07 22	06 03	N
<i>Hydra's</i> Heart _____	01	09 12	07 15	S

To know the Hour when any Star cometh upon the Meridian.

The Rule. First seek the Right Ascension of the Star, and also the Right Ascension of the Sun, in the Tables foregoing: From the Right-Ascension of the Star subtract the Right-Ascension of the Sun. But when the Right-Ascension of the Star is less than the Right-Ascension of the Sun, then add 24 Hours thereto, and the Remainder will shew you the Hour Afternoon when the Star cometh upon the Meridian; and if it does exceed 12 Hours, then subtract 12 Hours therefrom, and the Remainder shall shew the Hour and Minute of the Star's coming upon the Meridian after Midnight.

Ex. 1. Upon the 10th of April, I would know when the *Lion's Heart* cometh upon the Meridian: Therefore if you look in the Tables of Right-Ascension and Declination for that Star, you will find it to be 9 Hours 51'. Then look in the Tables of the Right-Ascension of the Sun, and right against the 10th of April you will find the Right-Ascension of the Sun to be 1 Hour 54', which subtracted from the Right-Ascension of the Star, there Remain 7 Hours 57', which is the Time that the Star cometh to the Meridian Afternoon.

Ex. 2. Upon the 5th of November, I desire to know when the *Pull's Eye* cometh upon the Meridian. The Right-Ascension thereof by the Tables you will find to be 4 Hours 17', the Right-Ascension of the Sun that Day is 15 Hours 23'. Therefore because the Right-Ascension of the Stars is less than the Right-Ascension of the Sun, add 24 Hours to the Right-Ascension of the Star, which maketh 28 Hours 17 min. From which subtract the Right-Ascension of the Sun, and the Remainder is 12 hours 54 min. from which I subtract 12 hours, and the Remainder is 54'. So that the said Star cometh upon the Meridian 54 min. after Midnight.

And here note, That the Table of Right-Ascension of the Sun is calculated for Noon every Day, and that it doth encrease by about 4 min. Each Day; so that it may be proportioned, by allowing for every 6 Hours after Noon one Minute.

A Table of the Latitudes and Longitudes of the principal Ports, Harbours, Capes, and Islands, in most of the known Parts of the World : Beginning from the Meridian of *London*. Collected from the best Charts, Descriptions, and Observations of several able and experienced Navigators of our own, and other Nations.

Names of Places.	Latitude N. or S.	Longitude E. or W.	Names of Places.	Latitude. N. or S.	Longitude E. or W.
The Sea-Coast of Greenland.	D. M.	D. M.	Coast of Lapland and Norway.	D. M.	D. M.
H Acluits Headland	80 06 N	14 12 E	Fox Nose	64 42 N	32 36 E
Fair Foreland	79 20 N	14 06 E	Cape Grace	65 35 N	38 25 E
Black Point	77 08 N	27 12 E	Cape Gallant	67 50 N	37 20 E
Point Look out	76 30 N	14 35 E	Cape Race	65 50 N	22 00 E
Cape Blanco	77 58 N	20 04 E	Island Kilduyn	69 15 N	32 00 E
Point Negro	77 12 N	22 32 E	North Cape	71 24 N	22 10 E
Hopeless Isles	77 10 N	21 00 E	Rofs Isles	67 02 N	08 10 E
Islands in the North-Sea.			Catness	61 55 N	02 50 E
Hope Island	76 20 N	27 13 E	Bomel	59 00 N	03 45 E
Cherry Island	74 30 N	20 05 E	Naze of Norway	57 50 N	06 45 E
S. P. of Trinity Island	71 16 N	10 05 W	The Sea-Coast in the Sound.		
Young's Foreland in Trinity Island	71 25 N	10 07 W	The Nyding	57 04 N	07 40 E
Sea-Coast of Nova-Zembla.			Cape Cole	59 25 N	12 46 E
Orange Island	78 20 N	73 35 E	Scarlet Island	56 10 N	11 54 E
Ice Point	78 00 N	75 44 E	Falsterborn	55 30 N	13 50 E
Admiralties	75 06 N	56 50 E	Abbe	60 27 N	20 12 E
Langeness	74 00 N	52 30 E	Wyburrough	61 05 N	35 00 E
Cross Point	72 20 N	52 40 E	Dagaret	59 16 N	20 46 E
Fretum Burrough	69 55 N	56 00 E	Dormamel	56 20 N	19 25 E
River <i>Obij</i> in the Tartarian Sea	69 15 N	62 53 E	Gotland	57 30 N	16 40 E
Mauritias Isle	69 30 N	44 20 E	Horrosound	55 45 N	14 56 E
Sea-Coast in the White-Sea.			Gothsoud	58 15 N	17 05 E
Archangel	64 30 N	37 45 E	Earth-Holme	55 36 N	14 30 E
Swelgenofe	69 13 N	43 30 E	Burnt-Holme	55 33 N	15 46 E
Cape Candenofo	69 20 N	41 32 E	Elfenore	56 20 N	12 35 E
Orologenofo	66 50 N	36 45 E	Coast of Flanders from the Scaw to Calice		
			The Scaw	57 23 N	09 46 E
			Bovenberg	56 21 N	05 55 E
			Holy Land	54 29 N	04 15 E
			The Texel	53 06 N	05 12 E
			The Brill	51 50 N	04 15 E
			Callis.	50 54 N	01 45 E

A Table of Latitude and Longitude.

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Names of Places.			Latitude. N. or S.	Longitude E. or W.	Names of Places.			Latitude. N. or S.	Longitude E. or W.
			D. M.	D. M.				D. M.	D. M.
Sea-Coast of Isleland.									
Langeness	66	38	N	17 05 W	Coswell-Point	54	37	N	06 42 W
Grinse	67	16	N	24 30 W	Fair Foreland	55	10	N	06 30 W
Maze	68	23	N	26 50 W	Aron Isle	54	55	N	09 45 W
Andifer	66	29	N	33 00 W	Black Rock	53	52	N	11 45 W
Snowhill	65	25	N	31 20 W	Sline Head	53	21	N	10 12 W
Alera Point	64	10	N	33 40 W	Blasques	52	00	N	11 53 W
Westmonia Isles	63	20	N	25 28 W	Cape Clear	51	08	N	10 06 W
Merchants Foreland	64	10	N	16 41 W	Old Head	51	40	N	09 05 W
Whale's Back	65	20	N	15 00 W	Hearn-Point	52	07	N	08 12 W
Islands near the Coast of Scotland.					Coast of France, Spain, and Portugal.				
St. Kilda	57	52	N	09 36 W	Sain Head	49	44	N	00 05 E
Sky Island	57	00	N	05 12 W	Cape de la Hague	49	47	N	01 33 W
Lewis Island	58	12	N	66 47 W	Caskets	49	13	N	01 56 W
Fro Islands	62	00	N	08 00 W	Guarnsey	49	33	N	02 28 W
Shetland	60	00	N	03 05 W	Jersey	49	20	N	02 12 W
Fair Isle	59	28	N	04 40 W	Ushant	48	30	N	05 23 W
Isles of Orkney.	59	10	N	03 16 W	Oleroon	45	56	N	00 38 W
Coasts of Scotland, England and Ireland.					Cape de Machia	43	35	N	03 07 W
Catness	58	56	N	01 42 W	Cape Pinas	43	45	N	06 04 W
Buchaness	57	50	N	00 36 W	Cape Ortegal	44	12	N	07 43 W
St. Abb's Head	56	27	N	04 12 W	Cape Finisterre	42	58	N	10 00 W
Tinmouth	55	08	N	03 00 W	The Rock of Lisbon	39	00	N	10 50 W
Flamborough Head	54	07	N	00 10 W	Cape St. Vincent	37	15	N	10 35 W
The Sporn	53	34	N	00 12 W	Cape St. Maria	36	48	N	09 24 W
Wintertonness	52	44	N	01 12 W	Straits of Gibraltar	35	32	N	06 56 W
Orfordness	52	12	N	01 04 W	Coast on the Main Continent in the Straits.				
The North Foreland	51	25	N	01 06 W	Cape de Gat	36	56	N	01 13 W
South Foreland	51	08	N	01 04 W	Cape St. Martin	38	50	N	01 42 E
Dungeness	50	56	N	00 47 W	Cape Dega Frito	41	52	N	03 12 E
Isle of Wight	50	40	N	00 48 W	Cape Larei	42	56	N	06 29 E
Portland	50	29	N	02 50 W	Cape Melle	43	50	N	08 20 E
The Start	50	08	N	03 46 W	Terraciana	41	25	N	13 25 E
The Lizard	49	56	N	05 23 W	Cape Sparteventura	38	00	N	17 43 E
Islands of Silly	49	56	N	06 44 W	Cape Collum	39	05	N	19 15 E
Londey Isle	51	20	N	04 41 W	Cape St. Maria	40	00	N	20 13 E
St. David's Head	52	00	N	05 20 W	Angello	41	48	N	17 50 E
Bardsey Isle	52	42	N	05 05 W	Aneana	43	54	N	14 02 E
Holy Head	53	25	N	04 57 W	Cape Cesta	43	26	N	16 44 E
Isle of Man	53	42	N	04 55 W	Ragufa	42	45	N	19 33 E

Cape

A Table of Latitude and Longitude.

Names of Places.	Latitude. N. or S.		Longitude E. or W.		Names of Places.	Latitude. N. or S.		Longitude E. or W.				
	D. M.		D. M.			D. M.		D. M.				
Cape Linga	40	44	20	58	E	Cephalonia	38	10	N	22	33	E
Cape Matopan	36	28	23	35	E	Zant	37	42	N	22	35	E
Cape St. Angelo	36	30	24	44	E	West end of Candia	35	20	N	24	30	E
Cape Doro	39	10	27	13	E	East end of Candia	35	15	N	28	12	E
Cape Barbarnou	38	08	28	22	E	Rhodes	36	40	N	29	47	E
Cape Saradoni	36	12	30	38	E	West end of Cyprus	35	25	N	33	22	E
Cape Pollopollo	34	56	37	32	E	East end of Cyprus	35	54	N	36	16	E
Cape de Becur	32	40	32	45	E	Sea-Coast of Barbary and Guiny.						
Cape Roatini	32	15	25	30	E	Cape Spartel	35	24	N	07	09	W
Cape Rozato	33	42	21	20	E	Cape Cantin	32	42	N	08	54	W
Cape Bona	37	12	32	32	E	Cape Badajor	27	06	N	15	30	W
Collo	37	10	06	50	E	Cape Blanco	19	26	N	17	20	W
Tunis	36	42	11	60	E	Cape Verde	14	43	N	17	22	W
Cape Falcon	35	55	00	06	W	Sirre Leone	07	32	N	13	12	W
Cape Tres Forcas	35	04	02	25	W	S. Side of St. Anne	06	41	N	16	48	W
Tangier	35	25	07	16	W	Cape de Palmas	04	00	N	07	12	W
Islands within the Straits.					Cape Tres Punctas	03	45	N	01	50	W	
Alboran	35	54	02	40	E	Cape Formosa	04	13	N	06	22	E
Formentara	38	40	01	36	E	Island Fernado	03	28	N	09	16	E
Ivica	39	00	03	36	E	Island Principas	01	45	N	09	00	E
Majorca	39	40	04	12	E	Island Chocos	00	37	N	12	28	W
Minorca	40	05	05	29	E	Island St. Thomas	00	00		09	20	E
Gallatta	37	47	10	48	E	Cape Lopes	01	25	S	16	12	E
C. Pulo in Sardinia	38	54	09	37	E	Cape Negro	16	45	S	14	26	E
C. Corso in Corfica.	42	50	09	34	E	Cape Voltas	29	32	S	16	35	E
Lilbo	42	16	11	15	E	C. Bona Esperanza	34	15	S	17	00	E
Palmerolla	40	51	14	36	E	Western Islands.						
Uftica	38	46	14	35	E	Corva	40	02	N	32	30	W
Maritimo	37	50	12	52	E	Flores	39	31	N	32	25	W
Pantalaria	36	56	13	40	E	Fyal	39	00	N	31	12	W
Limbadosa	35	55	14	15	E	Pico	38	32	N	28	57	W
Limosa	36	12	14	30	E	St. George	38	58	N	28	26	W
Malta	36	00	15	50	E	Tercera	39	33	N	26	51	W
C. Passaro in Sicilia	37	12	16	52	E	St. Michaels	38	06	N	24	12	W
Messina	38	17	16	52	E	St. Maries	37	00	N	23	47	W
Liffa	43	03	16	15	E	The Canary Islands.						
Trinity	41	50	17	15	E	Ferro	28	05	N	18	25	W
Palagosa	42	30	16	12	E	Palme	28	54	N	19	00	W
Augusta	42	52	16	37	E	Gomero	28	10	N	17	32	W
Malida	42	45	17	28	E	Pico Teneriffa	28	30	N	16	49	W
Corfu	39	50	21	30	E							

Madera

This Magnet, or Loadstone, is found in divers Parts of the World and most commonly in Iron Mines, and by some supposed to be of the Iron Ore.

Of these there are divers sorts, different each from other, as well in goodness, as in Colour, Weight and Force, but not in Property, (altho' many have judged the cause of the Variation of the Needle to be according to the Distance of the Mine from whence the Stone was taken, and the place where it is used, but there is no such thing) for all Stones whatsoever have one Direction.

The first and best sort of these Stones come out of *East India*, from the Coast of *China* and *Bengal*, and are of the colour of Iron, or Sanguine colour: These Stones are massy and weighty, and will draw or lift up the just weight of themselves in Iron or Steel, and some five times, ten times, and twenty times their own weight, and these are of the finest sort, and are commonly sold for their weight in Silver in the *East Indies* where they grow, because the best or finest are very rare to be found; for it is commonly an entire Stone, lying in the Earth by it self, and no piece or part of any other.

There is also another sort, of a reddish colour found in *Arabia*, and the Red-Sea, growing broad and flat, much like unto a Tile of a Chimney Hearth: These are not so weighty as those of *China*, but are very near as good, and the Virtue continueth long on the Compass or Needle that is touched upon these Stones.

There are of these Stones likewise in the *Levant*, near a Town called *Porto Feraro*, and are called there *Calamita Preta*, that is to say, the *Black Magnet*; because there is another sort that is white and light, like unto a piece of dry Fullers Clay, and are called *Calamita Blanca*. These black Stones are mingled with white Veins; they are of no great force, nor their Virtue of long continuance.

Also there are of these Stones in *High Germany*, that are full of Holes like a Honey-Comb, and lighter than the other, but better than they; these are of an Iron colour.

Another sort there are in *Norway*, in the Iron Mines, as in *Long-Sound*, and other Places; their colour is black, mixed with gray; these are also of an indifferent force.

There are also some in the Mines of *Caraca* and *Cantabria* in *Spain*; and some there are found in the West of *England*.

There are some also found in *Bobemia*, and several other Places.

Also these Stones are different one from another, as well in Force, as in Colour and Weight, yet all of one Operation in the Needle, shewing all one Point of Direction: Which is a most wonderful and admirable Providence of God to cause it so to be; for infinite would the Distractions be, if it were otherwise in the practical Use of the Compass: For true it is, that God is mighty and marvellous in all his Works, and truly his Power is greatly shewn in this wonderful Miracle of Nature.

Of the Attractive Virtue of the Loadstone.

That this Stone hath an Attractive Operation, is apparently manifest; for if you apply a piece of Iron unto either of the Poles, it will there hold it, and at a Distance will also draw or attract a small piece of Iron, according to the Vigour or Imbecility of the Stone; but what strength soever it hath, it may be artificially improved to be greater, then can by it self be discovered: Which is to be performed by applying a smooth and bright piece of Iron to either Pole of the Stone, and it will immediately deliver its Virtue unto it. The

Virtue being herein contracted in this piece of Iron, the Stone doth manifest it self to have ten times more strength; for this Cause therefore are Loadstones capped with Iron, for the Artificial Augmentation of their strength.

And this Virtue is freely communicated from its self to any thing else that is capable of its Reception; so that a piece of Steel, having received strength from the Stone, that will also attract another piece of Steel in proportion to that Virtue it hath received.

This Experiment I have often tried upon my Loadstone; for by touching of a Knife upon it, it will take up a Key of two Ounces weight; and that within the Sphere of the Stone it shall deliver the Virtue into a piece of Iron, and not touch the Stone at all: and likewise over the Stone, it shall cause one piece of Iron to hang to another. So wonderful is the attractive Quality of this Stone, manifested in these and the like Experiments.

Of the Sympathetical and Antipathetical Property of the Loadstone.

When a Needle is touched upon a Loadstone, the North and South-ends of this Needle will apply themselves respectively to those Poles from whence they received their Magnetical Life, to wit, the North-end of the Needle, to the South-end of the Stone, which denotes their mutual Sympathy; but putting the North-end of the Stone, to the South end of the Needle, when it is upon a Pin, the South-end of the Needle will immediately fly away; and if you put the South-end of the Stone to the North-end of the Needle, it will also discover its Antipathetical Nature, and fly away from it.

But a contrary Operation there is yet in the two Needles to that of the Loadstone; for if one of the Needles be hung upon a Pin, that you apply the North-end of the Needle to the North-end of that upon the Pin, it shall immediately fly away; which denoteth a contrary Operation in the Needle to that of the Loadstone, and the South-end of one will immediately come to the North-end of the other.

The same Property of Sympathetical Coition, and Antipathetical Repulsion, is also discovered by two Loadstones, floating in two little Boats in a great Basen of Water, the two Poles of either Stone being disposed parallel to the Plain of the Horizon; and if you put both the South-Poles together, they will avoid the Contract of one another by a natural Antipathy; but if the North-Pole of the one be direct to the South-Pole of the other, they will immediately manifest their natural Sympathy one to another, and will cleave together by a strong Attraction.

This is also apparently evident between the great Magnet the Earth, and a Loadstone; for if you put a Loadstone into a small string, and let it hang in the Air, or else to float in the Water in a Wooden Dish, and putting the North-end of the small Magnet towards the North-end of the great Magnet the Earth, it shall immediately change its Position, and turn its North-Pole towards the South-Pole of the said great Magnet. The same Experiment is also found with Magnetical Needles, or Mariners Compasses being placed near together, the North point of one will draw the South point of the other, and so will stand North or South *ad Infinitum*,

If a Loadstone be confusedly broken by Violence into many pieces, each of the pieces shall be an entire Loadstone, having both its Poles distinctly of it self, with all the other Properties that were in the Stone before it was broken.

But if a Loadstone be divided in the midst between the two Poles, in the Equinoctial, then it is absolutely two entire Loadstones; and those Parts which

which were the Equinoctials before are now become two Poles, and the two Poles that were Poles before, do continue the same.

But if a Stone be cut Meridionally quite thro' the two Poles, so that one Axis is now converted into two, and each of them remove into each Stone, so that it is also become two entire Loadstones, the *Axis* of either of them will retire into the Gravity of either Piece; and if you join these two Pieces together again, the two *Axis* will again become one, which is most admirable to behold.

But if you cut off a piece of the Stone at the very Pole, in a parallel Section the Virtue of that piece will immediately retire from it into the main Stone, and will scarcely have any Virtue at all therein, but applying this small piece that was cut off, to the same place again, the Stone will forthwith impart the same Virtue as was before, into this piece so cut off, so long as it doth abide in that place: But when it is removed, it doth again recall its Virtue from the said piece. This I have experienced in a Stone of a very considerable piece.

And in the same manner, if you apply a weak Stone to the Poles of a strong one, the strong Stone will impart of its Virtue to the weak Stone, making it to be as strong as it self, so long as it is its Neighbour; but when this weak Magnet deserts this neighbourly Proquintity, the strong Magnet will draw its Virtue to it self again, and will trust it no further than the Power of its recal.

To find the Poles of a Stone.

There are several ways for the Performance of this Experiment. First, you may have a thin piece of Steel about an Inch in length, and half of an Inch broad; this piece of thin Steel being bent circular and laid on the Stone, will immediately lie parallel to the *Axis* of the Stone, and direct which way the Poles do lie. Which being discovered near where they lie, you may find them more exactly by a small piece of sewing Needle; which being laid on the Stone, if it be near either of the Poles, will elevate one end thereof; then move it farther and farther, till it doth erect it self perpendicular, and that very point will be the Pole of the Stone.

Now to know which Pole it is, you may apply a small Needle of a Dial to it, and if the Pole draw the North-end of the Needle, then is that the North-Pole of the Stone; and the contrary.

Or otherwise you may find the Pole by a sewing Needle and Thread, by hanging it over the Stone where you suppose the Pole to be, and keep it a little short from the Stone, and the end of the Needle will directly point to the Pole of the Stone.

A delightful Experiment, representing the Engaging of Two Armies.

FOR the performance hereof, you must have a Brass or Pewter Plate, and upon this Plate put several little heaps of the Filings of Iron, with some short Bits of sewing Needles, and put them in order of a Battle, one Main Body against another, also with their Right and Left wings, and their Forlorn-hopes; this being done, bring the Loadstone under the Plate with one of the Poles upward, and put it first toward one of the Right wings of the Army, and they will immediately receive an Alarm, and as it were stand to their Arms; then move the Stone toward the other wing of the Enemy, and they also will receive the like Alarm; and then by moving the Stone to and fro under the Plate, you will put both Parties into a Motion, in a charging Posture, and one to charge the other in a desperate Engagement, and one to come within the

the other; and so you may at last engage the Main Bodies of the Army, and there you may see that sometimes they are Conquerors, and sometimes conquered, which is caused by the Motion of the Stone with your Hand under the Plate; and the short Bits of the Needles may represent their Generals and Commanders, which will be very full of Action, where you may see sometimes that there will be Twenty or more of the Common Soldiers to fall foul of the said Commanders; and if between these Armies you put small Breast-works and Trenches made with Sand, and Filings put in the Trenches, you will then have represented the sudden rising of them one against another, as if they lay in Ambush, waiting for an Opportunity against their Enemies.

To make a Sewing-Needle swim upon the Surface of the Water, and to play up and down like a Fish, and to find out the Magnetical Meridian.

TAKE a small Sewing-Needle, and touch the two Ends thereof upon the two Poles of the Stone: and having a Glass of Water before you, take the Needle very lightly between your Finger and Thumb, and lay it lightly on the Surface of the Water, so that it break not through, and there it will lie; then take a Knife that hath been touched with the Loadstone, and bring it to and fro upon the Edge of the Glass, and the Needle will follow it up and down, and will play up and down on the Superfices of the Water like a Fish; and then take away the Knife, and the Needle will immediately posite it self to the Meridian, pointing due North and South.

Such an inferiour Instrument as this may stand Men in great stead in time of great Straits and Exigencies, if they should be at Sea, and their Compasses be taken from them, for if you put a Needle, being touched, thro' a small piece of Cork, it will then perform this effect exceeding well in all Storms and Tempests whatsoever, being born up by the Cork on the top of the Water, and the Position thereof will be continually in the Magnetical Meridian.

To Infuse Magnetical Virtue into a Needle, without the help of a Loadstone

IRON being a Mineral of the Earth, and having a Sympathetical Quality with the Loadstone, acquiring this Verticity from the Magnetism of the Earth, being dispensed according to the various Positions thereof; for all Iron, whose Position is parallel to the Axis of the World, or if it be perpendicular to the Horizon, the Upper-part thereof shall have North, and the Lower part South Virtue; as Bars in Windows, Casements, Tongs and Fire-Forks, and all such things, &c. And according to the Length of the Time, of the Position of any such piece of Iron, the stronger Virtue it doth contract; So that I once made an Experiment upon a smooth piece of Iron, which had for several Years been in a perpendicular Posture, and I filed the upper-end thereof bright, and touched a small new Needle thereon, the South-end I touched upon the North or upper part of the Iron, and the North-end upon the South or lower end; and I found the Needle to play indifferently well, and to conform it self to the Magnetical Meridian.

The Reason of this is from the Nature of the Iron, it being a Metal deducted out of the Loadstone, or out of a Mine of that kind; the best Iron Mine and Loadstone is the same thing; for it being placed artificially in the Air, or upon the Water, moveth North and South, attracteth other Iron unto it, and performeth the same Conclusions as the Magnet it self.

Here followeth several necessary TABLES, with their Use and Application in the Art of Navigation.

The Moon's Age for the Year, 1714.

M.		D.	H.	M.	M.		D.	H.	M.
January.	New moon.	04	15	56	July.	First quart.	08	07	03
	First quart.	11	08	11		Full moon.	15	13	06
	Full moon.	19	03	06		Last quart.	22	05	26
	Last quart.	27	06	24		New moon.	29	18	40
February.	New moon.	03	02	25	August.	First quart.	06	22	07
	First quart.	09	20	04		Full moon.	13	20	52
	Full moon.	17	22	02		Last quart.	20	13	04
	Last quart.	25	21	50		New moon.	28	10	29
March.	New moon.	04	11	44	September.	First quart.	05	12	03
	First quart.	11	11	07		Full moon.	12	05	24
	Full moon.	19	15	31		Last quart.	19	00	37
	Last quart.	27	06	24		New moon.	27	03	35
April.	New moon.	02	20	43	October.	First quart.	04	23	03
	First quart.	10	04	39		Full moon.	11	14	28
	Full moon.	15	06	34		Last quart.	18	16	04
	Last quart.	25	13	04		New moon.	26	20	54
May.	New moon.	02	06	11	November.	First quart.	03	09	01
	First quart.	09	20	07		Full moon.	10	00	56
	Full moon.	17	18	56		Last quart.	17	11	03
	Last quart.	24	19	11		New moon.	25	12	46
June.	New moon.	21	16	47	December.	First quart.	02	17	02
	First quart.	08	14	27		Full moon.	09	13	20
	Full moon.	16	04	52		Last quart.	17	09	03
	Last quart.	22	23	08		New moon.	25	04	12
	New moon.	30	04	46					

In this Year 1714, we shall meet with Five Luminarian Eclipses, Three of the Sun and Two of the Moon.

The first will be a Solar Eclipse, on May the 2d, about 6 hours Afternoon in Taurus 22 Deg 24 min. invisible to us. The second will be a Lunar Defect on May the 18th, near 7 a Clock in the Morning, in Sagittarius 7 deg. 12 min. invisible to us. The third will be a Solar Deliquium, on July the 1st, about our 5 a Clock in the Morning, in Gemini 20 deg. 41 min. invisible. The fourth will be an Eclipse of the Sun, on October the 27th, near our 9 a Clock in the Morning, in Virgo 14 deg. 31 min. but not visible to us in England. The fifth will be a Lunar Deliquium, on November the 10th, a little past 1 a Clock Afternoon, in Taurus 28 deg. 50 min. It will be a great Eclipse to such as Inhabite our Antipodes, viz. not only Total, but nearly Central.

The Moon's Age for the Year, 1715.

M.		D.	H.	M.	M.		D.	H.	M.
January.	First quart.	01	01	08	July.	Full moon.	05	01	52
	Full moon.	08	03	52		Last quart.	12	01	12
	Last quart.	16	05	50		New moon.	18	23	47
	New moon.	23	15	34		First quart.	26	21	39
	First quart.	30	10	14	August.	Full moon.	03	12	18
February.	Full moon.	06	20	54		Last quart.	10	16	25
	Last quart.	15	01	55		New moon.	17	12	18
	New moon.	22	01	48		First quart.	25	14	37
	First quart.	28	20	03	September.	Full moon.	01	21	42
March.	Full moon.	08	14	47		Last quart.	08	13	21
	Last quart.	16	17	14		New moon.	16	03	19
	New moon.	23	10	40		First quart.	24	07	12
	First quart.	30	07	21	October.	Full moon.	01	06	44
April.	Full moon.	07	08	15		Last quart.	07	22	51
	Last quart.	15	06	09		New moon.	15	21	04
	New moon.	21	24	17		First quart.	23	22	51
	First quart.	25	20	03		Full moon.	30	16	13
May.	Full moon.	07	00	08	November.	Last quart.	06	12	09
	Last quart.	14	14	03		New moon.	14	15	15
	New moon.	21	04	34		First quart.	22	11	02
	First quart.	27	10	25		Full moon.	29	02	24
June.	Full moon.	05	10	19	December.	Last quart.	06	05	23
	Last quart.	12	20	03		New moon.	14	10	09
	New moon.	19	13	24		First quart.	21	28	12
	First quart.	27	03	54		Full moon.	28	13	50

Four Luminarian Eclipses will happen this Year 1715, in the following Order.

1. The first will be an Eclipse of the Sun, on April the 22d day somewhat after 9 in the Morn, in 8. 12 deg. 18 min. but not visible to us by reason of the Moon's North Latitude, tho' a great Eclipse of it self.
2. The second will be a Lunar Defect on May the 7th, somewhat after our Noon, in m 26 deg. 51 min. Invisible to us, but to our *Antipodes* the Moon will be 8 Digits darkned.
3. The third will be a Solar *Deliquium* on October the 16th, about our 9 a Clock in the Morning. This, (like that in April) will be an almost total Defect, but not to be seen of us, it is celebrated in 3 deg. and 13 min. of *Capricorn*.
4. The fourth will be a Lunar Obscuration, on October the 31st, at or about 4 in the Morning, It is made in 8. 18 deg. 7 min. and may be seen with us, if the Air be clear, to more than 8 Digits darkned.

The Moon's Age for the Year, 1716.

M.		D.	H.	M.		D.	H.
January.	Last quart.	05	01	July.	Last quart.	01	09
	New moon.	13	03		New moon.	07	12
	First quart.	20	06		First quart.	15	06
	Full moon.	27	04		Full moon.	23	10
February.	Last quart.	04	11	August.	Last quart.	30	04
	New moon.	12	06		New moon.	06	09
	First quart.	19	03		First quart.	13	11
	Full moon.	26	06		Full moon.	21	10
March.	Last quart.	05	07	September.	Last quart.	28	09
	New moon.	12	04		New moon.	04	08
	First quart.	19	10		First quart.	12	06
	Full moon.	26	09		Full moon.	20	09
April.	Last quart.	04	01	October.	Last quart.	27	04
	New moon.	11	03		New moon.	04	10
	First quart.	17	06		First quart.	12	02
	Full moon.	25	01		Full moon.	19	08
May.	Last quart.	03	03	November.	Last quart.	26	00
	New moon.	10	09		New moon.	03	03
	First quart.	17	04		First quart.	11	08
	Full moon.	25	04		Full moon.	18	07
June.	Last quart.	02	02	December.	Last quart.	24	11
	New moon.	08	05		New moon.	02	10
	First quart.	15	03		First quart.	10	12
	Full moon.	23	08		Full moon.	17	05
					Last quart.	24	01

In this Year there will be Two Eclipses only, and both of the Sun.

1. The first will happen on April the 11th Day.
 2. The second on October the 4th Day.
- Both Invisible.

The Moon's Age for the Year, 1717.

M.	D.	H.	M.	D.	H.
January.	New moon.	01 06	July.	First quart.	04 11
	First quart.	09 00		Full moon.	12 00
	Full moon.	16 04		Last quart.	20 09
	Last quart.	23 07		New moon.	26 12
	New moon.	31 00	August.	First quart.	02 10
Febr.	First quart.	07 10		Full moon.	11 03
	Full moon.	14 03		Last quart.	18 06
	Last quart.	22 03		New moon.	25 08
March.	New moon.	02 04	September.	First quart.	10 03
	First quart.	09 06		Full moon.	09 06
	Full moon.	16 03		Last quart.	17 01
	Last quart.	23 11		New moon.	23 06
	New moon.	31 03	October.	First quart.	01 10
April.	First quart.	07 01		Full moon.	09 09
	Full moon.	14 04		Last quart.	16 07
	Last quart.	22 06		New moon.	23 07
	New moon.	30 02		First quart.	31 07
May.	First quart.	06 07	November.	Full moon.	07 10
	Full moon.	14 06		Last quart.	14 03
	Last quart.	22 10		New moon.	21 11
	New moon.	29 10		First quart.	30 03
June.	First quart.	05 02	December.	Full moon.	07 09
	Full moon.	12 09		Last quart.	13 12
	Last quart.	20 10		New moon.	21 06
	New moon.	27 05		First quart.	29 10

Four Eclipses the Year 1717, Two of the Sun, and Two of the Moon.

1. Of the Moon, on *March* the 15th day, and will be a visible Eclipse.
2. Of the Sun, on *March* the 31st day, but this Eclipse will be invisible.
3. Will be an Eclipse of the Moon, on *September* the 9th day, visible to us in *England*.
- 4th. And last, will be a *Solar Deliquium*, on *September* the 23d day, but invisible.

The Moon's Age for the Year, 1718.

M.	D.	H.	M.	D.	H.
January.	Full moon.	05 08	July.	Full moon.	01 01
	Last quart.	12 01		Last quart.	09 04
	New moon.	20 01		New moon.	16 05
	First quart.	28 01		First quart.	23 08
February.	Full moon.	04 06	August.	Full moon.	31 04
	Last quart.	11 04		Last quart.	08 06
	New moon.	19 07		New moon.	15 01
	First quart.	26 12		First quart.	21 07
March.	Full moon.	05 03	September.	Full moon.	29 08
	Last quart.	11 08		Last quart.	06 06
	New moon.	20 11		New moon.	13 08
	First quart.	28 09		First quart.	20 09
April.	Full moon.	04 10	October.	Full moon.	29 00
	Last quart.	11 02		Last quart.	06 02
	New moon.	19 02		New moon.	12 06
	First quart.	26 04		First quart.	20 01
May.	Full moon.	03 00	November.	Full moon.	28 05
	Last quart.	11 08		Last quart.	04 11
	New moon.	19 01		New moon.	11 06
	First quart.	25 09		First quart.	18 10
June.	Full moon.	01 12	December.	Full moon.	26 09
	Last quart.	09 10		Last quart.	03 07
	New moon.	17 10		New moon.	10 08
	First quart.	24 20		First quart.	18 08
				Full moon.	26 10

The Year 1718, hath Four Eclipses, Two of the Sun and Two of the Moon.

The first will be a Solar Defect, on *February* 19th day, but not Visible to us.

The second will be an Invisible Eclipse of the Moon, on *March* the 5th day.

The third will be an Eclipse of the Sun on *August* the 14th day, Invisible as to us.

The fourth will be a Lunar Deliquium, on *August* the 19th day, Visible and Total.

The Moon's Age for the Year, 1719.

M.		D.	H.	M.		D.	H.
January.	Last quart.	01	16	July.	New moon.	05	20
	New moon.	09	01		First quart.	12	16
	First quart.	17	05		Full moon.	19	19
	Full moon.	24	10		Last quart.	27	21
	Last quart.	31	02	August.	New moon.	04	05
Febr.	New moon.	07	19		First quart.	10	21
	First quart.	15	23		Full moon.	18	09
	Full moon.	22	20		Last quart.	26	13
March.	Last quart.	01	13	September.	New moon.	02	14
	New moon.	09	13		First quart.	09	06
	First quart.	17	12		Full moon.	17	01
	Full moon.	24	06		Last quart.	25	04
	Last quart.	31	02	October.	New moon.	01	23
April.	New moon.	08	06		First quart.	08	17
	First quart.	15	06		Full moon.	16	19
	Full moon.	22	14		Last quart.	24	16
	Last quart.	29	18		New moon.	31	09
May.	New moon.	07	21	November.	First quart.	07	08
	First quart.	15	06		Full moon.	15	15
	Full moon.	21	22		Last quart.	23	04
	Last quart.	29	11		New moon.	29	19
June.	New moon.	06	10	December.	First quart.	07	04
	First quart.	13	11		Full moon.	15	07
	Full moon.	20	07		Last quart.	22	13
	Last quart.	28	03		New moon.	29	08

This Year hath Two Eclipses, viz. One of the Sun, and the other of the Moon.

The first will be of the Sun, *August* the 4th, at 5 of the clock in the Afternoon, Invisible.

The second of the Moon, *August* the 18th, about 9 in the Evening; there will be 5 Digits, that is almost half of the Moon's Body Eclipsed.

The Moon's Age for the Year, 1720.

M.		D.	H.	M.		D.	H.
January	First quart.	06	02	July	First quart.	01	13
	Full moon.	13	22		Full moon.	07	16
	Last quart.	20	21		Last quart.	15	17
	New moon.	27	22		New moon.	23	17
February	First quart.	04	22	August	First quart.	30	17
	Full moon.	11	23		Full moon.	06	14
	Last quart.	18	17		Last quart.	13	22
	New moon.	26	14		New moon.	21	15
March	First quart.	05	18	September	First quart.	28	23
	Full moon.	12	21		Full moon.	04	15
	Last quart.	19	14		Last quart.	12	17
	New moon.	26	18		New moon.	20	19
April	First quart.	03	21	October	First quart.	26	18
	Full moon.	10	18		Full moon.	04	19
	Last quart.	17	22		Last quart.	12	23
	New moon.	25	23		New moon.	19	13
May	First quart.	03	21	November	First quart.	26	16
	Full moon.	10	13		Full moon.	03	13
	Last quart.	16	22		Last quart.	11	14
	New moon.	25	14		New moon.	17	22
June	First quart.	01	18	December	First quart.	24	16
	Full moon.	08	20		Full moon.	02	19
	Last quart.	15	13		Last quart.	10	17
	New moon.	23	15		New moon.	17	20
					First quart.	24	22

This Year there will be Two Eclipses, and both of the Sun.

The First will be the 28th of *January*, about 10 a clock in the Morning Invisible.

The Second will be on the 24th of *July*, at 5 in the Morning, Invisible.

The Moon's Age for the Year, 1721.

M.	D.	H.	M.	D.	H.
January.	Full moon.	02 03	July.	Last quart.	04 18
	Last quart.	09 16		New moon.	12 21
	New moon.	16 08		First quart.	20 14
	First quart.	23 18		Full moon.	27 04
	Full moon.	31 20	August.	Last quart.	08 08
Febr.	Last quart.	08 01		New moon.	11 11
	New moon.	14 21		First quart.	18 20
	First quart.	22 16		Full moon.	25 13
March.	Full moon.	02 10	September.	Last quart.	02 01
	Last quart.	09 08		New moon.	10 01
	New moon.	16 10		First quart.	17 03
	First quart.	24 09		Full moon.	23 12
	Full moon.	31 22	October.	Last quart.	01 21
April.	Last quart.	07 14		New moon.	09 15
	New moon.	14 22		First quart.	16 18
	First quart.	23 03		Full moon.	23 15
	Full moon.	30 07		Last quart.	31 18
May.	Last quart.	06 22	November.	New moon.	08 02
	New moon.	14 15		First quart.	14 18
	First quart.	22 17		Full moon.	22 08
	Full moon.	29 14		Last quart.	30 04
June.	Last quart.	05 07	December.	New moon.	07 13
	New moon.	13 06		First quart.	14 05
	First quart.	21 06		Full moon.	22 02
	Full moon.	27 20		Last quart.	29 17

There will be Six Eclipses this Year, viz. Three of the Sun, and Three of the Moon.

The first will be of the Moon, January 2d, at 3 in the Afternoon Invisible.

The second will be of the Sun, January 16th at 8 at Night, Invisible.

The third of the Moon, June 28th, at 8 in the Morning, Invisible.

The fourth of the Sun, July 13th, at 9 in the Morning, visible; there will be 3 Digits Eclipsed.

The fifth of the Sun, December 8, about 1 in the Morning, Invisible.

The sixth of the Moon, Decemb. 22d, at 2 in the Afternoon, part Visible.

A Table of Latitude and Longitude.

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Names of Places.	Latitude.		Longitude.		Names of Places.	Latitude.		Longitude.	
	N. or S.	D. M.	E. or W.	D. M.		N. or S.	D. M.	E. or W.	D. M.
					Islands in East India.				
Madera	32	25	N	17 42 W	Romeyros	29	00	S	68 00 E
Port Sancto	33	10	N	16 28 W	John de Lisbon	27	00	S	54 25 E
Canaria	28	00	N	15 56 W	Diego Roize	19	12	S	62 00 E
Forteventura	28	00	N	13 27 W	St. Branda	15	06	S	65 35 E
Lancerotta	29	06	N	12 47 W	Dolgatias	15	20	S	64 15 E
Cape de Verde Islands.					Morossas	20	12	S	60 30 E
St. Antonio	17	45	N	24 56 W	Domascaicas	20	45	S	56 00 E
St. Vincent	17	45	N	24 50 W	St. Appollonia	21	15	S	52 00 E
St. Lucia	17	30	N	24 23 W	S. end of St. Lawrence	25	30	S	48 00 E
Isle Brava	14	26	N	26 17 W	N. end of St. Lawrence	12	26	S	52 32 E
Isle Fogo	14	45	N	25 39 W	Bassos de India	21	30	S	36 25 E
St. Jago	14	56	N	23 42 W	John de Nova	17	32	S	43 06 E
Mayo Isle	15	12	N	23 10 W	Mayotta	12	35	S	45 30 E
Isle of Sal	17	33	N	21 58 W	Comore	11	21	S	42 27 E
Bonavista	16	29	N	21 52 W	De Natal	08	25	S	50 00 E
					Casmolede	09	33	S	50 20 E
St. Matthews	02	30	S	13 06 E	De Almiranta	02	52	S	47 05 E
Island Anabona	02	00	S	06 12 E	Domescaicubas	03	20	S	62 25 E
Ascension	08	00	S	14 06 E	St. Hermanas	03	06	S	66 00 E
St. Helena	15	45	S	06 30 E	Diego Gratiosa	09	00	S	69 52 E
Island Degialica	37	56	S	06 42 E	De Gamo	02	45	S	81 02 E
Island Desistian	36	50	S	06 12 E	Adu	05	40	S	81 00 E
Coast of the Main Continent in East-India.					Apoluria	09	20	S	92 40 E
Cape Anguilhas	14	10	S	18 42 E	Island Prancel	10	25	S	75 10 E
Cape Corintes	24	07	S	36 30 E	Cubile	08	52	N	85 43 E
Cape de Guada	12	06	S	40 05 E	Molique	09	06	N	86 07 E
Cape de Guardafin	12	46	N	51 33 E	Andaro	11	28	N	87 26 E
Cape de Rasalgate	22	51	N	52 10 E	N. W. Point Sumatra	05	35	N	95 12 E
Surrat	21	13	N	71 46 E	S. E. end of Sumatra	05	13	S	104 16 E
Goa	15	30	N	73 07 E	Bantam	05	45	S	105 00 E
Cape Comerin	08	30	N	77 32 E	Batavia	06	25	S	106 10 E
S. W. P. of Ceylon	07	45	N	80 00 E	Combavia	08	16	S	120 33 E
River Bengal	22	10	N	115 49 E	Flores	08	46	S	122 45 E
River de Care	10	51	N	114 12 E	Timor	10	00	S	124 00 E
Siam	14	18	N	100 41 E	Ceram	03	00	S	127 00 E
Cambodia	11	20	N	104 00 E	Amboina	03	05	S	126 45 E
Vischers Point	22	32	N	108 00 E	S. end of Celebes	05	30	S	117 30 E
Point of Cavallos	25	15	N	123 00 E	N. Point of Celebes	02	40	N	122 25 E
Cape Somber	27	48	N	122 05 E	Middle of Gilolo	00	00		126 30 E
Nighai	36	50	N	122 00 E	Bachian	00	03	N	128 12 E
Corea.	35	00	N	125 00 E	Machian	00	14	N	128 08 E

A Table of Latitude and Longitude.

Names of Places.	Latitude. N. or S.	Longitude E. or W.	Names of Places.	Latitude. N. or S.	Longitude E. or W.
	D. M.	D. M.		D. M.	D. M.
Motir	00 24	128 06 E	Cape de Passao	00 00 N	86 25 W
Pottobackers	00 30	128 12 E	Payta	04 32 S	85 00 W
Tidore	00 42	124 00 E	Truxilla	08 10 S	83 00 W
Miserra	00 43	128 06 E	Villa la Nasca	15 12 S	80 10 W
Ternate	00 48	128 10 E	Arica	18 30 S	17 00 W
St. Johannes	04 12	120 46 E	Island Ferando	33 45 S	85 40 W
S. Point of Borneo	04 36 S	113 26 E	Baldivir	40 05 S	80 25 W
N. Point of Borneo	07 30	112 15 E	Port St. Cyprian	43 15 S	81 22 W
W. end of Mindano	06 49	123 24 E	West Entrance of } Magellan	52 00 S	82 15 W
Anamba	02 40	108 41 E	Cape Horn	57 30 S	78 45 W
Natura	03 30	109 40 E			
St. Juan	08 15	128 20 E			
Tandaia	12 42	122 33 E	Islands in the Great South-Sea.		
Masbat	11 50	125 36 E			
Sebu	09 55	125 00 E	Honder Island	14 05 S	140 30 W
Pandi	11 05	124 00 E	Water Islands	14 52 S	150 00 W
Mindora	13 10	117 29 E	Island Tiburones	12 00 S	162 00 W
Paragoa	09 42	118 30 E	St. Pedro	22 12 S	150 50 W
South-end of Lucon	12 42	125 42 E	P. Williams Islands	18 14 S	175 00 W
North-end of Lucon	18 40	123 50 E	Island of Good-Hope	17 14 S	177 36 E
Middle of Aynam	18 26	108 00 E	States Land	38 10 S	174 06 E
Formosa	23 30	124 00 E	Green Islands	04 05 S	154 00 E
Pirando Isle	34 00	125 40 E	Salteadores Isle	06 36 N	154 04 E
W. end of Japan	34 50	132 00 E	Miracomo	06 25 N	157 42 E
N. end of Cikoko	34 10	132 12 E	Island de Ladrões	10 05 N	152 00 E
Tonfa	33 20	135 00 E	Nadadores	04 20 N	168 56 E
N. end of Japan	40 06	145 22 E	Barbadoes Isles	07 10 N	177 05 E
Cape Froed in Jeso	42 49	165 20 E	St. Peter's Isle	11 15 N	173 00 W
C. Patience in Jeso	49 00	168 00 E	Harmair's Isle	15 12 N	156 10 E
The Coast of America in the South-Sea.			Coast on the Main Continent of America.		
Straights of Anian	57 00	126 00 W	Lemair's Strait	54 35 S	73 15 W
Cape Blanco	12 30	131 00 W	Cape Pennas	54 00 S	60 40 W
S. Francis Drake's B.	38 16	130 00 W	E. Entr. of Magellan	52 16 S	75 00 W
Island Peraros	30 00	124 10 W	Cape Blanco	47 28 S	68 15 W
Cape St. Lucas	23 05	112 00 W	Cape St. Antonio	36 50 S	57 25 W
Cape Corientes	19 16	110 30 W	Cape St. Maria	34 32 S	55 00 W
Aquatulco	16 45	94 10 W	Cape Frio	22 40 S	42 05 W
Gulf of Salina	10 00	89 40 W	Baja de toda Santos	13 30 S	40 15 W
Cape St. Maria	07 10	84 56 W	Cape St. Augustin	08 28 S	34 55 W
Cape Corintas	04 48	81 20 W	Black Point	03 12 S	35 00 W
Cape de Francisco	01 25	86 40 W	River Cassipore	04 00 N	50 00 W
			Suranam	07 10 N	56 04 W

A Table of Latitude and Longitude.

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Names of Places.	Latitude.		Longitude		Names of Places.	Latitude.		Longitude					
	N. or		E. or W.			N. or S.	E. or W.						
	D. M.		D. M.		Islands in the West-India.	D. M.		D. M.					
Cape three Points	11	20	N	62	57	W	Anguilla	18	45	N	62	42	W
Cape de Coquibocoa	13	06	N	71	12	W	St. Christophers	17	38	N	62	34	W
Cartagena	10	33	N	77	36	W	South-End Barbada	17	50	N	61	45	W
Cape de Gracias	14	37	N	86	04	W	Antego	17	15	N	61	44	W
Cape de Catoche	21	05	N	89	50	W	Guardalupa	16	16	N	61	26	W
Cape Rexo	22	45	N	102	39	W	Marigellanta	16	05	N	61	15	W
Cape Blanco	26	56	N	103	00	W	Dominica	15	44	N	61	12	W
Cape Escondido	29	50	N	92	20	W	Martineco	14	44	N	61	00	W
La Florida	25	05	N	81	30	W	St. Lucia	13	53	N	61	04	W
Cape Fair	34	38	N	75	00	W	Barbadoes	13	10	N	58	32	W
Cape Henry	37	00	N	74	00	W	St. Vincent	13	06	N	61	00	W
Cape Charles	37	26	N	73	35	W	Granada	11	56	N	61	30	W
Cape May	39	26	N	72	29	W	Tobago	11	10	N	59	00	W
E. end of Long-Island	40	55	N	70	00	W	Point de Gallaia	10	45	N	58	57	W
Cape Cod	42	14	N	67	52	W	Mevis	17	18	N	62	38	W
Cape Ann	43	00	N	72	00	W	Monferat	16	36	N	62	12	W
Cape Forcu	44	05	N	63	50	W	Margaretta	11	45	N	63	26	W
East end of the Isle of Sables	43	30	N	65	38	W	Tortogas	11	12	N	66	30	W
Cape Britain	45	33	N	59	06	W	Doikilla	12	20	N	67	30	W
Cape Raze	46	16	N	53	45	W	Bonayre	12	04	N	69	20	W
Conception Bay	47	50	N	53	22	W	Quiffa	12	26	N	66	10	W
Bay of Bulls	47	27	N	53	35	W	East-end of Hispaniola	18	52	N	68	04	W
Cape Bona Vista	49	22	N	53	40	W	W. end of Hispaniola	18	35	N	77	12	W
Pengwins Isle	50	54	N	54	12	W	P. Royal in Jamaica	18	15	N	76	10	W
Cape Gata	50	00	N	52	22	W	East-end of Cuba	20	16	N	74	12	W
Bell Isle	51	48	N	55	16	W	West-end of Cuba	21	40	N	84	46	W
Islelands in the West-Indies.							Camnamis	20	00	N	83	10	W
Bermudas	32	25	N	64	23	W	Great Caiman	20	15	N	80	22	W
Behama	27	12	N	78	04	W	Santa Villa	17	30	N	83	15	W
North-East Point of Laucaonique	27	52	N	79	40	W	Masquito	13	42	N	79	43	W
Signateo	25	20	N	74	10	W	Guanabo	16	30	N	86	42	W
Guatro	25	46	N	73	25	W	Guanabimo	16	12	N	88	30	W
Guamina	25	16	N	73	20	W	Cozumal	19	26	N	90	25	W
Tiango	24	32	N	71	50	W	Lafelleiranes	22	05	N	93	15	W
Majagana	22	56	N	71	46	W	The Northern Parts of America.						
Caicos	22	00	N	68	10	W	Cape Camas	53	39	N	151	10	W
Yhagua	22	21	N	72	26	W	Resolution Isles	61	12	N	64	25	W
Yamata	22	30	N	73	13	W	The King's Foreland	51	55	N	82	30	W
Samana	24	22	N	74	10	W	Queen Ann's Foreland	64	13	N	53	00	W
Yamina	24	25	N	75	30	W	Cape Charles	52	10	N	68	22	W
							N. end of Mansfield I.	53	40	N	74	00	W

A Table of Latitude and Longitude.

Names of Places.	Latitude.	Longitude	Names of Places.	Latitude.	Longitude
	N. or S.	E. or W.		N. or S.	E. or W.
	D. M.	D. M.		D. M.	D. M.
P. Rupert's River ----	51 22 N	78 20 W	Stir Dudley Digg's C.	76 28 N	55 26 W
Cape Monmouth ----	54 38 N	95 00 W	Sanderfon's Tower ---	68 10 N	63 52 W
Cape Henrietta ----	54 46 N	83 50 W	Cape Walsingham ---	63 19 N	71 26 W
Port Nelson ----	57 12 N	90 16 W	Cape Comfort ----	62 20 N	56 40 W
Cape Southampton ---	62 32 N	80 04 W	Cape Desolation ----	61 45 N	49 28 W
Seahorse Point ----	65 00 N	95 40 W	Cape Farewel ----	60 00 N	48 04 W

The Use of the Table of Latitude and Longitude of Places.

IN this Table there are Two Columns, the One shewing the Latitude, the Other the Longitude of Places: The Latitudes are distinguished by the Letters N and S, which shew the Latitude of the Place to be either Northerly or Southerly. The Longitudes are accounted either Easterly, or Westerly, from the Meridian of London. An Example or Two will make it plain.

Example 1.

What is the Latitude and Longitude of the *Lizard*, upon the Coast of *England*?
Against the *Lizard* you will find $49^{\circ} 56'$ North Latitude, and $05^{\circ} 23'$ West Longitude.

Example 2.

What is the Latitude and Longitude of *Bermudas*, one of the *West-India* Islands?

Against *Bermudas* you will find Lat. $32^{\circ} 25'$ N. Long. $64^{\circ} 23'$ W.

To find the difference of Longitude between any Two Places.

Take the Longitudes of the Two Places out of the Tables, and if they have both East, or both West Longitudes, their Difference; but if the one have an East, and the other a West Longitude, their Sum is the Difference of Longitude required.

Example 1.

What is the Difference of Longitude between *Bermudas*, and *Cape Race* in *Newfound-Land*?

The Longitude of *Bermudas* is $64^{\circ} 23'$ W.
of *Cape Race* $53^{\circ} 45'$ W.

The Remainder is the Difference of Longitude $10^{\circ} 38'$

Example 2.

What is the Difference of Longitude between *Cape Race*, and *Cape Bona Esperanza*?

The Longitude of *Cape Race* is $53^{\circ} 45'$ W.
of *Cape Bona Esperanza* $17^{\circ} 00'$ E.

The Sum is the Difference of Longitude $70^{\circ} 45'$

Here followeth a Table of Meridional Parts.

M	0 d.	1 d.	2 d.	3 d.	4 d.	5 d.	6 d.	7 d.	8 d.	9 d.	10 d.	11 d.	12 d.	13 d.	M
0	0	60	120	180	240	300	360	420	480	540	600	660	720	780	0
1	1	61	121	181	241	301	361	421	481	541	601	661	721	781	1
2	2	62	122	182	242	302	362	422	482	542	602	662	722	782	2
3	3	63	123	183	243	303	363	423	483	543	603	663	723	783	3
4	4	64	124	184	244	304	364	424	484	544	604	664	724	784	4
5	5	65	125	185	245	305	365	425	485	545	605	665	725	785	5
6	6	66	126	186	246	306	366	426	486	546	606	666	726	786	6
7	7	67	127	187	247	307	367	427	487	547	607	667	727	787	7
8	8	68	128	188	248	308	368	428	488	548	608	668	728	788	8
9	9	69	129	189	249	309	369	429	489	549	609	669	729	789	9
10	10	70	130	190	250	310	370	430	490	550	610	670	730	790	10
11	11	71	131	191	251	311	371	431	491	551	611	671	731	791	11
12	12	72	132	192	252	312	372	432	492	552	612	672	732	792	12
13	13	73	133	193	253	313	373	433	493	553	613	673	733	793	13
14	14	74	134	194	254	314	374	434	494	554	614	674	734	794	14
15	15	75	135	195	255	315	375	435	495	555	615	675	735	795	15
16	16	76	136	196	256	316	376	436	496	556	616	676	736	796	16
17	17	77	137	197	257	317	377	437	497	557	617	677	737	797	17
18	18	78	138	198	258	318	378	438	498	558	618	678	738	798	18
19	19	79	139	199	259	319	379	439	499	559	619	679	739	799	19
20	20	80	140	200	260	320	380	440	500	560	620	680	740	800	20
21	21	81	141	201	261	321	381	441	501	561	621	681	741	801	21
22	22	82	142	202	262	322	382	442	502	562	622	682	742	802	22
23	23	83	143	203	263	323	383	443	503	563	623	683	743	803	23
24	24	84	144	204	264	324	384	444	504	564	624	684	744	804	24
25	25	85	145	205	265	325	385	445	505	565	625	685	745	805	25
26	26	86	146	206	266	326	386	446	506	566	626	686	746	806	26
27	27	87	147	207	267	327	387	447	507	567	627	687	747	807	27
28	28	88	148	208	268	328	388	448	508	568	628	688	748	808	28
29	29	89	149	209	269	329	389	449	509	569	629	689	749	809	29
30	30	90	150	210	270	330	390	450	510	570	630	690	750	810	30
31	31	91	151	211	271	331	391	451	511	571	631	691	751	811	31
32	32	92	152	212	272	332	392	452	512	572	632	692	752	812	32
33	33	93	153	213	273	333	393	453	513	573	633	693	753	813	33
34	34	94	154	214	274	334	394	454	514	574	634	694	754	814	34
35	35	95	155	215	275	335	395	455	515	575	635	695	755	815	35
36	36	96	156	216	276	336	396	456	516	576	636	696	756	816	36
37	37	97	157	217	277	337	397	457	517	577	637	697	757	817	37
38	38	98	158	218	278	338	398	458	518	578	638	698	758	818	38
39	39	99	159	219	279	339	399	459	519	579	639	699	759	819	39
40	40	100	160	220	280	340	400	460	520	580	640	700	760	820	40
41	41	01	61	121	181	241	301	361	421	481	541	601	661	721	41
42	42	02	62	122	182	242	302	362	422	482	542	602	662	722	42
43	43	03	63	123	183	243	303	363	423	483	543	603	663	723	43
44	44	04	64	124	184	244	304	364	424	484	544	604	664	724	44
45	45	05	65	125	185	245	305	365	425	485	545	605	665	725	45
46	46	06	66	126	186	246	306	366	426	486	546	606	666	726	46
47	47	07	67	127	187	247	307	367	427	487	547	607	667	727	47
48	48	08	68	128	188	248	308	368	428	488	548	608	668	728	48
49	49	09	69	129	189	249	309	369	429	489	549	609	669	729	49
50	50	100	170	230	290	350	410	470	530	590	650	710	770	830	50
51	51	01	71	131	191	251	311	371	431	491	551	611	671	731	51
52	52	02	72	132	192	252	312	372	432	492	552	612	672	732	52
53	53	03	73	133	193	253	313	373	433	493	553	613	673	733	53
54	54	04	74	134	194	254	314	374	434	494	554	614	674	734	54
55	55	05	75	135	195	255	315	375	435	495	555	615	675	735	55
56	56	06	76	136	196	256	316	376	436	496	556	616	676	736	56
57	57	07	77	137	197	257	317	377	437	497	557	617	677	737	57
58	58	08	78	138	198	258	318	378	438	498	558	618	678	738	58
59	59	09	79	139	199	259	319	379	439	499	559	619	679	739	59

M	14d.	15d.	16d.	17d.	18d.	19d.	20d.	21d.	22d.	23d.	24d.	25d.	26d.	27d.	M
0	848	910	973	1035	1096	1157	1218	1279	1340	1401	1462	1523	1584	1645	0
1	49	11	74	135	196	257	318	379	440	501	562	623	684	745	1
2	50	12	75	137	198	259	320	381	442	503	564	625	686	747	2
3	51	13	76	138	199	260	321	382	443	504	565	626	687	748	3
4	52	14	77	139	200	261	322	383	444	505	566	627	688	749	4
5	53	15	78	140	201	262	323	384	445	506	567	628	689	750	5
6	54	16	79	141	202	263	324	385	446	507	568	629	690	751	6
7	55	17	80	142	203	264	325	386	447	508	569	630	691	752	7
8	56	18	81	143	204	265	326	387	448	509	570	631	692	753	8
9	57	19	82	144	205	266	327	388	449	510	571	632	693	754	9
10	58	20	83	145	206	267	328	389	450	511	572	633	694	755	10
11	59	21	84	146	207	268	329	390	451	512	573	634	695	756	11
12	60	22	85	147	208	269	330	391	452	513	574	635	696	757	12
13	61	23	86	148	209	270	331	392	453	514	575	636	697	758	13
14	62	24	87	149	210	271	332	393	454	515	576	637	698	759	14
15	63	25	88	150	211	272	333	394	455	516	577	638	699	760	15
16	64	26	89	151	212	273	334	395	456	517	578	639	700	761	16
17	65	27	90	152	213	274	335	396	457	518	579	640	701	762	17
18	66	28	91	153	214	275	336	397	458	519	580	641	702	763	18
19	67	29	92	154	215	276	337	398	459	520	581	642	703	764	19
20	68	30	93	155	216	277	338	399	460	521	582	643	704	765	20
21	69	31	94	156	217	278	339	400	461	522	583	644	705	766	21
22	70	32	95	157	218	279	340	401	462	523	584	645	706	767	22
23	71	33	96	158	219	280	341	402	463	524	585	646	707	768	23
24	72	34	97	159	220	281	342	403	464	525	586	647	708	769	24
25	73	35	98	160	221	282	343	404	465	526	587	648	709	770	25
26	74	36	99	161	222	283	344	405	466	527	588	649	710	771	26
27	75	37	100	162	223	284	345	406	467	528	589	650	711	772	27
28	76	38	01	163	224	285	346	407	468	529	590	651	712	773	28
29	77	39	02	164	225	286	347	408	469	530	591	652	713	774	29
30	78	40	03	165	226	287	348	409	470	531	592	653	714	775	30
31	79	41	04	166	227	288	349	410	471	532	593	654	715	776	31
32	80	42	05	167	228	289	350	411	472	533	594	655	716	777	32
33	81	43	06	168	229	290	351	412	473	534	595	656	717	778	33
34	82	44	07	169	230	291	352	413	474	535	596	657	718	779	34
35	83	45	08	170	231	292	353	414	475	536	597	658	719	780	35
36	84	46	09	171	232	293	354	415	476	537	598	659	720	781	36
37	85	47	10	172	233	294	355	416	477	538	599	660	721	782	37
38	86	48	11	173	234	295	356	417	478	539	600	661	722	783	38
39	87	49	12	174	235	296	357	418	479	540	601	662	723	784	39
40	88	50	13	175	236	297	358	419	480	541	602	663	724	785	40
41	89	51	14	176	237	298	359	420	481	542	603	664	725	786	41
42	90	52	15	177	238	299	360	421	482	543	604	665	726	787	42
43	91	53	16	178	239	300	361	422	483	544	605	666	727	788	43
44	92	54	17	179	240	301	362	423	484	545	606	667	728	789	44
45	93	55	18	180	241	302	363	424	485	546	607	668	729	790	45
46	94	56	19	181	242	303	364	425	486	547	608	669	730	791	46
47	95	57	20	182	243	304	365	426	487	548	609	670	731	792	47
48	96	58	21	183	244	305	366	427	488	549	610	671	732	793	48
49	97	59	22	184	245	306	367	428	489	550	611	672	733	794	49
50	98	60	23	185	246	307	368	429	490	551	612	673	734	795	50
51	99	61	24	186	247	308	369	430	491	552	613	674	735	796	51
52	00	62	25	187	248	309	370	431	492	553	614	675	736	797	52
53	01	63	26	188	249	310	371	432	493	554	615	676	737	798	53
54	02	64	27	189	250	311	372	433	494	555	616	677	738	799	54
55	03	65	28	190	251	312	373	434	495	556	617	678	739	800	55
56	04	66	29	191	252	313	374	435	496	557	618	679	740	801	56
57	05	67	30	192	253	314	375	436	497	558	619	680	741	802	57
58	06	68	31	193	254	315	376	437	498	559	620	681	742	803	58
59	07	69	32	194	255	316	377	438	499	560	621	682	743	804	59

M	18d.	19d.	20d.	21d.	22d.	23d.	24d.	25d.	26d.	27d.	28d.	29d.	30d.	31d.	M
0	1751	181	1888	1956	2048	2099	2171	2241	2318	2393	2468	2545	2623	2702	0
1	52	20	89	59	29	1101	73	43	19	94	69	46	24	03	1
2	53	22	91	60	31	02	74	47	20	95	71	47	25	04	2
3	54	23	92	61	32	03	75	48	22	96	72	49	27	06	3
4	56	24	93	63	33	04	76	49	23	98	73	50	28	07	4
5	57	25	94	64	34	05	77	50	24	99	75	51	29	08	5
6	58	26	95	65	35	07	79	52	25	100	76	53	30	10	6
7	59	27	96	66	37	08	80	53	27	01	77	54	32	11	7
8	60	28	98	67	38	09	81	54	28	03	78	55	33	12	8
9	61	29	00	68	39	10	82	55	29	04	80	56	34	14	9
10	1762	182	1900	1970	2040	2111	2183	2256	2330	2405	2481	2558	2636	2715	10
11	64	32	01	71	41	13	85	58	32	06	82	59	37	16	11
12	65	33	02	72	42	14	86	59	33	08	83	60	38	17	12
13	66	34	03	73	44	15	87	60	34	09	85	62	40	19	13
14	67	35	04	74	45	16	88	61	35	10	86	63	41	20	14
15	68	37	06	75	46	17	90	63	36	11	87	64	42	21	15
16	69	38	07	77	47	19	91	64	38	13	89	66	44	23	16
17	70	39	08	78	48	20	92	65	39	14	90	67	45	24	17
18	71	40	09	79	50	21	93	66	40	15	91	68	46	25	18
19	72	41	10	80	51	22	94	67	41	16	92	69	47	27	19
20	1774	183	1911	1981	2052	2123	2196	2269	2343	2418	2494	2571	2649	2728	20
21	75	43	13	82	53	25	97	70	44	19	95	71	50	29	21
22	76	45	14	84	54	26	98	71	45	20	96	73	51	31	22
23	77	46	15	85	55	27	99	72	46	21	97	75	53	32	23
24	78	47	16	86	57	28	100	74	48	23	99	76	54	33	24
25	79	48	17	87	58	29	02	75	49	24	100	77	55	35	25
26	81	49	18	88	59	31	03	76	50	25	01	78	57	36	26
27	82	50	20	89	60	32	04	77	51	26	03	80	58	37	27
28	83	51	21	91	61	33	05	78	53	28	04	81	59	39	28
29	84	52	22	92	62	34	06	80	54	29	05	82	61	40	29
30	1785	184	1922	1993	2064	2135	2208	2281	2355	2430	2506	2583	2662	2741	30
31	86	55	24	94	65	37	09	82	56	32	08	85	63	43	31
32	87	56	25	95	66	38	10	83	58	33	09	86	65	44	32

M	42d.	43d.	44d.	45d.	46d.	47d.	48d.	49d.	50d.	51d.	52d.	53d.	54d.	55d.	M
0	2781	2863	2946	3030	3116	3203	3292	3382	3475	3569	3665	3763	3865	3968	0
1	83	64	47	31	17	04	93	84	76	71	67	67	66	70	1
2	84	66	49	33	18	06	95	85	78	72	69	69	68	72	2
3	86	67	50	34	20	07	96	87	79	74	70	70	70	73	3
4	87	69	51	36	21	09	98	88	81	75	72	72	72	75	4
5	88	70	53	37	23	10	99	90	82	77	73	73	73	77	5
6	90	71	54	38	24	12	3301	91	84	78	75	75	75	79	6
7	91	73	56	40	26	13	02	93	85	80	77	77	77	80	7
8	92	74	57	41	27	14	04	94	87	82	78	78	78	82	8
9	04	75	58	43	29	16	05	96	89	83	80	79	80	84	9
10	2792	2877	2960	3044	3130	3217	3307	3397	3490	3585	3682	3780	3882	3986	10
11	97	78	61	46	31	19	08	99	92	86	83	82	83	87	11
12	98	80	63	47	33	20	10	3400	93	88	85	84	85	89	12
13	99	81	64	48	34	22	11	02	95	90	87	85	87	91	13
14	2801	82	65	50	36	23	13	03	96	91	88	87	89	93	14
15	02	84	67	51	37	25	14	05	98	93	90	89	90	94	15
16	03	85	68	53	39	26	16	07	99	94	91	90	92	96	16
17	05	86	69	54	40	28	17	08	3501	96	93	92	94	98	17
18	06	88	71	55	42	29	19	10	03	98	95	94	95	4000	18
19	07	89	72	57	43	31	20	11	04	00	96	96	97	01	19
20	2809	2890	2974	3058	3144	3232	3322	3413	3506	3600	3698	3797	3899	4003	20
21	10	92	75	60	46	34	23	14	07	02	3700	99	3901	05	21
22	11	93	76	61	47	35	25	16	09	04	01	3801	02	07	22
23	13	95	78	63	49	37	26	17	10	06	03	02	04	08	23
24	14	96	79	64	50	38	28	19	12	07	05	04	06	10	24
25	15	97	81	65	52	40	29	20	14	09	06	06	07	12	25
26	17	99	82	67	53	41	31	22	15	10	08	07	09	14	26
27	18	2900	83	68	55	42	32	23	17	12	09	09	11	15	27
28	20	02	85	70	56	44	34	25	18	14	11	11	13	17	28
29	21	03	86	71	57	45	35	27	20	15	13	13	14	19	29
30	2822	2904	2988	3073	3159	3247	3337	3428	3521	3617	3714	3814	3916	4021	30
31	24	06	89	74	60	48	38	30	23	18	16	16	18	22	31
32	25	07	90	75	62	50	40	31	25	20	18	17	20	24	32
33	26	08	92	77	63	51	41	33	26	21	19	19	22	26	33
34	28	10	93	78	65	53	43	34	28	23	21	21	23	28	34
35	29	11	95	80	66	54	44	36	29	25	23	23	25	30	35
36	30	13	96	81	68	56	46	37	31	26	24	24	26	32	36
37	32	14	98	83	69	57	47	39	32	28	26	26	28	33	37
38	33	15	99	84	71	59	49	40	34	30	28	27	30	35	38
39	34	17	3000	85	72	60	50	42	36	31	29	29	32	37	39
40	2836	2918	3002	3087	3173	3261	3351	3443	3537	3633	3731	3831	3933	4038	40
41	37	19	03	88	75	63	53	45	39	35	32	33	35	40	41
42	39	21	05	90	76	65	55	47	40	36	34	34	37	42	42
43	40	22	06	91	78	66	56	48	42	38	36	36	39	44	43
44	41	24	07	93	79	68	58	49	43	39	37	38	40	46	44
45	43	25	09	94	81	69	59	51	45	41	39	39	42	47	45
46	44	26	10	95	82	71	61	53	47	43	41	41	44	49	46
47	45	28	12	97	84	72	62	54	48	44	42	43	45	51	47
48	47	29	13	98	85	74	64	56	50	46	44	44	47	53	48
49	48	31	14	3100	87	75	65	57	51	48	46	46	49	54	49
50	2845	2927	3010	3095	3181	3267	3357	3449	3543	3639	3737	3838	3941	4046	50
51	51	33	17	03	90	78	68	61	55	51	49	49	52	58	51
52	52	35	19	04	91	80	70	62	56	52	51	51	54	60	52
53	54	36	20	05	92	81	71	64	58	54	52	53	56	62	53
54	55	37	22	07	94	83	73	65	59	56	54	55	58	63	54
55	56	39	23	08	95	84	74	67	61	57	56	56	59	65	55
56	58	40	24	10	97	86	76	68	62	59	57	58	61	67	56
57	59	42	26	11	98	87	78	70	64	61	59	60	63	69	57
58	60	43	27	13	3200	89	79	71	66	62	61	61	65	70	58
59	62	44	28	14	01	90	81	73	67	64	63	63	66	72	59

M	0 d.	1 d.	2 d.	3 d.	4 d.	5 d.	6 d.	7 d.	8 d.	9 d.	10 d.	11 d.	12 d.	13 d.	M
0	0	60	110	160	210	260	310	361	411	461	511	561	611	661	711
1	1	61	111	161	211	261	311	362	412	462	512	562	612	662	712
2	2	62	112	162	212	262	312	363	413	463	513	563	613	663	713
3	3	63	113	163	213	263	313	364	414	464	514	564	614	664	714
4	4	64	114	164	214	264	314	365	415	465	515	565	615	665	715
5	5	65	115	165	215	265	315	366	416	466	516	566	616	666	716
6	6	66	116	166	216	266	316	367	417	467	517	567	617	667	717
7	7	67	117	167	217	267	317	368	418	468	518	568	618	668	718
8	8	68	118	168	218	268	318	369	419	469	519	569	619	669	719
9	9	69	119	169	219	269	319	370	420	470	520	570	620	670	720
10	10	70	120	170	220	270	320	371	421	471	521	571	621	671	721
11	11	71	121	171	221	271	321	372	422	472	522	572	622	672	722
12	12	72	122	172	222	272	322	373	423	473	523	573	623	673	723
13	13	73	123	173	223	273	323	374	424	474	524	574	624	674	724
14	14	74	124	174	224	274	324	375	425	475	525	575	625	675	725
15	15	75	125	175	225	275	325	376	426	476	526	576	626	676	726
16	16	76	126	176	226	276	326	377	427	477	527	577	627	677	727
17	17	77	127	177	227	277	327	378	428	478	528	578	628	678	728
18	18	78	128	178	228	278	328	379	429	479	529	579	629	679	729
19	19	79	129	179	229	279	329	380	430	480	530	580	630	680	730
20	20	80	130	180	230	280	330	381	431	481	531	581	631	681	731
21	21	81	131	181	231	281	331	382	432	482	532	582	632	682	732
22	22	82	132	182	232	282	332	383	433	483	533	583	633	683	733
23	23	83	133	183	233	283	333	384	434	484	534	584	634	684	734
24	24	84	134	184	234	284	334	385	435	485	535	585	635	685	735
25	25	85	135	185	235	285	335	386	436	486	536	586	636	686	736
26	26	86	136	186	236	286	336	387	437	487	537	587	637	687	737
27	27	87	137	187	237	287	337	388	438	488	538	588	638	688	738
28	28	88	138	188	238	288	338	389	439	489	539	589	639	689	739
29	29	89	139	189	239	289	339	390	440	490	540	590	640	690	740
30	30	90	140	190	240	290	340	391	441	491	541	591	641	691	741
31	31	91	141	191	241	291	341	392	442	492	542	592	642	692	742
32	32	92	142	192	242	292	342	393	443	493	543	593	643	693	743
33	33	93	143	193	243	293	343	394	444	494	544	594	644	694	744
34	34	94	144	194	244	294	344	395	445	495	545	595	645	695	745
35	35	95	145	195	245	295	345	396	446	496	546	596	646	696	746
36	36	96	146	196	246	296	346	397	447	497	547	597	647	697	747
37	37	97	147	197	247	297	347	398	448	498	548	598	648	698	748
38	38	98	148	198	248	298	348	399	449	499	549	599	649	699	749
39	39	99	149	199	249	299	349	400	450	500	550	600	650	700	750
40	40	100	150	200	250	300	350	401	451	501	551	601	651	701	751
41	41	01	51	101	151	201	251	302	352	402	452	502	552	602	652
42	42	02	52	102	152	202	252	303	353	403	453	503	553	603	653
43	43	03	53	103	153	203	253	304	354	404	454	504	554	604	654
44	44	04	54	104	154	204	254	305	355	405	455	505	555	605	655
45	45	05	55	105	155	205	255	306	356	406	456	506	556	606	656
46	46	06	56	106	156	206	256	307	357	407	457	507	557	607	657
47	47	07	57	107	157	207	257	308	358	408	458	508	558	608	658
48	48	08	58	108	158	208	258	309	359	409	459	509	559	609	659
49	49	09	59	109	159	209	259	310	360	410	460	510	560	610	660
50	50	100	160	210	260	310	360	411	461	511	561	611	661	711	761
51	51	11	61	111	161	211	261	312	362	412	462	512	562	612	662
52	52	12	62	112	162	212	262	313	363	413	463	513	563	613	663
53	53	13	63	113	163	213	263	314	364	414	464	514	564	614	664
54	54	14	64	114	164	214	264	315	365	415	465	515	565	615	665
55	55	15	65	115	165	215	265	316	366	416	466	516	566	616	666
56	56	16	66	116	166	216	266	317	367	417	467	517	567	617	667
57	57	17	67	117	167	217	267	318	368	418	468	518	568	618	668
58	58	18	68	118	168	218	268	319	369	419	469	519	569	619	669
59	59	19	69	119	169	219	269	320	370	420	470	520	570	620	670

M	14d.	15d.	16d.	17d.	18d.	19d.	20d.	21d.	22d.	23d.	24d.	25d.	26d.	27d.	M
0	84	910	973	1035	1098	1161	1225	1289	1354	1419	1484	1550	1616	1683	0
1	49	11	74	35	99	63	25	90	55	20	85	51	17	85	1
2	50	12	75	37	100	63	27	91	56	21	86	52	19	86	2
3	51	13	76	38	01	65	28	92	57	22	87	53	20	87	3
4	52	14	77	39	02	66	29	93	58	23	88	54	21	88	4
5	54	16	78	40	03	67	30	94	59	24	89	55	22	89	5
6	55	17	79	41	04	68	31	95	60	25	90	56	23	90	6
7	56	18	80	42	05	69	32	96	61	26	91	57	24	91	7
8	57	19	81	43	06	70	33	97	62	27	92	58	25	92	8
9	58	20	82	44	07	71	34	98	63	28	93	59	26	93	9
10	59	21	83	45	08	72	35	99	64	29	94	60	27	94	10
11	60	22	84	47	10	73	37	01	65	30	96	61	29	96	11
12	61	23	85	48	11	74	38	02	66	31	97	62	31	97	12
13	62	24	86	49	12	75	39	03	67	32	98	63	32	98	13
14	63	25	87	50	13	76	40	04	68	33	99	64	33	99	14
15	64	26	88	51	14	77	41	05	69	34	100	65	34	100	15
16	65	27	89	52	15	78	42	06	70	35	01	66	35	01	16
17	66	28	90	53	16	79	43	07	71	36	02	67	36	02	17
18	67	29	91	54	17	80	44	08	72	37	03	68	37	03	18
19	68	30	92	55	18	81	45	09	73	38	04	69	38	04	19
20	69	31	93	56	19	82	46	10	74	39	05	70	39	05	20
21	70	32	94	57	20	83	47	11	75	40	06	71	40	06	21
22	71	33	95	58	21	84	48	12	76	41	07	72	41	07	22
23	72	34	96	59	22	85	49	13	77	42	08	73	42	08	23
24	73	35	97	60	23	86	50	14	78	43	09	74	43	09	24
25	74	36	98	61	24	87	51	15	79	44	10	75	44	10	25
26	75	37	99	62	25	88	52	16	80	45	11	76	45	11	26
27	76	38	100	63	26	89	53	17	81	46	12	77	46	12	27
28	77	39	01	64	27	90	54	18	82	47	13	78	47	13	28
29	78	40	02	65	28	91	55	19	83	48	14	79	48	14	29
30	79	41	03	66	29	92	56	20	84	49	15	80	49	15	30
31	80	42	04	67	30	93	57	21	85	50	16	81	50	16	31
32	81	43	05	68	31	94	58	22	86	51	17	82	51	17	32
33	82	44	06	69	32	95	59	23	87	52	18	83	52	18	33
34	83	45	07	70	33	96	60	24	88	53	19	84	53	19	34
35	84	46	08	71	34	97	61	25	89	54	20	85	54	20	35
36	85	47	09	72	35	98	62	26	90	55	21	86	55	21	36
37	86	48	10	73	36	99	63	27	91	56	22	87	56	22	37
38	87	49	11	74	37	100	64	28	92	57	23	88	57	23	38
39	88	50	12	75	38	01	65	29	93	58	24	89	58	24	39
40	89	51	13	76	39	02	66	30	94	59	25	90	59	25	40
41	90	52	14	77	40	03	67	31	95	60	26	91	60	26	41
42	91	53	15	78	41	04	68	32	96	61	27	92	61	27	42
43	92	54	16	79	42	05	69	33	97	62	28	93	62	28	43
44	93	55	17	80	43	06	70	34	98	63	29	94	63	29	44
45	94	56	18	81	44	07	71	35	99	64	30	95	64	30	45
46	95	57	19	82	45	08	72	36	100	65	31	96	65	31	46
47	96	58	20	83	46	09	73	37	01	66	32	97	66	32	47
48	97	59	21	84	47	10	74	38	02	67	33	98	67	33	48
49	98	60	22	85	48	11	75	39	03	68	34	99	68	34	49
50	99	61	23	86	49	12	76	40	04	69	35	100	69	35	50
51	00	62	24	87	50	13	77	41	05	70	36	01	70	36	51
52	01	63	25	88	51	14	78	42	06	71	37	02	71	37	52
53	02	64	26	89	52	15	79	43	07	72	38	03	72	38	53
54	03	65	27	90	53	16	80	44	08	73	39	04	73	39	54
55	04	66	28	91	54	17	81	45	09	74	40	05	74	40	55
56	05	67	29	92	55	18	82	46	10	75	41	06	75	41	56
57	06	68	30	93	56	19	83	47	11	76	42	07	76	42	57
58	07	69	31	94	57	20	84	48	12	77	43	08	77	43	58
59	08	70	32	95	58	21	85	49	13	78	44	09	78	44	59
60	09	71	33	96	59	22	86	50	14	79	45	10	79	45	60
61	10	72	34	97	60	23	87	51	15	80	46	11	80	46	61
62	11	73	35	98	61	24	88	52	16	81	47	12	81	47	62
63	12	74	36	99	62	25	89	53	17	82	48	13	82	48	63
64	13	75	37	100	63	26	90	54	18	83	49	14	83	49	64
65	14	76	38	01	64	27	91	55	19	84	50	15	84	50	65
66	15	77	39	02	65	28	92	56	20	85	51	16	85	51	66
67	16	78	40	03	66	29	93	57	21	86	52	17	86	52	67
68	17	79	41	04	67	30	94	58	22	87	53	18	87	53	68
69	18	80	42	05	68	31	95	59	23	88	54	19	88	54	69
70	19	81	43	06	69	32	96	60	24	89	55	20	89	55	70
71	20	82	44	07	70	33	97	61	25	90	56	21	90	56	71
72	21	83	45	08	71	34	98	62	26	91	57	22	91	57	72
73	22	84	46	09	72	35	99	63	27	92	58	23	92	58	73
74	23	85	47	10	73	36	100	64	28	93	59	24	93	59	74
75	24	86	48	11	74	37	01	65	29	94	60	25	94	60	75
76	25	87	49	12	75	38	02	66	30	95	61	26	95	61	76
77	26	88	50	13	76	39	03	67	31	96	62	27	96	62	77
78	27	89	51	14	77	40	04	68	32	97	63	28	97	63	78
79	28	90	52	15	78	41	05	69	33	98	64	29	98	64	79
80	29	91	53	16	79	42	06	70	34	99	65	30	99	65	80
81	30	92	54	17	80	43	07	71	35	100	66	31	100	66	81
82	31	93	55	18	81	44	08	72	36	01	67	32	01	67	82
83	32	94	56	19	82	45	09	73	37	02	68	33	02	68	83
84	33	95	57	20	83	46	10	74	38	03	69	34	03	69	84
85	34	96	58	21	84	47	11	75	39	04	70	35	04	70	85
86	35	97	59	22	85	48	12	76	40	05	71	36	05	71	86
87	36	98	60	23	86	49	13	77	41	06	72	37	06	72	87
88	37	99	61	24	87	50	14	78	42	07	73	38	07	73	88
89	38	100	62	25	88	51	15	79	43	08	74	39	08	74	89
90	39	01	63	26	89	52	16	80	44	09	75	40	09	75	90
91	40	02	64	27	90	53	17	81	45	10	76	41	10	76	91
92	41	03	65	28	91	54	18	82	46	11	77	42	11	77	92
93	42	04	66	29	92	55	19	83	47	12	78	43	12	78	93
94	43	05	67	30	93	56	20	84	48	13	79	44	13	79	94
95	44	06	68	31	94	57	21	85	49	14	80	45	14	80	95
96	45	07	69	32	95	58	22	86	50	15	81	46	15	81	96
97	46	08	70	33	96	59	23	87	51	16	82	47	16	82	97
98	47	09	71	34	97	60	24	88	52	17	83	48	17	83	98
99	48	10	72	35	98	61	25	89	53	18	84	49	18	84	99
100	49	11	73	36	99	62	26	90	54	19	85	50	19	85	100

M	18d.	19d.	20d.	21d.	22d.	23d.	24d.	25d.	26d.	27d.	28d.	29d.	30d.	31d.	M
0	1751	181	1888	1956	2028	2099	2171	2247	2318	2393	2468	2545	2623	2702	0
1	52	20	89	59	29	101	73	45	19	94	69	45	24	03	1
2	53	22	91	60	31	02	74	47	20	95	71	47	25	04	2
3	54	23	92	61	32	03	75	48	22	96	72	49	27	06	3
4	56	24	93	63	33	04	76	49	23	98	73	50	28	07	4
5	57	25	94	64	34	05	77	50	24	99	75	51	29	08	5
6	58	26	95	65	35	07	79	52	25	100	76	53	30	10	6
7	59	27	96	66	37	08	80	53	27	01	77	54	32	11	7
8	60	28	98	67	38	09	81	54	28	03	78	55	33	12	8
9	61	29	00	68	39	10	82	55	29	04	80	56	34	14	9
10	1762	183	1900	1970	2040	2111	2183	2256	2330	2405	2481	2558	2636	2715	10
11	64	32	01	71	41	13	85	58	32	06	82	59	37	16	11
12	65	33	02	72	42	14	86	59	33	08	83	60	38	17	12
13	66	34	03	73	43	15	87	60	34	09	85	62	40	19	13
14	67	35	04	74	44	16	88	61	35	10	86	63	41	20	14
15	68	37	06	75	46	17	90	63	36	11	87	64	42	21	15
16	69	38	07	77	47	19	91	64	38	13	89	66	44	23	16
17	70	39	08	78	48	20	92	65	39	14	90	67	45	24	17
18	71	40	09	79	50	21	93	66	40	15	91	68	46	25	18
19	72	41	10	80	51	22	01	67	41	16	92	69	48	27	19
20	1774	184	1911	1981	2051	2123	2196	2269	2343	2418	2494	2571	2649	2728	20
21	75	43	13	82	53	25	97	70	44	19	95	72	50	29	21
22	76	44	14	84	54	26	98	71	45	20	96	73	51	31	22
23	77	46	15	85	55	27	99	72	46	21	97	75	53	32	23
24	78	47	16	86	57	28	100	74	48	23	99	76	54	33	24
25	79	48	17	87	58	29	02	75	49	24	100	77	55	35	25
26	81	49	18	88	59	31	03	76	50	25	01	78	57	36	26
27	82	50	20	89	60	32	04	77	51	26	03	80	58	37	27
28	83	51	21	91	61	33	05	78	53	28	04	81	59	39	28
29	84	52	22	92	63	34	06	80	54	29	05	82	61	40	29
30	1785	185	1923	1993	2064	2135	2208	2281	2355	2430	2506	2584	2662	2741	30
31	86	55	24	94	65	37	09	82	56	32	08	85	63	43	31
32	87	56	25	95	66	38	10	83	58	33	09	86	65	44	32
33	89	57	26	97	67	39	11	85	59	34	10	88	66	45	33
34	90	58	28	98	69	40	13	86	60	35	12	89	67	47	34
35	91	59	29	99	70	41	14	87	61	37	13	90	69	48	35
36	92	61	30	100	71	43	15	88	63	38	14	91	70	49	36
37	93	62	31	01	72	44	16	90	64	39	15	93	71	51	37
38	94	63	32	02	73	45	17	91	65	40	17	94	73	52	38
39	95	64	33	03	74	46	19	92	66	42	18	95	74	54	39
40	1797	186	1935	2005	2076	2147	2220	2293	2368	2443	2519	2597	2675	2755	40
41	98	66	36	06	77	49	21	94	69	44	20	98	76	56	41
42	99	68	37	07	78	50	22	96	70	45	22	99	78	58	42
43	1800	69	38	08	79	51	23	97	71	47	23	100	79	59	43
44	01	70	39	09	80	52	25	98	73	48	24	01	80	60	44
45	02	71	40	11	82	53	26	99	74	49	26	03	82	61	45
46	03	72	42	12	83	55	27	100	75	50	27	04	83	63	46
47	04	73	43	13	84	56	28	01	76	52	28	06	84	64	47
48	06	74	44	14	85	57	30	03	78	53	29	07	86	66	48
49	07	76	45	15	86	58	31	04	79	54	31	08	87	67	49
50	1808	187	1946	2017	2088	2159	2232	2306	2380	2456	2532	2610	2688	2768	50
51	09	78	47	18	89	61	33	07	81	57	33	11	90	70	51
52	10	79	49	19	90	62	34	08	83	58	35	12	91	71	52
53	11	80	50	20	91	63	36	09	84	59	36	14	92	72	53
54	12	81	51	21	92	64	37	11	85	61	37	15	94	74	54
55	14	83	52	22	93	65	38	12	86	62	38	16	95	75	55
56	15	84	53	24	95	67	39	13	88	63	40	17	96	76	56
57	16	85	54	25	96	68	41	14	89	64	41	19	98	78	57
58	17	86	56	26	97	69	42	15	90	66	42	20	99	79	58
59	18	87	57	27	98	70	43	17	91	67	44	21	100	80	59

M.	41d.	42d.	44d.	43d.	46d.	47d.	48d.	45d.	49d.	50d.	51d.	52d.	53d.	54d.	55d.	M.
0	2781	2863	2946	3030	3116	3203	3292	3382	3473	3569	3663	3763	3863	3968	0	
1	83	64	47	31	17	04	93	84	76	71	67	67	66	70	1	
2	81	66	49	33	18	06	95	85	78	72	69	69	68	72	2	
3	86	67	50	34	20	07	96	87	79	74	70	70	71	73	3	
4	87	69	51	36	21	09	98	88	81	75	71	72	72	75	4	
5	88	70	53	37	23	10	99	90	82	77	73	73	73	77	5	
6	90	71	54	38	24	11	301	91	84	78	75	75	75	79	6	
7	91	73	56	40	26	13	02	93	85	80	77	77	77	80	7	
8	92	74	57	41	27	14	04	94	87	82	78	78	78	82	8	
9	04	75	58	42	29	16	05	96	89	83	80	79	80	84	9	
10	2795	2877	2960	3044	3130	3217	3307	3397	3490	3585	3682	3780	3882	3986	10	
11	87	78	61	46	31	19	08	99	92	86	83	82	83	87	11	
12	98	80	63	47	33	20	10	3400	93	88	85	84	85	89	12	
13	99	81	64	48	34	22	11	02	95	90	87	85	87	91	13	
14	2801	82	65	50	36	23	13	03	96	91	88	87	89	93	14	
15	02	84	67	51	37	25	14	05	98	93	90	89	91	94	15	
16	03	85	68	53	39	26	16	07	99	94	91	90	92	96	16	
17	05	86	69	54	40	28	17	08	3501	96	93	92	94	98	17	
18	06	88	71	55	42	29	19	10	03	98	95	94	95	4000	18	
19	07	89	72	57	43	31	20	11	04	00	96	96	97	01	19	
20	2809	2890	2974	3058	3144	3232	3322	3413	3506	3600	3698	3797	3899	4003	20	
21	10	91	75	60	46	34	23	14	07	02	3700	99	3901	05	21	
22	11	93	76	61	47	35	25	16	09	04	01	3801	02	07	22	
23	13	95	78	63	49	37	26	17	10	06	03	03	04	08	23	
24	14	96	79	64	50	38	28	19	12	07	05	04	06	10	24	
25	15	97	81	65	52	40	29	20	14	09	06	06	07	12	25	
26	17	99	82	67	53	41	31	22	15	10	08	07	09	14	26	
27	18	2900	83	68	55	42	32	23	17	12	09	09	11	15	27	
28	20	02	85	70	56	44	34	25	18	14	11	11	13	17	28	
29	21	03	86	71	57	45	35	27	20	15	13	12	14	19	29	
30	2812	2904	2988	3073	3159	3247	3337	3428	3521	3617	3714	3814	3916	4024	30	
31	24	06	89	74	60	48	38	31	23	18	16	16	18	22	31	
32	25	07	90	75	62	50	40	31	25	20	18	17	20	24	32	
33	26	08	92	77	63	51	41	33	26	21	19	19	22	26	33	
34	28	10	93	78	65	53	42	34	28	23	21	21	23	28	34	
35	29	11	95	80	66	54	44	36	29	25	23	23	25	30	35	
36	30	13	96	81	68	56	46	37	31	26	24	24	26	31	36	
37	32	14	98	83	69	57	47	39	32	28	26	26	28	33	37	
38	33	15	99	84	71	59	49	40	34	30	28	27	30	35	38	
39	34	17	3000	85	72	60	50	42	36	31	29	29	32	37	39	
40	2816	2918	3002	3087	3173	3261	3351	3443	3537	3633	3731	3831	3933	4038	40	
41	37	19	03	88	75	63	53	45	39	35	32	33	35	40	41	
42	39	21	05	90	76	65	55	47	40	36	34	34	37	42	42	
43	40	22	06	91	78	66	56	48	42	38	36	36	39	44	43	
44	41	24	07	93	79	68	58	49	43	39	37	38	40	46	44	
45	43	25	09	94	81	69	59	51	45	41	39	39	42	47	45	
46	44	26	10	95	82	71	61	53	47	43	41	41	44	49	46	
47	45	28	12	97	84	72	62	54	48	44	42	42	45	51	47	
48	47	29	13	98	85	74	64	56	50	46	44	44	47	53	48	
49	48	31	14	3100	87	75	65	57	51	48	46	46	49	54	49	
50	2819	2932	3016	3101	3188	3277	3367	3459	3553	3649	3747	3848	3951	4056	50	
51	51	33	17	93	96	78	68	61	55	51	49	49	52	58	51	
52	52	35	19	04	91	80	70	62	56	52	51	51	54	60	52	
53	54	36	20	05	92	81	71	64	58	54	52	53	56	62	53	
54	55	37	22	07	94	83	73	65	59	56	54	55	58	63	54	
55	56	39	23	08	95	84	74	67	61	57	56	56	59	65	55	
56	58	40	24	10	97	86	76	68	62	59	57	58	61	67	56	
57	59	42	26	11	98	87	78	70	64	61	59	60	63	69	57	
58	60	43	27	13	3200	89	79	71	66	62	61	61	65	70	58	
59	62	44	29	14	01	90	81	73	67	64	62	63	66	72	59	

January hath XXXI Days.

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Month	Week days.	Remarkable days, and southing of Stars at Midnight.	First Year.		Second Year.		Third Year.		Leap-Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
Month days.	1		☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			vs	South.	v	South.	v	South.	v	South.
1	A	Circumcisc.	22 13	21 39	21 58	21 41	21 44	21 43	21 29	21 46
2	B	Sun rise 8.	23 14	21 28	22 59	21 31	22 45	21 33	22 30	21 36
3	C		24 15	21 18	23 01	21 21	23 46	21 23	23 31	21 26
4	D		25 16	21 07	25 02	21 10	24 47	21 12	24 32	21 15
5	E		26 18	20 56	26 03	20 59	25 48	21 01	25 33	21 04
6	F	Epiphany.	27 19	20 44	27 04	20 47	26 49	20 50	26 34	20 53
7	G		28 20	20 32	28 05	20 35	27 50	20 38	27 35	20 41
8	A		29 21	20 19	29 06	20 22	28 51	20 25	28 36	20 29
9	B		☾. 22	20 06	☾. 07	20 10	29 52	20 13	29 37	20 16
10	C		01 23	19 53	01 08	19 56	☾. 53	20 00	☾. 38	20 03
11	D	Sol in Aqua.	02 24	19 38	02 09	19 43	01 54	19 46	01 39	19 50
12	E	Sun r. 7.45.	03 25	19 25	03 10	19 29	02 55	19 32	02 40	19 36
13	F		04 26	19 11	04 11	19 15	03 56	19 18	03 41	19 22
14	G		05 27	18 56	05 12	19 00	04 57	19 04	04 42	19 07
15	A		06 28	18 41	06 13	18 45	05 58	19 49	05 43	18 52
16	B		07 29	18 26	07 14	18 30	06 59	18 33	06 44	18 37
17	C		08 30	18 10	08 15	18 24	08 00	18 18	07 45	18 21
18	D		09 31	17 54	09 16	17 58	09 01	18 02	08 46	18 06
19	E		10 32	17 38	10 17	17 42	10 02	17 46	09 47	17 50
20	F		11 32	17 21	11 17	17 25	11 03	17 29	10 48	17 34
21	G	Sun r. 7.30.	12 33	17 04	12 18	17 08	12 03	17 13	11 49	17 17
22	A		13 34	16 47	13 19	16 51	13 04	16 55	12 50	17 00
23	B	Hydra's heart	14 35	16 29	14 20	16 34	14 05	16 38	13 50	16 42
24	C		15 35	16 12	15 21	16 16	15 06	16 20	14 51	16 25
25	D	Con.S.Paul.	16 36	15 53	16 21	15 58	16 07	16 02	15 52	16 07
26	E		17 37	15 35	17 22	15 39	17 07	15 44	16 53	15 48
27	F		18 38	15 16	18 23	15 21	18 08	15 25	17 53	15 30
28	G		19 38	14 57	19 23	15 02	19 09	15 07	18 54	15 11
29	A		20 39	14 38	20 24	14 43	20 09	14 48	19 55	14 52
30	B	K. Char. B.	21 40	14 19	21 24	14 23	21 10	14 28	20 55	14 33
31	C		22 40	13 59	22 25	14 04	22 11	14 09	21 56	14 13

February hath XXVIII Days.

Month	Week days.	Remarkable days, and southing of stars at midnight.	First Year.		Second Year.		Third Year.		Leap-Year.		
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.	
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.	
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
			☞	South	☞	South	☞	South	☞	South	
1	D	Purif. Mary Lions Heart.	23 41	13 39	23 26	13 44	23 11	13 49	22 57	13 54	
2	E		24 41	13 19	24 26	13 24	24 12	13 29	23 57	13 34	
3	F		25 42	12 59	25 27	13 04	25 12	13 09	24 58	13 14	
4	G		26 42	12 38	26 28	12 43	26 13	12 48	25 58	12 53	
5	A	Lions Neck. Sun r. 7 1. Sol in Pisces.	27 43	12 17	27 28	12 22	27 13	12 27	26 59	12 33	
6	B		28 43	11 56	28 28	12 01	28 14	12 06	27 59	12 12	
7	C		29 44	11 35	29 29	11 40	29 14	11 46	29 00	11 51	
8	D		☞. 44	11 14	☞ 29	11 19	☞. 15	11 24	☞. 00	11 30	
9	E		01 44	10 53	01 30	10 58	01 15	11 03	01 00	11 08	
10	F		02 45	10 31	02 30	10 36	02 15	10 41	02 01	10 47	
11	G		03 45	10 09	03 30	10 14	03 16	10 20	03 01	10 25	
12	A		04 45	09 47	04 31	09 52	04 16	09 58	04 01	10 03	
13	B		05 45	09 25	05 31	09 30	05 16	09 36	05 02	09 41	
14	C	Valentine.	06 46	09 03	06 31	09 08	06 16	09 14	06 02	09 19	
15	D	Sun r. 6. 45.	07 46	08 40	07 31	08 46	07 17	08 51	07 02	08 57	
16	E	Lower of	08 46	08 18	08 31	08 23	08 17	08 29	08 02	08 34	
17	F	two foremoſt									
18	G	in ☐ of the	09 46	07 55	09 32	08 01	09 17	08 06	09 02	08 12	
19	A	great Bear.	10 46	07 32	10 32	07 38	10 17	07 44	10 03	07 49	
20	B		11 46	07 10	11 32	07 15	11 17	07 21	11 03	07 26	
21	C		12 46	06 47	12 32	06 52	12 17	06 58	12 03	07 03	
22	D		13 46	06 24	13 32	06 29	13 17	06 35	13 03	06 40	
23	E	Sun r. 6. 30.	14 46	06 01	14 32	06 06	14 17	06 12	14 03	06 17	
24	F		15 46	05 37	15 32	05 43	15 17	05 49	15 03	05 54	
25	G	S. Matthias	16 46	05 14	16 32	05 20	16 17	05 25	16 03	05 31	
26	A		17 46	04 51	17 32	04 57	17 17	05 02	17 02	05 08	
27	B		18 46	04 27	18 31	04 33	18 17	04 39	18 02	04 44	
28	C		19 46	04 04	19 31	04 09	19 17	04 15	19 02	04 21	
29	D		20 45	03 40	20 31	03 46	20 16	03 52	20 02	03 57	
			When it is Leap-Year, February hath 29 days							21 02	03 34

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Month	Week days.	Remarkable days, and fou- ching of stars at midnight	First Year.		Second Year.		Third Year.		Leap-Year.									
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.								
Month days.	1		☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.								
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.								
			☉	South	☉	South	☉	South	☉	South								
1	D	<i>David.</i>	21	45	03	17	21	31	03	22	21	16	03	28	22	01	03	10
2	E	<i>Lion's Tail.</i>	22	45	02	53	22	30	02	59	22	16	03	04	23	01	02	47
3	F	<i>Lower of the</i>	23	45	02	29	23	30	02	35	23	16	02	41	24	01	02	32
4	G	<i>two latter, in</i>	24	44	02	05	24	30	02	11	24	15	02	17	25	00	01	59
5	A	<i>☐ of Great</i>	25	44	01	42	25	29	01	48	25	15	01	54	26	00	01	36
6	B	<i>Bear.</i>	26	43	01	18	26	29	01	24	26	14	01	30	27	00	01	12
7	C		27	43	00	54	27	28	01	00	27	14	01	06	27	59	00	48
8	D		28	42	00	31	28	28	00	37	28	13	00	43	28	59	00	25
9	E		29	42	00	07	29	27	00	13	29	13	00	19	29	58	00	01
10	F	<i>Sun r. 6. 4</i>	Y. 41	Nor. 16	Y. 27	Nor. 10	Y. 12	Nor. 5	Y. 57	Nor. 23								
11	G	<i>Upper of</i>	01	41	00	40	01	26	00	34	01	12	00	28	01	57	00	46
12	A	<i>two latter in</i>	02	40	01	04	02	25	00	58	02	11	00	52	02	56	01	10
13	B	<i>☐ of Great</i>	03	39	01	27	03	25	01	21	03	11	01	16	03	55	01	34
14	C	<i>Bear.</i>	04	39	01	51	04	24	01	45	04	10	01	39	04	55	01	57
15	D	<i>Sol in Aries.</i>	05	38	02	14	05	23	02	08	05	09	02	03	05	54	02	21
16	E		06	37	02	38	06	23	02	32	06	08	02	26	06	53	02	44
17	F		07	36	03	01	07	22	02	55	07	08	02	50	07	52	03	08
18	G	<i>Sun r. 5. 45.</i>	08	35	03	25	08	21	03	18	08	07	03	13	08	52	03	31
19	A		09	35	03	48	09	20	03	42	09	06	03	36	09	51	03	54
20	B		10	34	04	11	10	19	04	05	10	05	04	00	10	50	04	17
21	C	<i>Last but two</i>	11	33	04	34	11	18	04	29	11	04	04	23	11	49	04	41
22	D	<i>in gr. Bear's</i>	12	32	04	57	12	17	04	52	12	03	04	46	12	48	05	04
23	E	<i>Tail.</i>	13	31	05	20	13	16	05	15	13	02	05	09	13	47	05	27
24	F		14	30	05	43	14	15	05	38	14	01	05	32	14	46	05	46
25	G	<i>An. Mary.</i>	15	29	06	06	15	14	06	01	15	00	05	55	15	45	06	12
26	A	<i>Sun r. 5. 38.</i>	16	27	06	29	16	13	06	23	15	59	06	18	16	43	06	35
27	B		17	26	06	51	17	12	07	46	16	58	06	40	17	42	06	57
28	C		18	25	07	14	18	11	07	08	17	57	07	03	18	41	07	20
29	D	<i>Virg. Spike</i>	19	24	07	36	19	10	07	31	18	55	07	25	19	40	07	42
30	E	<i>Last but one</i>	20	23	07	58	20	08	07	53	19	54	07	48	20	39	08	04
31	F	<i>in gr. Bear's</i>	21	21	08	21	21	07	08	15	20	53	08	01	21	37	08	26
		<i>Tail.</i>																

		First Year.		Second Year.		Third Year.		Leap-Year.	
Remarkable days, and sou- thing of stars at midnight.		1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
		1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
		☉ pla.	☉ dec.	☉ pla	☉ dec	☉ pla.	☉ dec.	☉ pla.	☉ dec.
		D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
		r	North	r	North	r	North	r	North
1	G	Sun r. 5.15.	22 20 08 43	22 06 08 37	21 52 08 32	22 36 08 48			
2	A		23 19 09 05	23 04 08 59	22 50 08 54	23 35 09 10			
3	B		24 17 09 26	24 03 09 21	23 49 09 15	24 33 09 32			
4	C	Left in great Bear's Tail.	25 16 09 47	25 02 09 42	24 47 09 37	25 32 09 53			
5	D		26 14 10 09	26 00 10 03	25 46 09 59	26 30 10 14			
6	E		27 13 10 30	26 59 10 25	26 44 10 20	27 29 10 35			
7	F		28 11 11 51	27 57 10 46	27 43 10 41	28 27 10 56			
8	G	Sun r. 5.11.	29 10 11 12	28 56 11 07	28 41 11 02	29 26 11 17			
9	A	Sol in Taurus	8. 08 11 32	29 54 11 27	29 40 11 22	8. 24 11 38			
10	B	Dragons tail.	01 07 11 53	8. 52 11 48	8. 38 11 43	01 23 11 58			
11	C	Arcturus.	02 05 12 13	01 51 12 01	01 37 12 03	02 21 12 19			
12	D		03 03 12 33	02 49 12 28	02 35 12 23	03 19 12 38			
13	E		04 02 12 53	03 47 12 48	03 33 12 43	04 17 12 58			
14	F		05 00 13 13	04 46 13 08	04 32 13 03	05 16 13 18			
15	G		05 58 13 32	05 44 13 27	05 30 13 23	06 14 13 37			
16	A		06 56 13 51	06 42 13 47	06 28 13 42	07 12 13 56			
17	B		07 55 14 10	07 40 14 06	07 26 14 01	08 10 14 15			
18	C		08 53 14 29	08 39 14 24	08 24 14 20	09 09 14 34			
19	D	Sun r. 4.45.	09 51 14 47	09 37 14 43	09 23 14 39	10 07 14 52			
20	E	Southernmost Scale of Lib.	10 49 15 06	10 35 15 01	10 21 14 57	11 05 15 11			
21	F		11 47 15 24	11 33 15 19	11 19 15 15	12 03 15 28			
22	G		12 45 15 42	12 31 15 37	12 17 15 33	13 01 15 46			
23	A		13 43 15 59	13 29 15 55	13 15 15 51	13 59 16 04			
24	B		14 41 16 16	14 27 16 12	14 13 16 08	14 57 16 21			
25	C	Math. Ev.	15 39 16 33	15 25 16 19	15 11 16 25	15 55 16 38			
26	D	Upper of the two formost	16 37 16 50	16 23 16 46	16 09 16 42	16 53 16 54			
27	E		17 35 17 06	17 20 17 02	17 07 16 58	17 51 17 11			
28	F	Sun r. 4.30.	18 33 17 23	18 19 17 19	18 05 17 15	18 48 17 27			
29	G	in ☐ of the little Bear.	19 30 17 38	19 16 17 35	19 02 17 31	19 46 17 43			
30	A	Northernmost Scale in Lib.	20 28 17 54	20 14 17 50	19 00 17 46	20 44 17 58			

Month days.	Week days.	Remarkable days, and something of stars at midnight	First Year.		Second Year.		Third Year.		Leap-Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			☿	North	☿	North	☿	North	☿	North
1	B	<i>Phil. & Jac.</i>	21 26	18 09	21 12	18 06	20 58	18 02	21 42	18 13
2	C		22 24	18 24	22 10	18 21	21 56	18 17	22 40	18 28
3	D	Brightest in the Crown.	23 22	18 39	23 08	18 35	22 54	18 32	23 37	18 43
4	E	Brightest in Serp. Neck.	24 19	18 53	24 05	18 50	23 51	18 46	24 35	18 57
5	F	Sun r. 4. 15.	25 17	19 07	25 03	19 04	24 49	19 01	25 33	19 11
6	G		26 15	19 21	26 01	19 18	25 47	19 14	26 30	19 24
7	A		27 12	19 34	26 58	19 31	26 44	19 28	27 28	19 38
8	B		28 10	19 47	27 56	19 44	27 42	19 41	28 26	19 51
9	C	Scorpion's Forehead.	29 08	20 00	28 54	19 57	28 40	19 54	29 23	20 03
10	D		II. 05	20 12	29 51	20 10	29 37	20 06	II. 21	20 16
11	E	<i>Sol in Gemini</i>	01 03	20 25	II. 49	20 22	II. 35	20 18	01 15	20 28
12	F		02 00	20 36	01 46	20 33	01 32	20 30	02 16	20 39
13	G		02 58	20 48	02 44	20 45	02 30	20 42	03 14	20 50
14	A	Scorpion's Heart.	03 55	20 59	03 42	20 56	03 28	20 53	04 11	21 01
15	B		04 53	21 09	04 39	21 07	04 25	21 04	05 09	21 12
16	C		05 50	21 19	05 37	21 17	05 23	21 14	06 06	21 22
17	D		06 48	21 29	06 34	21 27	06 20	21 24	07 04	21 32
18	E	Sun r. 4.	07 45	21 39	07 31	21 36	07 17	21 34	08 01	21 41
19	F		08 43	21 48	08 29	21 45	08 15	21 43	08 59	21 50
20	G		09 40	21 57	09 26	21 54	09 12	21 52	09 56	21 59
21	A		10 38	22 05	10 24	22 03	10 10	22 01	10 53	22 07
22	B		11 35	22 13	11 21	22 11	11 07	22 09	11 51	22 15
23	C		12 32	22 21	12 18	22 19	12 05	22 17	12 48	22 23
24	D		13 30	22 28	13 16	22 26	13 02	22 24	13 45	22 30
25	E		14 27	22 35	14 13	22 33	13 59	22 31	14 43	22 36
26	F		15 24	22 41	15 11	22 40	14 57	22 38	15 40	22 43
27	G		16 22	22 47	16 08	22 46	15 54	22 44	16 37	22 49
28	A		17 19	22 53	17 05	22 51	16 51	22 50	17 35	22 54
29	B	K. Charles II.	18 16	22 58	18 02	22 57	17 49	22 55	18 32	22 58
30	C	Nat. & Rest	19 13	23 03	19 00	23 02	18 46	23 00	19 29	23 04
31	D	Sun r. 3. 50.	20 10	23 07	19 57	23 06	19 43	23 05	20 27	23 08

Month days.	Week days.	Remarkable days, and southing of Stars at Midnight.	First Year.		Second Year.		Third Year.		Leap Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			II	North.	II	North.	II	North.	II	North.
1	E		21	08	23	11	20	54	23	10
2	F		22	05	23	15	21	51	23	14
3	G		23	03	23	18	22	49	23	17
4	A		24	00	23	21	23	46	23	20
5	B		24	57	23	23	24	43	23	23
6	C		25	54	23	25	25	41	23	25
7	D		26	52	23	27	26	38	23	26
8	E		27	49	23	28	27	35	23	28
9	F		28	46	23	29	28	32	23	29
10	G	Sun r. 3.48.	29	43	23	29	29	29	23	29
11	A	Sol in Cancer.	☉. 40	23	29	☉. 27	23	29	☉. 13	23
12	B		01	38	23	29	01	23	23	29
13	C		02	35	23	28	02	21	23	28
14	D		03	32	23	27	03	18	23	27
15	E		04	29	23	25	04	15	23	25
16	F		05	26	23	23	05	13	23	23
17	G	Brightest in	06	24	23	20	06	10	23	21
18	A	the Harp.	07	21	23	17	07	07	23	18
19	B		08	18	23	14	08	04	23	14
20	C		09	15	23	10	09	01	23	11
21	D	Sun r. 3.50.	10	12	23	06	09	50	23	07
22	E		11	09	23	01	10	56	23	02
23	F		12	07	22	56	11	53	22	57
24	G	John Bapt.	13	04	22	51	12	50	22	52
25	A		14	01	22	45	13	47	22	46
26	B		14	58	22	39	14	44	22	40
27	C		15	55	22	32	15	42	22	34
28	D		16	52	22	25	16	39	22	27
29	E	Peter Ap.	17	50	22	18	17	36	22	20
30	F		18	47	22	10	18	33	22	12

July hath XXXI Days.

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Month days.	Week days.	Remarkable days, and sou-thing of stars at midnight.	First Year.		Second Year.		Third Year.		Leap-Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			☉ North.	☉ North.	☉ North.	☉ North.	☉ North.	☉ North.	☉ North.	☉ North.
1	A		19 44	22 02	19 30	22 04	19 17	22 05	20 00	21 59
2	B		20 42	21 53	20 28	21 55	20 14	21 57	20 57	21 51
3	C		21 39	21 44	21 25	21 46	21 11	21 49	21 54	21 42
4	D	Sun r. 4. 2.	22 36	21 35	22 22	21 37	22 08	21 40	22 51	21 32
5	E	Brightest	23 33	21 25	23 19	21 28	23 05	21 30	23 49	21 23
6	F	between	24 31	21 15	24 17	21 18	24 03	21 20	24 46	21 13
7	G	the Eagles	25 28	20 05	25 14	21 08	25 00	21 10	25 43	21 02
8	A	Shoulders.	26 25	20 54	26 11	20 57	25 57	21 00	26 41	20 51
9	B		27 22	20 43	27 08	20 46	26 55	20 49	27 38	20 40
10	C		28 20	20 33	28 06	20 35	27 52	20 38	28 35	20 29
11	D		29 17	20 20	29 03	20 23	28 49	20 26	29 33	20 17
12	E		☉. 14	20 08	☉. 00	20 11	29 46	20 14	☉. 30	20 05
13	F	Sol in Leo.	01 11	19 56	00 58	19 59	☉. 44	20 02	01 27	19 53
14	G		02 09	19 44	01 55	19 46	01 41	19 49	02 25	19 39
15	A		03 06	19 30	02 52	19 33	02 38	19 36	03 22	19 26
16	B		04 04	19 17	03 50	19 20	03 36	19 23	04 19	19 13
17	C	Sun r. 4. 15.	05 01	19 04	04 47	19 06	04 33	19 09	05 17	18 59
18	D		05 58	18 49	05 45	18 52	05 31	18 57	06 14	18 45
19	E	Swans Tail.	06 56	18 34	06 42	18 38	06 28	18 41	07 12	18 30
20	F	Dog Days	07 53	18 20	07 39	18 23	07 25	18 27	08 09	18 16
21	G	begin.	08 51	18 05	08 37	18 08	08 23	18 12	09 06	18 01
22	A		09 48	17 50	09 35	17 53	09 20	17 57	10 04	17 45
23	B		10 46	17 34	10 32	17 38	10 18	17 42	11 01	17 30
24	C		11 43	17 18	11 29	17 22	11 15	17 26	11 59	17 14
25	D	James Ap.	12 41	17 02	12 27	17 06	12 13	17 10	12 56	16 58
26	E	Sun r. 4. 30.	13 38	16 46	13 24	16 50	13 10	16 54	13 54	16 41
27	F		14 36	16 29	14 22	16 33	14 08	16 37	14 52	16 24
28	G		15 33	16 12	15 19	16 16	15 06	16 20	15 49	16 07
29	A		16 31	15 55	16 17	15 59	16 03	16 03	16 47	15 50
30	B		17 29	15 38	17 15	15 42	17 01	15 46	17 44	15 33
31	C		18 26	15 20	18 12	15 24	17 58	15 28	18 42	15 15

Month days.	Week days.	Remarkable days, and something of stars at midnight.	First Year.		Second Year.		Third Year.		Leap-Year.	
			1709.	1713	1710.	1714.	1711.	1715.	1712.	1716.
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			☉	North.	☉	North.	☉	North.	☉	North.
1	C		19 24	15 02	19 10	15 06	18 56	15 11	19 40	14 57
2	D		20 22	14 44	20 08	14 48	19 53	14 53	20 37	14 39
3	E	Sun r. 4.45.	21 19	14 25	21 05	14 30	20 51	14 34	21 35	14 20
4	F		22 17	14 07	22 03	14 11	21 49	14 16	22 33	14 10
5	G		23 15	13 48	23 01	13 52	22 47	13 57	23 31	13 42
6	A		24 13	13 29	23 59	13 33	23 45	13 38	24 28	13 23
7	B		25 10	13 09	24 56	13 14	24 42	13 19	25 26	13 04
8	C		26 08	12 50	25 54	12 54	25 40	12 59	26 24	12 44
9	D		27 06	12 30	26 52	12 35	26 38	12 40	27 22	12 24
10	E		28 04	12 10	27 50	12 15	27 36	12 20	28 20	12 04
11	F		29 02	11 50	28 48	11 55	28 34	12 00	29 18	11 44
12	G		☿ 00	11 30	29 46	11 35	29 32	11 40	☿. 16	11 24
13	A	Sol in Virgo.	00 58	11 09	☿. 44	11 14	☿. 30	10 19	01 14	11 04
14	B		01 56	10 48	01 42	10 53	01 28	10 59	02 12	10 43
15	C		02 54	10 28	02 39	10 33	02 26	10 38	03 10	10 22
16	D		03 52	10 17	03 37	10 12	03 24	10 17	04 08	10 01
17	E		04 50	09 43	04 35	09 51	04 22	09 56	05 06	09 40
18	F		05 48	09 24	05 34	09 29	05 20	09 35	06 04	09 18
19	G		06 46	09 03	06 32	09 08	06 18	09 13	07 02	08 57
20	A		07 44	08 41	07 30	08 46	07 16	08 52	08 00	08 35
21	B	Fomelbant.	08 42	08 19	08 28	08 25	08 14	08 30	08 58	08 13
22	C		09 40	07 57	09 27	08 03	09 12	08 08	09 57	07 52
23	D		10 39	07 35	10 25	07 41	10 11	07 46	10 55	07 29
24	E	Barthol. A.	11 37	07 13	11 23	07 19	11 09	07 24	11 53	07 07
25	F	First in Pegafus Wing,	12 35	06 51	12 21	06 56	12 07	07 02	12 51	06 45
26	G	and beginn.	13 34	06 28	13 20	06 34	13 06	06 40	13 50	06 23
27	A	of his Leg.	14 32	06 06	14 18	06 12	14 04	06 17	14 48	06 00
28	B	Dog days end.	15 31	05 43	15 16	05 49	15 02	05 55	15 46	05 37
29	C	Sun r. 5.30.	16 29	05 21	16 15	05 26	16 01	05 32	16 45	05 15
30	D		17 27	04 58	17 13	05 04	16 59	05 09	17 43	04 52
31	E		18 26	04 35	18 12	04 41	17 58	04 48	18 42	04 29

Month days.	Week days.	Remarkable days, and something of stars at midnight.	First Year.		Second Year.		Third Year.		Leap-Year.									
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.								
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.								
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.								
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.								
			☉ North	☉ North	☉ North	☉ North	☉ North	☉ North	☉ North	☉ North								
1	F	Lon. burnt 66	19	24	04	12	19	10	04	18	18	56	04	23	19	40	04	06
2	G		20	23	03	49	20	08	03	55	19	55	04	00	20	39	03	43
3	A		21	20	03	26	21	07	03	32	20	53	03	57	21	38	03	20
4	B		22	22	03	03	22	06	03	08	21	52	03	14	22	36	02	57
5	C	Sun r. 5. 45.	23	19	02	40	23	05	02	45	22	50	02	51	23	35	02	23
6	D		24	18	02	16	24	03	02	22	23	49	02	28	24	34	02	10
7	E		25	10	01	53	25	02	01	59	24	48	02	04	25	32	01	47
8	F		26	15	01	30	26	01	01	35	25	47	01	41	26	31	01	23
9	G	Andromeda's Head.	27	14	01	06	26	59	01	12	26	45	01	18	27	30	01	00
10	A		28	13	00	43	27	58	00	48	27	44	00	54	28	29	00	36
11	B		29	11	00	19	28	57	00	25	28	43	00	31	29	27	00	13
12	C		☉. 10	S.	04	29	56	00	02	29	41	00	07	☉. 26	S.	10		
13	D	Sun r. 6. o. Sol in Libra. End of Pegasus Wing.	01	09	00	27	☉. 55	S.	22	☉. 41	S.	16	01	25	00	34		
14	E		02	08	00	51	01	54	00	45	01	40	00	39	02	24	00	57
15	F		03	07	01	14	02	53	01	09	02	39	01	03	03	23	01	21
16	G		04	06	01	38	03	52	01	32	03	38	01	26	04	22	01	44
17	A	Sun r. 6. 15.	05	05	02	01	04	51	01	56	04	37	01	50	05	21	02	08
18	B		06	04	02	25	05	50	02	19	05	36	02	13	06	20	02	31
19	C		07	03	02	48	06	50	02	42	06	35	02	37	07	20	02	55
20	D		08	03	03	12	07	48	03	06	07	34	03	00	08	19	03	18
21	E	Matth. Ev. Pole Star.	09	02	03	36	08	47	03	29	08	33	03	24	09	18	03	41
22	F		10	00	03	58	09	47	03	53	09	32	03	47	10	17	04	05
23	G		11	00	04	22	10	46	04	16	10	32	04	10	11	16	04	28
24	A		12	00	04	45	11	45	04	39	11	31	04	33	12	16	04	51
25	B	Southernmost in Andromeda's Girdle.	12	59	05	08	12	45	05	02	12	30	04	57	13	16	05	14
26	C		13	58	05	31	13	44	05	25	13	29	05	20	14	14	05	37
27	D		14	58	05	54	14	43	05	48	14	29	05	43	15	14	06	00
28	E		15	57	06	17	15	43	06	11	15	28	06	06	16	13	06	23
29	F	Sun r. 6. 30. Mich. Arc.	16	57	06	40	16	42	06	34	16	28	06	29	17	13	06	46
30	G		17	56	07	03	17	41	06	57	17	27	06	52	18	12	07	09

Month days.	Week days.	Remarkable days, and something of stars at midnight	First Year.		Second Year.		Third Year.		Leap-Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			☿	South.	☿	South.	☿	South.	☿	South.
1	A		18 56	07 25	18 41	07 20	18 27	07 14	19 12	07 32
2	B		19 55	07 48	19 41	07 42	19 26	07 37	20 11	07 54
3	C		20 55	08 10	20 40	08 05	20 26	08 00	21 11	08 14
4	D		21 54	08 33	21 40	08 27	21 25	08 22	22 11	08 39
5	E	Sun r. 6. 45.	22 54	08 55	22 40	08 50	22 25	08 44	23 10	09 01
6	F		23 54	09 17	23 39	09 12	23 25	09 06	24 10	09 23
7	G		24 54	09 39	24 39	09 34	24 25	09 28	25 10	09 45
8	A		25 53	10 01	25 39	09 56	25 24	09 50	26 10	10 07
9	B		26 53	10 23	26 39	10 17	26 24	10 12	27 09	10 29
10	C		27 53	10 44	27 38	10 40	27 24	10 34	28 09	10 50
11	D	Andromeda's	28 53	11 06	28 38	11 00	28 24	10 55	29 09	11 11
12	E	Southernmost	29 53	11 27	29 38	11 22	29 24	11 17	m.	09 11 33
13	F	Foot.	m.	53 11 48	m.	38 11 43	m.	24 11 38	01 09	11 54
14	G	Sol in Scorpio.	01 53	12 09	01 38	12 03	01 24	11 59	02 09	12 14
15	A	Sun r. 7. 0.	02 53	12 29	02 38	12 24	02 23	12 19	03 09	12 35
16	B		03 53	12 50	03 38	12 45	03 23	12 40	04 09	12 55
17	C		04 53	13 10	04 38	13 05	04 24	13 00	05 09	13 16
18	D	Luke Evan.	05 53	13 30	05 38	13 25	05 24	13 21	06 09	13 36
19	E		06 53	13 40	06 38	13 45	06 24	13 40	07 09	13 55
20	F		07 53	14 10	07 39	14 05	07 24	14 00	08 09	14 15
21	G		08 53	14 29	08 39	14 24	08 24	14 20	09 10	14 34
22	A	Sun r. 7. 15.	09 53	14 48	09 39	14 44	09 24	14 39	10 10	14 54
23	B		10 54	15 07	10 39	15 03	10 25	14 58	11 10	15 12
24	C		11 54	15 26	11 39	15 21	11 25	15 17	12 10	15 31
25	D		12 54	15 44	12 40	15 40	12 25	15 35	13 11	15 49
26	E	Whales Jaw.	13 55	16 03	13 40	15 58	13 25	15 54	14 11	16 07
27	F		14 55	16 20	14 40	16 16	14 26	16 12	15 11	16 25
28	G	Sim. & Jud.	15 55	16 38	15 41	16 34	15 26	16 29	16 12	16 43
29	A	Perfius	16 56	16 55	16 41	16 51	16 27	16 47	17 12	17 00
30	B	right Side.	17 56	17 13	17 41	17 08	17 27	17 04	18 13	17 17
31	C	Sun r. 7. 30.	18 57	17 20	18 42	17 25	18 27	17 21	19 13	17 34

November hath XXX Days.

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Month	Week days.	Remarkable days, and Touching of Stars at Midnight.	First Year.		Second Year.		Third Year.		Leap Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
Month days.	1		1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
1	D	All Saints.	m	South.	m	South.	m	South.	m	South.
2	E		19 57	17 46	19 43	17 42	19 28	17 38	20 14	17 50
3	E		20 58	18 02	20 43	17 58	20 28	17 54	21 14	18 06
4	G	K. W. Nat.	21 58	18 18	21 44	18 14	21 29	18 01	22 15	18 21
5	A	Pow. Plot.	22 59	18 33	22 44	18 29	22 30	18 26	23 15	18 37
6	B		24 00	18 48	23 45	18 45	23 30	18 41	24 16	18 52
7	C		25 00	19 03	24 45	18 59	24 31	18 56	25 17	19 07
8	D	Sun r. 7.45.	26 01	19 18	25 46	19 14	25 32	19 11	26 17	19 22
9	E		27 02	19 32	26 47	19 28	26 32	19 25	27 18	19 36
10	F		28 02	19 46	27 47	19 42	27 33	19 39	28 19	19 49
11	G		29 03	19 59	28 48	19 56	28 33	19 52	29 19	20 02
12	A	Sol in Sagit.	7. 04	20 12	29 49	20 09	29 34	20 06	7. 20	20 15
13	B		01 04	20 25	7. 50	20 22	7. 35	20 19	01 21	20 28
14	C		02 05	20 37	01 50	20 34	01 36	20 31	02 22	20 40
15	D		03 06	20 49	02 51	20 46	02 36	20 43	03 23	20 52
16	E	Bull's Eye, or Aldebaran.	04 07	21 01	03 52	20 58	03 37	20 55	04 23	21 03
17	F		05 08	21 12	04 53	21 09	04 38	21 06	05 24	21 15
18	G		06 09	21 22	05 54	21 20	05 39	21 17	06 25	21 25
19	A	Sun r. 8.	07 10	21 33	06 55	21 30	06 40	21 28	07 26	21 35
20	B		08 10	21 43	07 56	21 40	07 41	21 38	08 27	21 45
21	C		09 11	21 52	08 57	21 50	08 42	21 48	09 28	21 54
22	D		10 12	22 01	09 58	21 59	09 43	21 57	10 29	22 03
23	E		11 13	22 10	10 59	22 08	10 44	22 06	11 30	22 12
24	F	Capella, or Goat.	12 14	22 18	12 00	22 16	11 45	22 14	12 31	22 20
25	G	Orion's Left Foot.	13 15	22 26	13 00	22 24	12 46	22 22	13 32	22 28
26	A		14 16	22 34	14 01	22 32	13 47	22 30	14 33	22 35
27	B	End of Bulls Horn.	15 17	22 41	15 02	22 39	14 48	22 37	15 34	22 42
28	C		16 18	22 47	16 03	22 45	15 49	22 44	16 35	22 48
29	D		17 19	22 53	17 05	22 52	16 50	22 50	17 36	22 54
30	E	Andr. Ap.	18 21	22 58	18 06	22 57	17 51	22 56	18 37	23 00
			19 22	23 03	19 07	23 02	18 52	23 01	19 38	23 05

Month	Day	Remarkable Days, and Raising of Halls at midnight.	First Year.		Second Year.		Third Year.		Leap Year.	
			1709.	1713.	1710.	1714.	1711.	1715.	1712.	1716.
			1717.	1721.	1718.	1722.	1719.	1723.	1720.	1724.
			☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.	☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			↑	South.	↑	South.	↑	South.	↑	South.
1	F	First in Ori-	20	23	23	08	20	08	23	07
2	G	on's Belt.	21	24	23	12	21	09	23	11
3	A	Last in Ori-	22	25	23	16	22	10	23	15
4	B	on's Belt.	23	26	23	20	23	11	23	19
5	C	Orion's right	24	27	23	22	24	12	23	22
6	D	Shoulder, &	25	28	23	24	25	13	23	24
7	E	Antares's	26	29	23	26	26	14	23	26
8	F	right Shoul-	27	30	23	28	27	16	23	28
9	G	der.	28	32	23	29	28	17	23	28
10	A		29	33	23	29	29	18	23	29
11	B	Sol in Capr.	30	34	23	29	30	19	23	29
12	C	Sun r. 8. 12.	01	35	23	29	01	20	23	29
13	D	Foot of the	02	36	23	27	02	21	23	28
14	E	great Dog.	03	37	23	26	03	23	23	27
15	F	Bright Foot	04	39	23	24	04	24	23	25
16	G	of Gemini.	05	40	23	22	05	25	23	22
17	A		06	41	23	19	06	26	23	19
18	B	Mouth of the	07	42	23	16	07	27	23	16
19	C	great Dog,	08	43	23	12	08	28	23	12
20	D	or Syllus.	09	45	23	08	09	30	23	09
21	E	The Apost.	10	46	23	03	10	31	23	04
22	F		11	47	22	58	11	32	22	59
23	G		12	48	22	52	12	33	22	53
24	A		13	49	22	46	13	34	22	47
25	B	Nat. Christ.	14	50	22	39	14	35	22	41
26	C	St. Stephen.	15	52	22	32	15	37	22	34
27	D	John Evan.	16	53	22	25	16	38	22	27
28	E	Intocents.	17	54	22	17	17	39	22	19
29	F	Castor.	18	55	22	09	18	40	22	11
30	G	Little Dog's	19	56	22	00	19	41	22	02
31	A	thigh. Pollox.	20	57	21	51	20	42	21	53

A Table of the Variation of the Sun's Declination in Hours.

Hours from the Meridian of London.

Diurn. Variat.	D. 15	D. 30	D. 45	D. 60	D. 75	D. 90	D. 105	D. 120	D. 135	D. 150	D. 165	12 18
Min.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.
2	00	00	00	00	00	00	01	01	01	01	01	01
3	00	00	00	00	01	01	01	01	01	01	01	01
4	00	00	00	01	01	01	01	01	01	02	02	02
5	00	00	01	01	01	01	01	02	02	02	02	02
6	00	00	01	01	01	01	02	02	02	02	03	03
7	00	01	01	01	01	02	02	03	03	03	03	03
8	00	01	01	01	02	02	02	03	03	03	04	04
9	00	01	01	01	02	02	03	03	03	04	04	04
10	00	01	01	02	02	02	03	03	04	04	05	05
11	00	01	01	02	02	03	03	04	04	05	05	05
12	00	01	01	02	02	03	03	04	04	05	05	06
13	01	01	02	02	03	03	04	04	05	05	06	06
14	01	01	02	02	03	03	04	05	05	06	06	07
15	01	01	02	02	03	04	04	05	06	06	07	07
16	01	01	02	03	03	04	05	05	06	07	07	08
17	01	01	02	03	04	04	05	06	06	07	08	08
18	01	01	02	03	04	04	05	06	07	07	08	09
19	01	02	02	03	04	05	06	06	07	08	09	09
20	01	02	02	03	04	05	06	06	07	08	09	10
21	01	02	03	03	04	05	06	07	08	09	10	10
22	01	02	03	04	05	05	06	07	08	09	10	11
23	01	02	03	04	05	06	07	08	09	10	11	11
24	01	02	03	04	05	06	07	08	09	10	11	12

Examples

Examples of the Use of the foregoing Tables, for the Sun's Declination
for Years to come, &c.

Example. 1. Suppose the Sun's Declination be required on the 21st of May, in the Year 1715, being the third after the Leap-Year.

In the Month of May, in the First Column, look the Day of the Month 21, and under the Third-Year, in the Column of \odot Dec. over against the 21st Day, you will find $22^{\circ} 01'$ Northerly, the Sun's Declination that Day at Noon for the Meridian of London.

Example. 2. Anno 1728, Septemb. 1. I would know the Sun's Declination; from 1728, rejecting the Hundreds and Scores, I divide the Residue, which is 8, by 4 the Remainder 0 shews it is a Leap-Year, under which Title, I find $4^{\circ} 6'$ North. Then from 1728, I subtract 1720, rests 8 Years; under which, against Sept. 1. (In the Table of Variation in Years) I find the Variation $1'$ South; which subtracted from the afore-found Declination $4^{\circ} 6'$ North, rests $4^{\circ} 5'$ North, the true Declination of the Sun.

And here note, That when the Declination and Variation are both North, or both South, their Sum is the true Declination; but if the one be North and the other South, it is their Difference.

For the Declination of the Sun out of the Meridian of London.

Anno 1717 April 11, at fix of the Clock Afternoon I would know the Sun's Declination. The 11th day at Noon, I find it in the Kalender $12^{\circ} 13'$, North; and the 12th day $12^{\circ} 33'$; therefore subtracting the lesser Declination $12^{\circ} 13'$ out of the greater, $12^{\circ} 33'$; the Residue $20'$ is the daily Encrease. Then in the Table of Variation in Hours, &c. under 6 Hours or 90° in the Head, and against $20'$ on the left-hand, I find $5'$ the proportional Part; which (because the Hour was Afternoon, and the Declination encreasing) added to the afore-found $12^{\circ} 13'$, the Sum is $12^{\circ} 18'$ North, the Declination.

Examp. For the Declination of the Sun, Anno 1711, Octob. 28, at 8 in the Morning; that is 4 Hours reckoned backward from Noon, In the Kalender, the Declination on Octob. 28. that Year is $16^{\circ} 29'$, and on the 27th day $16^{\circ} 12'$ South the Differences is $17'$; against which, under 4 Hours, or $60'$ in the Table of Variation in Hours, &c. I find the proportional Part $3'$; which (in this Example) Subtracted from $16^{\circ} 29'$, the remaining $16^{\circ} 26'$ South, the Declination sought. And thus may the true Declination of the Sun be easily found at all times, and in all Meridians, of which I suppose here will need no more Examples. The Sun's Horizontal Parallax is only 15 Seconds, therefore the Parallax need not to be applied at all. Also the Sun's Refraction is demonstratively equal to that of the Fixed Stars; which latter is, by the Observation of Tycho Brahe, in the Horizon $30'$, and is $0'$ in 20° of Altitude. Vid. Chap. 8, Sect. 1.

An Explanation of the precedent Kalendar.

IN each Page there are eleven Columns ; the first sheweth the Day of the Month ; the second, the Days of the Week expressed by the Week-day Letters, as in the Year 1713, in the Month of *April*, you will find C for *Saturday*, and D for *Sunday*, which is the Dominical Letter, for that Year, (as you see in the Page before the Kalendar.) The Third Column sheweth some remarkable Days, and the Southing of several Stars at Midnight, with their Declinations from the Equinoctial ; as in the aforesaid Month, you will find against the fourth day, there stands the *Last in the Great Bear's Tail*, which shews that the said Star comes to the Meridian the fourth day, at twelve of the Clock at Midnight. The fourth Column sheweth the Place of the Sun for the first Year after Leap Year, (according to Mr. *Flamsteed's* Table ;) as against the third of *April*, you will find the Sun, to be in $24^{\circ} 17'$ of *Aries*, The fifth Column sheweth the Declination of the Sun, for the first Year after Leap Year ; as against the third day aforesaid, you will find the Sun's Declination to be $9^{\circ} 25'$. And after the same manner the other six Columns are to be used ; as against the said third day of *April*, you will find in the sixth Column, in the second Year after Leap-Year, that the Sun's Declination to be $9^{\circ} 21'$; and in the eighth Column, and in the Third Year after Leap-Year, the Sun's Place is $23^{\circ} 49'$ in *Aries* ; and in the ninth Column, the Declination of the Sun is $9^{\circ} 15'$; and in the tenth Column, in the Leap-Year, the Sun's Place is $24^{\circ} 33'$ in *Aries* ; and in the eleventh Column, the Sun's Declination is $9^{\circ} 32'$.

How to find the Day of the Month, or Week-Day, for any Time past or to come, by the precedent Kalendar.

First you may find the Dominical Letter by the Table before the Kalendar, or else by the Rule delivered in Chap. 8. Sect. 3. and thereby you may discover the Day of the Month, as follows.

Ex. What Day of the Month was the first Monday in August, in the Year 1645 ?

By the former Rule you will find the Dominical Letter was E ; then turning to the Month of *August*, call E *Sunday*, and the F that follows is Monday, and the first Monday, is the 4th Day of the Month.

Ex. What Day of the Week will the tenth of February be in the Year 1708 ?

This Year will be Leap-Year, and in the Table hath two Dominical Letters, D and C ; the first of them serving from the first of *January* till the 25th of *February* and the other from thence to the Year's end ; Therefore against the 10th of *February* stands F ; calling D *Sunday*, E is Monday, and F is Tuesday, the Week-Day sought.

Ex. What Day of the Month was the second Thursday in the Month of August, in the Year 1708 ?

The Dominical Letter for the latter part of the Year is C, therefore C stands for Sunday, D for Monday, E for Tuesday, F for Wednesday, G for Thursday ; and against the second G in, *August*, is the 12th Day of the Month, which was required.

A Table of the Variation of the Sun's Declination, to be applied for Years to come, according to the Title on the Right hand; but for Years past, contrarily.

Years.	04	08	12	16	20	24	28	32	36	40	44	48	52	56	60	
Month Days.	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	
January,	1	00	01	01	01	02	02	02	03	03	03	03	04	04	04	North.
	11	00	01	01	01	02	02	03	03	04	04	04	05	05	05	
	21	00	01	01	02	02	03	03	04	04	05	05	06	06	07	
February,	1	01	01	02	02	03	03	04	05	05	06	06	07	08	08	
	11	01	01	02	03	03	04	05	05	06	07	08	08	09	10	
	21	01	01	02	03	03	04	05	05	06	07	08	08	09	10	
March,	1	01	01	02	03	04	04	05	06	06	07	08	08	09	10	
	11	01	01	02	03	04	04	05	06	06	07	08	09	09	10	
	21	01	01	02	03	04	04	05	06	06	07	08	08	09	10	
April,	1	01	01	02	03	03	04	05	05	06	07	07	08	08	09	
	11	01	01	02	03	03	04	04	05	06	06	07	08	08	09	
	21	01	01	02	02	03	03	04	05	05	06	06	07	07	08	
May,	1	00	01	01	02	02	03	03	04	04	05	05	06	06	07	
	11	00	01	01	02	02	02	03	03	03	04	04	05	05	05	
	21	00	01	01	01	01	02	02	02	02	03	03	03	04	04	
June,	1	00	00	00	01	01	01	01	01	01	01	01	02	02	02	South.
	11	00	00	00	00	00	00	00	00	00	00	00	00	00	00	
	21	00	00	00	01	01	01	01	01	01	01	01	02	02	02	
July,	1	00	01	01	01	01	02	02	02	02	03	03	03	04	04	
	11	00	01	01	02	02	02	03	03	03	04	04	05	05	05	
	21	00	01	01	02	02	03	03	04	04	05	05	06	06	07	
August,	1	01	01	02	02	03	03	04	05	05	06	06	07	07	08	
	11	01	01	02	03	03	04	04	05	06	06	07	08	08	09	
	21	01	01	02	03	03	04	05	05	06	07	08	08	09	10	
September,	1	01	01	02	03	04	04	05	06	06	07	08	09	09	10	
	11	01	01	02	03	04	04	05	06	06	07	08	09	09	10	
	21	01	01	02	03	04	04	05	06	06	07	08	09	09	10	
October,	1	01	01	02	03	03	04	05	05	06	07	08	08	09	10	
	11	01	01	02	03	03	04	05	06	06	07	08	08	09	10	
	21	01	01	02	02	03	03	04	05	05	06	06	07	07	08	
November,	1	00	01	01	02	02	03	03	04	04	05	05	06	06	07	
	11	00	01	01	02	02	02	03	03	03	04	04	05	05	05	
	21	00	01	01	01	01	02	02	02	02	03	03	03	04	04	
December,	1	00	00	00	01	01	01	01	01	01	01	02	02	02	02	
	11	00	00	00	00	00	00	00	00	00	00	00	00	00	00	
	21	00	00	00	01	01	01	01	01	01	01	02	02	02	02	

A Table of Difference

Diff.	1 Deg.		2 Deg.		1/4 Point		3 Deg.		4 Deg.		5 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	01.0	00.0	01.0	00.0	01.0	00.0	01.0	00.0	01.0	00.0	01.0	00.0	1
2	02.0	00.0	02.0	00.1	02.0	00.1	02.0	00.1	02.0	00.1	02.0	00.1	2
3	03.0	00.1	03.0	00.1	03.0	00.1	03.0	00.1	03.0	00.2	03.0	00.2	3
4	04.0	00.1	04.0	00.1	04.0	00.2	04.0	00.2	04.0	00.3	04.0	00.3	4
5	05.0	00.1	05.0	00.2	05.0	00.2	05.0	00.3	05.0	00.3	05.0	00.4	5
6	06.0	00.1	06.0	00.2	06.0	00.3	06.0	00.3	06.0	00.4	06.0	00.5	6
7	07.0	00.1	07.0	00.2	07.0	00.3	07.0	00.4	07.0	00.5	07.0	00.6	7
8	08.0	00.1	08.0	00.3	08.0	00.4	08.0	00.4	08.0	00.6	08.0	00.7	8
9	09.0	00.2	09.0	00.3	09.0	00.4	09.0	00.5	09.0	00.6	09.0	00.8	9
10	10.0	00.2	10.0	00.4	10.0	00.5	10.0	00.5	10.0	00.7	10.0	00.9	10
11	11.0	00.2	11.0	00.4	11.0	00.5	11.0	00.6	11.0	00.8	11.0	01.0	11
12	12.0	00.2	12.0	00.4	12.0	00.6	12.0	00.6	12.0	00.8	12.0	01.0	12
13	13.0	00.2	13.0	00.5	13.0	00.6	13.0	00.7	13.0	00.9	13.0	01.1	13
14	14.0	00.2	14.0	00.5	14.0	00.7	14.0	00.7	14.0	01.0	14.0	01.2	14
15	15.0	00.3	15.0	00.5	15.0	00.7	15.0	00.8	15.0	01.0	15.0	01.2	15
16	16.0	00.3	16.0	00.6	16.0	00.8	16.0	00.8	16.0	01.1	16.0	01.4	16
17	17.0	00.3	17.0	00.6	17.0	00.8	17.0	00.9	17.0	01.2	17.0	01.5	17
18	18.0	00.3	18.0	00.6	18.0	00.9	18.0	00.9	18.0	01.3	18.0	01.6	18
19	19.0	00.3	19.0	00.7	19.0	00.9	19.0	01.0	19.0	01.3	19.0	01.7	19
20	20.0	00.4	20.0	00.7	20.0	01.0	20.0	01.0	20.0	01.4	20.0	01.7	20
21	21.0	00.4	21.0	00.7	21.0	01.0	21.0	01.1	21.0	01.5	21.0	01.8	21
22	22.0	00.4	22.0	00.8	22.0	01.0	22.0	01.1	22.0	01.5	22.0	01.9	22
23	23.0	00.4	23.0	00.8	23.0	01.1	23.0	01.2	23.0	01.6	23.0	02.0	23
24	24.0	00.4	24.0	00.8	24.0	01.2	24.0	01.2	24.0	01.7	24.0	02.1	24
25	25.0	00.4	25.0	00.9	25.0	01.2	25.0	01.3	25.0	01.7	25.0	02.2	25
26	26.0	00.5	26.0	00.9	26.0	01.3	26.0	01.4	26.0	01.8	26.0	02.3	26
27	27.0	00.5	27.0	00.9	27.0	01.3	27.0	01.4	27.0	01.9	27.0	02.4	27
28	28.0	00.5	28.0	01.0	28.0	01.4	28.0	01.5	28.0	02.0	28.0	02.5	28
29	29.0	00.5	29.0	01.0	29.0	01.4	29.0	01.5	29.0	02.0	29.0	02.5	29
30	30.0	00.5	30.0	01.1	30.0	01.5	30.0	01.6	30.0	02.1	30.0	02.6	30
31	31.0	00.6	31.0	01.1	31.0	01.5	31.0	01.6	31.0	02.2	31.0	02.7	31
32	32.0	00.6	32.0	01.2	32.0	01.6	32.0	01.7	32.0	02.3	32.0	02.8	32
33	33.0	00.6	33.0	01.2	33.0	01.7	33.0	01.8	33.0	02.4	33.0	02.9	33
34	34.0	00.6	34.0	01.2	34.0	01.7	34.0	01.8	34.0	02.4	34.0	03.0	34
35	35.0	00.6	35.0	01.3	35.0	01.8	35.0	01.9	35.0	02.5	35.0	03.1	35
36	36.0	00.7	36.0	01.3	36.0	01.8	36.0	01.9	36.0	02.6	36.0	03.2	36
37	37.0	00.7	37.0	01.3	37.0	01.9	37.0	02.0	37.0	02.7	37.0	03.3	37
38	38.0	00.7	38.0	01.4	38.0	01.9	38.0	02.1	38.0	02.7	38.0	03.4	38
39	39.0	00.7	39.0	01.4	39.0	02.0	39.0	02.1	39.0	02.8	39.0	03.5	39
40	40.0	00.7	40.0	01.4	40.0	02.1	40.0	02.2	40.0	02.8	40.0	03.6	40
41	41.0	00.7	41.0	01.5	41.0	02.1	41.0	02.3	41.0	02.9	41.0	03.7	41
42	42.0	00.8	42.0	01.5	42.0	02.1	42.0	02.3	42.0	03.0	42.0	03.8	42
43	43.0	00.8	43.0	01.5	43.0	02.2	43.0	02.3	43.0	03.1	43.0	03.9	43
44	44.0	00.8	44.0	01.6	44.0	02.2	44.0	02.4	44.0	03.1	44.0	04.0	44
45	45.0	00.8	45.0	01.6	45.0	02.2	45.0	02.4	45.0	03.2	45.0	04.1	45
46	46.0	00.8	46.0	01.6	46.0	02.3	46.0	02.5	46.0	03.3	46.0	04.2	46
47	47.0	00.8	47.0	01.7	47.0	02.3	47.0	02.5	47.0	03.4	47.0	04.3	47
48	48.0	00.9	48.0	01.7	48.0	02.3	48.0	02.6	48.0	03.4	48.0	04.4	48
49	49.0	00.9	49.0	01.8	49.0	02.4	49.0	02.6	49.0	03.5	49.0	04.5	49
50	50.0	00.9	50.0	01.8	50.0	02.4	50.0	02.6	50.0	03.5	50.0	04.6	50
Diff.	89 Deg.	58 Deg.	74 Point	87 Deg.	86 Deg.	85 Deg.							Diff.

nn

Table of Difference

Diff.	1 Deg.	2 Deg.	3 Deg.	4 Deg.	5 Deg.	Diff.
	Lat. Dep.	Lat. Dep.	Lat. Dep.	Lat. Dep.	Lat. Dep.	
51	51.0 00.0	51.0 01.8	50.9 02.5	50.9 03.6	50.8 04.4	51
52	52.0 00.0	52.0 01.8	51.9 02.5	51.9 03.6	51.8 04.4	52
53	53.0 00.0	53.0 01.8	52.9 02.6	52.9 03.7	52.8 04.6	53
54	54.0 00.0	54.0 01.9	53.9 02.6	53.9 03.8	53.8 04.7	54
55	55.0 00.0	55.0 01.9	54.9 02.7	54.9 03.8	54.8 04.8	55
56	56.0 01.0	56.0 02.0	55.9 02.7	55.9 03.9	55.8 04.9	56
57	57.0 01.0	57.0 02.0	56.9 02.8	56.9 04.0	56.8 05.0	57
58	58.0 01.0	58.0 02.0	57.9 02.8	57.9 04.1	57.8 05.1	58
59	59.0 01.0	59.0 02.1	58.9 02.9	58.9 04.1	58.8 05.2	59
60	60.0 01.0	60.0 02.1	59.9 02.9	59.9 04.2	59.8 05.2	60
61	61.0 01.1	61.0 02.1	60.9 03.0	60.9 04.3	60.8 05.3	61
62	62.0 01.1	62.0 02.2	61.9 03.0	61.9 04.3	61.8 05.4	62
63	63.0 01.1	63.0 02.2	62.9 03.1	62.9 04.4	62.8 05.5	63
64	64.0 01.1	64.0 02.2	63.9 03.1	63.9 04.5	63.8 05.6	64
65	65.0 01.1	65.0 02.3	64.9 03.2	64.9 04.5	64.8 05.7	65
66	66.0 01.1	66.0 02.3	65.9 03.2	65.9 04.6	65.8 05.8	66
67	67.0 01.2	67.0 02.3	66.9 03.3	66.9 04.7	66.8 05.9	67
68	68.0 01.2	68.0 02.4	67.9 03.3	67.9 04.8	67.8 06.0	68
69	69.0 01.2	69.0 02.4	68.9 03.4	68.9 04.8	68.8 06.1	69
70	70.0 01.2	70.0 02.4	69.9 03.4	69.9 04.9	69.8 06.2	70
71	71.0 01.2	71.0 02.5	70.9 03.5	70.9 05.0	70.8 06.3	71
72	72.0 01.3	72.0 02.5	71.9 03.5	71.9 05.1	71.8 06.4	72
73	73.0 01.3	73.0 02.6	72.9 03.6	72.9 05.2	72.8 06.5	73
74	74.0 01.3	74.0 02.6	73.9 03.6	73.9 05.3	73.8 06.6	74
75	75.0 01.3	75.0 02.6	74.9 03.7	74.9 05.4	74.8 06.7	75
76	76.0 01.3	76.0 02.7	75.9 03.7	75.9 05.5	75.8 06.8	76
77	77.0 01.3	77.0 02.7	76.9 03.8	76.9 05.6	76.8 06.9	77
78	78.0 01.4	78.0 02.7	77.9 03.8	77.9 05.7	77.8 07.0	78
79	79.0 01.4	79.0 02.8	78.9 03.9	78.9 05.8	78.8 07.1	79
80	80.0 01.4	80.0 02.8	79.9 04.0	79.9 05.9	79.8 07.2	80
81	81.0 01.4	81.0 02.9	80.9 04.0	80.9 06.0	80.8 07.3	81
82	82.0 01.4	82.0 02.9	81.9 04.1	81.9 06.1	81.8 07.4	82
83	83.0 01.5	83.0 03.0	82.9 04.1	82.9 06.2	82.8 07.5	83
84	84.0 01.5	84.0 03.0	83.9 04.2	83.9 06.3	83.8 07.6	84
85	85.0 01.5	85.0 03.1	84.9 04.2	84.9 06.4	84.8 07.7	85
86	86.0 01.5	86.0 03.1	85.9 04.3	85.9 06.5	85.8 07.8	86
87	87.0 01.5	87.0 03.1	86.9 04.3	86.9 06.6	86.8 07.9	87
88	88.0 01.5	88.0 03.1	87.9 04.4	87.9 06.7	87.8 08.0	88
89	89.0 01.5	89.0 03.1	88.9 04.4	88.9 06.8	88.8 08.1	89
90	90.0 01.6	90.0 03.2	89.9 04.5	89.9 06.9	89.8 08.2	90
91	91.0 01.6	91.0 03.2	90.9 04.5	90.9 07.0	90.8 08.3	91
92	92.0 01.6	92.0 03.2	91.9 04.6	91.9 07.1	91.8 08.4	92
93	93.0 01.6	93.0 03.3	92.9 04.6	92.9 07.2	92.8 08.5	93
94	94.0 01.6	94.0 03.3	93.9 04.7	93.9 07.3	93.8 08.6	94
95	95.0 01.6	95.0 03.4	94.9 04.7	94.9 07.4	94.8 08.7	95
96	96.0 01.7	96.0 03.4	95.9 04.8	95.9 07.5	95.8 08.8	96
97	97.0 01.7	97.0 03.4	96.9 04.8	96.9 07.6	96.8 08.9	97
98	98.0 01.7	98.0 03.5	97.9 04.9	97.9 07.7	97.8 09.0	98
99	99.0 01.7	99.0 03.5	98.9 04.9	98.9 07.8	98.8 09.1	99
100	100.0 01.7	100.0 03.5	99.9 05.0	99.9 07.9	99.8 09.2	100
Diff.	Dep. Lat.	Dep. Lat.	Dep. Lat.	Dep. Lat.	Dep. Lat.	Diff.
	89 Deg.	88 Deg.	74 Point	87 Deg.	86 Deg. 85 Deg.	

of Latitude and Departure.

Diff.	Point		6 Deg.		7 Deg.		8 Deg.		Point		9 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	01.0	00.1	01.0	00.1	01.0	00.1	01.0	00.1	01.0	00.1	01.0	00.2	1
2	01.0	00.2	01.0	00.2	01.0	00.2	01.0	00.2	01.0	00.2	01.0	00.3	2
3	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.4	3
4	01.0	00.4	01.0	00.4	01.0	00.4	01.0	00.4	01.0	00.4	01.0	00.5	4
5	01.0	00.5	01.0	00.5	01.0	00.5	01.0	00.5	01.0	00.5	01.0	00.6	5
6	01.0	00.6	01.0	00.6	01.0	00.6	01.0	00.6	01.0	00.6	01.0	00.7	6
7	01.0	00.7	01.0	00.7	01.0	00.7	01.0	00.7	01.0	00.7	01.0	00.8	7
8	01.0	00.8	01.0	00.8	01.0	00.8	01.0	00.8	01.0	00.8	01.0	00.9	8
9	01.0	00.9	01.0	00.9	01.0	00.9	01.0	00.9	01.0	00.9	01.0	01.0	9
10	01.0	01.0	01.0	01.0	01.0	01.0	01.0	01.0	01.0	01.0	01.0	01.1	10
11	01.0	01.1	01.0	01.1	01.0	01.1	01.0	01.1	01.0	01.1	01.0	01.2	11
12	01.0	01.2	01.0	01.2	01.0	01.2	01.0	01.2	01.0	01.2	01.0	01.3	12
13	01.0	01.3	01.0	01.3	01.0	01.3	01.0	01.3	01.0	01.3	01.0	01.4	13
14	01.0	01.4	01.0	01.4	01.0	01.4	01.0	01.4	01.0	01.4	01.0	01.5	14
15	01.0	01.5	01.0	01.5	01.0	01.5	01.0	01.5	01.0	01.5	01.0	01.6	15
16	01.0	01.6	01.0	01.6	01.0	01.6	01.0	01.6	01.0	01.6	01.0	01.7	16
17	01.0	01.7	01.0	01.7	01.0	01.7	01.0	01.7	01.0	01.7	01.0	01.8	17
18	01.0	01.8	01.0	01.8	01.0	01.8	01.0	01.8	01.0	01.8	01.0	01.9	18
19	01.0	01.9	01.0	01.9	01.0	01.9	01.0	01.9	01.0	01.9	01.0	02.0	19
20	01.0	02.0	01.0	02.0	01.0	02.0	01.0	02.0	01.0	02.0	01.0	02.1	20
21	01.0	02.1	01.0	02.1	01.0	02.1	01.0	02.1	01.0	02.1	01.0	02.2	21
22	01.0	02.2	01.0	02.2	01.0	02.2	01.0	02.2	01.0	02.2	01.0	02.3	22
23	01.0	02.3	01.0	02.3	01.0	02.3	01.0	02.3	01.0	02.3	01.0	02.4	23
24	01.0	02.4	01.0	02.4	01.0	02.4	01.0	02.4	01.0	02.4	01.0	02.5	24
25	01.0	02.5	01.0	02.5	01.0	02.5	01.0	02.5	01.0	02.5	01.0	02.6	25
26	01.0	02.6	01.0	02.6	01.0	02.6	01.0	02.6	01.0	02.6	01.0	02.7	26
27	01.0	02.7	01.0	02.7	01.0	02.7	01.0	02.7	01.0	02.7	01.0	02.8	27
28	01.0	02.8	01.0	02.8	01.0	02.8	01.0	02.8	01.0	02.8	01.0	02.9	28
29	01.0	02.9	01.0	02.9	01.0	02.9	01.0	02.9	01.0	02.9	01.0	03.0	29
30	01.0	03.0	01.0	03.0	01.0	03.0	01.0	03.0	01.0	03.0	01.0	03.1	30
31	01.0	03.1	01.0	03.1	01.0	03.1	01.0	03.1	01.0	03.1	01.0	03.2	31
32	01.0	03.2	01.0	03.2	01.0	03.2	01.0	03.2	01.0	03.2	01.0	03.3	32
33	01.0	03.3	01.0	03.3	01.0	03.3	01.0	03.3	01.0	03.3	01.0	03.4	33
34	01.0	03.4	01.0	03.4	01.0	03.4	01.0	03.4	01.0	03.4	01.0	03.5	34
35	01.0	03.5	01.0	03.5	01.0	03.5	01.0	03.5	01.0	03.5	01.0	03.6	35
36	01.0	03.6	01.0	03.6	01.0	03.6	01.0	03.6	01.0	03.6	01.0	03.7	36
37	01.0	03.7	01.0	03.7	01.0	03.7	01.0	03.7	01.0	03.7	01.0	03.8	37
38	01.0	03.8	01.0	03.8	01.0	03.8	01.0	03.8	01.0	03.8	01.0	03.9	38
39	01.0	03.9	01.0	03.9	01.0	03.9	01.0	03.9	01.0	03.9	01.0	04.0	39
40	01.0	04.0	01.0	04.0	01.0	04.0	01.0	04.0	01.0	04.0	01.0	04.1	40
41	01.0	04.1	01.0	04.1	01.0	04.1	01.0	04.1	01.0	04.1	01.0	04.2	41
42	01.0	04.2	01.0	04.2	01.0	04.2	01.0	04.2	01.0	04.2	01.0	04.3	42
43	01.0	04.3	01.0	04.3	01.0	04.3	01.0	04.3	01.0	04.3	01.0	04.4	43
44	01.0	04.4	01.0	04.4	01.0	04.4	01.0	04.4	01.0	04.4	01.0	04.5	44
45	01.0	04.5	01.0	04.5	01.0	04.5	01.0	04.5	01.0	04.5	01.0	04.6	45
46	01.0	04.6	01.0	04.6	01.0	04.6	01.0	04.6	01.0	04.6	01.0	04.7	46
47	01.0	04.7	01.0	04.7	01.0	04.7	01.0	04.7	01.0	04.7	01.0	04.8	47
48	01.0	04.8	01.0	04.8	01.0	04.8	01.0	04.8	01.0	04.8	01.0	04.9	48
49	01.0	04.9	01.0	04.9	01.0	04.9	01.0	04.9	01.0	04.9	01.0	05.0	49
50	01.0	05.0	01.0	05.0	01.0	05.0	01.0	05.0	01.0	05.0	01.0	05.1	50
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
7 1/2 Point	84 Deg.		83 Deg.		82 Deg.		7 1/2 Point		81 Deg.		80 Deg.		Diff.

A Table of Difference

Lat.	1 Point		6 Deg.		7 Deg.		8 Deg.		1 Point		9 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	51.7	05.0	50.7	05.3	51.6	06.2	51.5	07.1	50.4	07.3	50.4	08.0	51
52	51.7	05.1	51.7	05.4	51.6	06.3	51.5	07.2	51.4	07.6	51.4	08.1	52
53	51.7	05.2	51.7	05.5	51.6	06.5	51.5	07.4	51.4	07.8	51.3	08.3	53
54	51.7	05.3	51.7	05.6	51.6	06.6	51.5	07.5	51.4	07.9	51.3	08.4	54
55	51.7	05.4	51.7	05.8	51.6	06.7	51.5	07.6	51.4	08.1	51.3	08.6	55
56	51.7	05.5	51.7	05.8	51.6	06.7	51.5	07.8	51.4	08.2	51.3	08.7	56
57	51.7	05.6	51.7	06.0	51.6	06.9	51.5	07.9	51.4	08.4	51.3	08.9	57
58	51.7	05.7	51.7	06.1	51.6	07.1	51.4	08.1	51.4	08.5	51.3	09.1	58
59	51.7	05.8	51.7	06.2	51.6	07.2	51.4	08.2	51.4	08.7	51.3	09.2	59
60	51.7	05.9	51.7	06.3	51.6	07.3	51.4	08.3	51.3	08.8	51.3	09.4	60
61	51.7	06.0	51.7	06.4	51.6	07.4	51.4	08.4	51.3	08.9	51.2	09.5	61
62	51.7	06.1	51.7	06.5	51.6	07.6	51.4	08.6	51.3	09.1	51.2	09.7	62
63	51.7	06.2	51.7	06.6	51.6	07.7	51.4	08.6	51.3	09.2	51.2	09.9	63
64	51.7	06.3	51.7	06.7	51.6	07.8	51.4	08.9	51.3	09.4	51.2	10.0	64
65	51.7	06.4	51.7	06.8	51.6	07.9	51.4	09.1	51.3	09.5	51.2	10.1	65
66	51.7	06.5	51.7	06.9	51.6	08.0	51.4	09.2	51.3	09.7	51.2	10.3	66
67	51.7	06.6	51.7	07.0	51.6	08.2	51.4	09.3	51.3	09.8	51.2	10.5	67
68	51.7	06.7	51.7	07.1	51.6	08.3	51.4	09.5	51.3	10.0	51.2	10.6	68
69	51.7	06.8	51.7	07.2	51.6	08.4	51.4	09.6	51.3	10.1	51.2	10.8	69
70	51.7	06.9	51.7	07.3	51.6	08.5	51.4	09.7	51.3	10.3	51.2	10.9	70
71	51.7	07.0	51.7	07.4	51.6	08.7	51.4	09.9	51.3	10.4	51.2	11.1	71
72	51.7	07.1	51.7	07.5	51.6	08.8	51.4	10.0	51.3	10.6	51.2	11.3	72
73	51.7	07.2	51.7	07.6	51.6	08.9	51.4	10.2	51.3	10.7	51.2	11.4	73
74	51.7	07.3	51.7	07.7	51.6	09.0	51.4	10.3	51.3	10.9	51.2	11.6	74
75	51.7	07.4	51.7	07.8	51.6	09.1	51.4	10.4	51.3	11.0	51.2	11.7	75
76	51.7	07.5	51.7	07.9	51.6	09.3	51.4	10.6	51.3	11.1	51.2	11.9	76
77	51.7	07.6	51.7	08.0	51.6	09.4	51.4	10.7	51.3	11.3	51.2	12.0	77
78	51.7	07.7	51.7	08.1	51.6	09.5	51.4	10.9	51.3	11.4	51.2	12.2	78
79	51.7	07.8	51.7	08.3	51.6	09.6	51.4	11.0	51.3	11.6	51.2	12.4	79
80	51.7	07.9	51.7	08.4	51.6	09.8	51.4	11.1	51.3	11.7	51.2	12.5	80
81	51.7	08.0	51.7	08.5	51.6	09.9	51.4	11.3	51.3	11.9	51.2	12.7	81
82	51.7	08.1	51.7	08.6	51.6	10.0	51.4	11.4	51.3	12.0	51.2	12.8	82
83	51.7	08.2	51.7	08.7	51.6	10.1	51.4	11.5	51.3	12.1	51.2	13.0	83
84	51.7	08.3	51.7	08.8	51.6	10.2	51.4	11.7	51.3	12.3	51.2	13.1	84
85	51.7	08.4	51.7	08.9	51.6	10.3	51.4	11.8	51.3	12.5	51.2	13.3	85
86	51.7	08.5	51.7	09.0	51.6	10.4	51.4	12.1	51.3	12.6	51.2	13.4	86
87	51.7	08.6	51.7	09.1	51.6	10.5	51.4	12.1	51.3	12.8	51.2	13.6	87
88	51.7	08.7	51.7	09.2	51.6	10.7	51.4	12.2	51.3	12.9	51.2	13.8	88
89	51.7	08.8	51.7	09.3	51.6	10.9	51.4	12.4	51.3	13.1	51.2	13.9	89
90	51.7	08.9	51.7	09.4	51.6	11.0	51.4	12.5	51.3	13.2	51.2	14.1	90
91	51.7	09.0	51.7	09.5	51.6	11.1	51.4	12.7	51.3	13.4	51.2	14.2	91
92	51.7	09.1	51.7	09.6	51.6	11.2	51.4	12.8	51.3	13.5	51.2	14.4	92
93	51.7	09.2	51.7	09.7	51.6	11.3	51.4	12.9	51.3	13.6	51.2	14.5	93
94	51.7	09.3	51.7	09.8	51.6	11.5	51.4	13.1	51.3	13.8	51.2	14.7	94
95	51.7	09.4	51.7	09.9	51.6	11.6	51.4	13.2	51.3	13.9	51.2	14.9	95
96	51.7	09.5	51.7	10.0	51.6	11.7	51.4	13.4	51.3	14.1	51.2	15.0	96
97	51.7	09.6	51.7	10.1	51.6	11.8	51.4	13.5	51.3	14.2	51.2	15.2	97
98	51.7	09.7	51.7	10.2	51.6	11.9	51.4	13.6	51.3	14.4	51.2	15.3	98
99	51.7	09.8	51.7	10.3	51.6	12.1	51.4	13.8	51.3	14.5	51.2	15.5	99
100	51.7	09.9	51.7	10.4	51.6	12.2	51.4	13.9	51.3	14.7	51.2	15.6	100
	De	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Diff.
	71 Point		84 Deg		83 Deg.		82 Deg.		74 Point		81 Deg		

of Latitude and Departure.

Diff.	10 Deg.		11 Deg.		12 Deg.		13 Deg.		14 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.3	1
2	02.0	00.3	02.0	00.4	02.0	00.4	02.0	00.4	02.0	00.5	2
3	03.0	00.5	03.0	00.6	03.0	00.6	03.0	00.7	03.0	00.7	3
4	04.0	00.7	04.0	00.8	04.0	00.8	04.0	00.9	04.0	01.0	4
5	05.0	00.9	05.0	01.1	05.0	01.1	05.0	01.2	05.0	01.2	5
6	06.0	01.2	06.0	01.3	06.0	01.4	06.0	01.5	06.0	01.6	6
7	07.0	01.4	07.0	01.5	07.0	01.6	07.0	01.7	07.0	01.8	7
8	08.0	01.6	08.0	01.7	08.0	01.8	08.0	01.9	08.0	02.0	8
9	09.0	01.7	09.0	01.9	09.0	02.1	09.0	02.2	09.0	02.3	9
10	10.0	01.9	10.0	02.1	10.0	02.3	10.0	02.4	10.0	02.5	10
11	11.0	02.1	11.0	02.3	11.0	02.5	11.0	02.7	11.0	02.9	11
12	12.0	02.3	12.0	02.5	12.0	02.7	12.0	02.9	12.0	03.1	12
13	13.0	02.4	13.0	02.7	13.0	02.9	13.0	03.1	13.0	03.3	13
14	14.0	02.6	14.0	02.9	14.0	03.1	14.0	03.4	14.0	03.6	14
15	15.0	02.8	15.0	03.0	15.0	03.3	15.0	03.6	15.0	03.9	15
16	16.0	02.9	16.0	03.2	16.0	03.5	16.0	03.8	16.0	04.1	16
17	17.0	03.1	17.0	03.4	17.0	03.7	17.0	04.0	17.0	04.4	17
18	18.0	03.3	18.0	03.6	18.0	03.9	18.0	04.2	18.0	04.6	18
19	19.0	03.5	19.0	03.8	19.0	04.1	19.0	04.4	19.0	04.8	19
20	20.0	03.6	20.0	04.0	20.0	04.3	20.0	04.6	20.0	04.9	20
21	21.0	03.8	21.0	04.2	21.0	04.5	21.0	04.8	21.0	05.1	21
22	22.0	04.0	22.0	04.4	22.0	04.7	22.0	05.0	22.0	05.3	22
23	23.0	04.2	23.0	04.6	23.0	04.9	23.0	05.2	23.0	05.5	23
24	24.0	04.3	24.0	04.8	24.0	05.1	24.0	05.4	24.0	05.7	24
25	25.0	04.5	25.0	05.0	25.0	05.3	25.0	05.6	25.0	05.9	25
26	26.0	04.7	26.0	05.1	26.0	05.4	26.0	05.7	26.0	06.0	26
27	27.0	04.9	27.0	05.3	27.0	05.6	27.0	05.9	27.0	06.2	27
28	28.0	05.0	28.0	05.5	28.0	05.8	28.0	06.1	28.0	06.4	28
29	29.0	05.2	29.0	05.7	29.0	06.0	29.0	06.3	29.0	06.6	29
30	30.0	05.4	30.0	05.9	30.0	06.2	30.0	06.5	30.0	06.8	30
31	31.0	05.5	31.0	06.1	31.0	06.4	31.0	06.7	31.0	07.0	31
32	32.0	05.7	32.0	06.3	32.0	06.6	32.0	06.9	32.0	07.2	32
33	33.0	05.9	33.0	06.5	33.0	06.8	33.0	07.1	33.0	07.4	33
34	34.0	06.1	34.0	06.7	34.0	07.0	34.0	07.3	34.0	07.6	34
35	35.0	06.3	35.0	06.9	35.0	07.2	35.0	07.5	35.0	07.8	35
36	36.0	06.4	36.0	07.1	36.0	07.4	36.0	07.7	36.0	08.0	36
37	37.0	06.6	37.0	07.3	37.0	07.6	37.0	07.9	37.0	08.2	37
38	38.0	06.8	38.0	07.4	38.0	07.8	38.0	08.1	38.0	08.4	38
39	39.0	06.9	39.0	07.6	39.0	08.0	39.0	08.3	39.0	08.6	39
40	40.0	07.1	40.0	07.8	40.0	08.2	40.0	08.5	40.0	08.8	40
41	41.0	07.3	41.0	08.0	41.0	08.4	41.0	08.7	41.0	09.0	41
42	42.0	07.5	42.0	08.2	42.0	08.6	42.0	08.9	42.0	09.2	42
43	43.0	07.7	43.0	08.4	43.0	08.8	43.0	09.1	43.0	09.4	43
44	44.0	07.8	44.0	08.6	44.0	09.0	44.0	09.3	44.0	09.6	44
45	45.0	08.0	45.0	08.8	45.0	09.2	45.0	09.5	45.0	09.8	45
46	46.0	08.1	46.0	09.0	46.0	09.4	46.0	09.7	46.0	10.0	46
47	47.0	08.3	47.0	09.2	47.0	09.6	47.0	09.9	47.0	10.2	47
48	48.0	08.5	48.0	09.3	48.0	09.8	48.0	10.1	48.0	10.4	48
49	49.0	08.7	49.0	09.5	49.0	10.0	49.0	10.3	49.0	10.6	49
50	50.0		50.0		50.0		50.0		50.0		50
Diff.	80 Deg.	79 Deg.	78 Deg.	77 Deg.	76 Deg.						Diff.

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A Table of Difference

Diff.	10 Deg.		11 Deg.		1 Point		12 Deg.		13 Deg.		14 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	50.2	08.8	50.1	09.7	50.0	10.0	50.0	10.0	49.7	11.5	49.5	13.3	51
52	51.1	09.0	51.0	09.9	51.0	10.1	50.9	11.1	50.7	11.7	50.5	12.8	52
53	52.1	09.2	52.0	10.1	52.0	10.3	51.8	11.3	51.6	11.9	51.4	12.8	53
54	53.1	09.4	53.0	10.3	53.0	10.5	52.8	11.5	52.6	12.1	52.4	13.1	54
55	54.2	09.5	54.0	10.5	54.0	10.7	53.8	11.7	53.6	12.4	53.4	13.3	55
56	55.1	09.7	55.0	10.7	54.9	10.9	54.8	11.6	54.5	12.6	54.3	13.5	56
57	56.1	09.9	56.0	10.8	55.9	11.1	55.8	11.8	55.5	12.8	55.3	13.8	57
58	57.1	10.1	57.0	11.1	56.9	11.3	56.7	12.1	56.5	13.0	56.3	14.0	58
59	58.1	10.2	57.9	11.3	57.9	11.5	57.7	12.3	57.5	13.3	57.2	14.3	59
60	59.1	10.4	58.9	11.4	58.8	11.7	58.7	12.5	58.5	13.5	58.2	14.5	60
61	60.1	10.6	59.9	11.6	59.8	11.9	59.7	12.7	59.4	13.7	59.2	14.8	61
62	61.1	10.8	60.9	11.8	60.8	12.1	60.6	12.9	60.4	13.9	60.2	15.0	62
63	62.0	10.9	61.8	12.0	61.8	12.3	61.6	13.1	61.4	14.2	61.1	15.2	63
64	63.0	11.1	62.8	12.2	62.8	12.5	62.6	13.3	62.3	14.4	62.1	15.5	64
65	64.0	11.3	63.8	12.4	63.7	12.7	63.6	13.5	63.3	14.6	63.1	15.7	65
66	65.0	11.5	64.8	12.6	64.7	12.9	64.6	13.7	64.3	14.8	64.0	16.0	66
67	66.0	11.6	65.8	12.8	65.7	13.1	65.5	13.9	65.3	15.1	65.0	16.2	67
68	67.0	11.8	66.7	13.0	66.7	13.3	66.5	14.1	66.2	15.3	66.0	16.4	68
69	68.0	12.0	67.7	13.2	67.7	13.5	67.5	14.3	67.2	15.5	66.9	16.7	69
70	68.9	12.2	68.7	13.4	68.7	13.7	68.5	14.5	68.2	15.7	67.9	16.9	70
71	69.9	12.3	69.7	13.5	69.6	13.9	69.4	14.8	69.1	16.0	68.9	17.2	71
72	70.9	12.5	70.7	13.7	70.6	14.0	70.4	15.0	70.1	16.2	69.9	17.4	72
73	71.9	12.7	71.7	13.9	71.6	14.0	71.4	15.2	71.1	16.4	70.8	17.6	73
74	72.9	12.8	72.6	14.1	72.6	14.4	72.4	15.4	72.1	16.6	71.8	17.9	74
75	73.9	13.0	73.6	14.3	73.6	14.6	73.4	15.6	73.1	16.9	72.8	18.1	75
76	74.8	13.2	74.6	14.5	74.5	14.8	74.3	15.8	74.0	17.1	73.7	18.4	76
77	75.8	13.4	75.6	14.7	75.5	15.0	75.3	16.0	75.0	17.3	74.7	18.6	77
78	76.8	13.5	76.6	14.9	76.5	15.2	76.3	16.2	76.0	17.5	75.7	18.9	78
79	77.8	13.7	77.5	15.1	77.5	15.4	77.3	16.4	77.0	17.8	76.6	19.1	79
80	78.8	13.9	78.5	15.3	78.5	15.6	78.2	16.6	77.9	18.0	77.6	19.3	80
81	79.8	14.1	79.5	15.5	79.4	15.8	79.2	16.8	78.9	18.2	78.6	19.4	81
82	80.8	14.2	80.5	15.6	80.4	16.0	80.2	17.0	79.9	18.4	79.6	19.8	82
83	81.7	14.4	81.5	15.8	81.4	16.2	81.2	17.2	80.9	18.7	80.5	20.1	83
84	82.7	14.6	82.5	16.0	82.4	16.4	82.2	17.5	81.8	18.9	81.5	20.3	84
85	83.7	14.8	83.1	16.2	83.4	16.6	83.1	17.7	82.8	19.1	82.5	20.6	85
86	84.7	14.9	84.4	16.4	84.3	16.8	84.1	17.8	83.8	19.3	83.4	20.9	86
87	85.7	15.2	85.4	16.6	85.3	17.0	85.1	18.1	84.8	19.6	84.4	21.2	87
88	86.7	15.3	86.4	16.8	86.3	17.2	86.1	18.3	85.7	19.8	85.4	21.5	88
89	87.6	15.4	87.4	17.0	87.3	17.4	87.1	18.5	86.7	20.0	86.4	21.7	89
90	88.6	15.6	88.1	17.2	88.3	17.6	88.0	18.7	87.7	20.2	87.3	21.9	90
91	89.6	15.8	89.3	17.4	89.2	17.8	89.0	18.9	88.7	20.5	88.3	22.0	91
92	90.6	16.0	90.3	17.6	90.2	17.9	90.0	19.1	89.6	20.7	89.3	22.2	92
93	91.6	16.1	91.3	17.7	91.2	18.1	91.0	19.3	90.6	20.9	90.2	22.5	93
94	92.6	16.3	92.3	17.9	92.2	18.3	91.9	19.5	91.6	21.1	91.2	22.7	94
95	93.5	16.5	93.3	18.1	93.2	18.5	92.9	19.7	92.6	21.4	92.2	23.0	95
96	94.5	16.7	94.2	18.3	94.2	18.7	93.9	20.0	93.5	21.6	93.1	23.2	96
97	95.5	16.8	95.2	18.5	95.1	18.9	94.9	20.2	94.5	21.8	94.1	23.5	97
98	96.5	17.0	96.2	18.7	96.1	19.1	95.9	20.4	95.5	22.0	95.1	23.7	98
99	97.5	17.2	97.2	18.9	97.1	19.3	96.8	20.6	96.5	22.3	96.1	24.0	99
100	98.5	17.4	98.2	19.1	98.1	19.5	97.8	20.8	97.4	22.5	97.0	24.2	100
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	80 Deg.		79 Deg.		7 Points		78 Deg.		77 Deg.		76 Deg.		

of Latitude and Departure.

Dist.	1 st Point		15 Deg.		16 Deg.		1 st Point		17 Deg.		18 Deg.		Dist.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.3	01.0	00.3	00.9	00.3	1
2	01.9	00.5	01.9	00.5	01.9	00.5	01.9	00.5	01.9	00.6	01.9	00.1	2
3	02.9	00.7	02.9	00.8	02.9	00.8	02.9	00.9	02.9	00.9	02.8	00.9	3
4	03.9	01.0	03.9	01.0	03.8	01.1	03.8	01.2	03.8	01.2	03.8	01.2	4
5	04.8	01.2	04.8	01.3	04.8	01.4	04.8	01.5	04.8	01.5	04.8	01.5	5
6	05.8	01.5	05.8	01.5	05.8	01.6	05.8	01.7	05.7	01.7	05.7	01.8	6
7	06.8	01.7	06.8	01.8	06.8	01.9	06.8	02.0	06.7	02.0	06.7	02.2	7
8	07.8	01.9	07.7	02.1	07.7	02.2	07.7	02.3	07.6	02.3	07.6	02.5	8
9	08.7	02.2	08.7	02.3	08.6	02.5	08.6	02.6	08.6	02.6	08.6	02.8	9
10	09.7	02.4	09.7	02.6	09.6	02.8	09.6	02.9	09.6	02.9	09.5	03.1	10
11	10.7	02.8	10.6	02.8	10.6	03.0	10.5	03.2	10.5	03.2	10.5	03.4	11
12	11.6	02.9	11.6	03.1	11.5	03.3	11.5	03.5	11.5	03.5	11.4	03.7	12
13	12.6	03.2	12.6	03.4	12.5	03.6	12.4	03.8	12.4	03.8	12.4	04.0	13
14	13.6	03.4	13.5	03.6	13.5	03.9	13.4	04.1	13.4	04.1	13.3	04.3	14
15	14.5	03.6	14.5	03.9	14.4	04.1	14.4	04.4	14.3	04.4	14.3	04.6	15
16	15.5	04.0	15.5	04.1	15.4	04.4	15.3	04.6	15.3	04.7	15.2	04.9	16
17	16.5	04.1	16.4	04.4	16.3	04.7	16.3	04.9	16.3	05.0	16.2	05.2	17
18	17.5	04.4	17.4	04.7	17.3	05.0	17.2	05.2	17.2	05.3	17.1	05.6	18
19	18.4	04.6	18.4	04.9	18.3	05.2	18.2	05.5	18.2	05.5	18.1	05.9	19
20	19.4	04.9	19.3	05.2	19.2	05.5	19.1	05.8	19.1	05.8	19.0	06.2	20
21	20.4	05.1	20.3	05.4	20.2	05.8	20.1	06.1	20.1	06.1	20.0	06.5	21
22	21.3	05.3	21.2	05.7	21.1	06.1	21.0	06.4	21.0	06.4	20.9	06.8	22
23	22.3	05.6	22.2	06.0	22.1	06.3	22.0	06.7	22.0	06.7	21.9	07.1	23
24	23.3	05.8	23.2	06.2	23.1	06.6	23.0	06.8	22.9	07.0	22.8	07.4	24
25	24.3	06.0	24.1	06.5	24.0	06.9	23.9	07.1	23.9	07.1	23.8	07.7	25
26	25.2	06.3	25.1	06.7	24.9	07.2	24.9	07.5	24.9	07.6	24.7	08.0	26
27	26.2	06.6	26.1	07.0	25.9	07.4	25.8	07.8	25.8	07.9	25.7	08.3	27
28	27.2	06.8	27.0	07.2	26.9	07.7	26.8	08.1	26.8	08.2	26.6	08.6	28
29	28.1	07.0	28.0	07.5	27.8	08.0	27.8	08.4	27.7	08.5	27.6	09.0	29
30	29.1	07.3	29.0	07.8	28.8	08.3	28.7	08.7	28.7	08.8	28.5	09.3	30
31	30.1	07.5	29.9	08.0	29.8	08.5	29.7	09.0	29.6	09.1	29.5	09.6	31
32	31.0	07.9	30.9	08.3	30.7	08.8	30.6	09.3	30.6	09.3	30.4	10.0	32
33	32.0	08.0	31.9	08.5	31.7	09.1	31.6	09.6	31.6	09.6	31.4	10.2	33
34	33.0	08.3	32.8	08.8	32.7	09.4	32.5	09.9	32.5	09.9	32.3	10.6	34
35	34.0	08.5	33.8	09.0	33.6	09.6	33.5	10.2	33.5	10.2	33.3	10.8	35
36	34.9	08.7	34.8	09.3	34.6	09.9	34.4	10.4	34.4	10.3	34.2	11.1	36
37	35.9	09.0	35.7	09.6	35.6	10.2	35.4	10.7	35.4	10.8	35.2	11.4	37
38	36.9	09.2	36.7	09.8	36.5	10.5	36.4	11.0	36.3	11.1	36.1	11.7	38
39	37.8	09.5	37.7	10.1	37.5	10.7	37.3	11.3	37.3	11.4	37.1	12.0	39
40	38.8	09.7	38.6	10.2	38.4	11.0	38.3	11.6	38.2	11.7	38.0	12.4	40
41	39.8	10.0	39.6	10.6	39.4	11.3	39.2	11.9	39.2	12.0	39.0	12.7	41
42	40.7	10.2	40.6	10.9	40.4	11.0	40.2	12.2	40.2	12.3	39.9	13.0	42
43	41.7	10.4	41.5	11.1	41.3	11.8	41.1	12.5	41.1	12.6	40.9	13.3	43
44	42.7	10.7	42.5	11.5	42.3	12.1	42.1	12.8	42.1	12.9	41.8	13.6	44
45	42.6	10.0	43.5	11.6	43.2	12.4	43.1	13.1	43.0	13.1	42.8	13.9	45
46	44.6	11.2	44.4	11.9	44.2	12.7	44.0	13.3	44.0	13.4	43.7	14.2	46
47	45.6	11.4	45.4	12.2	45.2	12.9	45.0	13.6	44.9	13.7	44.7	14.5	47
48	46.6	11.7	46.4	12.4	46.1	13.2	45.9	13.9	45.9	14.0	45.6	14.8	48
49	47.5	11.9	47.3	12.7	47.1	13.5	46.9	14.2	46.9	14.3	46.6	15.1	49
50	48.5	12.1	48.3	12.9	48.1	13.8	47.8	14.5	47.8	14.6	47.5	15.4	50
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	6 ¹ / ₄ Point	75 Deg.	74 Deg.	6 ¹ / ₄ Point	73 Deg.	72 Deg.							

A Table of Difference

Diff.	1 1/2 Point		15 Deg.		16 Deg.		1 1/2 Points		17 Deg.		18 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	49.3	12.4	49.3	13.2	49.0	14.0	48.8	14.8	48.8	14.9	48.3	15.8	51
52	50.4	12.6	50.2	13.5	49.0	14.3	49.7	15.1	49.7	15.2	49.4	16.1	52
53	51.4	12.9	51.2	13.7	50.9	14.6	50.7	15.3	50.7	15.3	50.4	16.4	53
54	52.4	13.1	52.2	14.0	51.9	14.9	51.7	15.7	51.6	15.8	51.3	16.7	54
55	53.3	13.1	53.1	14.2	52.9	15.2	52.6	16.0	52.6	16.1	52.3	17.0	55
56	54.3	13.6	54.1	14.5	53.8	15.4	53.6	16.2	53.5	16.4	53.3	17.3	56
57	55.3	13.8	55.1	14.8	54.8	15.7	54.5	16.5	54.5	16.7	54.2	17.6	57
58	56.3	14.1	56.0	15.0	55.7	16.0	55.5	16.8	55.5	17.0	55.2	17.9	58
59	57.2	14.3	57.0	15.3	56.7	16.3	56.5	17.1	56.4	17.2	56.1	18.2	59
60	58.2	14.6	58.0	15.5	57.7	16.5	57.4	17.4	57.4	17.5	57.1	18.5	60
61	59.2	14.8	58.9	15.8	58.6	16.8	58.4	17.7	58.3	17.8	58.0	18.8	61
62	60.1	15.1	59.9	16.1	59.6	17.1	59.3	18.0	59.3	18.1	59.0	19.2	62
63	61.1	15.3	60.8	16.3	60.5	17.4	60.3	18.3	60.2	18.4	59.9	19.5	63
64	62.1	15.5	61.8	16.6	61.5	17.6	61.2	18.6	61.2	18.7	60.9	19.8	64
65	63.0	15.8	62.8	16.8	62.5	17.9	62.2	18.9	62.2	19.0	61.8	20.1	65
66	64.0	16.0	63.7	17.1	63.4	18.2	63.2	19.2	63.1	19.3	62.8	20.4	66
67	65.0	16.3	64.7	17.4	64.4	18.5	64.1	19.4	64.1	19.6	63.7	20.7	67
68	66.0	16.5	65.7	17.6	65.4	18.7	65.1	19.7	65.0	19.9	64.7	21.0	68
69	66.9	16.8	66.6	17.9	66.3	19.0	66.0	20.0	66.0	20.2	65.6	21.3	69
70	67.9	17.0	67.6	18.1	67.3	19.3	67.0	20.3	66.9	20.5	66.6	21.6	70
71	68.9	17.2	68.6	18.3	68.3	19.6	67.9	20.6	67.9	20.8	67.5	21.9	71
72	69.8	17.5	69.5	18.6	69.2	19.8	68.9	20.9	68.8	21.0	68.4	22.2	72
73	70.8	17.7	70.5	18.9	70.2	20.1	69.8	21.2	69.8	21.3	69.4	22.6	73
74	71.8	18.0	71.5	19.1	71.1	20.4	70.8	21.5	70.8	21.6	70.4	22.9	74
75	72.7	18.2	72.4	19.4	72.1	20.7	71.8	21.8	71.7	21.9	71.3	23.2	75
76	73.7	18.5	73.4	19.7	73.0	20.9	72.7	22.1	72.7	22.2	72.3	23.5	76
77	74.7	18.7	74.4	19.9	74.0	21.2	73.7	22.3	73.6	22.5	73.2	23.8	77
78	75.7	18.9	75.3	20.2	75.0	21.5	74.6	22.6	74.6	22.8	74.2	24.1	78
79	76.6	19.2	76.3	20.4	75.9	21.8	75.6	22.9	75.5	23.1	75.1	24.4	79
80	77.6	19.4	77.3	20.7	76.9	22.0	76.6	23.2	76.5	23.4	76.1	24.7	80
81	78.6	19.7	77.2	21.0	77.9	22.3	77.5	23.5	77.5	23.7	77.0	25.0	81
82	79.5	19.9	79.2	21.2	78.8	22.6	78.5	23.8	78.4	24.0	78.0	25.3	82
83	80.5	20.3	80.2	21.5	79.8	22.9	79.4	24.1	79.4	24.3	78.9	25.6	83
84	81.5	20.4	81.1	21.7	80.8	23.1	80.4	24.4	80.3	24.5	79.9	26.0	84
85	82.4	20.7	82.1	22.0	81.7	23.4	81.3	24.7	81.3	24.8	80.8	26.3	85
86	83.4	20.9	83.1	22.3	82.7	23.7	82.3	25.0	82.3	25.1	81.8	26.6	86
87	84.4	21.1	84.0	22.5	83.6	24.0	83.3	25.2	83.2	25.4	82.7	26.9	87
88	85.4	21.4	85.0	22.8	84.6	24.2	84.2	25.5	84.1	25.7	83.7	27.2	88
89	86.3	21.6	86.0	23.0	85.6	24.5	85.2	25.8	85.1	26.0	84.6	27.5	89
90	87.3	21.9	86.9	23.3	86.5	24.8	86.1	26.1	86.1	26.3	85.6	27.8	90
91	88.3	22.1	87.9	23.5	87.5	25.1	87.1	26.4	87.0	26.6	86.5	28.1	91
92	89.2	22.4	88.9	23.8	88.4	25.3	88.0	26.7	88.0	26.9	87.5	28.4	92
93	90.2	22.6	89.8	24.1	89.4	25.6	89.0	27.0	88.9	27.2	88.4	28.7	93
94	91.2	22.8	90.8	24.3	90.4	25.9	90.0	27.3	89.9	27.5	89.4	29.0	94
95	92.1	23.1	91.8	24.6	91.3	26.2	90.9	27.6	90.8	27.8	90.3	29.3	95
96	93.1	23.3	92.7	24.8	92.3	26.4	91.9	27.9	91.8	28.1	91.3	29.7	96
97	94.1	23.6	93.7	25.1	93.2	26.7	92.8	28.2	92.8	28.4	92.3	30.0	97
98	95.2	23.8	94.7	25.4	94.2	27.0	93.8	28.4	93.7	28.6	93.2	30.3	98
99	96.0	24.1	95.6	25.6	95.2	27.3	94.7	28.7	94.7	28.9	94.2	30.6	99
100	97.0	24.3	96.6	25.9	96.1	27.6	95.7	29.0	95.6	29.2	95.1	30.9	100
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
	6 1/2 Point		75 Deg.		74 Deg.		6 1/2 Points		73 Deg.		72 Deg.		

of Latitude and Departure.

Diff.	19 Deg.		20 Deg.		21 Deg.		22 Deg.		2 Points		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	00.9	00.3	00.9	00.3	00.9	00.4	00.9	00.4	00.9	00.4	1
2	01.9	00.6	01.9	00.7	01.9	00.7	01.9	00.7	01.9	00.8	2
3	02.8	01.0	02.8	01.0	02.8	01.1	02.8	01.1	02.8	01.1	3
4	03.8	01.3	03.8	01.3	03.8	01.4	03.7	01.5	03.7	01.5	4
5	04.7	01.6	04.7	01.7	04.7	01.7	04.6	01.9	04.6	01.9	5
6	05.7	01.9	05.6	02.0	05.6	02.1	05.6	02.1	05.5	02.3	6
7	06.6	02.3	06.6	02.4	06.5	02.5	06.5	02.6	06.5	02.7	7
8	07.6	02.6	07.5	02.7	07.5	02.9	07.4	03.0	07.4	03.1	8
9	08.5	02.9	08.5	03.0	08.5	03.1	08.4	03.2	08.4	03.4	9
10	09.5	03.3	09.4	03.4	09.4	03.4	09.3	03.5	09.3	03.7	10
11	10.4	03.6	10.4	03.7	10.3	03.9	10.2	04.1	10.2	04.3	11
12	11.3	03.9	11.3	04.0	11.3	04.1	11.1	04.5	11.1	04.6	12
13	12.3	04.2	12.2	04.4	12.1	04.7	12.0	04.9	12.0	05.0	13
14	13.2	04.6	13.2	04.7	13.1	05.0	13.0	05.2	12.9	05.4	14
15	14.2	04.9	14.1	05.1	14.0	05.4	13.9	05.6	13.9	05.7	15
16	15.1	05.3	15.1	05.4	14.9	05.7	14.8	06.0	14.8	06.1	16
17	16.1	05.5	16.0	05.7	15.9	06.1	15.8	06.4	15.7	06.5	17
18	17.0	05.9	16.9	06.1	16.8	06.4	16.7	06.7	16.6	06.8	18
19	18.0	06.1	17.9	06.4	17.7	06.8	17.6	07.1	17.6	07.3	19
20	18.9	06.5	18.9	06.7	18.8	07.2	18.7	07.5	18.7	07.6	20
21	19.9	06.8	19.8	07.1	19.7	07.5	19.6	07.9	19.6	08.0	21
22	20.8	07.2	20.7	07.4	20.7	07.9	20.6	08.3	20.6	08.4	22
23	21.7	07.5	21.7	07.7	21.6	08.2	21.5	08.6	21.5	08.8	23
24	22.7	07.8	22.6	08.1	22.5	08.5	22.4	08.9	22.4	09.2	24
25	23.6	08.1	23.5	08.5	23.5	08.9	23.4	09.3	23.4	09.6	25
26	24.6	08.5	24.5	08.8	24.4	09.2	24.3	09.7	24.3	09.9	26
27	25.5	08.8	25.4	09.1	25.4	09.6	25.3	10.0	25.3	10.3	27
28	26.5	09.1	26.4	09.4	26.3	09.9	26.2	10.5	26.2	10.7	28
29	27.4	09.4	27.3	09.8	27.2	10.3	27.1	10.9	27.1	11.1	29
30	28.4	09.8	28.3	10.1	28.2	10.7	28.1	11.2	28.1	11.5	30
31	29.3	10.1	29.2	10.4	29.1	11.1	29.0	11.6	29.0	11.9	31
32	30.3	10.4	30.2	10.8	30.1	11.5	30.0	12.0	30.0	12.3	32
33	31.3	10.7	31.2	11.1	31.1	11.8	31.0	12.4	31.0	12.6	33
34	32.1	11.1	32.0	11.5	31.9	12.2	31.8	12.7	31.8	13.0	34
35	33.1	11.4	33.0	11.8	32.9	12.5	32.8	13.1	32.8	13.4	35
36	34.0	11.7	33.9	12.1	33.8	12.9	33.7	13.5	33.7	13.8	36
37	35.0	12.1	34.8	12.5	34.8	13.3	34.7	13.9	34.7	14.2	37
38	35.9	12.4	35.8	12.8	35.7	13.6	35.6	14.2	35.6	14.5	38
39	36.9	12.6	36.7	13.1	36.6	13.9	36.5	14.6	36.5	14.9	39
40	37.8	13.0	37.7	13.5	37.6	14.3	37.5	15.0	37.5	15.3	40
41	38.8	13.3	38.6	13.8	38.5	14.7	38.4	15.3	38.4	15.7	41
42	39.7	13.7	39.5	14.1	39.5	15.1	39.4	15.7	39.4	16.1	42
43	40.7	14.0	40.5	14.5	40.4	15.4	40.3	16.1	40.3	16.5	43
44	41.6	14.3	41.4	14.8	41.3	15.8	41.2	16.5	41.2	16.8	44
45	42.6	14.6	42.4	15.2	42.3	16.1	42.2	16.8	42.2	17.2	45
46	43.5	15.0	43.3	15.5	43.2	16.5	43.1	17.2	43.1	17.6	46
47	44.4	15.3	44.2	15.8	44.1	16.8	44.0	17.6	44.0	18.0	47
48	45.4	15.6	45.2	16.2	45.1	17.2	45.0	18.0	45.0	18.4	48
49	46.3	15.9	46.1	16.5	46.0	17.6	45.9	18.3	45.9	18.7	49
50	47.3	16.3	47.1	16.8	47.0	17.9	46.9	18.7	46.9	19.1	50
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
	71 Deg.	64 Point		70 Deg.	69 Deg.	68 Deg.		6 Points			

Handwritten signature or mark.

Table of Difference

Mile.	19 Deg.		20 Deg.		21 Deg.		22 Deg.		2 Points		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	48.2	16.6	48.0	17.1	47.9	17.4	47.6	18.3	47.3	19.1	51
52	48.2	16.9	48.0	17.5	48.0	17.8	48.5	18.6	48.2	19.4	52
53	50.1	17.3	49.9	17.9	49.8	18.1	49.5	19.0	49.1	19.8	53
54	51.1	17.6	50.8	18.2	50.7	18.5	50.4	19.3	50.1	20.2	54
55	52.0	17.9	51.8	18.5	51.7	18.8	51.3	19.7	51.0	20.6	55
56	52.9	18.2	52.7	18.9	52.6	19.2	52.3	20.1	51.9	21.0	56
57	53.9	18.6	53.7	19.2	53.6	19.5	53.2	20.4	52.8	21.3	57
58	54.8	18.9	54.6	19.5	54.5	19.8	54.1	20.8	53.8	21.7	58
59	55.8	19.2	55.5	19.9	55.4	20.2	55.1	21.1	54.7	22.1	59
60	56.7	19.5	56.5	20.2	56.4	20.5	56.0	21.5	55.6	22.5	60
61	57.7	19.9	57.4	20.5	57.3	20.9	56.9	21.9	56.5	22.8	61
62	58.6	20.2	58.4	20.9	58.3	21.2	57.9	22.2	57.5	23.2	62
63	59.6	20.5	59.3	21.2	59.2	21.5	58.8	22.6	58.4	23.6	63
64	60.5	20.8	60.3	21.6	60.1	21.9	59.7	22.9	59.3	24.0	64
65	61.5	21.2	61.2	21.9	61.1	22.2	60.7	23.3	60.3	24.3	65
66	62.4	21.5	62.1	22.2	62.0	22.6	61.6	23.6	61.2	24.7	66
67	63.3	21.8	63.1	22.6	63.0	22.9	62.5	24.9	62.1	25.1	67
68	64.3	22.1	64.0	22.9	63.9	23.3	63.5	24.4	63.0	25.5	68
69	65.2	22.5	65.0	23.2	64.8	23.6	64.4	24.7	64.0	25.8	69
70	66.2	22.8	65.9	23.6	65.8	23.9	65.3	25.1	64.9	26.2	70
71	67.1	23.1	66.8	23.9	66.7	24.3	66.3	25.4	65.8	26.6	71
72	68.1	23.3	67.8	24.2	67.7	24.6	67.2	25.8	66.7	27.0	72
73	69.0	23.8	68.7	24.6	68.6	25.0	68.1	25.2	67.7	27.3	73
74	70.0	24.1	69.7	24.9	69.5	25.3	69.1	26.5	68.6	27.7	74
75	70.9	24.4	70.6	25.3	70.5	25.6	70.0	26.9	69.5	28.1	75
76	71.9	24.7	71.6	25.6	71.4	26.0	70.9	27.2	70.5	28.5	76
77	72.8	25.1	72.5	25.9	72.4	26.3	71.9	27.6	71.4	28.8	77
78	73.7	25.4	73.4	26.3	73.3	26.7	72.8	27.7	72.3	29.2	78
79	74.7	25.7	74.4	26.6	74.2	27.0	73.7	28.3	73.2	29.6	79
80	75.6	26.0	75.3	26.9	75.2	27.4	74.7	28.7	74.2	30.0	80
81	76.6	26.4	76.3	27.3	76.1	27.7	75.6	29.0	75.1	30.3	81
82	77.5	26.7	77.2	27.6	77.1	28.0	76.5	29.4	76.0	30.7	82
83	78.5	27.0	78.1	28.0	78.0	28.4	77.5	29.7	76.9	31.1	83
84	79.4	27.3	79.1	28.3	78.9	28.7	78.4	30.1	77.9	31.5	84
85	80.4	27.7	80.1	28.6	79.9	29.1	79.3	30.5	78.7	31.8	85
86	81.3	28.0	81.0	29.0	80.8	29.4	80.3	30.8	79.7	32.2	86
87	82.3	28.3	81.9	29.3	81.8	29.7	81.2	31.2	80.7	32.6	87
88	83.2	28.6	82.0	29.6	82.7	30.1	82.1	31.5	81.6	33.0	88
89	84.1	29.0	83.8	30.0	83.6	30.4	83.1	31.9	82.5	33.4	89
90	85.1	29.3	84.7	30.3	84.6	30.8	84.0	32.3	83.4	33.7	90
91	86.0	29.6	85.7	30.7	85.5	31.1	84.9	32.6	84.4	34.1	91
92	87.0	29.9	86.6	31.0	86.4	31.5	85.7	33.0	85.3	34.5	92
93	88.0	30.3	87.6	31.3	87.4	31.8	86.3	33.3	86.2	34.8	93
94	88.9	30.6	88.5	31.7	88.3	32.1	87.7	33.7	87.2	35.2	94
95	89.8	30.9	89.4	32.0	89.3	32.5	88.7	34.0	88.1	35.6	95
96	90.8	31.3	90.1	32.3	90.2	32.8	89.6	34.4	89.0	35.9	96
97	91.7	31.6	91.3	32.7	91.1	33.2	90.5	34.8	89.9	36.3	97
98	92.7	31.9	92.3	33.0	92.1	33.5	91.5	35.1	90.9	36.7	98
99	93.6	32.2	93.2	33.3	93.0	33.9	92.4	35.5	91.7	37.1	99
100	94.5	32.6	94.1	33.7	94.0	34.2	93.4	35.8	92.7	37.5	100
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
	71 Deg.		64 Point		70 Deg.		69 Deg.		68 Deg.		6 Points

of Latitude and Departure.

Diff.	23 Deg.	24 Deg.	25 Deg.	2 1/2 Point	26 Deg.	27 Deg.	Diff.
	Lat. Dep	Lat. Dep	Lat. Dep	Lat. Dep	Lat. Dep	Lat. Dep	
1	00.9 00.4	00.9 00.4	00.9 00.4	00.9 00.4	00.9 00.4	00.9 00.4	1
2	01.8 00.8	01.8 00.8	01.8 00.8	01.8 00.8	01.8 00.8	01.8 00.8	2
3	02.8 01.2	02.7 01.2	02.7 01.2	02.7 01.2	02.7 01.2	02.7 01.2	3
4	03.7 01.6	03.6 01.6	03.6 01.7	03.6 01.7	03.6 01.7	03.6 01.8	4
5	04.6 01.9	04.6 02.0	04.5 02.1	04.5 02.1	04.5 02.2	04.5 02.3	5
6	05.5 02.3	05.5 02.4	05.4 02.5	05.4 02.6	05.4 02.6	05.3 02.7	6
7	06.4 02.7	06.4 02.8	06.3 03.0	06.3 03.0	06.3 03.1	06.2 03.2	7
8	07.4 03.1	07.3 03.2	07.2 03.4	07.2 03.4	07.2 03.5	07.1 03.6	8
9	08.3 03.5	08.2 03.7	08.2 03.8	08.1 03.8	08.1 03.9	08.0 04.1	9
10	09.2 03.9	09.1 04.1	09.1 04.2	09.0 04.3	09.0 04.4	08.9 04.5	10
11	10.1 04.3	10.0 04.5	10.0 04.6	09.9 04.7	09.9 04.8	09.8 05.0	11
12	11.0 04.7	11.0 04.9	10.9 05.1	10.8 05.1	10.8 05.3	10.7 05.4	12
13	12.0 05.1	11.9 05.3	11.8 05.5	11.7 05.6	11.7 05.7	11.6 05.8	13
14	12.9 05.5	12.8 05.7	12.7 05.9	12.7 05.9	12.6 06.1	12.5 06.4	14
15	13.8 05.9	13.7 06.1	13.6 06.3	13.6 06.4	13.5 06.6	13.4 06.8	15
16	14.7 06.2	14.6 06.5	14.5 06.8	14.5 06.6	14.4 07.0	14.3 07.3	16
17	15.6 06.6	15.5 06.9	15.4 07.2	15.4 07.3	15.3 07.4	15.1 07.7	17
18	16.6 07.0	16.4 07.3	16.3 07.5	16.3 07.7	16.2 07.9	16.0 08.2	18
19	17.5 07.4	17.4 07.7	17.3 08.0	17.2 08.1	17.1 08.3	16.9 08.6	19
20	18.4 07.8	18.3 08.1	18.1 08.4	18.1 08.5	18.0 08.8	17.8 09.1	20
21	19.3 08.2	19.2 08.5	19.0 08.9	19.0 09.0	18.9 09.2	18.7 09.5	21
22	20.2 08.6	20.1 08.9	19.9 09.3	19.9 09.4	19.8 09.9	19.6 10.0	22
23	21.2 09.0	21.0 09.3	20.8 09.7	20.8 09.8	20.7 10.1	20.5 10.4	23
24	22.1 09.4	21.9 09.8	21.7 10.1	21.7 10.3	21.6 10.5	21.4 10.9	24
25	23.0 09.8	22.8 10.2	22.7 10.6	22.6 10.7	22.5 11.0	22.3 11.3	25
26	23.9 10.2	23.7 10.6	23.6 11.0	23.5 11.1	23.4 11.4	23.2 11.8	26
27	24.8 10.5	24.7 11.0	24.5 11.4	24.4 11.5	24.3 11.8	24.1 12.3	27
28	25.8 10.9	25.6 11.4	25.4 11.8	25.3 12.0	25.2 12.3	24.9 12.7	28
29	26.7 11.3	26.5 11.8	26.3 12.2	26.2 12.4	26.1 12.7	25.8 13.2	29
30	27.6 11.7	27.4 12.2	27.2 12.7	27.1 12.8	27.0 13.1	26.7 13.6	30
31	28.5 12.1	28.3 12.6	28.1 13.1	28.0 13.3	27.9 13.6	27.6 14.1	31
32	29.5 12.5	29.2 13.0	29.0 13.5	28.9 13.7	28.8 14.0	28.5 14.5	32
33	30.4 12.9	30.1 13.4	29.9 13.9	29.8 14.1	29.6 14.4	29.4 15.0	33
34	31.3 13.3	31.1 13.8	30.8 14.4	30.7 14.5	30.6 14.9	30.3 15.4	34
35	32.2 13.7	32.0 14.2	31.7 14.8	31.6 15.0	31.5 15.3	31.2 15.9	35
36	33.1 14.1	32.9 14.6	32.6 15.2	32.5 15.4	32.4 15.8	32.1 16.3	36
37	34.1 14.4	33.8 15.0	33.5 15.6	33.4 15.8	33.2 16.2	33.0 16.8	37
38	35.0 14.8	34.7 15.4	34.4 16.0	34.3 16.2	34.1 16.6	33.9 17.2	38
39	35.9 15.2	35.6 15.9	35.3 16.5	35.3 16.7	35.0 17.1	34.7 17.7	39
40	36.8 15.6	36.5 16.3	36.2 16.9	36.2 17.1	35.9 17.5	35.6 18.2	40
41	37.7 16.0	37.4 16.7	37.2 17.3	37.1 17.5	36.8 18.0	36.5 18.6	41
42	38.7 16.4	38.4 17.1	38.1 17.7	38.0 18.0	37.7 18.4	37.4 19.1	42
43	39.6 16.8	39.3 17.5	39.0 18.2	38.9 18.4	38.6 18.8	38.3 19.5	43
44	40.5 17.2	40.2 17.9	39.9 18.6	39.8 18.8	39.5 19.3	39.2 20.0	44
45	41.4 17.6	41.1 18.3	40.8 19.0	40.7 19.2	40.4 19.7	40.1 20.4	45
46	42.3 18.0	42.0 18.7	41.7 19.4	41.6 19.7	41.3 20.2	41.0 20.9	46
47	43.3 18.4	42.9 19.1	42.6 19.9	42.5 20.1	42.2 20.6	41.9 21.3	47
48	44.2 18.8	43.8 19.5	43.5 20.3	43.4 20.5	43.1 21.0	42.8 21.8	48
49	45.1 19.2	44.8 19.9	44.4 20.7	44.3 20.9	44.0 21.5	43.7 22.3	49
50	46.0 19.5	45.7 20.3	45.3 21.1	45.2 21.4	44.9 21.9	44.5 22.7	50
Diff.	Dep Lat.	Dep Lat.	Dep Lat.	Dep Lat.	Dep Lat.	Dep Lat.	Diff.
	67 Deg.	66 Deg.	65 Deg.	5 1/2 Point	64 Deg.	63 Deg.	

A Table of Difference

Diff.	23 Deg.		24 Deg.		25 Deg.		24 Points		26 Deg.		27 Deg.		Diff.
	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	
51	46.9	19.9	46.6	20.7	46.2	21.3	46.1	21.8	45.8	22.3	45.4	23.2	51
52	47.9	20.3	47.5	21.1	47.1	22.0	47.0	22.2	46.7	22.8	46.3	23.6	52
53	48.8	20.7	48.4	21.5	48.0	22.4	47.9	22.7	47.6	23.2	47.2	24.1	53
54	49.7	21.1	49.3	22.0	48.9	22.8	48.8	23.1	47.5	23.7	48.1	24.5	54
55	50.6	21.5	50.2	22.4	49.8	23.2	49.7	23.5	48.4	24.1	49.0	24.9	55
56	51.5	21.9	51.1	22.8	50.7	23.7	50.6	23.9	50.3	24.5	49.6	25.4	56
57	52.5	22.3	52.1	23.2	51.7	24.1	51.5	24.4	51.2	25.0	50.8	25.9	57
58	53.4	22.7	53.0	23.6	52.6	24.5	52.4	24.8	52.1	25.4	51.7	26.3	58
59	54.3	23.0	53.9	24.0	53.5	24.9	53.3	25.2	53.0	26.9	52.6	26.8	59
60	55.2	23.4	54.8	24.4	54.4	25.4	54.2	25.6	53.9	26.3	53.5	27.2	60
61	56.1	23.8	55.7	24.8	55.3	25.8	55.1	26.1	54.8	26.7	54.4	27.7	61
62	57.1	24.2	56.6	25.2	56.2	26.2	56.0	26.5	55.7	27.1	55.2	28.1	62
63	58.0	24.6	57.5	25.6	57.1	26.6	56.9	26.9	56.6	27.6	56.1	28.6	63
64	58.9	25.0	58.5	26.0	58.0	27.0	57.9	27.4	57.5	28.0	57.0	29.5	64
65	59.8	25.4	59.4	26.4	58.9	27.5	58.8	27.8	58.4	28.5	57.9	29.1	65
66	60.7	25.8	60.3	26.8	59.8	27.9	59.7	28.2	59.3	28.9	58.8	30.0	66
67	61.7	26.2	61.2	27.2	60.7	28.3	60.6	28.6	60.2	29.4	59.7	30.4	67
68	62.6	26.6	62.1	27.7	61.6	28.7	61.5	29.1	61.1	29.8	60.6	30.9	68
69	63.5	27.0	63.0	28.1	62.5	29.2	62.4	29.5	62.0	30.2	61.5	31.3	69
70	64.4	27.3	63.9	28.5	63.4	29.6	63.3	29.9	62.9	30.7	62.4	31.8	70
71	65.4	27.7	64.9	28.9	64.3	30.0	64.2	30.4	63.8	31.1	63.3	32.2	71
72	66.3	28.1	65.8	29.3	65.2	30.4	65.1	30.8	64.7	31.6	64.2	32.7	72
73	67.2	28.5	66.7	29.7	66.1	30.8	66.0	31.2	65.6	32.0	65.0	33.1	73
74	68.1	28.9	67.6	30.1	67.1	31.3	66.9	31.6	66.5	32.4	65.9	33.6	74
75	69.0	29.3	68.5	30.5	68.0	31.7	67.8	32.1	67.4	32.9	66.8	34.1	75
76	70.0	29.7	69.4	30.9	68.9	32.1	68.7	32.5	68.3	33.3	67.7	34.5	76
77	70.9	30.1	70.3	31.3	69.8	32.5	69.6	32.9	69.2	33.7	68.6	35.0	77
78	71.8	30.5	71.2	31.7	70.7	33.0	70.5	33.3	70.1	34.2	69.5	35.4	78
79	72.7	30.9	72.1	32.1	71.6	33.4	71.4	33.8	71.0	34.6	70.4	35.9	79
80	73.6	31.3	73.1	32.5	72.5	33.8	72.3	34.2	71.9	35.1	71.3	36.3	80
81	74.6	31.6	74.0	32.9	73.4	34.2	73.2	34.6	72.8	35.5	72.2	36.8	81
82	75.5	32.0	74.9	33.3	74.3	34.7	74.1	35.1	73.7	35.9	73.1	37.2	82
83	76.4	32.4	75.8	33.8	75.2	35.1	75.0	35.5	74.6	36.4	74.2	37.7	83
84	77.3	32.8	76.7	34.2	76.1	35.5	75.9	35.9	75.5	36.8	74.8	38.1	84
85	78.2	33.2	77.6	34.6	77.0	35.9	76.8	36.3	76.4	37.3	75.7	38.6	85
86	79.2	33.6	78.6	35.0	77.9	36.3	77.7	36.8	77.3	37.7	76.6	39.0	86
87	80.1	34.0	79.5	35.4	78.8	36.8	78.6	37.2	78.2	38.1	77.5	39.5	87
88	81.0	34.4	80.4	35.8	79.7	37.2	79.5	37.6	79.1	38.6	78.4	40.0	88
89	81.9	34.8	81.3	36.2	80.7	37.6	80.5	38.1	80.0	39.0	79.3	40.4	89
90	82.8	35.2	82.2	36.6	81.6	38.0	81.4	38.5	80.9	39.4	80.2	40.9	90
91	83.7	35.6	83.1	37.0	82.5	38.5	82.3	38.9	81.8	39.8	81.1	41.3	91
92	84.7	35.9	84.0	37.4	83.4	38.9	83.2	39.3	82.7	40.3	82.0	41.8	92
93	85.6	36.3	85.0	37.8	84.3	39.3	84.1	39.8	83.6	40.8	82.9	42.2	93
94	86.5	36.7	85.9	38.2	85.2	39.7	85.0	40.2	84.5	41.2	83.8	42.7	94
95	87.4	37.1	86.8	38.6	86.1	40.1	85.9	40.6	85.4	41.6	84.6	43.1	95
96	88.4	37.5	87.7	39.0	87.0	40.6	86.8	41.0	86.3	42.1	85.5	43.6	96
97	89.3	37.9	88.6	39.4	87.9	41.0	87.7	41.5	87.2	42.5	86.4	44.0	97
98	90.2	38.3	89.5	39.9	88.8	41.4	88.6	41.9	88.1	43.0	87.3	44.5	98
99	91.1	38.7	90.4	40.3	89.7	41.8	89.5	42.3	89.0	43.4	88.2	44.9	99
100	92.0	39.1	91.4	40.7	90.6	42.3	90.4	42.7	89.9	43.5	89.1	45.4	100
Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.
67 Deg.		66 Deg.		65 Deg.		54 Points		64 Deg.		63 Deg.			

of Latitude and Departure.

Diff.	20 Deg.		2 ½ Point		29 Deg.		30 Deg.		2 ¼ Point		31 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	1
2	01.8	00.9	01.8	00.9	01.7	01.0	01.7	01.0	01.7	01.0	01.7	01.0	2
3	02.6	01.4	02.6	01.4	02.6	01.4	02.6	01.5	02.6	01.5	02.6	01.5	3
4	03.5	01.9	03.5	01.9	03.5	01.9	03.5	02.0	03.4	02.1	03.4	02.1	4
5	04.4	02.3	04.4	02.4	04.4	02.4	04.3	02.5	04.3	02.5	04.3	02.6	5
6	05.3	02.8	05.3	02.8	05.3	02.9	05.2	03.0	05.1	03.1	05.1	03.1	6
7	06.2	03.3	06.2	03.3	06.1	03.4	06.1	03.5	06.0	03.6	06.1	03.6	7
8	07.1	03.8	07.1	03.8	07.0	03.9	06.9	04.0	06.9	04.1	06.9	04.1	8
9	07.9	04.2	07.9	04.2	07.9	04.4	07.8	04.5	07.7	04.6	07.7	04.6	9
10	08.8	04.7	08.8	04.7	08.7	04.8	08.7	05.0	08.6	05.1	08.6	05.1	10
11	09.7	05.2	09.7	05.2	09.6	05.3	09.5	05.5	09.4	05.6	09.4	05.7	11
12	10.6	05.6	10.6	05.6	10.5	05.8	10.4	06.0	10.3	06.2	10.3	06.2	12
13	11.5	06.1	11.5	06.1	11.4	06.3	11.3	06.5	11.1	06.7	11.1	06.7	13
14	12.4	06.6	12.3	06.6	12.2	06.8	12.1	07.0	12.0	07.2	12.0	07.2	14
15	13.2	07.0	13.2	07.1	13.1	07.3	12.0	07.9	12.9	07.7	12.9	07.7	15
16	14.1	07.5	14.1	07.5	14.0	07.7	13.9	08.0	13.7	08.2	13.7	08.2	16
17	15.0	08.0	15.0	08.0	14.9	08.2	14.7	08.5	14.6	08.7	14.6	08.8	17
18	15.9	08.4	15.9	08.5	15.7	08.7	15.6	09.0	15.4	09.2	15.4	09.3	18
19	16.8	08.9	16.8	08.9	16.6	09.2	16.5	09.5	16.3	09.8	16.3	09.8	19
20	17.7	09.4	17.6	09.4	17.5	09.7	17.3	10.0	17.1	10.3	17.1	10.3	20
21	18.5	09.9	18.5	09.9	18.4	10.2	18.2	10.5	18.0	10.8	18.0	10.8	21
22	19.4	10.3	19.4	10.3	19.3	10.7	19.0	11.0	18.9	11.3	18.9	11.3	22
23	20.3	10.8	20.3	10.8	20.1	11.1	19.9	11.5	19.7	11.8	19.7	11.8	23
24	21.2	11.3	21.2	11.3	21.0	11.6	20.8	12.0	20.6	12.3	20.6	12.4	24
25	22.1	11.7	22.0	11.8	21.9	12.1	21.6	12.5	21.4	12.8	21.4	12.9	25
26	23.0	12.2	22.9	12.3	22.7	12.6	22.5	13.0	22.3	13.4	22.3	13.4	26
27	23.8	12.7	23.8	12.7	23.6	13.1	23.4	13.5	23.1	13.9	23.1	13.9	27
28	24.7	13.1	24.7	13.2	24.5	13.6	24.2	14.0	24.0	14.4	24.0	14.4	28
29	25.6	13.6	25.6	13.7	25.4	14.1	25.1	14.5	24.9	14.9	24.9	14.9	29
30	26.5	14.1	26.5	14.1	26.2	14.5	26.0	15.0	25.7	15.4	25.7	15.4	30
31	27.4	14.5	27.3	14.6	27.1	15.0	26.8	15.5	26.6	15.9	26.6	16.0	31
32	28.2	15.0	28.2	15.1	28.0	15.5	27.7	16.0	27.4	16.4	27.4	16.5	32
33	29.1	15.5	29.1	15.5	28.9	16.0	28.6	16.5	28.3	17.0	28.3	17.0	33
34	30.1	16.0	30.0	16.0	29.7	16.5	29.5	17.0	29.2	17.5	29.1	17.5	34
35	30.9	16.4	30.9	16.5	30.6	17.0	30.2	17.5	30.0	18.0	30.0	18.0	35
36	31.8	16.9	31.7	17.0	31.5	17.4	31.1	18.0	30.9	18.6	30.9	18.5	36
37	32.7	17.4	32.6	17.4	32.4	17.9	32.0	18.5	31.7	19.0	31.7	19.1	37
38	33.5	17.9	33.5	17.9	33.2	18.4	32.9	19.0	32.5	19.5	32.6	19.6	38
39	34.4	18.3	34.4	18.4	34.1	18.9	33.8	19.5	33.4	20.0	33.4	20.1	39
40	35.3	18.8	35.3	18.9	35.0	19.1	34.6	20.0	34.3	20.6	34.3	20.6	40
41	36.2	19.2	36.1	19.3	35.8	19.9	35.5	20.5	35.2	21.1	35.1	21.1	41
42	37.1	19.7	37.0	19.8	36.7	20.4	36.4	21.0	36.0	21.6	36.0	21.6	42
43	38.0	20.1	37.9	20.3	37.6	20.8	37.2	21.5	36.9	22.1	36.9	22.1	43
44	38.8	20.6	38.8	20.7	38.5	21.3	38.1	22.0	37.7	22.6	37.7	22.6	44
45	39.7	21.1	39.7	21.2	39.3	21.8	39.0	22.5	38.6	23.1	38.6	23.1	45
46	40.6	21.6	40.6	21.7	40.2	22.3	39.8	23.0	39.5	23.6	39.4	23.7	46
47	41.5	22.1	41.4	22.2	41.1	22.8	40.7	23.5	40.3	24.2	40.3	24.2	47
48	42.4	22.5	42.3	22.6	42.0	23.3	41.6	24.0	41.2	24.7	41.2	24.7	48
49	43.3	23.1	43.2	23.2	42.8	23.7	42.4	24.5	42.0	25.2	42.0	25.2	49
50	44.1	23.5	44.1	23.6	43.7	24.2	43.3	25.0	42.9	25.7	42.9	25.7	50
Diff.	62 Deg.		5 ½ Point		61 Deg.		60 Deg.		5 ¼ Point		59 Deg.		Diff.
	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	

A Table of Difference

Diff.	28 Deg.		2 $\frac{1}{2}$ Points		29 Deg.		30 Deg.		2 $\frac{1}{2}$ Points		31 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	45.0	23.9	45.0	24.0	44.6	24.7	44.2	25.5	43.7	25.2	43.7	26.3	51
52	45.9	24.4	45.9	24.5	45.5	25.2	45.0	26.0	44.6	26.7	44.6	26.8	52
53	46.8	24.9	46.7	25.0	46.5	25.7	45.0	26.5	45.5	27.2	45.4	27.3	53
54	47.7	25.3	47.6	25.5	47.2	26.2	46.8	27.0	46.3	27.8	45.3	27.8	54
55	48.6	25.8	48.5	25.0	48.1	25.7	47.6	27.5	47.2	28.2	47.1	28.3	55
56	49.4	26.3	49.4	26.4	49.0	27.1	48.5	28.0	47.9	28.8	48.0	28.8	56
57	50.3	26.8	50.3	26.9	49.8	27.6	49.4	28.5	48.9	29.3	48.9	29.4	57
58	51.2	27.3	51.2	27.3	50.7	28.1	50.2	29.0	49.7	29.8	49.7	29.9	58
59	52.1	27.7	52.0	27.8	51.6	28.6	51.1	29.5	50.6	30.3	50.6	30.4	59
60	53.0	28.2	52.0	28.3	52.5	29.1	52.0	30.0	51.5	30.8	51.4	30.8	60
61	53.9	28.6	53.8	28.7	52.3	29.6	52.8	30.5	52.3	31.4	52.3	31.4	61
62	54.7	29.1	54.7	29.2	53.2	30.1	53.7	31.0	53.4	31.9	53.1	31.9	62
63	55.6	29.6	55.6	29.7	54.1	30.5	54.6	31.5	54.0	32.4	54.0	32.4	63
64	56.5	30.0	56.4	30.2	55.0	31.0	55.4	32.0	54.9	32.9	54.9	33.0	64
65	57.4	30.5	57.1	30.5	56.8	31.5	56.3	32.5	55.7	33.4	55.7	33.5	65
66	58.3	31.0	58.2	31.1	57.7	32.0	57.2	33.0	56.6	33.9	56.6	34.0	66
67	59.2	31.4	59.1	31.6	58.6	32.5	58.0	33.5	57.5	34.4	57.4	34.5	67
68	60.0	31.9	60.0	32.0	59.5	33.0	58.9	34.0	58.3	35.0	58.3	35.0	68
69	60.9	32.4	60.8	32.5	60.3	33.4	59.7	34.5	59.2	35.5	59.1	35.5	69
70	61.8	32.9	61.7	33.0	61.2	33.9	60.6	35.0	60.0	36.0	60.0	36.0	70
71	62.7	33.3	62.6	33.5	62.1	34.4	61.5	35.5	60.9	36.5	60.9	36.6	71
72	63.6	33.8	63.5	33.9	63.0	34.9	62.3	36.0	61.8	37.0	61.7	37.1	72
73	64.4	34.3	64.4	34.4	63.8	35.4	63.2	36.5	62.6	37.5	62.6	37.6	73
74	65.3	34.7	65.3	34.9	64.7	35.9	64.1	37.0	63.5	38.0	63.5	38.1	74
75	66.2	35.2	66.1	35.1	65.6	36.4	64.0	37.5	64.3	38.5	64.3	38.6	75
76	67.1	35.7	67.0	35.6	66.5	36.8	65.8	38.0	65.2	39.0	65.1	39.1	76
77	68.0	36.1	67.9	36.3	67.3	37.3	66.7	38.5	66.0	39.6	66.0	39.7	77
78	68.9	36.6	68.8	36.8	68.2	37.8	67.5	39.0	66.9	40.1	66.9	40.2	78
79	69.7	37.1	69.7	37.2	69.1	38.3	68.4	39.5	67.8	40.6	67.7	40.7	79
80	70.6	37.6	70.5	37.7	70.0	38.8	69.1	40.0	68.6	41.1	68.6	41.2	80
81	71.5	38.0	71.4	38.2	70.8	39.3	70.1	40.5	69.3	41.6	69.4	41.7	81
82	72.4	38.5	72.3	38.6	71.7	39.7	70.9	41.0	70.3	42.1	70.3	42.2	82
83	73.3	39.0	73.2	39.1	72.6	40.2	71.9	41.5	71.2	42.7	71.1	42.7	83
84	74.2	39.4	74.1	39.6	73.5	40.7	72.7	42.0	72.1	43.2	72.0	43.3	84
85	75.1	39.9	75.0	40.1	74.3	41.2	73.6	42.5	72.9	43.7	72.9	43.8	85
86	75.9	40.4	75.8	40.5	75.2	41.7	74.5	43.0	73.8	44.2	73.7	44.3	86
87	76.8	40.8	76.7	41.0	76.1	42.2	75.3	43.5	74.6	44.7	74.6	44.8	87
88	77.7	41.3	77.6	41.5	77.0	42.7	76.2	44.0	75.5	45.2	75.4	45.3	88
89	78.6	41.8	78.5	41.9	77.8	43.1	77.1	44.5	76.3	45.8	76.3	45.8	89
90	79.5	42.2	79.4	42.4	78.7	43.6	77.9	45.0	77.2	46.3	77.1	46.3	90
91	80.3	42.7	80.2	42.9	79.6	44.1	78.8	45.5	78.1	46.8	78.0	46.9	91
92	81.2	43.2	81.1	43.4	80.5	44.6	79.7	46.0	78.9	47.3	78.9	47.4	92
93	82.1	43.6	82.0	43.8	81.3	45.1	80.5	46.5	79.8	47.8	79.7	47.9	93
94	83.0	44.1	82.9	44.3	82.2	45.6	81.4	47.0	80.6	48.3	80.6	48.4	94
95	83.9	44.6	83.8	44.8	83.1	46.1	82.3	47.5	81.5	48.8	81.4	48.9	95
96	84.8	45.1	84.7	45.2	84.0	46.5	83.1	48.0	82.3	49.3	82.3	49.4	96
97	85.6	45.5	85.5	45.7	84.8	47.0	84.0	48.5	83.2	49.9	83.1	50.0	97
98	86.5	46.0	86.4	46.2	85.7	47.5	84.9	49.0	84.1	50.4	84.0	50.5	98
99	87.4	46.5	87.3	46.7	86.6	48.0	85.7	49.5	84.9	50.9	84.9	51.0	99
100	88.3	46.9	88.2	47.1	87.5	48.5	86.6	50.0	85.7	51.4	85.7	51.5	100
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
	62 Deg.	5 $\frac{1}{2}$ Points		61 Deg.	60 Deg.	5 $\frac{1}{2}$ Points		59 Deg.					

of Latitude and Departure.

Diff.	32 Deg.		33 Deg.		3 Point		34 Deg.		35 Deg.		36 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	00.8	00.5	00.8	00.5	00.8	00.6	00.8	00.6	00.8	00.6	00.8	00.6	1
2	01.7	01.1	01.7	01.1	01.7	01.1	01.6	01.1	01.6	01.1	01.6	01.1	2
3	02.5	01.6	02.5	01.6	02.5	01.7	02.5	01.7	02.5	01.7	02.5	01.7	3
4	03.4	02.1	03.4	02.2	03.3	02.2	03.3	02.2	03.3	02.3	03.3	02.3	4
5	04.2	02.6	04.2	02.7	04.1	02.8	04.1	02.8	04.1	02.9	04.1	02.9	5
6	05.1	03.2	05.0	03.3	05.0	03.3	05.0	03.4	04.9	03.3	04.8	03.3	6
7	05.9	03.7	05.9	03.8	05.8	03.9	05.8	03.9	05.7	04.0	05.7	04.1	7
8	06.8	04.2	06.7	04.4	06.6	04.4	06.6	04.5	06.5	04.6	06.5	04.7	8
9	07.6	04.8	07.5	04.9	07.5	05.0	07.5	05.0	07.4	05.2	07.3	05.3	9
10	08.5	05.3	08.4	05.4	08.3	05.6	08.1	05.6	08.1	05.7	08.1	05.9	10
11	09.3	05.8	09.2	06.0	09.1	06.1	09.1	06.1	09.0	06.3	08.9	06.5	11
12	10.2	06.4	10.1	06.5	10.0	06.7	09.9	06.7	09.8	06.9	09.7	07.0	12
13	11.0	06.9	10.9	07.1	10.8	07.2	10.8	07.3	10.8	07.5	10.5	07.6	13
14	11.9	07.4	11.7	07.6	11.6	07.8	11.6	07.8	11.5	08.0	11.3	08.1	14
15	12.7	07.9	11.6	08.2	12.5	08.3	12.4	08.4	12.3	08.6	12.1	08.8	15
16	13.6	08.5	13.4	08.7	13.3	08.9	13.3	08.9	13.1	09.2	12.9	09.4	16
17	14.4	09.0	14.3	09.3	14.1	09.4	14.1	09.5	13.9	09.8	13.7	10.0	17
18	15.3	09.5	15.0	09.8	15.0	10.0	15.0	10.1	14.7	10.3	14.6	10.6	18
19	16.1	10.1	15.1	10.3	15.8	10.6	15.7	10.6	15.6	10.9	15.4	11.2	19
20	17.0	10.6	16.8	10.9	16.6	11.1	16.6	11.2	16.4	11.5	16.2	11.8	20
21	17.8	11.1	17.6	11.4	17.5	11.7	17.4	11.7	17.2	12.0	17.0	12.3	21
22	18.6	11.7	18.5	12.0	18.3	12.3	18.2	12.3	18.0	12.6	17.8	12.9	22
23	19.5	12.3	19.3	12.5	19.1	12.8	19.0	12.8	18.8	13.2	18.7	13.5	23
24	20.3	12.7	20.1	13.1	20.0	13.3	19.9	13.4	19.7	13.8	19.4	14.1	24
25	21.2	13.3	21.0	13.6	20.7	13.9	20.7	14.0	20.5	14.3	20.1	14.7	25
26	22.0	13.8	21.8	14.2	21.6	14.4	21.5	14.5	21.3	14.9	21.0	15.3	26
27	22.9	14.3	21.6	14.7	22.4	15.0	22.4	15.1	22.1	15.5	21.8	15.9	27
28	23.7	14.8	23.5	15.2	23.3	15.5	23.2	15.6	22.9	16.1	22.6	16.5	28
29	24.6	15.4	24.3	15.8	24.1	16.1	24.0	16.2	23.8	16.6	23.5	17.0	29
30	25.4	15.9	25.2	16.3	24.9	16.7	24.9	16.8	24.6	17.2	24.3	17.6	30
31	26.3	16.4	26.0	16.9	25.8	17.2	25.7	17.3	25.4	17.8	25.1	18.2	31
32	27.1	17.0	26.8	17.4	26.6	17.8	26.5	17.9	26.2	18.3	25.9	18.8	32
33	28.0	17.5	27.7	18.0	27.4	18.3	27.4	18.4	27.0	18.9	26.7	19.4	33
34	28.8	18.5	28.5	18.5	28.3	18.9	28.2	19.0	27.9	19.5	27.5	20.0	34
35	29.7	18.0	29.4	19.1	29.1	19.4	29.0	19.6	28.7	20.1	28.3	20.6	35
36	30.5	19.1	30.2	19.6	29.9	20.0	29.5	20.1	29.3	20.6	29.1	21.2	36
37	31.4	19.6	31.0	20.1	30.8	20.6	30.7	20.7	30.3	21.8	29.9	21.7	37
38	32.2	20.1	31.9	20.7	31.6	21.1	31.5	21.2	31.1	21.8	30.7	22.3	38
39	33.1	20.7	32.7	21.2	32.4	21.7	32.3	21.8	32.0	22.3	31.5	22.9	39
40	34.0	21.2	33.6	21.8	33.2	22.2	33.1	22.4	32.8	22.9	32.4	23.5	40
41	34.8	21.7	34.4	22.5	34.0	22.8	34.0	22.9	33.6	23.5	33.2	24.1	41
42	35.6	22.3	35.2	22.9	34.9	23.3	34.8	23.5	34.4	24.1	34.0	24.7	42
43	36.5	22.8	36.1	23.4	35.7	23.9	35.6	24.0	35.2	24.6	34.8	25.3	43
44	37.3	23.3	36.9	24.0	36.6	24.4	36.5	24.5	36.0	25.2	35.6	25.9	44
45	38.1	23.8	37.7	24.5	37.4	25.0	37.3	25.2	36.9	25.8	36.4	26.4	45
46	39.0	24.4	38.6	25.0	38.2	25.5	38.1	25.7	37.7	26.4	37.2	27.0	46
47	39.9	24.9	39.4	25.6	39.1	26.1	39.0	26.3	38.5	26.9	38.0	27.6	47
48	40.7	25.4	40.3	26.1	39.9	26.7	39.8	26.8	39.3	27.5	38.8	28.2	48
49	41.5	26.0	41.1	26.7	40.7	27.2	40.6	27.4	40.4	28.1	39.6	28.8	49
50	42.4	26.5	41.9	27.2	41.6	27.8	41.4	28.0	41.0	28.7	40.4	29.4	50
	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	
	58 Deg.		57 Deg.		5 Point		56 Deg.		55 Deg.		54 Deg.		

A Table of Difference

Difference	23 Deg.		33 Deg.		3 Point		34 Deg.		35 Deg.		36 Deg.		Difference
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	43.2	27.0	42.8	27.8	42.4	28.3	42.3	28.5	41.8	29.2	41.3	30.0	51
52	44.1	27.6	43.6	28.3	43.2	28.9	43.1	29.1	42.6	29.8	42.1	30.6	52
53	44.9	28.1	44.5	28.9	44.1	29.4	43.9	29.6	43.4	30.4	42.9	31.2	53
54	45.8	28.6	45.3	29.4	44.9	30.0	44.5	30.2	44.2	31.0	43.7	31.7	54
55	46.6	29.1	46.1	30.0	45.7	30.6	45.6	30.7	45.1	31.5	44.5	32.3	55
56	47.5	29.7	47.0	30.5	46.0	31.1	46.4	31.3	45.9	32.1	45.3	32.9	56
57	48.3	30.2	47.8	31.0	47.4	31.7	47.3	31.9	46.7	32.7	46.1	33.5	57
58	49.2	30.7	48.7	31.6	48.2	32.2	48.1	32.4	47.5	33.3	46.9	34.1	58
59	50.0	31.3	49.5	32.1	48.0	32.8	48.9	33.0	48.3	33.8	47.7	34.7	59
60	50.9	31.8	50.3	32.7	49.9	33.1	49.7	33.5	49.1	34.4	48.5	35.3	60
61	51.7	32.3	51.2	33.2	50.7	33.9	50.6	34.1	50.0	34.9	49.3	35.9	61
62	52.6	32.9	52.0	33.8	51.5	34.4	51.4	34.7	50.8	35.6	50.2	36.4	62
63	53.4	33.4	52.9	34.3	52.4	35.0	52.2	35.2	51.6	36.1	51.0	37.0	63
64	54.3	33.9	53.7	34.9	53.2	35.5	53.1	35.8	52.4	36.7	51.8	37.6	64
65	55.1	34.4	54.5	35.4	54.0	36.1	53.9	36.3	53.2	37.3	52.6	38.2	65
66	56.0	35.0	55.3	35.9	54.9	36.7	54.7	36.9	54.1	37.9	53.4	38.8	66
67	56.8	35.5	56.2	36.5	55.7	37.2	55.5	37.5	54.9	38.4	54.2	39.4	67
68	57.7	36.0	57.0	37.0	56.5	37.8	56.4	38.0	55.7	39.0	55.0	40.0	68
69	58.5	36.6	57.9	37.6	57.4	38.3	57.2	38.6	56.5	39.6	55.8	40.6	69
70	59.4	37.1	58.7	38.1	58.2	38.9	58.0	39.1	57.3	40.1	56.6	41.1	70
71	60.2	37.6	59.6	38.7	59.0	39.4	58.9	39.7	58.2	40.7	57.4	41.7	71
72	61.0	38.1	60.4	39.2	59.8	40.0	59.7	40.3	59.0	41.3	58.2	42.3	72
73	61.9	38.7	61.2	39.8	60.7	40.6	60.5	40.8	59.8	41.9	59.1	42.9	73
74	62.7	39.2	62.1	40.3	61.5	41.1	61.3	41.4	60.6	42.4	59.9	43.5	74
75	63.6	39.7	62.9	40.8	62.4	41.7	62.2	41.9	61.4	43.0	60.7	44.1	75
76	64.4	40.3	63.8	41.5	63.2	42.2	63.0	42.5	62.3	43.6	61.5	44.7	76
77	65.3	40.8	64.6	41.9	64.0	42.8	63.8	43.0	63.1	44.2	62.3	45.3	77
78	66.1	41.3	65.4	42.5	64.8	43.3	64.7	43.6	63.9	44.7	63.1	45.8	78
79	67.0	41.9	66.3	43.0	65.7	43.9	65.5	44.2	64.7	45.3	63.9	46.4	79
80	67.8	42.4	67.1	43.6	66.5	44.4	66.1	44.7	65.5	45.9	64.7	47.0	80
81	68.7	42.9	68.0	44.1	67.3	45.0	67.1	45.3	66.4	46.5	65.5	47.6	81
82	69.5	43.4	68.8	44.7	68.2	45.5	68.0	45.8	67.2	47.0	66.3	48.2	82
83	70.4	44.0	69.6	45.2	69.0	46.1	68.8	46.4	68.0	47.6	67.1	48.8	83
84	71.2	44.5	70.5	45.8	69.8	46.7	69.6	47.0	68.8	48.2	68.0	49.4	84
85	72.1	45.0	71.3	46.3	70.7	47.2	70.5	47.5	69.6	48.8	68.8	50.0	85
86	72.9	45.6	72.1	46.8	71.5	47.8	71.3	48.1	70.5	49.3	69.6	50.5	86
87	73.8	46.1	73.0	47.3	72.3	48.3	72.1	48.6	71.3	49.9	70.4	51.1	87
88	74.6	46.6	73.8	47.9	73.2	48.9	72.9	49.2	72.1	50.5	71.2	51.7	88
89	75.5	47.2	74.7	48.5	74.0	49.4	73.8	49.8	72.9	51.0	72.0	52.3	89
90	76.2	47.7	75.5	49.0	74.8	50.0	74.6	50.3	73.7	51.6	72.8	52.9	90
91	77.2	48.2	76.3	49.6	75.7	50.6	75.4	50.9	74.5	52.2	73.6	53.5	91
92	78.0	48.7	77.2	50.1	76.5	51.1	76.3	51.4	75.4	52.8	74.4	54.1	92
93	78.9	49.3	78.0	50.6	77.3	51.7	77.1	52.0	76.2	53.3	75.2	54.7	93
94	79.7	49.8	78.9	51.2	78.2	52.2	77.9	52.6	77.0	53.9	76.0	55.2	94
95	80.6	50.3	79.7	51.7	79.0	52.8	78.8	53.1	77.8	54.5	76.9	55.8	95
96	81.4	50.9	80.5	52.3	79.8	53.3	79.6	53.7	78.6	55.1	77.7	56.4	96
97	82.3	51.4	81.4	52.8	80.6	53.9	80.4	54.2	79.5	55.6	78.5	57.0	97
98	83.1	51.9	82.2	53.4	81.5	54.4	81.3	54.8	80.3	56.2	79.3	57.6	98
99	84.0	52.5	83.1	53.9	82.3	55.0	82.1	55.4	81.1	56.8	80.1	58.2	99
100	84.8	53.0	83.9	54.5	83.1	55.6	82.9	55.9	81.9	57.4	80.9	58.8	100
	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	
Difference	58 Deg.		57 Deg.		5 Point		56 Deg.		55 Deg.		54 Deg.		Difference

of Latitude and Departure.

Diff.	36 Point		37 Deg.		38 Deg.		39 Deg.		37 Point		40 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
1	00.8	00.6	00.8	00.6	00.8	00.6	00.8	00.7	00.8	00.6	00.8	00.6	1
2	01.6	01.2	01.6	01.2	01.6	01.2	01.5	01.3	01.5	01.3	01.5	01.3	2
3	02.4	01.8	02.4	01.8	02.4	01.8	02.3	01.9	02.3	01.9	02.3	01.9	3
4	03.2	02.4	03.2	02.4	03.1	02.5	03.0	02.5	03.1	02.5	03.1	02.6	4
5	04.0	03.0	04.0	03.0	03.9	03.1	03.9	03.1	03.9	03.1	03.8	03.2	5
6	04.8	03.6	04.8	03.6	04.7	03.7	04.6	03.9	04.6	03.9	04.6	03.9	6
7	05.6	04.2	05.6	04.2	05.5	04.3	05.4	04.4	05.4	04.4	05.4	04.5	7
8	06.4	04.8	06.4	04.8	06.3	04.9	06.2	05.0	06.2	05.1	06.1	05.1	8
9	07.2	05.4	07.2	05.4	07.1	05.5	07.0	05.7	07.0	05.7	06.9	05.8	9
10	08.0	06.0	08.0	06.0	07.9	06.2	07.8	06.1	07.7	06.3	07.7	06.4	10
11	08.8	06.6	08.8	06.6	08.7	06.8	08.5	06.9	08.5	07.0	08.4	07.1	11
12	09.6	07.1	09.6	07.2	09.4	07.4	09.3	07.5	09.3	07.6	09.2	07.7	12
13	10.4	07.7	10.4	07.8	10.2	08.1	10.1	08.2	10.0	08.2	10.0	08.4	13
14	11.2	08.3	11.2	08.4	11.0	08.7	10.9	08.8	10.8	08.9	10.7	09.0	14
15	12.0	08.9	12.0	09.0	11.8	09.3	11.6	09.4	11.6	09.5	11.5	09.6	15
16	12.8	09.5	12.8	09.6	12.6	09.8	12.4	10.1	12.4	10.1	12.3	10.3	16
17	13.6	10.1	13.6	10.2	13.4	10.5	13.2	10.7	13.1	10.8	13.0	10.9	17
18	14.5	10.7	14.4	10.8	14.2	11.1	13.9	11.3	13.9	11.4	13.8	11.6	18
19	15.3	11.3	15.2	11.4	15.0	11.7	14.8	12.0	14.7	12.0	14.5	12.2	19
20	16.1	11.9	16.0	12.0	15.8	12.3	15.5	12.6	15.5	12.7	15.3	12.9	20
21	16.9	12.5	16.8	12.6	16.5	12.9	16.3	13.2	16.2	13.3	16.1	13.5	21
22	17.7	13.1	17.6	13.2	17.3	13.5	17.1	13.8	17.0	14.0	16.8	14.1	22
23	18.5	13.7	18.4	13.8	18.1	14.2	17.9	14.5	17.8	14.6	17.6	14.8	23
24	19.3	14.3	19.2	14.4	19.0	14.8	18.6	15.1	18.5	15.2	18.4	15.4	24
25	20.1	14.9	20.0	15.0	19.7	15.4	19.4	15.7	19.3	15.9	19.1	16.1	25
26	20.9	15.5	20.8	15.6	20.5	16.0	20.2	16.4	20.1	16.5	19.9	16.7	26
27	21.7	16.1	21.6	16.2	21.3	16.6	21.0	17.0	20.9	17.1	20.7	17.4	27
28	22.5	16.7	22.4	16.8	22.1	17.2	21.8	17.6	21.6	17.8	21.4	18.0	28
29	23.3	17.3	23.2	17.4	22.8	17.8	22.5	18.3	22.4	18.4	22.2	18.6	29
30	24.1	17.9	24.0	18.0	23.6	18.5	23.3	18.9	23.2	19.0	23.0	19.3	30
31	24.9	18.5	24.8	18.6	24.4	19.1	24.1	19.5	24.0	19.7	23.7	19.9	31
32	25.7	19.1	25.6	19.2	25.2	19.7	24.9	20.1	24.7	20.3	24.5	20.6	32
33	26.5	19.7	26.4	19.9	26.0	20.3	25.6	20.8	25.5	20.9	25.3	21.2	33
34	27.3	20.3	27.2	20.5	26.8	20.9	26.4	21.4	26.3	21.6	26.0	21.9	34
35	28.1	20.9	28.0	21.1	27.6	21.5	27.2	22.0	27.0	22.2	26.8	22.5	35
36	28.9	21.4	28.7	21.7	28.4	22.1	27.7	22.7	27.8	22.8	27.6	23.1	36
37	29.7	22.0	29.5	22.3	29.2	22.8	28.8	23.3	28.6	23.5	28.3	23.8	37
38	30.5	22.6	30.3	22.9	29.9	23.4	29.5	23.9	29.4	24.1	29.1	24.4	38
39	31.3	23.2	31.1	23.5	30.7	24.0	30.3	24.5	30.1	24.7	29.9	25.1	39
40	32.1	23.8	31.9	24.1	31.5	24.6	31.1	25.2	30.9	25.4	30.6	25.7	40
41	32.9	24.4	32.7	24.7	32.3	25.2	31.9	25.8	31.7	26.0	31.4	26.4	41
42	33.7	25.0	33.5	25.3	33.1	25.9	32.6	26.4	32.5	26.6	32.2	27.0	42
43	34.5	25.6	34.3	25.9	33.9	26.5	33.4	27.1	33.2	27.3	32.9	27.6	43
44	35.3	26.2	35.1	26.5	34.7	27.1	34.2	27.7	34.0	27.9	33.7	28.3	44
45	36.1	26.8	35.9	27.1	35.5	27.7	35.0	28.3	34.8	28.5	34.5	28.9	45
46	36.9	27.4	36.7	27.7	36.3	28.3	35.7	29.0	35.6	29.2	35.2	29.6	46
47	37.7	28.0	37.5	28.3	37.0	28.9	36.5	29.6	36.3	29.8	36.0	30.3	47
48	38.5	28.6	38.3	28.9	37.8	29.5	37.8	30.3	37.1	30.4	36.8	30.9	48
49	39.3	29.2	39.1	29.5	38.6	30.2	38.1	30.8	37.9	31.1	37.5	31.5	49
50	40.1	29.8	39.9	30.1	39.4	30.8	38.9	31.5	38.6	31.7	38.3	32.1	50
Diff.	41 Point		53 Deg.		52 Deg.		51 Deg.		41 Point		50 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	

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A Table of Difference

Diff.	3 1/2 Point		37 Deg.		38 Deg.		39 Deg.		3 1/2 Point		40 Deg.		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	41.0	30.4	40.7	30.7	40.2	31.4	39.6	32.1	39.4	32.3	39.1	32.8	51
52	41.8	31.0	41.5	31.3	41.0	32.0	40.4	32.7	40.2	33.0	39.8	33.4	52
53	42.6	31.6	42.3	31.9	41.8	32.6	41.2	33.3	41.0	33.6	40.6	34.1	53
54	43.4	32.2	43.1	32.5	42.5	33.2	42.0	34.0	41.7	34.3	41.4	34.7	54
55	44.2	32.8	43.9	33.1	43.3	33.9	42.7	34.6	42.5	34.9	42.1	35.4	55
56	45.0	33.3	44.7	33.8	44.1	34.5	43.5	35.2	43.3	35.5	42.9	36.0	56
57	45.8	33.9	45.5	34.3	44.9	35.1	44.3	35.9	44.1	36.2	43.7	36.6	57
58	46.6	34.5	46.3	34.9	45.7	35.8	45.1	36.5	44.8	36.8	44.4	37.3	58
59	47.4	35.1	47.1	35.5	46.5	36.3	45.8	37.1	45.6	37.4	45.2	37.9	59
60	48.2	35.7	47.9	36.1	47.3	36.9	46.6	37.8	46.4	38.1	46.0	38.6	60
61	49.0	36.3	48.7	36.7	48.1	37.5	47.4	38.4	47.1	38.7	46.7	39.2	61
62	49.8	36.9	49.5	37.3	48.9	38.2	48.2	39.0	47.9	39.3	47.5	39.9	62
63	50.6	37.5	50.3	37.9	49.6	38.8	49.0	39.6	48.7	40.0	48.3	40.5	63
64	51.4	38.1	51.1	38.5	50.4	39.4	49.7	40.3	49.5	40.6	49.0	41.2	64
65	52.2	38.7	51.9	39.1	51.2	40.0	50.5	40.9	50.2	41.2	49.8	41.8	65
66	53.0	39.3	52.7	39.7	52.0	40.6	51.3	41.5	51.0	41.9	50.5	42.4	66
67	53.8	39.9	53.5	40.3	52.8	41.2	52.1	42.2	51.8	42.5	51.3	43.1	67
68	54.6	40.5	54.3	40.9	53.6	41.9	52.8	42.8	52.6	43.1	52.1	43.7	68
69	55.4	41.1	55.1	41.5	54.4	42.5	53.6	43.4	53.3	43.8	52.9	44.4	69
70	56.2	41.7	55.9	42.1	55.2	43.1	54.4	44.0	54.1	44.4	53.6	45.0	70
71	57.0	42.3	56.7	42.7	55.9	43.7	55.2	44.7	54.9	45.0	54.4	45.6	71
72	57.8	42.9	57.5	43.3	56.7	44.3	55.9	45.3	55.7	45.7	55.1	46.3	72
73	58.6	43.5	58.3	43.9	57.5	44.9	56.7	45.9	56.4	46.3	55.9	46.9	73
74	59.4	44.1	59.1	44.5	58.3	45.6	57.5	46.6	57.2	46.9	56.7	47.6	74
75	60.2	44.7	59.9	45.1	59.2	46.2	58.3	47.2	58.0	47.6	57.4	48.2	75
76	61.0	45.3	60.7	45.7	60.0	46.8	59.1	47.8	58.7	48.2	58.2	48.9	76
77	61.8	45.9	61.5	46.3	60.7	47.4	59.0	48.5	59.5	48.8	59.0	49.5	77
78	62.7	46.5	62.3	46.9	61.5	48.0	60.6	49.1	60.3	49.5	59.7	50.1	78
79	63.5	47.1	63.1	47.5	62.3	48.6	61.4	49.7	61.1	50.1	60.5	50.8	79
80	64.3	47.7	63.0	48.1	63.0	49.3	62.2	50.3	61.8	50.7	61.3	51.4	80
81	65.1	48.3	64.7	48.7	63.8	49.9	62.9	51.0	62.6	51.4	62.0	52.1	81
82	65.9	48.8	65.5	49.3	64.6	50.5	63.7	51.6	63.4	52.0	62.8	52.7	82
83	66.7	49.4	66.3	49.6	65.4	51.1	64.5	52.2	64.2	52.6	63.6	53.4	83
84	67.5	50.0	67.1	50.5	66.2	51.7	65.3	52.9	64.9	53.3	64.3	54.0	84
85	68.3	50.6	67.9	51.1	67.0	52.3	66.1	53.5	65.7	53.9	65.1	54.6	85
86	69.1	51.2	68.7	51.7	67.8	52.9	66.8	54.1	66.5	54.6	65.9	55.3	86
87	69.9	51.8	69.5	52.4	68.6	53.5	67.6	54.8	67.3	55.2	66.6	55.9	87
88	70.7	52.4	70.3	53.0	69.3	54.2	68.4	55.4	68.0	55.8	67.4	56.6	88
89	71.5	53.0	71.1	53.6	70.1	54.8	69.2	56.0	68.8	56.5	68.2	57.2	89
90	72.3	53.6	71.9	54.2	70.9	55.4	69.9	56.6	69.6	57.1	68.9	57.4	90
91	73.1	54.2	72.7	54.8	71.7	56.0	70.7	57.3	70.3	57.7	69.7	58.5	91
92	73.9	54.8	73.5	55.5	72.5	56.6	71.5	57.9	71.1	58.4	70.5	59.1	92
93	74.7	55.4	74.3	56.0	73.3	57.3	72.3	58.5	71.9	59.0	71.3	59.8	93
94	75.5	56.0	75.1	56.6	74.1	57.9	73.0	59.2	72.7	59.6	72.0	60.4	94
95	76.3	56.6	75.9	57.2	74.9	58.5	73.8	59.8	73.4	60.3	72.8	61.7	95
96	77.1	57.2	76.7	57.8	75.6	59.1	74.6	60.4	74.2	60.9	73.5	62.7	96
97	77.9	57.8	77.5	58.4	76.4	59.7	75.4	61.0	75.0	61.5	74.3	63.1	97
98	78.7	58.4	78.3	59.0	77.2	60.3	76.2	61.7	75.7	62.2	75.2	63.0	98
99	79.5	59.0	79.1	59.6	78.0	60.9	76.9	62.3	76.5	62.8	75.8	63.6	99
100	80.3	59.6	79.9	60.2	78.8	61.6	77.7	63.0	77.3	63.4	76.6	64.3	100
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
	4 1/2 Point		53 Deg.		52 Deg.		51 Deg.		4 1/2 Points		50 Deg.		

of Latitude and Departure.

Diff.	41 Deg.		42 Deg.		3 $\frac{1}{4}$ Point		43 Deg.		44 Deg.		4 Points		Diff.
	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	
1	00.7	00.7	00.7	00.7	00.7	00.7	00.7	00.7	00.7	00.7	00.7	00.7	1
2	01.5	01.3	01.5	01.3	01.5	01.3	01.5	01.4	01.4	01.4	01.4	01.4	2
3	02.3	02.0	02.3	02.0	02.2	02.0	02.2	02.0	02.2	02.1	02.1	02.1	3
4	03.0	02.6	03.0	02.7	03.0	02.7	02.9	02.7	02.9	02.8	02.8	02.8	4
5	03.8	03.3	03.7	03.1	03.7	03.4	03.6	03.4	03.6	03.5	03.5	03.5	5
6	04.5	03.9	04.5	04.0	04.4	04.0	04.4	04.1	04.3	04.3	04.2	04.2	6
7	05.3	04.6	05.2	04.7	05.2	04.7	05.1	04.8	05.0	04.9	04.9	04.9	7
8	06.0	05.2	05.9	05.3	05.9	05.4	05.8	05.5	05.7	05.6	05.7	05.7	8
9	06.8	05.9	06.7	06.0	06.7	06.0	06.6	06.1	06.5	06.2	06.4	06.4	9
10	07.5	06.6	07.4	06.7	07.4	06.7	07.3	06.8	07.2	06.9	07.1	07.1	10
11	08.3	07.2	08.2	07.4	08.1	07.4	08.0	07.5	07.9	07.6	07.8	07.8	11
12	09.1	07.9	08.9	08.0	08.9	08.1	08.8	08.2	08.6	08.3	08.5	08.5	12
13	09.8	08.5	09.7	08.7	09.6	08.7	09.5	08.9	09.3	09.0	09.2	09.2	13
14	10.6	09.2	10.4	09.4	10.4	09.4	10.2	09.5	10.1	09.7	09.9	09.9	14
15	11.3	09.8	11.1	10.0	11.1	10.1	11.0	10.2	10.8	10.4	10.6	10.6	15
16	12.1	10.5	11.9	10.7	11.9	10.7	11.7	10.9	11.5	11.1	11.3	11.3	16
17	12.8	11.1	12.6	11.4	12.6	11.4	12.4	11.6	12.2	11.8	12.0	12.0	17
18	13.6	11.8	13.4	12.0	13.3	12.1	13.2	12.3	12.9	12.5	12.7	12.7	18
19	14.3	12.5	14.1	12.7	14.1	12.8	13.9	13.0	13.7	13.3	13.4	13.4	19
20	15.1	13.1	14.9	13.4	14.8	13.4	14.6	13.6	14.4	13.9	14.1	14.1	20
21	15.8	13.8	15.6	14.0	15.6	14.1	15.4	14.3	15.1	14.6	14.8	14.8	21
22	16.6	14.4	16.3	14.7	16.3	14.8	16.1	15.0	15.8	15.3	15.5	15.5	22
23	17.4	15.1	17.1	15.4	17.0	15.4	16.8	15.7	16.5	16.0	16.3	16.3	23
24	18.1	15.7	17.8	16.1	17.8	16.1	17.5	16.4	17.3	16.7	17.0	17.0	24
25	18.9	16.4	18.6	16.7	18.5	16.8	18.3	17.1	18.0	17.4	17.7	17.7	25
26	19.4	17.1	19.3	17.5	19.3	17.6	19.0	17.7	18.7	18.1	18.4	18.4	26
27	20.4	17.7	20.1	18.1	20.0	18.1	19.7	18.4	19.4	18.8	19.1	19.1	27
28	21.1	18.4	20.8	18.7	20.7	18.8	20.5	19.1	20.1	19.4	19.8	19.8	28
29	21.9	19.0	21.5	19.4	21.5	19.5	21.2	19.8	20.9	20.0	20.5	20.5	29
30	22.6	19.7	22.3	20.1	22.2	20.1	21.9	20.5	21.6	20.8	21.2	21.2	30
31	23.4	20.3	23.0	20.7	23.0	20.8	22.6	21.1	22.3	21.5	21.9	21.9	31
32	24.1	21.0	23.8	21.4	23.7	21.5	23.4	21.8	23.0	22.2	22.6	22.6	32
33	24.9	21.6	24.5	22.1	24.4	22.2	24.1	22.5	23.7	22.9	23.3	23.3	33
34	25.6	22.3	25.3	22.7	25.2	22.8	24.9	23.2	24.5	23.6	24.0	24.0	34
35	26.4	23.0	26.0	23.4	25.9	23.5	25.6	23.9	25.2	24.3	24.7	24.7	35
36	27.2	23.6	26.7	24.1	26.7	24.2	26.3	24.5	25.9	25.0	25.4	25.4	36
37	27.9	24.3	27.5	24.7	27.4	24.8	27.0	25.1	26.6	25.7	26.1	26.1	37
38	28.7	24.9	28.2	25.4	28.2	25.5	27.8	25.9	27.3	26.4	26.9	26.9	38
39	29.4	25.6	29.0	26.1	28.9	26.2	28.5	26.6	28.0	27.1	27.6	27.6	39
40	30.2	26.2	29.7	26.8	29.6	26.9	29.2	27.3	28.8	27.8	28.3	28.3	40
41	31.0	26.9	30.5	27.4	30.4	27.5	30.0	28.0	29.5	28.5	29.0	29.0	41
42	31.7	27.5	31.2	28.1	31.1	28.2	30.7	28.6	30.2	29.2	29.7	29.7	42
43	32.5	28.2	31.9	28.8	31.9	28.9	31.4	29.3	30.9	29.9	30.4	30.4	43
44	33.2	28.9	32.7	29.4	32.6	29.5	32.2	30.0	31.6	30.6	31.1	31.1	44
45	34.0	29.5	33.4	30.1	33.3	30.2	32.9	30.7	32.4	31.3	31.8	31.8	45
46	34.7	30.2	34.2	30.8	34.1	30.9	33.6	31.4	33.1	32.0	32.5	32.5	46
47	35.5	30.8	34.9	31.4	34.8	31.6	34.4	32.1	33.8	32.6	33.2	33.2	47
48	36.3	31.5	35.7	32.1	35.6	32.2	35.1	32.7	34.5	33.3	33.9	33.9	48
49	37.0	32.1	36.4	32.8	36.3	32.9	35.8	33.4	35.2	34.0	34.6	34.6	49
50	37.7	32.8	37.2	33.5	37.0	33.6	36.6	34.1	36.0	34.7	35.3	35.3	50
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	49 Deg.		48 Deg.		4 $\frac{1}{4}$ Point		47 Deg.		46 Deg.		4 Points		
Diff.													Diff.

A Table of Difference

Diff.	41 Deg.		42 Deg.		3 $\frac{1}{2}$ Point		43 Deg.		44 Deg.		4 Points		Diff.
	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
51	38.5	33.5	37.9	34.1	37.8	34.2	37.3	34.8	36.7	35.4	36.1	36.1	51
52	39.2	34.1	38.6	34.8	38.5	34.9	38.0	35.5	37.4	36.1	36.8	36.8	52
53	40.0	34.8	39.4	35.5	39.3	35.6	38.8	36.1	38.1	36.8	37.5	37.5	53
54	40.8	35.4	40.1	36.1	40.0	35.3	39.5	36.8	38.8	37.5	38.2	38.2	54
55	41.5	36.0	40.9	36.8	40.7	36.9	40.2	37.5	39.6	38.2	38.9	38.9	55
56	42.3	36.7	41.6	37.5	41.5	37.0	41.0	38.2	40.3	38.9	39.6	39.6	56
57	43.0	37.4	42.4	38.1	42.3	38.3	41.7	38.9	41.0	39.6	40.3	40.3	57
58	43.8	38.1	43.1	38.8	43.0	38.9	42.4	39.5	41.7	40.3	41.0	41.0	58
59	44.5	38.7	43.8	39.5	43.7	39.6	43.1	40.2	42.4	41.0	41.7	41.7	59
60	45.1	39.4	44.6	40.1	44.5	40.4	43.8	40.9	43.2	41.7	42.4	42.4	60
61	46.0	40.0	45.3	40.8	45.2	41.0	44.6	41.7	43.9	42.4	43.1	43.1	61
62	46.8	40.7	46.1	41.5	45.9	41.6	45.3	42.3	44.6	43.1	43.8	43.8	62
63	47.6	41.3	46.8	42.2	46.7	42.3	46.1	43.0	45.3	43.8	44.5	44.5	63
64	48.3	42.0	47.5	42.8	47.4	43.0	46.8	43.6	46.0	44.5	45.3	45.3	64
65	49.1	42.6	48.3	43.5	48.2	43.6	47.5	44.3	46.8	45.1	46.0	46.0	65
66	49.8	43.3	49.0	44.2	48.9	44.3	48.3	45.0	47.5	45.8	46.7	46.7	66
67	50.6	44.0	49.8	44.8	49.6	45.0	49.0	45.7	48.2	46.5	47.4	47.4	67
68	51.3	44.6	50.5	45.5	50.4	45.7	49.7	46.4	48.9	47.2	48.1	48.1	68
69	52.1	45.3	51.3	46.2	51.1	46.3	50.5	47.1	49.6	47.9	48.8	48.8	69
70	52.8	45.9	52.0	46.8	51.9	47.0	51.2	47.7	50.3	48.6	49.5	49.5	70
71	53.6	46.6	52.8	47.5	52.6	47.7	51.9	48.4	51.1	49.3	50.2	50.2	71
72	54.3	47.2	53.5	48.2	53.3	48.3	52.7	49.1	51.8	50.0	50.9	50.9	72
73	55.1	47.9	54.2	48.8	54.1	49.0	53.4	49.8	52.5	50.7	51.6	51.6	73
74	55.9	48.5	55.0	49.5	54.8	49.7	54.1	50.5	53.2	51.4	52.3	52.3	74
75	56.6	49.2	55.7	50.2	55.6	50.4	54.8	51.1	53.9	52.1	53.0	53.0	75
76	57.4	49.9	56.5	50.9	56.3	51.0	55.6	51.8	54.7	52.8	53.7	53.7	76
77	58.1	50.5	57.2	51.5	57.1	51.7	56.3	52.5	55.4	53.5	54.4	54.4	77
78	58.9	51.2	58.0	52.1	57.8	52.4	57.0	53.2	56.1	54.2	55.1	55.1	78
79	59.6	51.8	58.7	52.8	58.5	53.0	57.8	53.9	56.8	54.9	55.9	55.9	79
80	60.4	52.5	59.4	53.5	59.3	53.7	58.5	54.6	57.5	55.6	56.6	56.6	80
81	61.1	53.1	60.2	54.2	60.0	54.4	59.2	55.2	58.3	56.3	57.3	57.3	81
82	61.9	53.8	60.9	54.9	60.8	55.1	60.0	55.9	59.1	57.0	58.0	58.0	82
83	62.6	54.5	61.7	55.5	61.5	55.7	60.7	56.6	59.7	57.6	58.7	58.7	83
84	63.4	55.1	62.4	56.2	62.2	56.4	61.4	57.3	60.4	58.3	59.4	59.4	84
85	64.2	55.9	63.2	56.9	63.0	57.1	62.2	58.0	61.1	59.0	60.1	60.1	85
86	64.9	56.4	63.9	57.5	63.7	57.7	63.0	58.6	61.9	59.7	60.8	60.8	86
87	65.7	57.1	64.7	58.2	64.5	58.4	63.6	59.3	62.6	60.4	61.5	61.5	87
88	66.4	57.7	65.4	58.9	65.2	59.1	64.4	60.0	63.3	61.1	62.2	62.2	88
89	67.2	58.4	66.1	59.6	65.9	59.8	65.1	60.7	64.0	61.8	62.9	62.9	89
90	67.9	59.0	66.9	60.2	66.7	60.4	65.8	61.4	64.7	62.5	63.6	63.6	90
91	68.7	59.7	67.6	60.9	67.4	61.1	66.5	62.1	65.5	63.2	64.3	64.3	91
92	69.4	60.4	68.4	61.6	68.2	61.8	67.3	62.7	66.2	63.9	65.0	65.0	92
93	70.2	61.0	69.1	62.2	68.9	62.4	68.2	63.4	66.9	64.6	65.8	65.8	93
94	71.0	61.7	69.9	62.9	69.6	63.1	68.7	64.1	67.6	65.3	66.5	66.5	94
95	71.7	62.3	70.5	63.5	70.4	63.8	69.5	64.8	68.3	66.0	67.2	67.2	95
96	72.5	63.0	71.3	64.2	71.1	64.5	70.2	65.5	69.1	66.7	67.9	67.9	96
97	73.2	63.6	72.1	64.9	71.9	65.1	70.9	66.1	69.8	67.4	68.6	68.6	97
98	74.0	64.3	72.8	65.5	72.6	65.8	71.7	66.8	70.5	68.1	69.3	69.3	98
99	74.7	65.0	73.6	66.2	73.4	66.5	72.4	67.5	71.2	68.8	70.0	70.0	99
100	75.5	65.6	74.2	66.9	74.1	67.2	73.1	68.2	71.9	69.5	70.7	70.7	100
Diff.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Diff.
	49 Deg.		48 Deg.		4 $\frac{1}{2}$ Point		47 Deg.		45 Deg.		4 Points		

The Use and Explanation of the Table of Difference of Latitude and Departure

This is a Table larger and better contrived than any of this Nature yet Extant, giving the difference of Latitude and Departure, to any distance not exceeding 100, in Minutes and Tenth-parts, to every Degree and Quarter-point of the Compass; and may be used to a greater distance, being taken out at twice or thrice according to the quantity of the distance, as shall be shown in the Use.

The Course stands at the head and foot of the Table, to every Degree and Quarter-point of the Compass; at the head it begins at 1 deg. so 2 deg. $\frac{1}{4}$ Point, &c. increasing to 45 deg. or 4 Points. At the foot it begins at 45 deg. or 4 Points, so 46 deg. 47 deg. $4\frac{1}{4}$ Points, &c. increasing backwards to 90 deg. or 8 Points. The distance stands in the two outmost Columns, under the Title *Dist.* which on the Left-hand Page begins at 1, and runs to 50; on the Right-hand Page it begins at 51, and runs to 100. The difference of Latitude and Departure stands under the Course at the head, and over it at the foot of the Table.

The Use of the Table.

This Table is very useful in Navigation, especially in working a *Traverse*.

Example 1.

The Course and Distance given, to find the difference of Latitude and Departure by the Table.

Suppose a Ship sails N.N.E. $\frac{1}{4}$ East, 95 min. and the difference of Latitude and Departure required.

On the Right-hand Page (because the distance is above 50) and at the top because it is under 4 Points, look for $2\frac{1}{4}$ Points, which is the Course; under which, and against 95 the distance, under the Title *Lat.* stands 81. 5, which is 81 min. $\frac{5}{10}$, the difference of Latitude; and under the Title *Dep.* stands 48. 8, which is 48 min. $\frac{8}{10}$, which is the Departure required.

Example 2.

Suppose a Ship sail South 56 deg. Westerly 48 min. the Difference of Latitude and Departure required.

On the Left-hand Page (because the distance is less than 50) and at the bottom (because it is above 45 deg.) look for 56 deg. the Course; over which and against 48 the distance, over the Title *Lat.* stands 26. 8, that is 26 min. $\frac{8}{10}$, the difference of Latitude; and over the Title *Dep.* stands 39. 8, that is 39 min. $\frac{8}{10}$, the Departure required.

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Example.

Example.

Suppose a Ship sail North-west by North 160 min. and the difference of Latitude and Departure required by the Table.

On the Right-hand Page on the top, look for 3 Points, the Course. Now because the Table goes but to 100, take for 100 first; therefore under 3 Points, and against 100, under the Title *Lat.* stands 83. 1, that is 83 min. $\frac{1}{10}$ the difference of Latitude; and under the Title *Dep.* stands 55. 6, that is 55 min. $\frac{6}{10}$ the Departure; then for 60, under 3 Points, and against 60, under the Title *Lat.* stands 49. 9, that is 49 min. $\frac{9}{10}$ the difference of Latitude; and under the Title *Dep.* stands 33. 3, that is 33 min. $\frac{3}{10}$ the Departure, then add the difference of Latitude and Departure for 60, to the difference of Latitude and Departure for 100, and the sum is 133 min. the difference of Latitude, and 88 $\frac{2}{10}$ the Departure required.

This Table is also useful in the Resolution of the rest of the Problems of *Plain Sailing*, which for brevity sake are omitted; but the general Use of it is the exact working of a Traverse.

Example. 1

Suppose a Ship bound to a certain Port, sails S. E. by South, 49 min. then E. S. E. $\frac{1}{2}$ East, 52 min. then East by North $\frac{1}{2}$ East, 62 min. then S. S. W $\frac{1}{2}$ W, 57 min. then South $\frac{1}{2}$ East, 39 min. to find the difference of Latitude and Departure that the Ship hath made.

Set down the several Courses and Distances; first allow for Lee-way if any: Then proceed to look out the difference of Latitude and Departure from each Course and Distance (by the Directions before given) in the Table, placing them in their proper Columns, (*viz.*) If the Course be Northerly, the difference of Latitude must be put in to the North Column, if Southerly, in the South Column; if it be Easterly, the Departure must be put in the East Column; if Westerly, in the West Column as was before directed: Then having framed the Table, add up the Columns of difference of Latitude and Departure, and subtract the lesser difference of Latitude and Departure from the greater, and the Remainder is the difference of Latitude and Departure the Ship hath made.

The TABLE.

Courses.	Distance.	Diff. Lat.		Departure.	
		North	South	East.	West.
S. E. by S.	49		40.7	27.2	
E. S. E. $\frac{1}{2}$ E.	52		15.1	49.7	
E. by N. $\frac{1}{2}$ E.	62	06.1		61.7	
S. S. W. $\frac{1}{2}$ W.	57		50.3		26.8
S. $\frac{1}{2}$ E.	39		38.8	03.8	
		06.1	44.9	142.4	26.8
			6.1	26.8	
		1138.8	115.6		

The whole difference of Latitude is 138 $\frac{8}{10}$ South, the Departure 115 $\frac{6}{10}$ East.

The Use of the Table.

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The Course being given in degrees, which often happens by reason of Allowance for the Variation of the Compass, and in the like Cases.

Suppose a Ship bound to a certain Port, sails North-Westerly 34° , Min. (or Miles) 65. Then North-West 67° , Min. 56. Then South-West 78° , Min. 48. Then North-East 23° , Min. 54. Then North-East 6° , Min. 36, and the difference of Latitude and Departure required.

The T A B L E.

Courses.	Distance.	Diff. Lat.		Departure.	
		North	South	East.	West.
N. W. 34°	65	53.9			36.3
N. W. 67°	56	21.9			51.5
S. W. 78°	48		10.0		47.0
N. E. 32°	54	49.7		21.1	
N. E. 06°	36	35.8		03.8	
		161.3	10.0	24.9	134.8
		10.0			24.9
		151.3			109.9

The whole difference of Latitude is $151 \frac{1}{10}$. North, the Departure $109 \frac{9}{10}$. West.

A Journal of our Voyage. intended by God's Permission, from the Lizard, in the Latitude 50 deg. 00 min. North, Longitude (from the Pike of Tineriff) 12 deg. 37. min. to the Island of Barbadoes, in the Latitude 13 deg. 12 min. N. Longitude 319 deg. 40 min. The Difference of Longitude between the Lizard and Barbadoes is 52 deg. 57 min. the Course S. W. $\frac{1}{2}$, Distance 2821 min. March 22 day 1714. The Lizard bears North, distant 30 min.

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Days.

Days.	Month & Latit. by Observ.	The Course Corrected.	Dist. in min.	North.	South- ing. min.	East- ing. min.	West- ing. min.	Lat. by reckon. D. M.	East Diff. min.	West Long. min.
22	March	Lizard South.	30		30.0			49.30		
23		South-West.	112		79.2		79.2	48.11		120.5
24	47° 00'	S.W. by S. $\frac{1}{2}$ W.	72		55.6		45.7	47.15		68.1
		Correction by Observ.			15.0		11.0	47.00		16.0
25		S.W. by South	96		79.8		53.3	45.40		75.2
26		S.W. by South	79		65.7		43.9	44.34		62.8
27	42 37	S.W. by South	134		114.4		76.7	42.39		106.2
28		S. S. W. $\frac{1}{4}$ W.	129		110.7		66.3	40.48		88.8
29		S. S. W.	70		61.5		27.6	39.41		36.4
30	37 44	S. S. W. $\frac{1}{2}$ W.	109		90.0		8.00	38.11		62.0
		Correction by Observ.			27.0		16.0	37.44		20.0
1	April	South-West.	85		60.4		60.1	36.44		75.0
2		W. S. W.	20		7.6		18.5	36.34		24.1
3		S. by W. $\frac{1}{2}$ W.	32		30.6		9.3	36.05		11.9
4	34 10	South by W.	120		117.7		23.4	34.07		27.9
		Correct. by Obser.	3.			1.0		34.10	1.0	
5		S. by W. $\frac{1}{2}$ W.	164		156.9		47.6	31.33		56.7
6	29 37	S. S. W.	125		115.5		47.9	29.37		55.9
7		S.W. by South	110		91.4		61.2	28.06		69.5
8		S.W. by South	122		101.4		67.8	26.25		76.2
9	24 43	South-West	116		82.0		82.0	25.03		91.0
		Correction by Observ.			20.0		11.0	24.43		12.0
10		South-West	97		68.6		68.6	23.34		75.0
11		South-West	96		67.9		67.9	22.26		74.0
12		South-West	114		80.6		80.6	21.05		88.0
13		South-West	118		83.5		83.5	19.41		89.0
14		S. W. by W.	110		61.2		91.4	18.40		96.2
15		W. S. W.	91		34.8		84.1	18.05		89.4

How to keep a Journal at Sea.

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Days.	Month & Latit. by Observat.	The Course Corrected.	Diff. in min.	North.	South- ing min.	East- ing min.	West- ing min.	Lat. by reckon D. M.	East Diff. min.	West Long. min.
	1706.		<i>brought from the other side.</i>					18.05	1.0	1667.3
16	April.	W. S. W.	91		34.8		84.1	17.30		87.0
17		W. S. W.	84		32.1		77.6	16.58		82.0
18		W. S. W.	107		41.0		98.9	16.17		103.7
19		W. S. W.	103		39.5		95.2	15.37		99.0
20	14. 43	W. S. W.	110		44.4		107.2	14.53		111.0
		Correction by Observ.			10.0		15.9	14.43		16.0
21		W. by S.	210		21.5		107.9	14.21		114.1
22		W. by S.	120		23.4		117.7	13.58		119.1
23		W. by S.	106		20.7		104.0	13.37		108.7
24		W. by S.	100		19.5		94.1	13.17		103.8
25		W. by S.	120		23.4		117.7	12.54		118.7
26	13° 12'	W. by N.	100	19.5			98.1	13.14		103.1
27		West.	130				130.0	13.12		133.5
28		West.	136				136.0	13.12		135.0
29	13° 12'	West.	69				69.0	13.12		70.8

The whole difference of Longitude is 3177.6, or 3178 min. which is 52 deg. 58 min. Westerly.

The Explanation of this Journal.

In this *Journal* there are eleven Columns; the first contains the *Days* of the *Month*; the second the *Month* of the *Year*, and *Latitude* by *Observation*; the third, the *Course Corrected*, by the allowance for *Lee-way*, or for the *Variation* of the *Compass*, if there be any; the fourth, the *Distance sailed*; the fifth, sixth, seventh, and eighth, the *Northing*, *Southing*, *Easting*, and *Westing*, being the Difference of *Latitude* and *Departure* of the several *Courses* and *Distances*; the ninth, the *Latitude* by *Dead-Reckoning*; the tenth, the *East Diff. Longitude*; the eleventh, the *West Diff. Longitude*.

Here I would advise all that are desirous to give a good account of their *Reckoning*, to any that have Reason or Authority to demand it, that they keep a particular account of that which they take off the *Log-Board* every Day at Noon, either in the same Book where they keep their *Reckoning*, or else in a Book distinctly for that purpose, called a *Log-Book*.

Now

Now the Manner of proceeding in this Journal, by the help of the Table of Latitude and Departure is very facile, as follows: The 22^d of March at Noon, I find the *Lizard* to bear North, and to be distant about 10 Leagues, or 30 Miles or Minutes; therefore I am to the Southward of the *Lizard* 30', which 30' I place in the South Column, and that makes my Latitude $49^{\circ} 30'$.

The 23^d day my Course is S. W. and the Distance 112', to find the Difference of Latitude and Departure by the Table of Latitude and Departure, according to Prob. 1. The Difference of Latitude is 79.2, and the Departure 79.2: Because the Course is South-Westerly, I place the Diff. Lat. in the South Column, and my Departure in the West Column, 79', or $1^{\circ} 19'$ subtracted from $40^{\circ} 30'$, gives the Latitude $48^{\circ} 11'$.

How to find the Difference of Longitude.

To find the Difference of Longitude in the two last Columns, you have both Latitudes $48^{\circ} 11'$, and $49^{\circ} 30'$ (the present Latitude and the Latitude of the Day before) and the Course S. W. by which you may find the Diff. Longitude, according to the Proportion in Chap. 6. Prob. 3. of *Mercator's Sailing*; saying, *As Radius to the Meridional Diff. Long* This Proportion being wrought by the Logarithms, or *Gunter's Scale* which may serve in this case) you will find the Diff. Longitude 120' which place in the West Column, because your Course is Westerly.

The 24th Day is wrought after the manner of the 23^d, having the Course and Distance given to find the Diff. Latitude, Departure, and Diff. Longitude as was shewed before.

How to correct your Reckoning by Observation of the Latitude.

On the 24th of March, by a good Observation, I find my Latitude to be 47° , whereas by my Reckoning I should be in the Lat. $47^{\circ} 15'$, so that the difference is 15' more Southerly: Therefore to correct my Latitude, I place 15' in the South Column, which subtracted from $47^{\circ} 15'$, makes my Latitude by Reckoning to agree with the Observation. To Correct your Departure, you must consider, whether the Fault may be imputed to your Course, or to your Distance: If your Course be well steered, and you find no Current, nor any Variation of the Compass, then your distance is faulty; but if you cannot trust to the Course steered, then your best way is to correct your Latitude only, not meddling with your Departure. If there be a Current, and you know which way the Current sets, and how fast, then find the Diff. Lat. and Departure of the Current, and add or subtract that Latitude and Departure to or from the Ship's Diff. Lat. and Departure, according as the Current doth further or hinder your Ship in her Course. But if you only by some probable Reason conjecture there is a Current, then give what allowance you think meet in Diff. Lat. and Departure, and see if that will reform your Reckoning in your Latitude. If so, you have guessed well; but if it will not, it is to be supposed that you are mistaken in your conjecture, or that there is some other cause of this Error in your Reckoning.

If the Compass varies (as most commonly it doth) then finding what the Variation is, and which way it is, you must allow it in the Ship's Course. But if you cannot impute the Error to any of these, (as I said before) the Distance is faulty; and this is that which usually makes the Difference between the Lat. observed, and the Lat. by your Reckoning; And this I take to be the Cause of the Error this 24th day of March, and generally in this Reckoning.

Now

Now to correct your Departure and Diff. Longitude, you must add up the North, South, East and West Columns, from the Day that you correct, to the beginning of your Journal-Tables: If it be the first Correction you have made, or from the Day of Correction to the last Correction; if it be the second, third, fourth Correction, &c. then subtract the Sums of the North and South Columns from each other, and likewise of the East and West, and say by the Rule of Proportion: As the Diff. of the North and South Columns, to the Diff. of the East and West Columns; so is the Difference between the Latitudes by Observation and Reckoning, to the Diff. in the Departure, and for the Diff. between the Latitudes by Observation and Reckoning, to the Meridional Difference for those Latitudes; so is the Diff. in the Departure, to the Diff. in the Longitude.

Example. The 24th day you will find the Sum of the North Column 00, the Sum of the South Column (leaving out 15, the Error) 164.8, min. and therefore their Diff. is 164. 8. The Sum of the East Column is 00 min. of the West Column 124. 9. and their Diff. 124. 9. Then the Operation by the Logarithm will be,

As the Diff. of the North and South Columns,	164.8,	Co. Ar.
To the Diff. of the East and West Columns	124.9.	7.78304
So is the Diff. between the two Latitudes,	15.0,	2.09656
To the Difference in the Departure.		1.17609
	11	71 05569

Place this 11 min. in the West Column, because the Sum of the West Column exceeds the Sum of the East Column,

In this Operation we neglect the Tenths of the Departure, as not to be regarded.

The Operation for the Difference in the Longitude.

The two Latitudes are 47 deg. 15 min. and 47 deg. 00 min. by which in the Table of Meridional Parts you will find the Meridional Diff. Lat. 22. min. Therefore.

As the Diff. between the two Latitudes,	15'	Co. Ar.
To the Merid. Diff. of those Lat.	22	8.82391
So is the Diff. in the Departure,	11	1.34242
To the Diff. in the Longitude,	16	1.04139
		71.20772

This 16' is placed in the West Column, because the Departure is Westerly.

After the same manner are the Corrections made in this Journal on the 30th of March, the 4th, the 9th, and the 20th days of April, the Error being supposed to be in the estimate Distance.

If your Ship sail several Courses in 24 hours, you must find your Diff. Latitude and Departure, working a Traverse, according to Prob. 7. in the Use of the Table of Latitude and Departure; your Diff. Lat. will give you what Latitude the Ship is in, then have you Two Latitudes, viz. the Lat. the Ship was in the day before at Noon, and the Lat. the Ship is now in, by which you may find the Meridional Diff. Lat. by the Table of Merid. Parts according to Chap. 6. Prob. 1. of Mercator's Sailing. Then for your Diff. Longitude, say,

As the Diff. Latitude found by the Traverse,

To the Diff. Latitude in Meridional Parts:

So is the Departure found by the Traverse

To the Diff. Longitude for that Traverse.

To

270 The Use of the Table of Logarithms.

To find the whole Diff. Longitude of the two Ports between which you make your Voyage.

Add up the Columns of East and West diff. of Longitude, and subtract the one from the other, the Remainder reduced in degrees and minutes, is the Diff. Longitude sought.

In this Journal, the Diff. of the East and West Columns of Longitude is 3177.6 , or $3178'$, which reduc'd into degrees and minutes, makes $52^{\circ} 58'$, the Diff. Long. between the *Lizard* and the *Barbadoes*.

The Use of the Table of Ten Chiliads, or Ten Thousand Logarithms.

1. **A** Ny Number given under 10000? To find the Logarithm thereof. The Left-hand Column of every Page contains Numbers increasing in their natural Order from 1 to 999. The other five Columns of each Page contains the Logarithm, of all Numbers, from 1 to 9999. These Columns on the Left-hand Page are distinguished with the Figures, 0, 1, 2, 3, 4; those on the Right-hand Page with 5, 6, 7, 8, 9.

The Numbers in the Left-hand Column, by the supply of those Figures on the top of the other Columns, do extend to 9999, and are to be read cross both Pages.

If the Number propounded to find its Logarithms consist of one Place; as suppose, you were to find the Logarithm of (7,) look for (7) among the Figures on the top of the Columns, and right against (0) in the Left-hand Column, and under (7) you will find 0.8450980 , which is the Log. of 7.

If the Number propounded consist of two Places, as (68;) look the first Figure (6) in the Left-hand Column, and the last Figure (8) at the top of the Page; then right against (6) and under (8) you will find 1.8325089 , which is the Log. of 68.

If the Number consist of three Places, as 574, look for the two first Figures (57) in the Left-hand Column, and the last Figure (4) at the top of the Page; then right against (57) and under (4) you will find 2.7589119 , which is the Log. of 574.

If the Number consist of four Places, as 9499, look the three first Figures (949) in the Left-hand Column, and the last Figure (9) at the top of the Page; so right against (949) and under (9) you will find 3.9776779 , which is the Log. of 9499.

2. A Log. being given, to find the correspondent Number.

Note, If the first Figure of the given Log. be (0), the Number sought consists of one Place; if it be (1), it consists of two Places; if it be (2) of three Places; if it be (3), of four Places.

Let the Log. be 0.9030900 ; this Log. will be found in the first Line of the Table against (0); for if you look in the first Line, crossing both Pages, under (8) upon the Right-hand Page, you will find the given Log. which shews that (8) is the Number sought.

Let the Log. be 1.9190781 ; look down the second Column of the left hand Page among those Log's, and you will find the nearest, being less than the given Log. to be 1.9030900 , and the Number against it in the Left-hand Column is (8); then look cross the Pages in the same Line against (8), and under (3) at the top of the Page, you will find the Log. given, therefore the Number sought is 83.

Let the Log. be 2.8318691 ; look down the second Column of the Left-hand Page, until you find a Log. being the nearest less than the given Log. which will be 2.8260748 , and the Number against it, in the Left-hand Column, is 67; then look

cross

The Use of the Table of Logarithms. 271

cross both Pages in the same Line against 67, and under 9 (at the top of the Page) you will find the given Log. therefore the Number sought is 679.

Let 3.9802761 be the Log. given, look down the second Column as before, and you will find the nearest less to be 3.9800034, and the Number against it 954; and crossing the Pages, as before directed, under (6) you will have the given Log. Therefore the Number sought is 9556.

Let the Log. given be 3.9664379; if you look in the Table, according to the former Directions, you cannot find any Log. the same with this here given; and this is commonly the Case in the Use of these Tables; but then you must find the nearest, being less than the Log. given which is 3.9664233, and the Number answering thereto is 9256, which is the nearest in whole Numbers.

The Use of the Table of Artificial, or Logarithmical Sines, Tangents, and Secants.

THIS Table contains the Logarithmical Sines, Tangents and Secants, of every Degree and Minute of the Quadrant.

1. To find the Sine, Tangent, or Secant of any Degree and Minute.

If the Degree be less than 45, your Sine, Tangent, or Secant, is found in those Columns which are distinguished by the Words (*Sine*) (*Tang.*) (*Secant*) at the head of the Table.

But if the Degrees exceeds 45 then your Sine, Tangent or Secant, is found in those Columns which are distinguished by these Words (*Sine*) (*Tang.*) (*Secant*) at the foot of the Table.

Suppose you were to find the Log. Sine, Tangent, or Secant of $32^{\circ} 12'$: Look for 32° at the head of the Table, and upon the Left-hand Page, in the Column of Minutes, under the Letter (M) you will find 12, and against 12, and under *Sine* at the head of the Table, you will find 9.7266264, which is the Log. Sine of $32^{\circ} 12'$; and against 12, and under (*Tang.*) you have 9.7991569, the Log. Tang. of $32^{\circ} 12'$; and against 12, and under (*Secant*) you have 10.0725305, the Log. Secant of $32^{\circ} 12'$.

Suppose you were to find the Log. Sine, Tangent or Secant of $37^{\circ} 47'$: Look for 37 deg. at the head of the Table, and upon the Right-hand Page (because the Minutes exceed 30) in the Column of Min. under (M) you must look for 47 min. and against 47 min. and under (*Sine*) at the head of the Table, you will find 9.7872317, the Sine of 37 deg. 47 min. And against 47, and under (*Tang.*) you will find 9.8894214, the Tang. of 37 deg. 47 min. And against 47, and under (*Secant*) you will find 10.1021897, the Secant of 37 deg. 47 min.

Suppose you were to find the Log. Sine, Tangent, or Secant of $64^{\circ} 15'$: Turn to 64° at the Foot of the Table, and upon the Right-hand Page, in the Column of Minutes, over the Letter (M) look upwards for 15'; against 15', and over (*Sine*) at the foot of the Table, you will find 9.9545793 the Sine $64^{\circ} 15'$; and against 15', and over (*Tang.*) you will find 10.3166443 the Tangent of $64^{\circ} 15'$. And against 15', and over (*Secant*) you will find 10.3620649, the Secant of $64^{\circ} 15'$.

Suppose you were to find the Log. Sine, Tangent, or Secant of $78^{\circ} 45'$: Turn to 78° at the foot of the Table, and upon the Left-hand Page, (because the Minutes

exceed 30) in the Column of Minutes, over (M.) look for 45, against 45, and over (Sine) you find the Sine of $78^{\circ} 45'$ to be 9.9915739, and the Tangent in the same Line over (Tang.) to be 10.7013382; and the Secant over (Secant) to be 10.7097643.

2. A Log. Sine, Tangent, or Secant being given; to find the Degrees and Minutes answering thereto.

This is but the Converse of the former; but that you may the more readily turn to the deg. and min. required, take this brief Direction.

If it be a Sine, and the five first Figures be less than 9.8494, or a Tangent less than Radius, or 10.0000000; or a Secant, and the six first Figures less than 10.1505; then it is a Sine, Tangent, or Secant of less than 45° , and is to be sought in those Columns distinguished with (Sine) (Tang.) (Secant) at the Head of the Table; but if the Sine, Tangent, or Secant, exceed these respective Numbers, then the Degrees answering thereto are more than 45° , and they are to be found in those Columns distinguished by (Sine) (Tang.) (Secant) at the foot of the Table.

Suppose you were to find the Degree and Minute corresponding to this Sine 9.7035329: This being less than 45, I run over the Columns of Sines distinguished by (Sine) at the top, and under 30° , and against 21', I find the given Sine.

Suppose I were to find the Degree and Minute corresponding to this Tang. 10.386293: This being greater than 45, I run over the Columns of Tangents, distinguished by (Tang.) at the foot of the Table, and over 67° , and against 39' I find the nearest less, viz. 10.3860000, and therefore the deg. and min. corresponding are $67^{\circ} 39'$.

1. Note; If you are to find the Sine-Complement, Tangent-Complement, or Secant-Complement of any Degree and Minute; as suppose you were to find the Sine-Complement of $39^{\circ} 17'$, subtract $39^{\circ} 17'$ from $90^{\circ} 00'$, and look the Sine of the Remainder, (or Complement to 90°) viz. the Sine of $50^{\circ} 43'$.

2. Note, If you are to find the Sine, Tangent, or Secant of any Number of Degrees and Minutes exceeding 90; as suppose you were to find the Tangent, of $127^{\circ} 39'$ subtract $127^{\circ} 39'$ from $180^{\circ} 00'$ and find the Tangent of the Remainder, viz. the Tangent $52^{\circ} 21'$, which is also the Tangent $127^{\circ} 39'$, as was required.

TABLE OF

Logarithms,

FOR

Numbers increasing in their Natural Order from
1 to 10000.

WITH

A TABLE of Artificial SINES, TANGENTS,
and SECANTS, the Radius 10.000000, and to every
Degree and Minute

OF THE

QUADRANT.

Carefully Corrected.

LONDON: Printed for Richard Mount, at
Postern-Row on Tower-Hill, 1717.

A TABLE of Logarithms,

Num.	0	1	2	3	4
0	0.0000000	0.0000000	0.3010300	0.4771212	0.6020600
1	1.0000000	1.0413927	1.0791812	1.1139433	1.1461280
2	1.3010300	1.3222193	1.3424227	1.3617278	1.3802112
3	1.4771212	1.4913617	1.5051500	1.5185139	1.5314789
4	1.6020600	1.6127838	1.6232493	1.6334684	1.6434527
5	1.6989700	1.7075702	1.7160033	1.7242759	1.7323937
6	1.7781512	1.7853298	1.7923917	1.7993403	1.8061800
7	1.8450980	1.8512583	1.8573323	1.8633228	1.8692317
8	1.9030900	1.9084850	1.9138138	1.9190781	1.9242793
9	1.9542423	1.9590414	1.9637878	1.9684829	1.9731278
10	2.0000000	2.0043214	2.0086002	2.0128372	2.0170333
11	2.0413927	2.0453230	2.0492180	2.0530784	2.0569048
12	2.0791812	2.0827854	2.0863598	2.0899051	2.0934217
13	2.1139433	2.1172713	2.1205739	2.1238516	2.1271048
14	2.1461280	2.1492191	2.1522883	2.1553360	2.1583625
15	2.1760912	2.1789769	2.1818436	2.1846914	2.1875207
16	2.2041200	2.2068259	2.2095150	2.2121876	2.2148438
17	2.2304489	2.2329961	2.2355284	2.2380461	2.2405492
18	2.2552725	2.2576786	2.2600714	2.2624511	2.2648178
19	2.2787536	2.2810333	2.2833012	2.2855573	2.2878017
20	2.3010300	2.3031960	2.3053513	2.3074960	2.3096301
21	2.3222193	2.3242824	2.3263358	2.3283796	2.3304138
22	2.3424227	2.3443923	2.3463530	2.3483048	2.3502480
23	2.3617278	2.3636120	2.3654880	2.3673559	2.3692158
24	2.3802112	2.3820170	2.3838153	2.3856063	2.3873898
25	2.3979400	2.3996737	2.4014005	2.4031205	2.4048337
26	2.4149733	2.4166403	2.4183013	2.4199557	2.4216039
27	2.4313637	2.4329693	2.4345689	2.4361626	2.4377505
28	2.4471580	2.4487063	2.4502491	2.4517864	2.4533183
29	2.4623980	2.4638930	2.4653828	2.4668676	2.4683473
30	2.4771212	2.4785665	2.4800069	2.4814426	2.4828736
31	2.4913617	2.4927604	2.4941546	2.4955443	2.4969296
32	2.5051500	2.5065050	2.5078559	2.5092023	2.5105450
33	2.5185139	2.5198280	2.5211381	2.5224442	2.5237464
34	2.5314789	2.5327544	2.5340261	2.5352941	2.5365584
35	2.5440680	2.5453071	2.5465426	2.5477747	2.5490033
36	2.5563025	2.5575302	2.5587086	2.5599056	2.5611014

from 1 to 10000.

Num.	5	6	7	8	9
0	0.6989700	0.7781312	0.8450980	0.9030900	0.9542425
1	1.1760912	1.2041200	1.2304489	1.2552725	1.2787536
2	1.3979400	1.4149733	1.4313637	1.4471580	1.4623980
3	1.5440680	1.5563025	1.5682017	1.5797836	1.5910646
4	1.6532125	1.6627578	1.6720978	1.6812412	1.6901961
5	1.7403627	1.7481880	1.7558748	1.7634280	1.7708520
6	1.8129133	1.8195439	1.8260748	1.8325089	1.8388491
7	1.8750612	1.8808136	1.8864907	1.8920946	1.8976271
8	1.9294189	1.9344984	1.9395192	1.9444827	1.9493900
9	1.9777236	1.9822712	1.9867717	1.9912261	1.9956352
10	2.0211893	2.0253058	2.0293838	2.0334237	2.0374265
11	2.0606978	2.0644580	2.0681858	2.0718820	2.0755469
12	2.0969100	2.1003705	2.1038037	2.1072099	2.1105897
13	2.1303337	2.1335389	2.1367205	2.1398791	2.1430148
14	2.16113680	2.1643528	2.1673173	2.1702617	2.1731862
15	2.1903317	2.1931246	2.1958996	2.1986571	2.2013971
16	2.2174839	2.2201081	2.2227165	2.2253093	2.2278867
17	2.2430380	2.2455127	2.2479732	2.2504200	2.2528530
18	2.2671717	2.2695129	2.2718416	2.2741578	2.2764618
19	2.2900346	2.2922561	2.2944662	2.2966652	2.2988531
20	2.3117538	2.3138672	2.3159703	2.3180633	2.3201463
21	2.3324384	2.3344537	2.3364597	2.3384565	2.3404441
22	2.3521825	2.3541084	2.3560258	2.3579348	2.3598355
23	2.3710678	2.3729120	2.3747483	2.3765770	2.3783979
24	2.3891661	2.3909351	2.3926969	2.3944517	2.3961993
25	2.4065402	2.4082399	2.4099331	2.4116197	2.4132997
26	2.4232459	2.4248816	2.4265112	2.4281348	2.4297522
27	2.4393327	2.4409091	2.4424797	2.4440448	2.4456042
28	2.4548448	2.4563660	2.4578818	2.4593925	2.4608978
29	2.4698220	2.4712917	2.4727064	2.4742162	2.4756712
30	2.4842998	2.4857214	2.4871384	2.4885507	2.4899585
31	2.4982303	2.4996871	2.5010594	2.5024271	2.5037907
32	2.5118834	2.5132176	2.5145477	2.5158738	2.5171959
33	2.5250448	2.5263393	2.5276299	2.5289167	2.5301997
34	2.5378191	2.5390761	2.5403295	2.5415792	2.5428254
35	2.5502283	2.5514500	2.5526682	2.5538830	2.5550944
36	2.5622929	2.5634811	2.5646661	2.5658478	2.5670263

A TABLE of Logarithms,

Num.	0	1	2	3	4
37	2.5682017	2.5693739	2.5705429	2.5717088	2.5728716
38	2.5797836	2.5809250	2.5820634	2.5831988	2.5843312
39	2.5910646	2.5921767	2.5932861	2.5943925	2.5954962
40	2.6020600	2.6031444	2.6042260	2.6053050	2.6063813
41	2.6138418	2.6148972	2.6159500	2.6170003	2.6180483
42	2.6223453	2.6234221	2.6245312	2.6256340	2.6267358
43	2.6334684	2.6344773	2.6354837	2.6364879	2.6374897
44	2.6434527	2.6444386	2.6454223	2.6464037	2.6473830
45	2.6532125	2.6541765	2.6551384	2.6560982	2.6570558
46	2.6627578	2.6637009	2.6646420	2.6655810	2.6665180
47	2.6720978	2.6730209	2.6739420	2.6748611	2.6757783
48	2.6812412	2.6821451	2.6830470	2.6839471	2.6848454
49	2.6901961	2.6910815	2.6919651	2.6928469	2.6937269
50	2.6989700	2.6998377	2.7007037	2.7015680	2.7024305
51	2.7070702	2.7084208	2.7092700	2.7101174	2.7109631
52	2.7160033	2.7168376	2.7176705	2.7185017	2.7193313
53	2.7242759	2.7250945	2.7259116	2.7267272	2.7275412
54	2.7323937	2.7331973	2.7339993	2.7347998	2.7355989
55	2.7403627	2.7411516	2.7419391	2.7427251	2.7435097
56	2.7481880	2.7489628	2.7497363	2.7505084	2.7512791
57	2.7558748	2.7566362	2.7573960	2.7581547	2.7589119
58	2.7634280	2.7641766	2.7649230	2.7656685	2.7664128
59	2.7708520	2.7715871	2.7723217	2.7730547	2.7737864
60	2.7781512	2.7788745	2.7795965	2.7803173	2.7810369
61	2.7853298	2.7860412	2.7867514	2.7874605	2.7881684
62	2.7923917	2.7930916	2.7937904	2.7944880	2.7951846
63	2.7993405	2.8000293	2.8007171	2.8014037	2.8020892
64	2.8061800	2.8068580	2.8075350	2.8082110	2.8088859
65	2.8129133	2.8135810	2.8142476	2.8149132	2.8155777
66	2.8195439	2.8202014	2.8208580	2.8215135	2.8221681
67	2.8260748	2.8267225	2.8273693	2.8280151	2.8286599
68	2.8325089	2.8331471	2.8337844	2.8344207	2.8350561
69	2.8388491	2.8394780	2.8401061	2.8407332	2.8413595
70	2.8450980	2.8457180	2.8463371	2.8469553	2.8475726
71	2.8512582	2.8518696	2.8524800	2.8530895	2.8536982
72	2.8573325	2.8579353	2.8585372	2.8591383	2.8597386
73	2.8633229	2.8639174	2.8645111	2.8651040	2.8656960

from 1 to 10000.

Num.	5	6	7	8	9
37	2.5740313	2.5751878	2.5763413	2.5774918	2.5786392
38	2.5854607	2.5865873	2.5877110	2.5888317	2.5899496
39	2.5965971	2.5976952	2.5987905	2.5998831	2.6009729
40	2.6074550	2.6085260	2.6095944	2.6106602	2.6117233
41	2.6180481	2.6190933	2.6201360	2.6211763	2.6222140
42	2.6283889	2.6294096	2.6304279	2.6314438	2.6324573
—	—	—	—	—	—
43	2.6384892	2.6394865	2.6404814	2.6414741	2.6424645
44	2.6483600	2.6493348	2.6503075	2.6512780	2.6522463
45	2.6580114	2.6589648	2.6599162	2.6608655	2.6618127
46	2.6674529	2.6683859	2.6693169	2.6702458	2.6711728
47	2.6766936	2.6776069	2.6785184	2.6794279	2.6803355
48	2.6857417	2.6866362	2.6875290	2.6884198	2.6893088
—	—	—	—	—	—
49	2.6946052	2.6954817	2.6963564	2.6972293	2.6981005
50	2.7032914	2.7041505	2.7050079	2.7058637	2.7067178
51	2.7118072	2.7126497	2.7134905	2.7143297	2.7151673
52	2.7201593	2.7209857	2.7218106	2.7226339	2.7234557
53	2.7283538	2.7291647	2.7299743	2.7307822	2.7315888
54	2.7363965	2.7371926	2.7379873	2.7387805	2.7395723
—	—	—	—	—	—
55	2.7442930	2.7450748	2.7458552	2.7466342	2.7474118
56	2.7520484	2.7528164	2.7535830	2.7543483	2.7551123
57	2.7596678	2.7604225	2.7611758	2.7619278	2.7626786
58	2.7671558	2.7678976	2.7686381	2.7693773	2.7701153
59	2.7745170	2.7752462	2.7759743	2.7767012	2.7774268
60	2.7817554	2.7824526	2.7831887	2.7839036	2.7846173
—	—	—	—	—	—
61	2.7888751	2.7895807	2.7902852	2.7909885	2.7916906
62	2.7958800	2.7965743	2.7972675	2.7979596	2.7986506
63	2.8027737	2.8034571	2.8041394	2.8048206	2.8055008
64	2.8095597	2.8102325	2.8109043	2.8115750	2.8122447
65	2.8162413	2.8169038	2.8175654	2.8182259	2.8188854
66	2.8228216	2.8234742	2.8241258	2.8247765	2.8254261
—	—	—	—	—	—
67	2.8293035	2.8299467	2.8305887	2.8312297	2.8318698
68	2.8356906	2.8363241	2.8369567	2.8375884	2.8382192
69	2.8419848	2.8426092	2.8432328	2.8438554	2.8444772
70	2.8481891	2.8488047	2.8494194	2.8500332	2.8506462
71	2.8543060	2.8549130	2.8555191	2.8561244	2.8567289
72	2.8603380	2.8609366	2.8615344	2.8621314	2.8627275
73	2.8662873	2.8668778	2.8674675	2.8680564	2.8686444

A T A B L E of Logarithms.

Num.	0	1	2	3	4
74	2.8692317	2.8698182	2.8704039	2.8709888	2.8715729
75	2.8750613	2.8756399	2.8762178	2.8767950	2.8773713
76	2.8808136	2.8813846	2.8819550	2.8825245	2.8830933
77	2.8864907	2.8870544	2.8876173	2.8881795	2.8887410
78	2.8920946	2.8926510	2.8932067	2.8937618	2.8943161
79	2.8976271	2.8981765	2.8987252	2.8992732	2.8998205
80	2.9030900	2.9036325	2.9041744	2.9047155	2.9052560
81	2.9084850	2.9090208	2.9095560	2.9100905	2.9106244
82	2.9138138	2.9143431	2.9148718	2.9153998	2.9159272
83	2.9190781	2.9196010	2.9201233	2.9206450	2.9211660
84	2.9242793	2.9247960	2.9253121	2.9258276	2.9263424
85	2.9294189	2.9299296	2.9304396	2.9309490	2.9314579
86	2.9344984	2.9350031	2.9355073	2.9360108	2.9365137
87	2.9395192	2.9400181	2.9405165	2.9410142	2.9415114
88	2.9444827	2.9449759	2.9454686	2.9459607	2.9464523
89	2.9493900	2.9498777	2.9503648	2.9508514	2.9513375
90	2.9542425	2.9547248	2.9552005	2.9556877	2.9561684
91	2.9590414	2.9595184	2.9599948	2.9604708	2.9609462
92	2.9637878	2.9642596	2.9647309	2.9652017	2.9656720
93	2.9684829	2.9689497	2.9694159	2.9698816	2.9703469
94	2.9731278	2.9735896	2.9740509	2.9745117	2.9749720
95	2.9777236	2.9781805	2.9786369	2.9790929	2.9795484
96	2.9822712	2.9827234	2.9831750	2.9836263	2.9840770
97	2.9867717	2.9872192	2.9876663	2.9881128	2.9885589
98	2.9912261	2.9916690	2.9921115	2.9925535	2.9929951
99	2.9956352	2.9960736	2.9965117	2.9969492	2.9973864
100	3.0000000	3.0004341	3.0008677	3.0013009	3.0017337
101	3.0043214	3.0047511	3.0051805	3.0056094	3.0060379
102	3.0086002	3.0090257	3.0094509	3.0098756	3.0102999
103	3.0128372	3.0132587	3.0136796	3.0141003	3.0145205
104	3.0170333	3.0174507	3.0178677	3.0182843	3.0187005
105	3.0211893	3.0216027	3.0220157	3.0224284	3.0228406
106	3.0253059	3.0257154	3.0261245	3.0265333	3.0269416
107	3.0293838	3.0297895	3.0301948	3.0305997	3.0310043
108	3.0334227	3.0338257	3.0342273	3.0346284	3.0350293
109	3.0374265	3.0378247	3.0382226	3.0386202	3.0390173
110	3.0413927	3.0417873	3.0421816	3.0425755	3.0429691

from 1 to 10000.

Num	5	6	7	8	9
74	2.8721563	2.8727388	2.8733206	2.8739016	2.8744818
75	2.8779469	2.8785218	2.8790959	2.8796692	2.8802418
76	2.8836615	2.8842288	2.8847953	2.8853612	2.8859263
77	2.8893017	2.8898617	2.8904210	2.8909796	2.8915374
78	2.8948696	2.8954225	2.8959747	2.8965262	2.8970770
79	2.9003671	2.9009131	2.9014583	2.9020029	2.9025468
80	2.9057959	2.9063350	2.9068735	2.9074114	2.9079485
81	2.9111576	2.9116901	2.9122220	2.9127533	2.9132839
82	2.9164539	2.9169800	2.9175055	2.9180303	2.9185545
83	2.9216865	2.9222063	2.9227254	2.9232440	2.9237620
84	2.9268367	2.9273704	2.9278834	2.9283958	2.9289077
85	2.9319661	2.9324738	2.9329808	2.9334873	2.9339932
86	2.9370161	2.9375179	2.9380191	2.9385197	2.9390198
87	2.9420080	2.9425041	2.9429996	2.9434945	2.9439889
88	2.9469433	2.9474337	2.9479236	2.9484130	2.9489018
89	2.9518230	2.9523080	2.9527924	2.9532763	2.9537597
90	2.9566486	2.9571287	2.9576073	2.9580858	2.9585639
91	2.9614211	2.9618955	2.9623693	2.9628427	2.9633155
92	2.9661417	2.9666110	2.9670797	2.9675480	2.9680157
93	2.9708116	2.9712758	2.9717396	2.9722028	2.9726656
94	2.9754318	2.9758911	2.9763500	2.9768083	2.9772662
95	2.9800034	2.9804579	2.9809119	2.9813655	2.9818186
96	2.9845273	2.9849771	2.9854265	2.9858753	2.9863238
97	2.9890046	2.9894498	2.9898946	2.9903388	2.9907827
98	2.9934362	2.9938769	2.9943171	2.9947569	2.9951963
99	2.9978231	2.9982593	2.9986951	2.9991305	2.9995655
100	3.0021661	3.0025980	3.0030295	3.0034605	3.0038911
101	3.0064660	3.0068937	3.0073209	3.0077478	3.0081742
102	3.0107239	3.0111473	3.0115704	3.0119931	3.0124154
103	3.0149403	3.0153597	3.0157787	3.0161973	3.0166155
104	3.0191163	3.0195317	3.0199467	3.0203613	3.0207755
105	3.0232324	3.0236639	3.0240750	3.0244857	3.0248960
106	3.0273496	3.0277572	3.0281644	3.0285712	3.0289777
107	3.0314685	3.0318123	3.0322157	3.0326188	3.0330214
108	3.0354897	3.0358298	3.0362294	3.0366289	3.0370279
109	3.0394141	3.0398105	3.0402066	3.0406023	3.0409977
110	3.0433623	3.0437551	3.0441476	3.0445398	3.0449315

A TABLE of Logarithms,

Num.	0	1	2	3	4
111	3.0453230	3.0457140	3.0461048	3.0464952	3.0468852
112	3.0492180	3.0496056	3.0499928	3.0503797	3.0507663
113	3.0530784	3.0534626	3.0538464	3.0542299	3.0546130
114	3.0569048	3.0572856	3.0576661	3.0580462	3.0584260
115	3.0606978	3.0610753	3.0614525	3.0618293	3.0622058
116	3.0644580	3.0648322	3.0652061	3.0655797	3.0659530
117	3.0681859	3.0685569	3.0689276	3.0692980	3.0696681
118	3.0718820	3.0722499	3.0726175	3.0729847	3.0733517
119	3.0755470	3.0759118	3.0762762	3.0766404	3.0770043
120	3.0791812	3.0795430	3.0799045	3.0802656	3.0806265
121	3.0827854	3.0831441	3.0835026	3.0838608	3.0842187
122	3.0863598	3.0867157	3.0870712	3.0874264	3.0877814
123	3.0899051	3.0902580	3.0906107	3.0909631	3.0913151
124	3.0934217	3.0937718	3.0941216	3.0944711	3.0948204
125	3.0969100	3.0972573	3.0976043	3.0979511	3.0982975
126	3.1003705	3.1007151	3.1010593	3.1014033	3.1017471
127	3.1038037	3.1041455	3.1044871	3.1048284	3.1051694
128	3.1072100	3.1075491	3.1078880	3.1082266	3.1085650
129	3.1105897	3.1109262	3.1112625	3.1115985	3.1119343
130	3.1139433	3.1142773	3.1146110	3.1149444	3.1152776
131	3.1172713	3.1176027	3.1179338	3.1182647	3.1185954
132	3.1205739	3.1209023	3.1212314	3.1215598	3.1218880
133	3.1238516	3.1241780	3.1245042	3.1248301	3.1251558
134	3.1271048	3.1274288	3.1277525	3.1280760	3.1283993
135	3.1303338	3.1306553	3.1309767	3.1312978	3.1316187
136	3.1335389	3.1338581	3.1341771	3.1344958	3.1348144
137	3.1367206	3.1370374	3.1373541	3.1376705	3.1379867
138	3.1398791	3.1401937	3.1405080	3.1408222	3.1411361
139	3.1430148	3.1433271	3.1436392	3.1439511	3.1442628
140	3.1461280	3.1464381	3.1467480	3.1470577	3.1473671
141	3.1492191	3.1495270	3.1498347	3.1501422	3.1504494
142	3.1522883	3.1525941	3.1528996	3.1532049	3.1535100
143	3.1553360	3.1556396	3.1559430	3.1562462	3.1565491
144	3.1583625	3.1586640	3.1589653	3.1592663	3.1595672
145	3.1613680	3.1616674	3.1619666	3.1622656	3.1625644
146	3.1643528	3.1646502	3.1649474	3.1652443	3.1655411
147	3.1673173	3.1676127	3.1679078	3.1682027	3.1684975

from -1 to 10000.

Num	5	6	7	8	9
111	3.0472749	3.0476642	3.0480532	3.0484418	3.0488301
112	.0511525	.0515384	.0519239	.0523091	.0526939
113	.0549958	.0553783	.0557605	.0561423	.0565237
114	.0588055	.0591846	.0595634	.0599419	.0603200
115	.0625820	.0629578	.0633333	.0637085	.0640834
116	.0663259	.0666985	.0670708	.0674428	.0678145
117	3.0700379	3.0704073	3.0707765	3.0711453	3.0715138
118	.0737183	.0740847	.0744507	.0748164	.0751818
119	.0773679	.0777312	.0780941	.0784568	.0788192
120	.0809870	.0813473	.0817073	.0820669	.0824263
121	.0845763	.0849336	.0852906	.0856473	.0860037
122	.0881361	.0884905	.0888446	.0891984	.0895519
123	3.0916669	3.0920185	3.0923696	3.0927206	3.0930712
124	.0951693	.0955180	.0958664	.0962146	.0965624
125	.0986437	.0989896	.0993353	.0996806	.1000257
126	.1020905	.1024337	.1027766	.1031192	.1034616
127	.1055102	.1058506	.1061909	.1065308	.1068705
128	.1089031	.1092410	.1095785	.1099159	.1102529
129	3.1122698	3.1126050	3.1129400	3.1132746	3.1136091
130	.1156105	.1159432	.1162756	.1166077	.1169336
131	.1189257	.1192559	.1195858	.1199154	.1202448
132	.1222159	.1225435	.1228709	.1231981	.1235250
133	.1254813	.1258064	.1261314	.1264561	.1267806
134	.1287223	.1290450	.1293676	.1296899	.1300119
135	3.1319393	3.1322597	3.1325798	3.1328998	3.1332194
136	.1351326	.1354507	.1357685	.1360861	.1364034
137	.1383027	.1386184	.1389339	.1392492	.1395643
138	.1414498	.1417632	.1420765	.1423895	.1427022
139	.1445742	.1448854	.1451964	.1455072	.1458177
140	.1476763	.1479853	.1482941	.1486026	.1489110
141	3.1507564	3.1510632	3.1513698	3.1516762	3.1519824
142	.1538149	.1541195	.1544240	.1547282	.1550322
143	.1568519	.1571544	.1574568	.1577589	.1580608
144	.1598678	.1601683	.1604685	.1607686	.1610684
145	.1628630	.1631614	.1634595	.1637575	.1640553
146	.1658376	.1661340	.1664301	.1667260	.1670218
147	.1687920	.1690863	.1693805	.1696744	.1699682

A T A B L E of Logarithms,

Num.	0	1	2	3	4
148	3.1702617	3.1705550	3.1708482	3.1711411	3.1714339
149	.1731863	.1734776	.1737688	.1740598	.1743506
150	.1760913	.1763807	.1766699	.1769590	.1772478
151	.1789769	.1792645	.1795518	.1798389	.1801259
152	.1818436	.1821292	.1824146	.1826999	.1829850
153	.1846914	.1849752	.1852588	.1855421	.1858253
154	3.1875207	3.1878026	3.1880844	3.1883659	3.1886473
155	.1903317	.1906118	.1908917	.1911714	.1914510
156	.1931246	.1934029	.1936810	.1939590	.1942367
157	.1958996	.1961762	.1964525	.1967287	.1970047
158	.1986571	.1989319	.1992065	.1994809	.1997552
159	.2013971	.2016702	.2019431	.2022158	.2024883
160	3.2041200	3.2043913	3.2046625	3.2049335	3.2052044
161	.2068259	.2070955	.2073650	.2076344	.2079035
162	.2095150	.2097830	.2100508	.2103185	.2105860
163	.2121876	.2124540	.2127201	.2129862	.2132521
164	.2148438	.2151086	.2153732	.2156376	.2159018
165	.2174839	.2177471	.2180100	.2182728	.2185355
166	3.2201081	3.2203696	3.2206310	3.2208922	3.2211533
167	.2227165	.2229764	.2232363	.2234959	.2237554
168	.2253093	.2255677	.2258259	.2260841	.2263421
169	.2278867	.2281436	.2284003	.2286570	.2289134
170	.2304489	.2307043	.2309596	.2312146	.2314696
171	.2329961	.2332500	.2335038	.2337574	.2340108
172	3.2355284	3.2357809	3.2360331	3.2362853	3.2365373
173	.2380461	.2382971	.2385479	.2387986	.2390491
174	.2405492	.2407988	.2410481	.2412974	.2415465
175	.2430380	.2432861	.2435341	.2437819	.2440296
176	.2455127	.2457593	.2460059	.2462523	.2464986
177	.2479733	.2482186	.2484637	.2487087	.2489536
178	3.2504200	3.2506639	3.2509077	3.2511513	3.2513948
179	.2528530	.2530956	.2533380	.2535803	.2538224
180	.2552725	.2555137	.2557548	.2559957	.2562365
181	.2576786	.2579184	.2581582	.2583978	.2586373
182	.2600714	.2603099	.2605484	.2607867	.2610248
183	.2624511	.2626883	.2629255	.2631625	.2633993
184	.2648178	.2650538	.2652896	.2655253	.2657609

from 1 to 10000.

Num.	5	6	7	8	9
148	3.1717264	3.1720188	3.1723110	3.1726029	3.1728947
149	.1746412	.1749316	.1752218	.1755118	.1758016
150	.1775365	.1778250	.1781132	.1784013	.1786892
151	.1804126	.1806992	.1809856	.1812718	.1815578
152	.1832698	.1835545	.1838390	.1841233	.1844075
153	.1861084	.1863912	.1866739	.1869563	.1872386
154	3.1889285	3.1892095	3.1894903	3.1897709	3.1900514
155	.1917304	.1920096	.1922886	.1925674	.1928461
156	.1945143	.1947917	.1950690	.1953460	.1956229
157	.1972806	.1975562	.1978317	.1981070	.1983821
158	.2000293	.2003032	.2005769	.2008505	.2011239
159	.2027607	.2030329	.2033049	.2035768	.2038485
160	3.2054750	3.2057455	3.2060159	3.2062869	3.2065560
161	.2081725	.2084413	.2087100	.2089785	.2092468
162	.2108534	.2111205	.2113876	.2116544	.2119211
163	.2135178	.2137833	.2140487	.2143139	.2145789
164	.2161659	.2164298	.2166936	.2169572	.2172206
165	.2187980	.2190603	.2193225	.2195845	.2198464
166	3.2214142	3.2216750	3.2219356	3.2221960	3.2224563
167	.2240148	.2242740	.2245331	.2247920	.2250507
168	.2265999	.2268576	.2271151	.2273724	.2276296
169	.2291697	.2294258	.2296818	.2299377	.2301934
170	.2317244	.2319790	.2322335	.2324879	.2327421
171	.2342641	.2345173	.2347703	.2350232	.2352759
172	3.2367891	3.2370408	3.2372923	3.2375437	3.2377950
173	.2392995	.2395497	.2397998	.2400498	.2402996
174	.2417954	.2420442	.2422929	.2425414	.2427898
175	.2442771	.2445245	.2447718	.2450189	.2452658
176	.2467447	.2469907	.2472365	.2474823	.2477278
177	.2491984	.2494430	.2496874	.2499317	.2501759
178	3.2516382	3.2518814	3.2521246	3.2523675	3.2526103
179	.2540645	.2543063	.2545481	.2547897	.2550312
180	.2564772	.2567177	.2569581	.2571984	.2574386
181	.2588766	.2591158	.2593549	.2595939	.2598327
182	.2612629	.2615008	.2617385	.2619762	.2622137
183	.2636361	.2638727	.2641092	.2643455	.2645817
184	.2659964	.2662317	.2664660	.2667020	.2669369

A TABLE of Logarithms,

Num	0	1	2	3	4
185	3.2671717	3.2674064	3.2676410	3.2678754	3.2681097
186	.2695129	.2697464	.2699797	.2702128	.2704459
187	.2718416	.2720738	.2723058	.2725378	.2727696
188	.2741578	.2743888	.2746196	.2748503	.2750809
189	.2764618	.2766915	.2769211	.2771506	.2773800
190	.2787536	.2789821	.2792105	.2794388	.2796669
191	3.2810334	3.2812607	3.2814879	3.2817150	3.2819419
192	.2833012	.2835274	.2837534	.2839793	.2842051
193	.2855573	.2857823	.2860071	.2862318	.2864565
194	.2878017	.2880255	.2882492	.2884728	.2886963
195	.2900346	.2902573	.2904798	.2907022	.2909246
196	.2922561	.2924776	.2926990	.2929203	.2931415
197	3.2944562	3.2946866	3.2949069	3.2951271	3.2953471
198	.2966652	.2968845	.2971036	.2973227	.2975417
199	.2988531	.2990713	.2992893	.2995073	.2997251
200	.3010300	.3012471	.3014641	.3016809	.3018977
201	.3031951	.3034121	.3036280	.3038438	.3040595
202	.3053514	.3055663	.3057811	.3059959	.3062105
203	3.3074960	3.3077099	3.3079237	3.3081374	3.3083509
204	.3096302	.3098430	.3100557	.3102684	.3104809
205	.3117539	.3119657	.3121774	.3123889	.3126004
206	.3138672	.3140780	.3142887	.3144992	.3147097
207	.3159703	.3161801	.3163897	.3165993	.3168087
208	.3180633	.3182721	.3184807	.3186893	.3188977
209	3.3201463	3.3203540	3.3205617	3.3207692	3.3209767
210	.3222193	.3224260	.3226327	.3228393	.3230457
211	.3242825	.3244882	.3246939	.3248995	.3251050
212	.3263359	.3265407	.3267454	.3269500	.3271545
213	.3283796	.3285834	.3287872	.3289909	.3291944
214	.3304138	.3306167	.3308195	.3310222	.3312248
215	3.3324385	3.3326404	3.3328423	3.3330440	3.3332457
216	.3344537	.3346548	.3348557	.3350565	.3352572
217	.3364597	.3366598	.3368598	.3370597	.3372595
218	.3384565	.3386557	.3388547	.3390537	.3392526
219	.3404441	.3406424	.3408405	.3410386	.3412366
220	.3424227	.3426209	.3428173	.3430145	.3432116
221	.3443923	.3445887	.3447851	.3449814	.3451776

from 1 to 10000.

Num	5	6	7	8	9
185	3.2683439	3.2685780	3.2688119	3.2690457	3.2692794
186	.2706788	.2709116	.2711443	.2713769	.2716093
187	.2730013	.2732328	.2734643	.2736956	.2739268
188	.2753113	.2755417	.2757719	.2760020	.2762320
189	.2776092	.2778383	.2780673	.2782962	.2785250
190	.2798950	.2801229	.2803507	.2805784	.2808059
191	3.2821688	3.2823955	3.2826221	3.2828486	3.2830750
192	.2844307	.2846563	.2848817	.2851070	.2853322
193	.2866819	.2869054	.2871296	.2873538	.2875778
194	.2889196	.2891428	.2893659	.2895889	.2898118
195	.2911468	.2913688	.2915908	.2918127	.2920344
196	.2933626	.2935835	.2938044	.2940251	.2942457
197	3.2955671	3.2957869	3.2960067	3.2962263	3.2964458
198	.2977605	.2979792	.2981979	.2984164	.2986348
199	.2999429	.3001605	.3003781	.3005955	.3008128
200	.3021144	.3023309	.3025474	.3027637	.3029799
201	.3042751	.3044905	.3047057	.3049212	.3051363
202	.3064250	.3066394	.3068537	.3070679	.3072820
203	3.3085644	3.3087778	3.3089910	3.3092402	3.3094172
204	.3106933	.3109056	.3111178	.3113299	.3115420
205	.3128118	.3130231	.3132343	.3134454	.3136563
206	.3149200	.3151303	.3153405	.3155505	.3157605
207	.3170181	.3172273	.3174365	.3176455	.3178545
208	.3191061	.3193143	.3195224	.3197305	.3199384
209	3.3211840	3.3213913	3.3215984	3.3218055	3.3220124
210	.3232521	.3234584	.3236645	.3238706	.3240766
211	.3253104	.3255157	.3257209	.3259260	.3261310
212	.3273589	.3275633	.3277675	.3279716	.3281757
213	.3293979	.3296012	.3298045	.3200077	.3302108
214	.3314273	.3316297	.3318320	.3320343	.3322364
215	3.3334473	3.3336488	3.3338501	3.3340514	3.3342526
216	.3354579	.3356583	.3358589	.3360593	.3362596
217	.3374593	.3376589	.3378584	.3380579	.3382572
218	.3394514	.3396501	.3398488	.3300473	.3402458
219	.3414345	.3416323	.3418301	.3420277	.3422252
220	.3434086	.3436055	.3438023	.3439991	.3441957
221	.3453737	.3455698	.3457657	.3459615	.3461573

A T A B L E of Logarithms,

Num.	0	1	2	3	4
222	3.3463530	3.3465486	3.3467441	3.3469395	3.3471348
223	.3483049	.3484996	.3486942	.3488887	.3490832
224	.3502480	.3504419	.3506356	.3508293	.3510228
225	.3521825	.3523755	.3525684	.3527612	.3529539
226	.3541084	.3543006	.3544926	.3546845	.3548764
227	.3560259	.3562171	.3564083	.3565994	.3567905
228	3.3579348	3.3581253	3.3583156	3.3585059	3.3586961
229	.3598355	.3600251	.3602146	.3604040	.3605934
230	.3617278	.3619166	.3621053	.3622939	.3624825
231	.3636120	.3638000	.3639878	.3641756	.3643633
232	.3654880	.3656751	.3658622	.3660492	.3662361
233	.3673559	.3675423	.3677285	.3679147	.3681008
234	3.3692159	3.3694014	3.3695869	3.3697723	3.3699576
235	.3710679	.3712526	.3714373	.3716219	.3718065
236	.3729120	.3730960	.3732799	.3734637	.3736475
237	.3747483	.3749316	.3751147	.3752977	.3754807
238	.3765769	.3767594	.3769418	.3771240	.3773062
239	.3783979	.3785796	.3787612	.3789427	.3791241
240	3.3802112	3.3803922	3.3805730	3.3807538	3.3809345
241	.3820170	.3821972	.3823773	.3825573	.3827373
242	.3838154	.3839948	.3841741	.3843534	.3845326
243	.3856063	.3857850	.3859636	.3861421	.3863206
244	.3873898	.3875678	.3877457	.3879235	.3881012
245	.3891661	.3893433	.3895205	.3896975	.3898746
246	3.3909351	3.3911116	3.3912880	3.3914644	3.3916407
247	.3926969	.3928727	.3930485	.3932241	.3933997
248	.3944517	.3946268	.3948018	.3949767	.3951516
249	.3961993	.3963737	.3965480	.3967223	.3968964
250	.3979400	.3981137	.3982873	.3984608	.3986343
251	.3996737	.3998467	.4000196	.4001925	.4003653
252	3.4014005	3.4015728	3.4017451	3.4019172	3.4020893
253	.4031205	.4032921	.4034637	.4036352	.4038066
254	.4048337	.4050047	.4051755	.4053464	.4055171
255	.4065402	.4067105	.4068807	.4070508	.4072209
256	.4082400	.4084096	.4085791	.4087486	.4089180
257	.4099331	.4101021	.4102710	.4104398	.4106085
258	.4116197	.4117880	.4119562	.4121244	.4122925

from 1 to 10000.

Num.	5	6	7	8	9
222	3.3473300	3.3475252	3.3477202	3.3479152	3.3481101
223	.3492775	.3494718	.3496660	.3498601	.3500541
224	.3512163	.3514097	.3516031	.3517963	.3519895
225	.3531465	.3533391	.3535316	.3537239	.3539162
226	.3550682	.3552599	.3554515	.3556430	.3558345
227	.3569814	.3571723	.3573630	.3575537	.3577443
228	3.3588862	3.3590762	3.3592652	3.3594560	3.3596458
229	.3607827	.3609719	.3611610	.3613500	.3615390
230	.3626709	.3628593	.3630476	.3632358	.3634239
231	.3645510	.3647386	.3649260	.3651134	.3653007
232	.3664236	.3666097	.3667963	.3669830	.3671695
233	.3682869	.3684728	.3686587	.3688445	.3690302
234	3.3701428	3.3703280	3.3705131	3.3706981	3.3708830
235	.3719909	.3721753	.3723596	.3725438	.3727279
236	.3738311	.3740147	.3741983	.3743817	.3745651
237	.3756636	.3758464	.3760292	.3762118	.3763944
238	.3774884	.3776704	.3778524	.3780343	.3782161
239	.3793055	.3794868	.3796680	.3798492	.3800302
240	3.3881151	3.3812956	3.3814761	3.3816565	3.3818368
241	.3829171	.3830969	.3832766	.3834563	.3836359
242	.3847117	.3848908	.3850698	.3852487	.3854275
243	.3864990	.3866773	.3868555	.3870337	.3872118
244	.3882789	.3884565	.3886340	.3888114	.3889888
245	.3900515	.3902284	.3904052	.3905819	.3907585
246	3.3918169	3.3919931	3.3921691	3.3923452	3.3925211
247	.3935752	.3937506	.3939260	.3941013	.3942765
248	.3953264	.3955011	.3956758	.3958504	.3960249
249	.3970705	.3972446	.3974185	.3975924	.3977662
250	.3988077	.3989811	.3991543	.3993275	.3995007
251	.4005380	.4007106	.4008832	.4010557	.4012282
252	3.4022614	3.4024333	3.4026052	3.4027771	3.4029488
253	.4039780	.4041492	.4043205	.4044916	.4046627
254	.4056878	.4058584	.4060289	.4061994	.4063698
255	.4073909	.4075608	.4077307	.4079005	.4080703
256	.4090874	.4092567	.4094259	.4095950	.4097641
257	.4107772	.4109459	.4111144	.4112829	.4114513
258	.4124605	.4126285	.4127964	.4129643	.4131320

A T A B L E of Logarithms,

Num.	0	1	2	3	4
259	3.4132998	3.4134674	3.4136350	3.4138025	3.4139700
260	.4149733	.4151404	.4153073	.4154742	.4156410
261	.4166405	.4168069	.4169732	.4171394	.4173056
262	.4183013	.4184670	.4186327	.4187983	.4189638
263	.4199557	.4201208	.4202859	.4204509	.4206158
264	.4216039	.4217684	.4219328	.4220972	.4222614
265	3.4232459	3.4234097	3.4235735	3.4237372	3.4239009
266	.4248816	.4250449	.4252080	.4253712	.4255342
267	.4265113	.4266739	.4268365	.4269990	.4271614
268	.4281348	.4282968	.4284588	.4286207	.4287825
269	.4297523	.4299137	.4300751	.4302364	.4303976
270	.4313638	.4315246	.4316853	.4318460	.4320067
271	3.4329693	3.4331295	3.4332897	3.4334498	3.4336098
272	.4345689	.4347285	.4348881	.4350476	.4352071
273	.4361626	.4363218	.4364807	.4366396	.4367985
274	.4377506	.4379090	.4380674	.4382258	.4383841
275	.4393327	.4394906	.4396484	.4398062	.4399639
276	.4409091	.4410664	.4412237	.4413809	.4415380
277	3.4424798	3.4426365	3.4427932	3.4429499	3.4431065
278	.4440448	.4442010	.4443571	.4445132	.4446692
279	.4456042	.4457598	.4459154	.4460709	.4462264
280	.4471580	.4473131	.4474681	.4476231	.4477780
281	.4487063	.4488608	.4490153	.4491697	.4493241
282	.4502491	.4504031	.4505570	.4507109	.4508647
283	3.4517864	3.4519399	3.4520932	3.4522466	3.4523998
284	.4533183	.4534712	.4536241	.4537769	.4539296
285	.4548449	.4549972	.4551495	.4553018	.4554540
286	.4563660	.4565179	.4566696	.4568213	.4569731
287	.4578819	.4580332	.4581844	.4583356	.4584868
288	.4593925	.4595433	.4596940	.4598446	.4599953
289	3.4608978	3.4610481	3.4611983	3.4613484	3.4614985
290	.4623980	.4625477	.4626974	.4628470	.4629966
291	.4638930	.4640422	.4641914	.4643405	.4644895
292	.4653828	.4655316	.4656802	.4658288	.4659774
293	.4668676	.4670158	.4671640	.4673120	.4674601
294	.4683473	.4684950	.4686427	.4687903	.4689378
295	.4698220	.4699692	.4701163	.4702634	.4704105

from 1 to 10000.

Num.	5	6	7	8	9
259	3.4141374	3.4143047	3.4144719	3.4146391	3.4148063
260	.4158077	.4159744	.4161410	.4163076	.4164741
261	.4174717	.4176377	.4178037	.4179696	.4181355
262	.4191293	.4192947	.4194601	.4196254	.4197906
263	.4207806	.4209454	.4211101	.4212748	.4214394
264	.4224257	.4225898	.4227539	.4229180	.4230820
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265	3.4240645	3.4242281	3.4243915	3.4245550	3.4247183
266	.4256972	.4258601	.4260230	.4261858	.4263486
267	.4273238	.4274861	.4276484	.4278106	.4279727
268	.4289443	.4291060	.4292677	.4294293	.4295908
269	.4305588	.4307199	.4308809	.4310419	.4312029
270	.4321673	.4323278	.4324883	.4326487	.4328090
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271	3.4337698	3.4339298	3.4340896	3.4342494	3.4344092
272	.4353665	.4355258	.4356851	.4358444	.4360035
273	.4369573	.4371161	.4372748	.4374334	.4375920
274	.4385423	.4387005	.4388587	.4390167	.4391747
275	.4401216	.4402792	.4404368	.4405943	.4407517
276	.4416951	.4418522	.4420092	.4421661	.4423229
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277	3.4432630	3.4434195	3.4435759	3.4437322	3.4438885
278	.4448252	.4449811	.4451370	.4452928	.4454485
279	.4463818	.4465372	.4466925	.4468477	.4470029
280	.4479329	.4480877	.4482424	.4483971	.4485517
281	.4494784	.4496326	.4497868	.4499410	.4500951
282	.4510185	.4511721	.4513258	.4514794	.4516329
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283	3.4525531	3.4527062	3.4528593	3.4530124	3.4531654
284	.4540823	.4542349	.4543875	.4545400	.4546924
285	.4556061	.4557582	.4559102	.4560622	.4562142
286	.4571246	.4572762	.4574277	.4575791	.4577305
287	.4586378	.4587889	.4589399	.4590908	.4592417
288	.4601458	.4602963	.4604468	.4605972	.4607475
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289	3.4616486	3.4617986	3.4619485	3.4620984	3.4622482
290	.4631461	.4632956	.4634450	.4635944	.4637437
291	.4646386	.4647875	.4649364	.4650853	.4652341
292	.4661259	.4662743	.4664227	.4665711	.4667194
293	.4676081	.4677560	.4679039	.4680518	.4681996
294	.4690853	.4692327	.4693801	.4695275	.4696748
295	.4705575	.4707044	.4708513	.4709982	.4711450

A T A B L E of Logarithms,

Num.	0	1	2	3	4
296	3.4712917	3.4714384	3.4715850	3.4717317	3.4718782
297	.4727564	.4729027	.4730488	.4731949	.4733410
298	.4742163	.4743620	.4745076	.4746533	.4747988
299	.4756712	.4758164	.4759616	.4761067	.4762518
300	.4771212	.4772660	.4774107	.4775553	.4776999
301	.4785665	.4787108	.4788550	.4789991	.4791432
302	3.4800069	3.4801507	3.4802945	3.4804381	3.4805818
303	.4814426	.4815859	.4817292	.4818724	.4820156
304	.4828736	.4830164	.4831592	.4833019	.4834446
305	.4842998	.4844422	.4845845	.4847268	.4848690
306	.4857214	.4858633	.4860052	.4861470	.4862888
307	.4871384	.4872798	.4874212	.4875626	.4877039
308	3.4885507	3.4886917	3.4888326	3.4889735	3.4891144
309	.4899585	.4900990	.4902395	.4903799	.4905203
310	.4913617	.4915018	.4916418	.4917818	.4919217
311	.4927604	.4929000	.4930396	.4931791	.4933186
312	.4941546	.4942938	.4944329	.4945720	.4947110
313	.4955443	.4956831	.4958218	.4959604	.4960990
314	3.4969296	3.4970679	3.4972062	3.4973444	3.4974825
315	.4983106	.4984484	.4985862	.4987240	.4988617
316	.4996871	.4998245	.4999619	.5000992	.5002365
317	.5010593	.5011962	.5013332	.5014701	.5016069
318	.5024271	.5025637	.5027002	.5028366	.5029731
319	.5037907	.5039268	.5040629	.5041989	.5043349
320	3.5051500	3.5052857	3.5054213	3.5055569	3.5056925
321	.5065050	.5066403	.5067755	.5069107	.5070459
322	.5078559	.5079907	.5081255	.5082603	.5083950
323	.5092025	.5093370	.5094713	.5096057	.5097400
324	.5105450	.5106790	.5108130	.5109469	.5110808
325	.5118834	.5120170	.5121505	.5122841	.5124175
326	3.5132176	3.5133508	3.5134840	3.5136171	3.5137501
327	.5145478	.5146805	.5148133	.5149460	.5150787
328	.5158738	.5160062	.5161386	.5162709	.5164031
329	.5171959	.5173279	.5174598	.5175917	.5177236
330	.5185139	.5186455	.5187771	.5189086	.5190400
331	.5198280	.5199592	.5200903	.5202214	.5203525
332	.5211381	.5212689	.5213996	.5215303	.5216610

from 1 to 10000.

Num.	5	6	7	8	9
296	3.4720247	3.4721711	3.4723175	3.4724639	3.4726102
297	.4734870	.4736329	.4737788	.4739247	.4740705
298	.4749443	.4750898	.4752352	.4753806	.4755259
299	.4763968	.4765418	.4766867	.4768316	.4769765
300	.4778445	.4779890	.4781334	.4782778	.4784222
301	.4792873	.4794313	.4795753	.4797192	.4798631
302	3.4807254	3.4808689	3.4810124	3.4811559	3.4812993
303	.4821587	.4823018	.4824448	.4825878	.4827307
304	.4835873	.4837299	.4838725	.4840150	.4841574
305	.4850112	.4851533	.4852954	.4854375	.4855795
306	.4864305	.4865721	.4867138	.4868554	.4869969
307	.4878451	.4879863	.4882275	.4881686	.4884097
308	3.4892552	3.4893959	3.4895366	3.4896773	3.4898179
309	.4906607	.4908009	.4909412	.4910814	.4922216
310	.4920616	.4922014	.4923413	.4924810	.4926207
311	.4934580	.4935974	.4937368	.4938761	.4940154
312	.4948500	.4949890	.4951279	.4952667	.4954056
313	.4962375	.4963761	.4965145	.4966529	.4967913
314	3.4976206	3.4977587	3.4978967	3.4980347	3.4981727
315	.4989994	.4991370	.4992746	.4994121	.4995496
316	.5003737	.5005109	.5006481	.5007852	.5009222
317	.5017437	.5018805	.5020172	.5021539	.5022905
318	.5031094	.5032458	.5033821	.5035183	.5036545
319	.5044709	.5046068	.5047426	.5048785	.5050142
320	3.5058280	3.5059635	3.5060990	3.5062344	3.5063697
321	.5071810	.5073160	.5074511	.5075860	.5077210
322	.5085297	.5086644	.5087990	.5089335	.5090680
323	.5098743	.5100085	.5101427	.5102768	.5104109
324	.5112147	.5113485	.5114823	.5116160	.5117497
325	.5123510	.5126844	.5128178	.5129511	.5130844
326	3.5138832	3.5140162	3.5141491	3.5142820	3.5144149
327	.5152113	.5153439	.5154764	.5156089	.5157414
328	.5165354	.5166676	.5167997	.5169318	.5170639
329	.5178554	.5179872	.5181189	.5182506	.5183823
330	.5191715	.5193028	.5194342	.5195655	.5196968
331	.5204835	.5206145	.5207455	.5208764	.5210073
332	.5217916	.5219222	.5220528	.5221833	.5223138

A T A B L E of Logarithms,

Num.	0	1	2	3	4
333	3.5224442	3.5225746	3.5227050	3.5228353	3.5229656
334	.5237465	.5238765	.5240064	.5241364	.5242663
335	.5250448	.5251744	.5253040	.5254335	.5255631
336	.5263393	.5264685	.5265977	.5267269	.5268560
337	.5276299	.5277588	.5278876	.5280163	.5281451
338	.5289167	.5290452	.5291736	.5293020	.5294303
339	3.5301997	3.5303278	3.5304558	3.5305839	3.5307118
340	.5314789	.5316066	.5317343	.5318619	.5319895
341	.5327544	.5328817	.5330090	.5331362	.5332635
342	.5340261	.5341531	.5342800	.5344069	.5345338
343	.5352941	.5354207	.5355473	.5356738	.5358003
344	.5365584	.5366847	.5368109	.5369370	.5370631
345	3.5378191	3.5379450	3.5380708	3.5381966	3.5383223
346	.5390761	.5392016	.5393271	.5394525	.5395779
347	.5403295	.5404546	.5405797	.5407048	.5408298
348	.5415792	.5417040	.5418288	.5419535	.5420781
349	.5428254	.5429498	.5430742	.5431986	.5433229
350	.5440690	.5441921	.5443161	.5444401	.5445641
351	3.5453071	3.5454308	3.5455545	3.5456781	3.5458017
352	.5465427	.5466660	.5467894	.5469126	.5470359
353	.5477747	.5478977	.5480207	.5481436	.5482665
354	.5490033	.5491259	.5492486	.5493712	.5494937
355	.5502283	.5503507	.5504730	.5505952	.5507174
356	.5514500	.5515720	.5516939	.5518158	.5519377
357	3.5526682	3.5527898	3.5529114	3.5530330	3.5531545
358	.5538830	.5540043	.5541256	.5542468	.5543680
359	.5550944	.5552154	.5553362	.5554572	.5555781
360	.5563025	.5564231	.5565437	.5566643	.5567848
361	.5575072	.5576275	.5577477	.5578680	.5579881
362	.5587086	.5588285	.5589484	.5590683	.5591882
363	3.5599066	3.5600262	3.5601458	3.5602654	3.5603849
364	.5611014	.5612207	.5613399	.5614592	.5615785
365	.5622929	.5624118	.5625308	.5626497	.5627685
366	.5634811	.5635997	.5637183	.5638369	.5639555
367	.5646661	.5647844	.5649027	.5650209	.5651392
368	.5658478	.5659658	.5660838	.5662017	.5663196
369	.5670264	.5671440	.5672617	.5673793	.5674969

from 1 to 10000.

Num.	5	6	7	8	9
333	3.5230958	3.5232260	3.5233562	3.5234863	3.5236164
334	.5243961	.5245259	.5246557	.5247854	.5249151
345	.5256925	.5258219	.5259513	.5260807	.5262100
336	.5269851	.5271141	.5272431	.5273721	.5275010
337	.5282738	.5284024	.5285311	.5286596	.5287882
338	.5295587	.5296869	.5298152	.5299434	.5300716
339	3.5308398	3.5309677	3.5310955	3.5312234	3.5313512
340	.5321171	.5322446	.5323721	.5324996	.5326270
341	.5333907	.5335179	.5336450	.5337721	.5338991
342	.5346606	.5347874	.5349141	.5350408	.5351675
343	.5359267	.5360532	.5361795	.5363059	.5364322
344	.5371892	.5373153	.5374413	.5375672	.5376932
345	3.5384481	3.5385737	3.5386994	3.5388250	3.5389506
346	.5397032	.5398286	.5399538	.5400791	.5402043
347	.5409548	.5410798	.5412047	.5413296	.5414544
348	.5422028	.5423274	.5424519	.5425765	.5427010
349	.5434472	.5435714	.5436956	.5438198	.5439439
350	.5446880	.5448119	.5449358	.5450596	.5451834
351	3.5459253	3.5460489	3.5461724	3.5462958	3.5464193
352	.5471591	.5472823	.5474055	.5475286	.5476517
353	.5483894	.5485123	.5486351	.5487578	.5488806
354	.5496162	.5497387	.5498612	.5499836	.5501060
355	.5508392	.5509618	.5510839	.5512059	.5513280
356	.5520595	.5521813	.5523031	.5524248	.5525465
357	3.5532760	.5533975	3.5535189	3.5536403	3.5537617
358	.5544892	3.5546103	.5547314	.5548524	.5549735
359	.5556989	.5558197	.5559404	.5560612	.5561818
360	.5569053	.5570257	.5571461	.5572665	.5573869
361	.5581083	.5582284	.5583485	.5584686	.5585886
362	.5593080	.5594278	.5595476	.5596673	.5597870
363	3.5605044	3.5606239	3.5607433	3.5608627	3.5609820
364	.5616975	.5618167	.5619358	.5620548	.5621739
365	.5628874	.5630062	.5631250	.5632437	.5633624
366	.5640740	.5641925	.5643109	.5644293	.5645477
367	.5652573	.5653755	.5654936	.5656117	.5657298
368	.5664375	.5665553	.5666731	.5667909	.5669087
369	.5676144	.5677320	.5678494	.5679669	.5680843

A TABLE of Logarithms,

Num.	0	1	2	3	4
370	3.5682017	3.5683191	3.5684364	3.5685537	3.5686710
371	.5693739	.5694910	.5696080	.5697249	.5698419
372	.5705429	.5706597	.5707764	.5708930	.5710097
373	.5717088	.5718252	.5719416	.5720580	.5721743
374	.5728716	.5729877	.5731038	.5732198	.5733358
375	.5740313	.5741471	.5742628	.5743786	.5744943
376	3.5751878	3.5753033	3.5754188	3.5755342	3.5756496
377	.5763413	.5764565	.5765717	.5766868	.5768019
378	.5774917	.5776067	.5777215	.5778363	.5779511
379	.5786392	.5787538	.5788683	.5789828	.5790973
380	.5797836	.5790979	.5800121	.5801263	.5802405
381	.5809250	.5810389	.5811529	.5812668	.5813807
382	3.5820634	3.5821770	3.5822907	3.5824043	3.5825179
383	.5831988	.5833122	.5834255	.5835388	.5836521
384	.5843312	.5844443	.5845574	.5846704	.5847834
385	.5854607	.5855735	.5856863	.5857990	.5859117
386	.5865873	.5866998	.5868123	.5869247	.5870371
387	.5877110	.5878232	.5879353	.5880475	.5881596
388	3.5888317	3.5889436	3.5890555	3.5891674	3.5892792
389	.5899496	.5900612	.5901728	.5902844	.5903959
390	.5910646	.5911759	.5912873	.5913985	.5915098
391	.5921768	.5922878	.5923988	.5925098	.5926208
392	.5932861	.5933960	.5935076	.5936183	.5937290
393	.5943925	.5945030	.5946135	.5947239	.5948344
394	3.5954962	3.5956064	3.5957166	3.5958268	3.5959369
395	.5965971	.5967070	.5968169	.5969268	.5970367
396	.5976952	.5978048	.5979145	.5980241	.5981336
397	.5987905	.5988999	.5990092	.5991186	.5992279
398	.5998831	.5999922	.6001013	.6002103	.6003193
399	.6009729	.6010817	.6011905	.6012993	.6014081
400	3.6020600	3.6021685	3.6022771	3.6023856	3.6024941
401	.6031444	.6032527	.6033609	.6034692	.6035774
402	.6042261	.6043341	.6044421	.6045500	.6046580
403	.6053050	.6054128	.6055215	.6056282	.6057359
404	.6063814	.6064888	.6065963	.6067037	.6068111
405	.6074550	.6075622	.6076694	.6077766	.6078837
406	.6085260	.6086330	.6087399	.6088468	.6089537

from 1 to 10000.

Num	5	6	7	8	9
370	3.5687882	3.5689054	3.5690226	3.5691397	3.5692568
371	.5699588	.5700757	.5701026	.5703094	.5704262
372	.5711263	.5712428	.5713594	.5714759	.5715924
373	.5722906	.5724069	.5725231	.5726393	.5727555
374	.5734518	.5735678	.5736837	.5737990	.5739154
375	.5746099	.5747256	.5748412	.5749568	.5750723
376	3.5757650	3.5758803	3.5759956	3.5761109	3.5762261
377	.5769169	.5770320	.5771470	.5772620	.5773769
378	.5780659	.5781806	.5782953	.5784100	.5785246
379	.5792118	.5793262	.5794406	.5795550	.5796693
380	.5803547	.5804688	.5805829	.5806969	.5808110
381	.5814945	.5816084	.5817222	.5818359	.5819497
382	3.5826314	3.5827450	3.5828585	3.5829719	3.5830854
383	.5837654	.5838786	.5839918	.5841050	.5842181
384	.5848963	.5850093	.5851222	.5852351	.5853479
385	.5860244	.5861370	.5862496	.5863622	.5864748
386	.5871495	.5872618	.5873742	.5874865	.5875987
387	.5882717	.5883838	.5884958	.5886078	.5887198
388	3.5893910	3.5895028	3.5896145	3.5897262	3.5898379
389	.5905075	.5906189	.5907304	.5908418	.5909532
390	.5916210	.5917322	.5918434	.5919546	.5920657
391	.5927318	.5928427	.5929536	.5930644	.5931753
392	.5938397	.5939503	.5940609	.5941715	.5942820
393	.5949447	.5950551	.5951654	.5952757	.5953860
394	3.5960470	3.5961571	3.5962671	3.5963771	3.5964871
395	.5971465	.5972563	.5973660	.5974758	.5975855
396	.5982432	.5983527	.5984622	.5985717	.5986811
397	.5993371	.5994464	.5995556	.5996648	.5997739
398	.6004283	.6005373	.6006462	.6007551	.6008640
399	.6015168	.6016255	.6017341	.6018428	.6019514
400	3.6026025	3.6027109	3.6028193	3.6029277	3.6030361
401	.6036855	.6037937	.6039018	.6040099	.6041180
402	.6047659	.6048738	.6049816	.6050895	.6051973
403	.6058435	.6059512	.6060587	.6061663	.6062738
404	.6069185	.6070259	.6071332	.6072405	.6073478
405	.6079909	.6080979	.6082050	.6083120	.6084190
406	.6090605	.6091674	.6092742	.6093809	.6094877

A T A B L E of Logarithms.

Num.	0	1	2	3	4
407	3.6095944	3.6097011	3.6098078	3.6099144	3.6000210
408	.6106602	.6107666	.6108730	.6109794	.6110857
409	.6117233	.6118295	.6119356	.6129407	.6120418
410	.6127839	.6128898	.6129957	.6131015	.6132073
411	.6138418	.6139475	.6140531	.6141587	.6142643
412	.6148972	.6150026	.6151080	.6152133	.6153187
413	3.6159501	3.6160552	3.6161603	4.6162654	3.6163705
414	.6170003	.6171052	.6172101	.6173149	.6174197
415	.6180481	.6181527	.6182573	.6183619	.6184665
416	.6190933	.6191977	.6193021	.6194064	.6195107
417	.6201360	.6202402	.6203443	.6204484	.6205524
418	.6211763	.6212802	.6213840	.6214879	.6215917
419	3.6222140	3.6223177	3.6224213	3.6225249	3.6226284
420	.6232493	.6233527	.6234560	.6235594	.6236627
421	.6242821	.6243852	.6244884	.6245915	.6246945
422	.6253124	.6254153	.6255182	.6256211	.6257239
423	.6263404	.6264430	.6265457	.6266483	.6267509
424	.6273659	.6274683	.6275707	.6276730	.6277754
425	3.6283889	3.6284911	3.6285933	3.6286954	3.6287975
426	.6294096	.6295115	.6296134	.6297153	.6298172
427	.6304279	.6305296	.6306312	.6307329	.6308345
428	.6314438	.6315452	.6316467	.6317481	.6318495
429	.6324573	.6325585	.6326597	.6327609	.6328620
430	.6334685	.6335694	.6336704	.6337713	.6338723
431	3.6344773	3.6345780	3.6346788	3.6347795	3.6348801
432	.6354837	.6355843	.6356848	.6357852	.6358857
433	.6364879	.6365882	.6366884	.6367887	.6368889
434	.6374897	.6375898	.6376898	.6377898	.6378898
435	.6384893	.6385891	.6386889	.6387888	.6388884
436	.6394865	.6395861	.6396857	.6397852	.6398847
437	3.6404814	3.6405808	3.6406802	3.6407795	3.6408788
438	.6414741	.6415733	.6416724	.6417715	.6418705
439	.6424645	.6425634	.6426623	.6427612	.6428601
440	.6434527	.6435514	.6436500	.6437487	.6438473
441	.6444386	.6445371	.6446355	.6447339	.6448323
442	.6454223	.6455205	.6456187	.6457169	.6458151
443	.6464037	.6465017	.6465997	.6466977	.6467957

from 1 to 10000.

Num.	5	6	7	8	9
407	3.6101276	3.6102342	3.6103407	3.6104472	3.6105537
408	.6111921	.6112984	.6114046	.6115109	.6116171
409	.6122539	.6123599	.6124660	.6125720	.6126779
410	.6133132	.6134189	.6135247	.6136304	.6137361
411	.6143698	.6144754	.6145809	.6146863	.6147918
412	.6154240	.6155292	.6156345	.6157397	.6158449
413	3.6164755	3.6165805	3.6166855	3.6167905	3.6168954
414	.6175245	.6176293	.6177340	.6178387	.6179434
415	.6185710	.6186755	.6187800	.6188845	.6189889
416	.6196150	.6197193	.6198235	.6199277	.6200319
417	.6206565	.6207605	.6208645	.6209684	.6210724
418	.6216955	.6217992	.6219034	.6220067	.6221104
419	3.6227320	3.6228355	3.6229390	3.6230424	3.6231459
420	.6237660	.6238693	.6239725	.6240757	.6241789
421	.6247976	.6249006	.6250036	.6251066	.6252095
422	.6258267	.6259295	.6260322	.6261350	.6262377
423	.6268534	.6269559	.6270585	.6271610	.6272634
424	.6278777	.6279800	.6280823	.6281845	.6282867
425	3.6288996	3.6290916	3.6291036	3.6292057	3.6293076
426	.6299190	.6300208	.6301226	.6302244	.6303262
427	.6309361	.6310377	.6311392	.6312408	.6313423
428	.6319508	.6320522	.6321535	.6322548	.6323560
429	.6329632	.6330643	.6331659	.6332664	.6333674
430	.6339732	.6340740	.6341749	.6342757	.6343765
431	3.6349808	3.6350814	3.6351800	3.6352826	3.6353832
432	.6359861	.6360865	.6361869	.6362872	.6363870
433	.6369891	.6370893	.6371894	.6372895	.6373896
434	.6379898	.6380897	.6381896	.6382895	.6383894
435	.6389882	.6390879	.6391876	.6392872	.6393869
436	.6399842	.6400837	.6401832	.6402826	.6403820
437	3.6409781	3.6410773	3.6411765	3.6412758	3.6413749
438	.6419696	.6420686	.6421676	.6422666	.6423656
439	.6429589	.6430577	.6431565	.6432552	.6433540
440	.6439459	.6440445	.6441431	.6442416	.6443401
441	.6449307	.6450291	.6451274	.6452257	.6453240
442	.6459133	.6460114	.6461095	.6462076	.6463057
443	.6468936	.6469915	.6470894	.6471873	.6472851

A TABLE of Logarithms,

Num	0	1	2	3	4
444	3.6473830	3.6474808	3.6475785	3.6476763	3.6477740
445	.6483600	.6484570	.6485552	.6486527	.6487502
446	.6493349	.6494322	.6495296	.6496269	.6497242
447	.6503075	.6504047	.6505018	.6505989	.6506960
448	.6512780	.6513749	.6514719	.6515687	.6516656
449	.6522463	.6523430	.6524397	.6525364	.6526331
450	3.6532125	3.6533090	3.6534055	3.6535019	3.6535984
451	.6541765	.6542728	.6543691	.6544653	.6545616
452	.6551384	.6552345	.6553306	.6554266	.6555226
453	.6560982	.6561941	.6562899	.6563857	.6564815
454	.6570559	.6571515	.6572471	.6573427	.6574383
455	.6580114	.6581068	.6582023	.6582976	.6583930
456	3.6589648	3.6590601	3.6591553	3.6592505	3.6593456
457	.6599162	.6600112	.6601062	.6602012	.6602962
458	.6608655	.6609603	.6610551	.6611499	.6612446
459	.6618127	.6619073	.6620019	.6620964	.6621910
460	.6627578	.6628522	.6629466	.6630410	.6631353
461	.6637009	.6637951	.6638893	.6639835	.6640776
462	3.6646420	3.6647360	3.6648299	3.6649239	3.6650178
463	.6655810	.6656748	.6657685	.6658623	.6659560
464	.6665180	.6666116	.6667051	.6667987	.6668922
465	.6674530	.6675463	.6676397	.6677331	.6678264
466	.6683859	.6684791	.6685723	.6686654	.6687585
467	.6693169	.6694099	.6695028	.6695958	.6696887
468	3.6702459	3.6703386	3.6704314	3.6705242	3.6706169
469	.6711728	.6712654	.6713580	.6714506	.6715431
470	.6720979	.6721903	.6722826	.6723750	.6724673
471	.6730209	.6731131	.6732053	.6732974	.6733896
472	.6739420	.6740340	.6741260	.6742179	.6743099
473	.6748611	.6749529	.6750447	.6751365	.6752283
474	3.6757783	3.6758700	3.6759615	3.6760531	3.6761447
475	.6766936	.6767850	.6768764	.6769678	.6770592
476	.6776069	.6776982	.6777894	.6778806	.6779718
477	.6785184	.6786094	.6787004	.6787914	.6788824
478	.6794279	.6795187	.6796096	.6797004	.6797912
479	.6803355	.6804262	.6805168	.6806074	.6806980
480	.6812412	.6813317	.6814222	.6815126	.6816030

from 1 to 10000.

Num.	5	6	7	8	9
444	3.6478718	3.6479695	3.6480671	3.6481648	3.6482624
445	.6488477	.6489452	.6490426	.6491401	.6492375
446	.6498215	.6499187	.6500160	.6501132	.6502104
447	.6507930	.6508901	.6509871	.6510841	.6511811
448	.6517624	.6518593	.6519561	.6520528	.6521496
449	.6527297	.6528263	.6529229	.6530195	.6531160
450	3.6536948	3.6537912	3.6538876	3.6539839	3.6540802
451	.6546578	.6547539	.6548501	.6549462	.6550423
452	.6556186	.6557145	.6558105	.6559064	.6560023
453	.6565773	.6566730	.6567688	.6568645	.6569602
454	.6575339	.6576294	.6577250	.6578205	.6579159
455	.6584884	.6585837	.6586790	.6587743	.6588696
456	3.6594408	3.6595359	3.6596310	3.6597261	3.6598212
457	.6603911	.6604860	.6605809	.6606758	.6607706
458	.6613393	.6614340	.6615287	.6616234	.6617181
459	.6622855	.6623800	.6624745	.6625690	.6626634
460	.6632296	.6633239	.6634182	.6635125	.6636067
461	.6641717	.6642658	.6643599	.6644539	.6645480
462	3.6651117	3.6652056	3.6652995	3.6653933	3.6654872
463	.6660497	.6661434	.6662371	.6663307	.6664244
464	.6669857	.6670792	.6671727	.6672661	.6673595
465	.6679197	.6680130	.6681062	.6681995	.6682927
466	.6688516	.6689447	.6690378	.6691308	.6692239
467	.6697816	.6698745	.6699674	.6700602	.6701530
468	3.6707096	3.6708023	3.6708950	3.6709876	3.6710802
469	.6716356	.6717281	.6718206	.6719130	.6720054
470	.6725596	.6726519	.6727442	.6728365	.6729287
471	.6734817	.6735738	.6736659	.6737579	.6738500
472	.6744018	.6744937	.6745856	.6746775	.6747693
473	.6753200	.6754117	.6755034	.6755951	.6756867
474	3.6762362	3.6763277	3.6764192	3.6765107	3.6766022
475	.6771505	.6772418	.6773332	.6774244	.6775157
476	.6780629	.6781540	.6782452	.6783362	.6784273
477	.6789734	.6790643	.6791552	.6792461	.6793370
478	.6798819	.6799727	.6800634	.6801541	.6802448
479	.6807886	.6808792	.6809697	.6810602	.6811507
480	.6816934	.6817838	.6818741	.6819645	.6820548

A T A B L E of Logarithms,

Num.	0	1	2	3	4
481	3.6821451	3.6822354	3.6823256	3.6824159	3.6825061
482	.6830478	.6831371	.6832272	.6833173	.6834073
483	.6839471	.6840370	.6841269	.6842168	.6843066
484	.6848454	.6849351	.6850248	.6851145	.6852041
485	.6857417	.6858313	.6859208	.6860103	.6860998
486	.6866363	.6867256	.6868149	.6869043	.6869936
487	3.6875290	3.6876181	3.6877073	3.6877954	3.6878855
488	.6884198	.6885088	.6885978	.6886867	.6887757
489	.6893089	.6893977	.6894864	.6895752	.6896640
490	.6901961	.6902847	.6903733	.6904619	.6905505
491	.6910815	.6911699	.6912584	.6913468	.6914352
492	.6919651	.6920534	.6921416	.6922298	.6923180
493	3.6928469	3.6929350	3.6930231	3.6931111	3.6931991
494	.6937269	.6938148	.6939027	.6939906	.6940785
495	.6946051	.6946929	.6947806	.6948683	.6949560
496	.6954817	.6955692	.6956568	.6957443	.6958318
497	.6963564	.6964438	.6965311	.6966185	.6967058
498	.6972293	.6973165	.6974037	.6974909	.6975780
499	3.6981005	3.6981876	3.6982746	3.6983616	3.6984485
500	.6989700	.6990569	.6991437	.6992305	.6993173
501	.6998377	.6999244	.7000111	.7000977	.7001843
502	.7007037	.7007902	.7008767	.7009632	.7010496
503	.7015680	.7016543	.7017405	.7018269	.7019132
504	.7024305	.7025167	.7026028	.7026890	.7027751
505	3.7032914	3.7033774	3.7034633	3.7035493	3.7036352
506	.7041505	.7042363	.7043221	.7044079	.7044937
507	.7050080	.7050936	.7051792	.7052649	.7053505
508	.7058637	.7059492	.7060347	.7061201	.7062055
509	.7067178	.7068030	.7068884	.7069737	.7070589
510	.7075702	.7076553	.7077405	.7078256	.7079107
511	3.7084209	3.7085059	3.7085908	3.7086758	3.7087607
512	.7092700	.7093548	.7094396	.7095244	.7096091
513	.7101174	.7102020	.7102866	.7103713	.7104559
514	.7109631	.7110476	.7111321	.7112165	.7113010
515	.7118072	.7118915	.7119759	.7120601	.7121444
516	.7126497	.7127339	.7128180	.7129021	.7129862
517	.7134905	.7135745	.7136585	.7137425	.7138264

from 1 to 10000.

Num.	5	6	7	8	9
481	3.6825963	3.6826865	3.6827766	3.6828668	3.6829569
482	.6834972	.6835873	.6836773	.6837673	.6838572
483	.6843965	.6844863	.6845761	.6846659	.6847556
484	.6852938	.6853834	.6854730	.6855626	.6856522
485	.6861892	.6862787	.6863681	.6864575	.6865469
486	.6870828	.6871721	.6872613	.6873506	.6874398
487	3.6879746	3.6880637	3.6881528	3.6882418	3.6883308
488	.6888646	.6889535	.6890423	.6891312	.6892200
489	.6897527	.6898414	.6899301	.6900188	.6901074
490	.6906390	.6907275	.6908161	.6909046	.6909930
491	.6915235	.6916119	.6917002	.6917885	.6918768
492	.6924062	.6924944	.6925826	.6926707	.6927588
493	3.6932872	3.6933752	3.6934631	3.6935511	3.6936390
494	.6941663	.6942541	.6943419	.6944297	.6945174
495	.6950437	.6951311	.6952189	.6953065	.6953941
496	.6959193	.6960067	.6960942	.6961816	.6962690
497	.6967931	.6968804	.6969676	.6970549	.6971421
498	.6976652	.6977523	.6978394	.6979264	.6980135
499	3.6985355	3.6986224	3.6987093	3.6987963	3.6988831
500	.6994041	.6994908	.6995776	.6996643	.6997510
501	.7002709	.7003575	.7004441	.7005307	.7006172
502	.7011361	.7012225	.7013089	.7013953	.7014816
503	.7019995	.7020857	.7021719	.7022582	.7023444
504	.7028612	.7029472	.7030333	.7031193	.7032054
505	3.7037212	3.7038071	3.7038929	3.7039788	3.7040647
506	.7045794	.7046652	.7047509	.7048366	.7049223
507	.7054360	.7055216	.7056072	.7056927	.7057782
508	.7062910	.7063764	.7064617	.7065471	.7066324
509	.7071442	.7072294	.7073146	.7073998	.7074850
510	.7079957	.7080808	.7081659	.7082509	.7083359
511	3.7088456	3.7089305	3.7090154	3.7091003	3.7091851
512	.7096939	.7097786	.7098633	.7099480	.7100327
513	.7105404	.7106250	.7107096	.7107941	.7108786
514	.7113854	.7114698	.7115542	.7116385	.7117229
515	.7122287	.7123129	.7123971	.7124813	.7125655
516	.7130703	.7131544	.7132385	.7133225	.7134065
517	.7139104	.7139943	.7140782	.7141620	.7142459

A TABLE of Logarithms,

Num.	0	1	2	3	4
518	3.7143298	3.7144136	3.7144974	3.7145812	3.7146650
519	.7151674	.7152510	.7153347	.7154183	.7155019
520	.7160033	.7160869	.7161703	.7162538	.7163373
521	.7168377	.7169211	.7170044	.7170877	.7171710
522	.7176705	.7177537	.7178369	.7179200	.7180032
523	.7185017	.7185847	.7186677	.7187507	.7188337
524	3.7193313	3.7194142	3.7194970	3.7195799	3.7196627
525	.7201593	.7202420	.7203247	.7204074	.7204901
526	.7209857	.7210683	.7211508	.7212334	.7213159
527	.7218106	.7218930	.7219754	.7220578	.7221401
528	.7226339	.7227162	.7227984	.7228806	.7229628
529	.7234557	.7235378	.7236198	.7237019	.7237839
530	3.7242759	3.7243578	3.7244397	3.7245216	3.7246035
531	.7250945	.7251763	.7252581	.7253398	.7254215
532	.7259116	.7259933	.7260749	.7261565	.7262380
533	.7267272	.7268087	.7268901	.7269716	.7270531
534	.7275413	.7276226	.7277039	.7277852	.7278664
535	.7283538	.7284349	.7285161	.7285972	.7286784
536	3.7291648	3.7292458	3.7293268	3.7294078	3.7294888
537	.7299743	.7300551	.7301360	.7302168	.7302977
538	.7307823	.7308630	.7309437	.7310244	.7311051
539	.7315888	.7316693	.7317499	.7318304	.7319109
540	.7323938	.7324742	.7325546	.7326350	.7327153
541	.7331973	.7332775	.7333578	.7334380	.7335182
542	3.7339993	3.7340794	3.7341595	3.7342396	3.7343197
543	.7347998	.7348798	.7349598	.7350397	.7351196
544	.7355989	.7356787	.7357585	.7358383	.7359181
545	.7363965	.7364762	.7365558	.7366355	.7367151
546	.7371926	.7372722	.7373517	.7374312	.7375107
547	.7379873	.7380667	.7381461	.7382254	.7383048
548	3.7387806	3.7388595	3.7389390	3.7390182	3.7390974
549	.7395723	.7396514	.7397305	.7398096	.7398886
550	.7403627	.7404416	.7405206	.7405995	.7406784
551	.7411516	.7412304	.7413092	.7413880	.7414668
552	.7419391	.7420177	.7420964	.7421750	.7422537
553	.7427251	.7428037	.7428822	.7429607	.7430392
554	.7435098	.7435881	.7436665	.7437449	.7438232

from 1 to 10000.

N.m.	5	6	7	8	9
51	3.7147488	3.7148323	3.7149162	3.7150000	3.7150837
519	.7155856	.7156691	.7157527	.7158363	.7159198
520	.7164207	.7165042	.7165876	.7166710	.7167544
521	.7172543	.7173376	.7174208	.7175041	.7175873
522	.7180863	.7181694	.7182525	.7183356	.7184186
523	.7189167	.7189996	.7190826	.7191655	.7192484
524	3.7197455	3.7198283	3.7199111	3.7199938	3.7200766
525	.7205727	.7205554	.7207380	.7208206	.7209032
526	.7213984	.7214809	.7215633	.7216458	.7217282
527	.7222225	.7223048	.7223871	.7224694	.7225517
528	.7230450	.7231272	.7232093	.7232914	.7233736
529	.7238660	.7239480	.7240300	.7241120	.7241939
530	3.7246854	3.7247672	3.7248491	3.7249309	3.7250127
531	.7255033	.7255850	.7256667	.7257483	.7258300
532	.7263196	.7264012	.7264827	.7265642	.7266457
533	.7271344	.7272158	.7272972	.7273786	.7274599
534	.7279477	.7280290	.7281101	.7281914	.7282726
535	.7287595	.7288406	.7289216	.7290027	.7290838
536	3.7295697	3.7296507	3.7297316	3.7298125	3.7298934
537	.7303785	.7304593	.7305400	.7306208	.7307015
538	.7311857	.7312663	.7313470	.7314276	.7315082
539	.7319914	.7320719	.7321524	.7322329	.7323133
540	.7327957	.7328760	.7329564	.7330367	.7331170
541	.7335985	.7336787	.7337588	.7338390	.7339191
542	3.7343997	3.7344797	3.7345598	3.7346398	3.7347198
543	.7351995	.7352794	.7353593	.7354392	.7355191
544	.7359979	.7360776	.7361574	.7362371	.7363168
545	.7367948	.7368744	.7369540	.7370335	.7371131
546	.7375902	.7376696	.7377491	.7378285	.7379079
547	.7383841	.7384634	.7385427	.7386220	.7387013
548	3.7391766	3.7392558	3.7393350	3.7394141	3.7394932
549	.7399677	.7400467	.7401257	.7402047	.7402837
550	.7407573	.7408362	.7409151	.7409939	.7410728
551	.7415455	.7416243	.7417030	.7417817	.7418604
552	.7423323	.7424109	.7424895	.7425680	.7426466
553	.7431176	.7431961	.7432745	.7433530	.7434314
554	.7439015	.7439799	.7440582	.7441365	.7442147

A TABLE of Logarithms,

Num.	0	1	2	3	4
555	3.7442930	3.7443712	3.7444495	3.7445277	3.7446059
556	.7450748	.7451529	.7452310	.7453091	.7453871
557	.7458552	.7459332	.7460111	.7460890	.7461670
558	.7466342	.7467120	.7467898	.7468676	.7469454
559	.7474118	.7474895	.7475672	.7476448	.7477225
560	.7481880	.7482656	.7483431	.7484206	.7484981
561	3.7489629	3.7490403	3.7491177	3.7491950	3.7492724
562	.7497363	.7498136	.7498908	.7499681	.7500453
563	.7505084	.7505855	.7506626	.7507398	.7508168
564	.7512791	.7513561	.7514331	.7515100	.7515870
565	.7520484	.7521253	.7522022	.7522790	.7523558
566	.7528164	.7528932	.7529699	.7530466	.7531232
567	3.7535831	3.7536596	3.7537362	3.7538128	3.7538893
568	.7543483	.7544248	.7545012	.7545777	.7546541
569	.7551123	.7551886	.7552649	.7553412	.7554175
570	.7558749	.7559510	.7560272	.7561034	.7561795
571	.7566361	.7567122	.7567882	.7568642	.7569402
572	.7573960	.7574719	.7575479	.7576237	.7576996
573	3.7581546	3.7582304	3.7583062	3.7583819	3.7584577
574	.7589119	.7589875	.7590632	.7591388	.7592144
575	.7596678	.7597434	.7598189	.7598944	.7599699
576	.7604225	.7604979	.7605733	.7606486	.7607240
577	.7611758	.7612511	.7613263	.7614016	.7614768
578	.7619278	.7620030	.7620781	.7621532	.7622283
579	3.7626786	3.7627536	3.7628286	3.7629035	3.7629785
580	.7634280	.7635029	.7635777	.7636526	.7637274
581	.7641761	.7642509	.7643256	.7644003	.7644750
582	.7649230	.7649976	.7650722	.7651468	.7652214
583	.7656686	.7657430	.7658175	.7658920	.7659664
584	.7664128	.7664872	.7665616	.7666359	.7667102
585	3.7671559	3.7672301	3.7673043	3.7673785	3.7674527
586	.7678976	.7679717	.7680458	.7681199	.7681940
587	.7686381	.7687121	.7687860	.7688600	.7689339
588	.7693773	.7694512	.7695250	.7695988	.7696727
589	.7701153	.7701890	.7702627	.7703364	.7704101
590	.7708520	.7709256	.7709992	.7710728	.7711463
591	.7715875	.7716610	.7717344	.7718079	.7718813

from 1 to 10000.

N ^o	5	6	7	8	9
555	3.7446841	3.7447622	3.7448404	3.7449185	3.7449967
556	.7454652	.7455432	.7456212	.7456992	.7457772
557	.7462449	.7463228	.7464006	.7464785	.7465564
558	.7470232	.7471009	.7471787	.7472564	.7473341
559	.7478001	.7478777	.7479553	.7480329	.7481105
560	.7485756	.7486531	.7487306	.7488080	.7488854
561	3.7493498	3.7494271	3.7495044	3.7495817	3.7496590
562	.7501225	.7501997	.7502769	.7503541	.7504312
563	.7508939	.7509710	.7510480	.7511251	.7512021
564	.7516639	.7517409	.7518178	.7518947	.7519716
565	.7524326	.7525094	.7525862	.7526629	.7527397
566	.7531999	.7532766	.7533532	.7534292	.7535065
567	3.7539659	3.7540424	3.7541189	3.7541954	3.7542719
568	.7547305	.7548069	.7548832	.7549596	.7550359
569	.7554937	.7555700	.7556462	.7557224	.7557987
570	.7562556	.7563318	.7564079	.7564840	.7565600
571	.7570162	.7570922	.7571682	.7572441	.7573201
572	.7577755	.7578513	.7579272	.7580030	.7580788
573	3.7585334	3.7586091	3.7586848	3.7587605	3.7588362
574	.7592900	.7593656	.7594412	.7595168	.7595923
575	.7600453	.7601208	.7601962	.7602717	.7603471
576	.7607993	.7608746	.7609500	.7610253	.7611005
577	.7615520	.7616272	.7617024	.7617775	.7618527
578	.7623034	.7623784	.7624535	.7625285	.7626035
579	3.7630534	3.7631284	3.7632033	3.7632782	3.7633531
580	.7638022	.7638770	.7639518	.7640266	.7641014
581	.7645497	.7646244	.7646991	.7647737	.7648484
582	.7652959	.7653705	.7654450	.7655195	.7655941
583	.7660409	.7661153	.7661897	.7662641	.7663385
584	.7667845	.7668588	.7669331	.7670074	.7670816
585	3.7675269	3.7676011	3.7676752	3.7677492	3.7678235
586	.7682680	.7683421	.7684161	.7684901	.7685641
587	.7690079	.7690818	.7691557	.7692296	.7693035
588	.7697465	.7698203	.7698940	.7699678	.7700416
589	.7704838	.7705575	.7706311	.7707048	.7707784
590	.7712199	.7712934	.7713670	.7714405	.7715140
591	.7719547	.7720282	.7721016	.7721750	.7722483

A TABLE of Logarithms,

Num	0	1	2	3	4
592	3.7723217	3.7723951	3.7724684	3.7725417	3.7726150
593	.7730547	.7731279	.7732011	.7732743	.7733475
594	.7737864	.7738596	.7739326	.7740057	.7740788
595	.7745170	.7745899	.7746629	.7747359	.7748088
596	.7752463	.7753191	.7753920	.7754648	.7755375
597	.7759743	.7760471	.7761198	.7761925	.7762652
598	3.7767012	3.7767738	3.7768464	3.7769190	3.7769916
599	.7774268	.7774993	.7775718	.7776443	.7777167
600	.7781513	.7782236	.7782960	.7783683	.7784407
601	.7788745	.7789467	.7790190	.7790912	.7791634
602	.7795905	.7796626	.7797348	.7798069	.7798790
603	.7803173	.7803893	.7804613	.7805333	.7806053
604	3.7810369	3.7811088	3.7811807	3.7812526	3.7813245
605	.7817554	.7818272	.7818989	.7819707	.7820424
606	.7824726	.7825443	.7826159	.7826876	.7827592
607	.7831887	.7832602	.7833318	.7834033	.7834748
608	.7839035	.7839750	.7840464	.7841178	.7841892
609	.7846173	.7846886	.7847599	.7848311	.7849024
610	3.7853298	3.7854010	3.7854722	3.7855434	3.7856145
611	.7860412	.7861123	.7861833	.7862544	.7863254
612	.7867514	.7868224	.7868933	.7869643	.7870352
613	.7874605	.7875313	.7876021	.7876730	.7877438
614	.7881683	.7882391	.7883098	.7883805	.7884512
615	.7888751	.7889457	.7890163	.7890869	.7891575
616	3.7895807	3.7896512	3.7897217	3.7897922	3.7898626
617	.7902852	.7903555	.7904259	.7904963	.7905666
618	.7909885	.7910587	.7911290	.7911992	.7912695
619	.7916906	.7917608	.7918309	.7919011	.7919712
620	.7923917	.7924617	.7925318	.7926018	.7926718
621	.7930916	.7931615	.7932314	.7933014	.7933712
622	3.7937904	3.7938602	3.7939300	3.7939998	3.7940696
623	.7944880	.7945578	.7946274	.7946971	.7947668
624	.7951846	.7952542	.7953238	.7953933	.7954629
625	.7958800	.7959495	.7960190	.7960884	.7961578
626	.7965743	.7966437	.7967131	.7967824	.7968517
627	.7972675	.7973368	.7974060	.7974753	.7975445
628	.7979596	.7980288	.7980979	.7981671	.7982362

from 1 to 10000.

Nun.	5	6	7	8	9
592	3.7726884	3.7727616	3.7728349	3.7729082	3.7729814
593	.7734207	.7734939	.7735670	.7736402	.7737133
594	.7741519	.7742249	.7742979	.7743710	.7744440
595	.7748818	.7749547	.7750276	.7751005	.7751734
596	.7756104	.7756832	.7757560	.7758288	.7759010
597	.7763379	.7764106	.7764833	.7765559	.7766286
598	3.7770642	3.7771367	3.7772093	3.7772818	3.7773543
599	.7777892	.7778616	.7779340	.7780065	.7780789
600	.7785130	.7785853	.7786576	.7787299	.7788022
601	.7792356	.7793078	.7793800	.7794522	.7795243
602	.7799571	.7800291	.7801012	.7801732	.7802453
603	.7806773	.7807492	.7808212	.7808931	.7809650
604	3.7813963	3.7814681	3.7815400	3.7816118	3.7816836
605	.7821141	.7821859	.7822576	.7823293	.7824010
606	.7828308	.7829024	.7829740	.7830456	.7831171
607	.7835463	.7836178	.7836892	.7837607	.7838321
608	.7842606	.7843319	.7844033	.7844746	.7845460
609	.7849737	.7850450	.7851162	.7851874	.7852586
610	3.7856857	3.7857568	3.7858279	3.7858990	3.7859701
611	.7863965	.7864675	.7865385	.7866095	.7866805
612	.7871861	.7871770	.7872479	.7873188	.7873896
613	.7878146	.7878853	.7879561	.7880269	.7880976
614	.7885219	.7885926	.7886632	.7887339	.7888045
615	.7892281	.7892986	.7893691	.7894397	.7895102
616	3.7899331	3.7900035	3.7900739	3.7901444	3.7902148
617	.7906370	.7907073	.7907776	.7908479	.7909182
618	.7913397	.7914099	.7914801	.7915503	.7916205
619	.7920413	.7921114	.7921815	.7922516	.7923216
620	.7927418	.7928118	.7928817	.7929517	.7930217
621	.7934411	.7935110	.7935809	.7936507	.7937206
622	3.7941394	3.7942091	3.7942789	3.7943486	3.7944183
623	.7948365	.7949061	.7949757	.7950454	.7951150
624	.7955324	.7956020	.7956715	.7957410	.7958106
625	.7962273	.7962967	.7963662	.7964356	.7965050
626	.7969211	.7969904	.7970597	.7971290	.7971983
627	.7976137	.7976829	.7977521	.7978213	.7978905
628	.7983053	.7983744	.7984435	.7985125	.7985816

A TABLE of Logarithms,

No.	0	1	2	3	4
629	3.7986506	3.7987197	3.7987887	3.7988577	3.7989267
630	.7993405	.7994095	.7994784	.7995473	.7996162
631	.8000294	.8000982	.8001670	.8002358	.8003046
632	.8007171	.8007858	.8008545	.8009232	.8009919
633	.8014037	.8014723	.8015409	.8016095	.8016781
634	.8020893	.8021578	.8022262	.8022947	.8023632
635	3.8027737	3.8028421	3.8029105	3.8029789	3.8030472
636	.8034571	.8035254	.8035937	.8036619	.8037302
637	.8041394	.8042076	.8042758	.8043439	.8044121
638	.8048207	.8048887	.8049568	.8050248	.8050929
639	.8055009	.8055688	.8056368	.8057047	.8057726
640	.8061800	.8062478	.8063157	.8063835	.8064513
641	3.8068580	3.8069258	3.8069935	3.8070612	3.8071290
642	.8075350	.8076027	.8076703	.8077379	.8078055
643	.8082110	.8082785	.8083460	.8084136	.8084811
644	.8088859	.8089533	.8090207	.8090881	.8091555
645	.8095597	.8096270	.8096944	.8097617	.8098290
646	.8102325	.8102997	.8103670	.8104342	.8105013
647	3.8109043	3.8109714	3.8110385	3.8111056	3.8111727
648	.8115750	.8116420	.8117090	.8117760	.8118430
649	.8122447	.8123116	.8123785	.8124454	.8125123
650	.8129134	.8129802	.8130470	.8131138	.8131805
651	.8135810	.8136477	.8137144	.8137811	.8138478
652	.8142476	.8143142	.8143808	.8144474	.8145140
653	3.8149132	3.8149794	3.8150462	3.8151127	3.8151791
654	.8155777	.8156441	.8157105	.8157769	.8158433
655	.8162413	.8163076	.8163739	.8164402	.8165064
656	.8169038	.8169700	.8170362	.8171024	.8171686
657	.8175645	.8176315	.8176976	.8177636	.8178297
658	.8182259	.8182919	.8183579	.8184239	.8184898
659	3.8188854	3.8189513	3.8190172	3.8190831	3.8191489
660	.8195439	.8196097	.8196755	.8197413	.8198071
661	.8202015	.8202672	.8203328	.8203985	.8204642
662	.8208580	.8209236	.8209892	.8210548	.8211203
663	.8215135	.8215790	.8216445	.8217100	.8217755
664	.8221681	.8222335	.8222989	.8223643	.8224296
665	.8228216	.8228869	.8229522	.8230175	.8230828

from 1 to 10000.

Num.	5	6	7	8	9
629	3.7989957	3.7990647	3.7991337	3.7992027	3.7992710
630	.7996851	.7997540	.7998228	.7998917	.7999605
631	.8003734	.8004421	.8005109	.8005796	.8006484
632	.8010605	.8011292	.8011978	.8012665	.8013351
633	.8017466	.8018152	.8018837	.8019522	.8020208
633	.8024316	.8025001	.8025685	.8026369	.8027053
635	3.8031156	3.8031839	3.8032522	3.8033205	3.8033888
636	.8037984	.8038666	.8039348	.8040031	.8040712
637	.8044802	.8045483	.8046164	.8046845	.8047526
638	.8051609	.8052289	.8052969	.8053649	.8054329
639	.8058405	.8059085	.8059763	.8060442	.8061121
640	.8065191	.8065869	.8066547	.8067225	.8067903
641	3.8071967	3.8072643	3.8073320	3.8073997	3.8074674
642	.8078732	.8079407	.8080083	.8080759	.8081434
643	.8085485	.8086160	.8086835	.8087510	.8088184
644	.8092229	.8092903	.8093577	.8094250	.8094924
645	.8098962	.8099635	.8100308	.8100983	.8101653
646	.8105685	.8106357	.8107029	.8107700	.8108371
647	3.8112398	3.8113068	3.8113739	3.8114409	3.8115080
648	.8119100	.8119769	.8120439	.8121108	.8121778
649	.8125792	.8126460	.8127129	.8127797	.8128465
650	.8132473	.8133141	.8133808	.8134475	.8135143
651	.8139144	.8139811	.8140477	.8141144	.8141810
652	.8145805	.8146471	.8147136	.8147801	.8148467
653	3.8152456	3.8153120	3.8153785	3.8154449	3.8155113
654	.8159096	.8159760	.8160423	.8161087	.8161750
655	.8165727	.8166389	.8167052	.8167714	.8168376
656	.8172347	.8173009	.8173670	.8174331	.8174993
657	.8178958	.8179618	.8180278	.8180939	.8181599
658	.8185558	.8186217	.8186877	.8187536	.8188195
659	3.8192148	3.8192806	3.8193465	3.8194123	3.8194781
660	.8198728	.8199386	.8200043	.8200700	.8201358
661	.8205298	.8205955	.8206611	.8207268	.8207924
662	.8211859	.8212514	.8213170	.8213825	.8214480
663	.8218409	.8219064	.8219718	.8220372	.8221027
664	.8224950	.8225603	.8226257	.8226910	.8227563
665	.8231481	.8232133	.8232786	.8233438	.8234090

A TABLE of Logarithms,

Num.	0	1	2	3	4
666	3.8234742	3.8235394	3.8236046	3.8236698	3.8237350
667	.8241258	.8241909	.8242560	.8243211	.8243862
668	.8247765	.8248415	.8249065	.8249715	.8250364
669	.8254261	.8254910	.8255559	.8256208	.8256857
670	.8260748	.8261396	.8262044	.8262692	.8263340
671	.8267225	.8267872	.8268519	.8269166	.8269813
672	3.8273693	3.8274339	3.8274985	3.8275631	3.8276277
673	.8280151	.8280796	.8281441	.8282086	.8282731
674	.8286599	.8287243	.8287887	.8288532	.8289176
675	.8293038	.8293681	.8294324	.8294967	.8295611
676	.8299467	.8300109	.8300752	.8301394	.8302036
677	.8305887	.8306528	.8307169	.8307811	.8308452
678	3.8312297	3.8312937	3.8313578	3.8314218	3.8314858
679	.8318698	.8319337	.8319977	.8320616	.8321255
680	.8325089	.8325728	.8326366	.8327005	.8327643
681	.8331471	.8332109	.8332746	.8333384	.8334021
682	.8337844	.8338480	.8339117	.8339754	.8340390
683	.8344207	.8344843	.8345479	.8346114	.8346750
684	3.8350561	3.8351196	3.8351831	3.8352465	3.8353100
685	.8356906	.8357540	.8358174	.8358807	.8359441
686	.8363241	.8363874	.8364507	.8365140	.8365773
687	.8369567	.8370199	.8370832	.8371463	.8372095
688	.8375884	.8376516	.8377147	.8377778	.8378409
689	.8382192	.8382822	.8383453	.8384083	.8384713
690	3.8388491	3.8389120	3.8389750	3.8390379	3.8391008
691	.8394780	.8395409	.8396037	.8396666	.8397294
692	.8401061	.8401688	.8402316	.8402943	.8403571
693	.8407332	.8407959	.8408586	.8409212	.8409838
694	.8413595	.8414220	.8414846	.8415472	.8416097
695	.8419848	.8420473	.8421098	.8421722	.8422347
696	3.8426092	3.8426716	3.8427340	3.8427964	3.8428588
697	.8432328	.8432951	.8433574	.8434197	.8434819
698	.8438554	.8439176	.8439798	.8440420	.8441042
699	.8444772	.8445393	.8446014	.8446635	.8447256
700	.8450980	.8451601	.8452221	.8452841	.8453461
701	.8457180	.8457800	.8458419	.8459038	.8459658
702	.8463371	.8463990	.8464608	.8465227	.8465845

from 1 to 10000.

Num.	5	6	7	8	9
666	3.8238002	3.8238653	3.8239305	3.8239956	3.8240607
667	.8244513	.8245163	.8245814	.8246464	.8247114
668	.8251017	.8251664	.8252313	.8252966	.8253612
669	.8257506	.8258154	.8258803	.8259451	.8260100
670	.8263988	.8264635	.8265283	.8265931	.8266578
671	.8270460	.8271107	.8271753	.8272400	.8273046
672	3.8276923	3.8277569	3.8278214	3.8278860	3.8279505
673	.8283376	.8284021	.8284665	.8285310	.8285955
674	.8289820	.8290463	.8291107	.8291751	.8292394
675	.8296254	.8296896	.8297539	.8298182	.8298824
676	.8302678	.8303320	.8303962	.8304603	.8305245
677	.8309093	.8309734	.8310375	.8311016	.8311656
678	3.8315499	3.8316139	3.8316778	3.8317418	3.8318058
679	.8321895	.8322534	.8323173	.8323812	.8324450
680	.8328281	.8328919	.8329558	.8330195	.8330833
681	.8334659	.8335296	.8335933	.8336570	.8337207
682	.8341037	.8341663	.8342299	.8342935	.8343571
683	.8347385	.8348021	.8348656	.8349291	.8349926
684	3.8353753	3.8354369	3.8355003	3.8355638	3.8356272
685	.8360075	.8360708	.8361341	.8361975	.8362608
686	.8366405	.8367038	.8367670	.8368303	.8368935
687	.8372727	.8373359	.8373990	.8374622	.8375253
688	.8379039	.8379670	.8380301	.8380931	.8381562
689	.8385343	.8385973	.8386602	.8387232	.8387861
690	3.8391637	3.8392266	3.8392895	3.8393523	3.8394152
691	.8397922	.8398550	.8399178	.8399806	.8400433
692	.8404198	.8404825	.8405452	.8406079	.8406706
693	.8410465	.8411091	.8411717	.8412343	.8412969
694	.8416722	.8417348	.8417973	.8418598	.8419223
695	.8422971	.8423596	.8424220	.8424844	.8425468
696	3.8429211	3.8429835	3.8430458	3.8431081	3.8431705
697	.8435442	.8436065	.8436687	.8437310	.8437932
698	.8441664	.8442286	.8442907	.8443529	.8444150
699	.8447877	.8448498	.8449119	.8449739	.8450360
700	.8454081	.8454701	.8455321	.8455941	.8456561
701	.8460277	.8460896	.8461515	.8462134	.8462752
702	.8466463	.8467081	.8467700	.8468318	.8468935

A TABLE of Logarithms,

Num.	0	1	2	3	4
703	3.8469553	3.8470171	3.8470789	3.8471406	3.8472024
704	.8475727	.8476343	.8476960	.8477577	.8478193
705	.8481891	.8482507	.8483123	.8483739	.8484355
706	.8488047	.8488662	.8489277	.8489892	.8490507
707	.8494194	.8494808	.8495423	.8496037	.8496651
708	.8500333	.8500946	.8501559	.8502172	.8502786
709	3.8506462	3.8507075	3.8507687	3.8508300	3.8508912
710	.8512583	.8513195	.8513807	.8514418	.8515030
711	.8518696	.8519307	.8519917	.8520528	.8521139
712	.8524800	.8525410	.8526020	.8526629	.8527239
713	.8530895	.8531504	.8532113	.8532722	.8533331
714	.8536982	.8537590	.8538198	.8538806	.8539414
715	3.8543060	3.8543668	3.8544275	3.8544882	3.8545489
716	.8549130	.8549737	.8550343	.8550949	.8551556
717	.8555192	.8555797	.8556403	.8557008	.8557614
718	.8561244	.8561849	.8562454	.8563059	.8563663
719	.8567289	.8567893	.8568497	.8569101	.8569704
720	.8573325	.8573928	.8574531	.8575134	.8575737
721	3.8579353	3.8579955	3.8580557	3.8581159	3.8581761
722	.8585372	.8585973	.8586575	.8587176	.8587777
723	.8591383	.8591984	.8592584	.8593185	.8593785
724	.8597386	.8597985	.8598585	.8599185	.8599784
725	.8603380	.8603979	.8604578	.8605177	.8605776
726	.8609366	.8609964	.8610562	.8611160	.8611758
727	3.8615344	3.8615941	3.8616539	3.8617136	3.8617733
728	.8621314	.8621910	.8622507	.8623103	.8623699
729	.8627275	.8627871	.8628467	.8629062	.8629658
730	.8633229	.8633823	.8634418	.8635013	.8635608
731	.8639174	.8639768	.8640362	.8640956	.8641550
732	.8645111	.8645704	.8646297	.8646890	.8647483
733	3.8651040	3.8651632	3.8652225	3.8652817	3.8653409
734	.8656961	.8657552	.8658144	.8658735	.8659327
735	.8662873	.8663464	.8664055	.8664646	.8665236
736	.8668778	.8669368	.8669958	.8670548	.8671138
737	.8674675	.8675264	.8675853	.8676442	.8677031
738	.8680564	.8681152	.8681749	.8682329	.8682917
739	.8686444	.8687032	.8687620	.8688207	.8688794

from 1 to 10000.

Num.	5	6	7	8	9
703	3.8472641	3.8473258	3.8473876	3.8474493	3.8475110
704	.8478810	.8479426	.8480043	.8480659	.8481275
705	.8484970	.8485586	.8486201	.8486817	.8487432
706	.8491122	.8491736	.8492351	.8492965	.8493580
707	.8497264	.8497878	.8498492	.8499106	.8499719
708	.8503399	.8504011	.8504624	.8505237	.8505850
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709	3.8509524	3.8510136	3.8510748	3.8511360	3.8511972
710	.8515641	.8516252	.8516863	.8517474	.8518085
711	.8521749	.8522359	.8522970	.8523580	.8524109
712	.8527849	.8528458	.8529068	.8529677	.8530286
713	.8533940	.8534548	.8535157	.8535765	.8536374
714	.8540022	.8540630	.8541238	.8541845	.8542453
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715	3.8546096	3.8546703	3.8547310	3.8547917	3.8548524
716	.8552162	.8552768	.8553374	.8553980	.8554586
717	.8558219	.8558824	.8559429	.8560035	.8560640
718	.8564268	.8564872	.8565476	.8566081	.8566685
719	.8570308	.8570912	.8571515	.8572118	.8572722
720	.8576340	.8576943	.8577545	.8578148	.8578750
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721	3.8582363	3.8582965	3.8583567	3.8584169	3.8584770
722	.8588379	.8588980	.8589581	.8590181	.8590782
723	.8594385	.8594986	.8595586	.8596186	.8596786
724	.8600384	.8600983	.8601583	.8602182	.8602781
725	.8606374	.8606973	.8607571	.8608170	.8608768
726	.8612356	.8612954	.8613552	.8614149	.8614747
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727	3.8618330	3.8618927	3.8619524	3.8620120	3.8620717
728	.8624296	.8624892	.8625488	.8626084	.8626679
729	.8630253	.8630848	.8631443	.8632039	.8632634
730	.8636202	.8636797	.8637391	.8637985	.8638580
731	.8642143	.8642737	.8643331	.8643924	.8644517
732	.8648076	.8648669	.8649262	.8649855	.8650447
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733	3.8654001	3.8654593	3.8655185	3.8655777	3.8656369
734	.8659918	.8660509	.8661100	.8661691	.8662282
735	.8665827	.8666417	.8667008	.8667598	.8668188
736	.8671728	.8672317	.8672907	.8673496	.8674086
737	.8677620	.8678209	.8678798	.8679387	.8679975
738	.8683505	.8684093	.8684681	.8685269	.8685857
739	.8689382	.8689969	.8690556	.8691143	.8691730

A TABLE of Logarithms,

Num.	0	1	2	3	4
740	3.8692317	3.8692904	3.8693491	3.8694077	3.8694664
741	.8698182	.8698768	.8699345	.8699940	.8700526
742	.8704039	.8704624	.8705209	.8705795	.8706380
743	.8709888	.8710473	.8711057	.8711641	.8712226
744	.8715729	.8716313	.8716897	.8717480	.8718064
745	.8721563	.8722146	.8722728	.8723311	.8723894
746	3.8727388	3.8727970	3.8728552	3.8729134	3.8729716
747	.8733206	.8733788	.8734369	.8734950	.8735531
748	.8739016	.8739597	.8740177	.8740757	.8741338
749	.8744818	.8745398	.8745978	.8746557	.8747137
750	.8750613	.8751192	.8751771	.8752349	.8752928
751	.8756399	.8756974	.8757556	.8758134	.8758712
752	3.8762178	3.8762756	3.8763333	3.8763911	3.8764488
753	.8767950	.8768526	.8769103	.8769680	.8770256
754	.8773713	.8774289	.8774865	.8775441	.8776017
755	.8779469	.8780045	.8780620	.8781195	.8781770
756	.8785281	.8785792	.8786367	.8786941	.8787515
757	.8790959	.8791532	.8792106	.8792680	.8793253
758	3.8796692	3.8797265	3.8797838	3.8798411	3.8798983
759	.8802418	.8802990	.8803562	.8804134	.8804706
760	.8808136	.8808707	.8809279	.8809850	.8810421
761	.8813847	.8814417	.8814988	.8815558	.8816129
762	.8819550	.8820120	.8820689	.8821259	.8821829
763	.8825245	.8825815	.8826384	.8826953	.8827522
764	3.8830934	3.8831502	3.8832070	3.8832639	3.8833207
765	.8836614	.8837182	.8837750	.8838317	.8838885
766	.8842288	.8842855	.8843421	.8843988	.8844555
767	.8847954	.8848520	.8849086	.8849652	.8850218
768	.8853612	.8854178	.8854743	.8855308	.8855874
769	.8859263	.8859828	.8860393	.8860957	.8861522
770	3.8864907	3.8865471	3.8866035	3.8866599	3.8867163
771	.8870544	.8871107	.8871670	.8872233	.8872796
772	.8876173	.8876736	.8877298	.8877860	.8878423
773	.8881795	.8882357	.8882918	.8883480	.8884042
774	.8887410	.8887971	.8888532	.8889093	.8889653
775	.8893017	.8893577	.8894138	.8894698	.8895258
776	.8898617	.8899177	.8899736	.8900296	.8900855

from 1 to 10000.

Nur.	5	6	7	8	9
740	3.8695251	3.8695837	3.8696423	3.8697010	3.8697596
741	.8701112	.8701697	.8702283	.8702868	.8703454
742	.8706965	.8707549	.8708134	.8708719	.8709394
743	.8712810	.8713394	.8713978	.8714562	.8715146
744	.8718647	.8719230	.8719814	.8720397	.8720980
745	.8724476	.8725059	.8725641	.8726224	.8726806
746	3.8730298	3.8730880	3.8731461	3.8732043	3.8732625
747	.8736112	.8736693	.8737274	.8737855	.8738435
748	.8741918	.8742498	.8743078	.8743658	.8744238
749	.8747716	.8748296	.8748875	.8749454	.8750034
750	.8753507	.8754086	.8754664	.8755243	.8755821
751	.8759290	.8759868	.8760445	.8761023	.8761601
752	3.8765065	3.8765642	3.8766219	3.8766796	3.8767373
753	.8770833	.8771409	.8771985	.8772561	.8773137
754	.8776592	.8777168	.8777743	.8778319	.8778894
755	.8782345	.8782919	.8783494	.8784069	.8784643
756	.8788089	.8788663	.8789237	.8789811	.8790385
757	.8793826	.8794400	.8794973	.8795546	.8796119
758	3.8799556	3.8800128	3.8800701	3.8801273	3.8801846
759	.8805278	.8805850	.8806421	.8806993	.8807564
760	.8810992	.8811663	.8812134	.8812705	.8813276
761	.8816699	.8817269	.8817840	.8818410	.8818980
762	.8822398	.8822968	.8823537	.8824107	.8824676
763	.8828090	.8828659	.8829228	.8829797	.8830365
764	3.8833775	3.8834343	3.8834911	3.8835479	3.8836047
765	.8839452	.8840019	.8840586	.8841154	.8841721
766	.8845122	.8845688	.8846255	.8846821	.8847387
767	.8850784	.8851350	.8851915	.8852481	.8853047
768	.8856439	.8857004	.8857569	.8858134	.8858699
769	.8862086	.8862651	.8863215	.8863779	.8864343
770	3.8867726	3.8868290	3.8868854	3.8869417	3.8869980
771	.8873359	.8873922	.8874485	.8875048	.8875610
772	.8878985	.8879547	.8880109	.8880671	.8881233
773	.8884603	.8885165	.8885726	.8886287	.8886848
774	.8890214	.8890775	.8891336	.8891896	.8892457
775	.8895818	.8896378	.8896938	.8897498	.8898058
776	.8901415	.8901974	.8902533	.8903092	.8903651

A TABLE of Logarithms,

Num.	0	1	2	3	4
777	3.8904210	3.8904769	3.8905328	3.8905887	3.8906445
778	.8909796	.8910354	.8910912	.8911470	.8912028
779	.8915375	.8915932	.8916489	.8917047	.8917604
780	.8920946	.8921503	.8922059	.8922616	.8923173
781	.8926510	.8927066	.8927622	.8928178	.8928734
782	.8932068	.8932623	.8933178	.8933733	.8934288
783	3.8937618	3.8938172	3.8938727	3.8939281	3.8939836
784	.8943161	.8943715	.8944268	.8944822	.8945376
785	.8948697	.8949250	.8949803	.8950356	.8950909
786	.8954225	.8954778	.8955330	.8955883	.8956435
787	.8959747	.8960299	.8960851	.8961403	.8961954
788	.8965262	.8965813	.8966364	.8966915	.8967466
789	3.8970770	3.8971320	3.8971871	3.8972421	3.8972971
790	.8976271	.8976821	.8977370	.8977920	.8978469
791	.8981765	.8982314	.8982863	.8983412	.8983960
792	.8987252	.8987800	.8988348	.8988897	.8989445
793	.8992732	.8993279	.8993827	.8994375	.8994922
794	.8998205	.8998752	.8999299	.8999846	.9000392
795	3.9003671	3.9004218	3.9004764	3.9005310	3.9005856
796	.9009131	.9009676	.9010222	.9010767	.9011313
797	.9014583	.9015128	.9015673	.9016218	.9016762
798	.9020029	.9020573	.9021117	.9021661	.9022205
799	.9025468	.9026011	.9026555	.9027098	.9027641
800	.9030900	.9031443	.9031985	.9032528	.9033071
801	3.9036325	3.9036867	3.9037409	3.9037951	3.9038493
802	.9041744	.9042285	.9042827	.9043368	.9043909
803	.9047155	.9047695	.9048237	.9048778	.9049318
804	.9052560	.9053101	.9053641	.9054181	.9054721
805	.9057960	.9058498	.9059038	.9059577	.9060116
806	.9063351	.9063889	.9064428	.9064967	.9065505
807	3.9068735	3.9069273	3.9069812	3.9070350	3.9070887
808	.9074114	.9074651	.9075188	.9075726	.9076263
809	.9079485	.9080022	.9080559	.9081095	.9081632
810	.9084850	.9085386	.9085922	.9086458	.9086994
811	.9090209	.9090744	.9091279	.9091815	.9092350
812	.9095560	.9096095	.9096630	.9097165	.9097699
813	.9100905	.9101440	.9101974	.9102508	.9103042

from 1 to 10000.

Num.	5	6	7	8	9
777	3.8907004	3.8907562	3.8908121	3.8908679	3.8909238
778	.8912586	.8913144	.8913702	.8914259	.8914817
779	.8918161	.8918718	.8919275	.8919832	.8920389
780	.8923729	.8924285	.8924842	.8925398	.8925954
781	.8929290	.8929846	.8930401	.8930957	.8931512
782	.8934843	.8935398	.8935953	.8936508	.8937063
783	3.8940390	3.8940944	3.8941498	3.8942053	3.8942607
784	.8945929	.8946483	.8947037	.8947590	.8948143
785	.8951462	.8952015	.8952568	.8953120	.8953673
786	.8956987	.8957539	.8958091	.8958643	.8959195
787	.8962506	.8963057	.8963608	.8964160	.8964711
788	.8968017	.8968568	.8969118	.8969669	.8970220
789	3.8973521	3.8974071	3.8974621	3.8975171	3.8975721
790	.8979019	.8979568	.8980117	.8980667	.8981216
791	.8984509	.8985058	.8985606	.8986155	.8986703
792	.8989993	.8990541	.8991089	.8991636	.8992184
793	.8995469	.8996017	.8996564	.8997111	.8997658
794	.9000939	.9001486	.9002032	.9002579	.9003125
795	3.9006402	3.9006948	3.9007494	3.9008039	3.9008585
796	.9011858	.9012403	.9012948	.9013493	.9014038
797	.9017307	.9017851	.9018396	.9018940	.9019485
798	.9022749	.9023293	.9023837	.9024381	.9024924
799	.9028185	.9028728	.9029271	.9029814	.9030357
800	.9033613	.9034156	.9034698	.9035241	.9035783
801	3.9039035	3.9039577	3.9040119	3.9040661	3.9041202
802	.9044450	.9044992	.9045533	.9046074	.9046615
803	.9049859	.9050399	.9050940	.9051480	.9052020
804	.9055261	.9055800	.9056340	.9056880	.9057420
805	.9060656	.9061195	.9061734	.9062273	.9062812
806	.9066044	.9066582	.9067121	.9067659	.9068197
807	3.9071425	3.9071963	3.9072501	3.9073038	3.9073576
808	.9076800	.9077337	.9077874	.9078411	.9078948
809	.9082169	.9082705	.9083241	.9083778	.9084314
810	.9087530	.9088066	.9088602	.9089137	.9089673
811	.9092885	.9093420	.9093955	.9094490	.9095025
812	.9098234	.9098768	.9099303	.9099837	.9100371
813	.9103576	.9104109	.9104643	.9105177	.9105710

A T A B L E of Logarithms,

<i>Num.</i>	0	1	2	3	4
814	3.9106244	3.9106778	3.9107311	3.9107844	3.9108378
815	.9111576	.9112109	.9112642	.9113174	.9113707
816	.9116902	.9117434	.9117966	.9118498	.9119030
817	.9122220	.9122752	.9123284	.9123815	.9124346
818	.9127533	.9128064	.9128595	.9129126	.9129656
819	.9132839	.9133369	.9133899	.9134430	.9134960
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820	3.9138139	3.9138668	3.9139198	3.9139727	3.9140257
821	.9143432	.9143961	.9144489	.9145018	.9145547
822	.9148718	.9149246	.9149775	.9150303	.9150831
823	.9153998	.9154526	.9155054	.9155581	.9156109
824	.9159272	.9159799	.9160326	.9160853	.9161380
825	.9164539	.9165066	.9165592	.9166118	.9166645
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826	3.9169800	3.9170326	3.9170852	3.9171378	3.9171903
827	.9175055	.9175580	.9176105	.9176630	.9177155
828	.9180303	.9180828	.9181253	.9181877	.9182401
829	.9185545	.9186069	.9186593	.9187117	.9187640
830	.9190781	.9191304	.9191827	.9192350	.9192873
831	.9196010	.9196533	.9197055	.9197578	.9198100
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832	3.9201233	3.9201755	3.9202277	3.9202799	3.9203321
833	.9206450	.9206971	.9207493	.9208014	.9208535
834	.9211661	.9212181	.9212702	.9213222	.9213743
835	.9216865	.9217385	.9217905	.9218425	.9218945
836	.9222063	.9222582	.9223102	.9223621	.9224140
837	.9227255	.9227773	.9228292	.9228811	.9229330
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838	3.9232440	3.9232958	3.9233477	3.9233995	3.9234513
839	.9237620	.9238137	.9238655	.9239172	.9239690
840	.9242793	.9243310	.9243827	.9244344	.9244860
841	.9247960	.9248476	.9248993	.9249509	.9250025
842	.9253121	.9253637	.9254152	.9254668	.9255184
843	.9258276	.9258791	.9259306	.9259821	.9260336
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844	3.9263424	3.9263939	3.9264453	3.9264968	3.9265482
845	.9268567	.9269081	.9269595	.9270109	.9270622
846	.9273704	.9274217	.9274730	.9275243	.9275757
847	.9278834	.9279347	.9279859	.9280372	.9280885
848	.9283959	.9284471	.9284983	.9285495	.9286007
849	.9289077	.9289588	.9290100	.9290611	.9291123
850	.9294189	.9294700	.9295211	.9295722	.9296233

from 1 to 10000.

Num.	5	6	7	8	9
814	3.9108911	3.9109444	3.9109977	3.9110510	3.9111043
815	.9114240	.9114772	.9115305	.9115837	.9116369
816	.9119563	.9120094	.9120626	.9121157	.9121689
817	.9124878	.9125409	.9125940	.9126471	.9127002
818	.9130187	.9130717	.9131248	.9131778	.9132309
819	.9135490	.9136019	.9136549	.9137079	.9137609
820	3.9140786	3.9141315	3.9141844	3.9142373	3.9142903
821	.9146076	.9146604	.9147133	.9147661	.9148190
822	.9151359	.9151887	.9152415	.9152943	.9153471
823	.9156636	.9157163	.9157691	.9158218	.9158745
824	.9161907	.9162433	.9162960	.9163487	.9164013
825	.9167171	.9167697	.9168223	.9168749	.9169275
826	3.9172429	3.9172954	3.9173479	3.9174005	3.9174530
827	.9177680	.9178205	.9178730	.9179254	.9179779
828	.9182925	.9183449	.9183973	.9184497	.9185021
829	.9188164	.9188687	.9189211	.9189734	.9190258
830	.9193396	.9193919	.9194442	.9194965	.9195488
831	.9198623	.9199145	.9199667	.9200189	.9200711
832	3.9203842	3.9204364	3.9204886	3.9205407	3.9205929
833	.9209056	.9209577	.9210098	.9210619	.9211140
834	.9214263	.9214784	.9215304	.9215824	.9216345
835	.9219465	.9219984	.9220504	.9221024	.9221543
836	.9224659	.9225179	.9225698	.9226217	.9226736
837	.9229848	.9230367	.9230885	.9231404	.9231922
838	3.9235031	3.9235549	3.9236066	3.9236584	3.9237102
839	.9240208	.9240724	.9241242	.9241759	.9242276
840	.9245377	.9245894	.9246410	.9246927	.9247444
841	.9250541	.9251057	.9251573	.9252089	.9252605
842	.9255699	.9256215	.9256730	.9257245	.9257761
843	.9260851	.9261366	.9261880	.9262395	.9262910
844	3.9265997	3.9266511	3.9267025	3.9267539	3.9268053
845	.9271136	.9271650	.9272163	.9272677	.9273190
846	.9276270	.9276783	.9277296	.9277808	.9278321
847	.9281397	.9281909	.9282422	.9282934	.9283446
848	.9286518	.9287030	.9287542	.9288054	.9288565
849	.9291634	.9292145	.9292656	.9293167	.9293678
850	.9296743	.9297254	.9297764	.9298275	.9298785

A TABLE of Logarithms,

Num.	0	1	2	3	4
851	3.9299296	3.9299806	3.9300316	3.9300826	3.9301336
852	.9304396	.9304906	.9305445	.9305925	.9306434
853	.9309490	.9309999	.9310508	.9311017	.9311526
854	.9314579	.9315087	.9315596	.9316104	.9316612
855	.9319661	.9320169	.9320677	.9321185	.9321692
856	.9324738	.9325245	.9325752	.9326259	.9326767
857	3.9329808	3.9330315	3.9330822	3.9331328	3.9331835
858	.9334873	.9335379	.9335885	.9336391	.9336897
859	.9339932	.9340437	.9340943	.9341448	.9341953
860	.9344984	.9345489	.9345994	.9346499	.9347004
861	.9350032	.9350536	.9351040	.9351544	.9352049
862	.9355073	.9355576	.9356080	.9356584	.9357087
863	3.9360108	3.9360611	3.9361114	3.9361617	3.9362120
864	.9365137	.9365640	.9366143	.9366645	.9367148
865	.9370161	.9370663	.9371165	.9371667	.9372169
866	.9375179	.9375680	.9376182	.9376683	.9377184
867	.9380191	.9380692	.9381193	.9381693	.9382194
868	.9385197	.9385698	.9386198	.9386698	.9387198
869	3.9390198	3.9390697	3.9391197	3.9391697	3.9392196
870	.9395193	.9395692	.9396191	.9396690	.9397189
871	.9400182	.9400680	.9401179	.9401677	.9402176
872	.9405165	.9405663	.9406161	.9406659	.9407157
873	.9410142	.9410640	.9411137	.9411635	.9412132
874	.9415114	.9415611	.9416108	.9416605	.9417101
875	3.9420081	3.9420577	3.9421073	3.9421569	3.9422065
876	.9425041	.9425537	.9426032	.9426528	.9427024
877	.9429996	.9430491	.9430986	.9431481	.9431976
878	.9434945	.9435440	.9435934	.9436429	.9436923
879	.9439889	.9440383	.9440877	.9441371	.9441865
880	.9444827	.9445320	.9445814	.9446307	.9446800
881	3.9449759	3.9450252	3.9450745	3.9451238	3.9451730
882	.9454686	.9455178	.9455671	.9456163	.9456655
883	.9459607	.9460099	.9460591	.9461082	.9461574
884	.9464523	.9465014	.9465505	.9465996	.9466487
885	.9469433	.9469923	.9470414	.9470905	.9471395
886	.9474337	.9474827	.9475317	.9475807	.9476297
887	.9479236	.9479726	.9480215	.9480705	.9481194

from 1 to 10000.

Num.	5	6	7	8	9
851	3.9301847	3.9302357	2.9302866	3.9303376	3.9303886
852	.9306944	.9307453	.9307963	.9308472	.9308981
853	.9312035	.9312544	.9313053	.9313561	.9314070
854	.9317121	.9317629	.9318137	.9318645	.9319153
855	.9322200	.9322708	.9323215	.9323723	.9324230
856	.9327274	.9327781	.9328288	.9328795	.9329301
857	3.9332341	3.9332848	3.9333354	3.9333860	3.9334367
858	.9337403	.9337909	.9338415	.9337920	.9339426
859	.9342459	.9342964	.9343469	.9343974	.9344479
860	.9347509	.9348013	.9348518	.9349022	.9349527
861	.9352553	.9353057	.9353561	.9354065	.9354569
862	.9357591	.9358095	.9358598	.9359101	.9359605
863	3.9362623	3.9363126	3.9363629	3.9364132	3.9364635
864	.9367650	.9368152	.9368655	.9369157	.9369659
865	.9372671	.9373172	.9373674	.9374176	.9374677
866	.9377686	.9378187	.9378688	.9379189	.9379690
867	.9382695	.9383195	.9383696	.9384196	.9384697
868	.9387698	.9388198	.9388698	.9389198	.9389698
869	3.9392696	3.9393195	3.9393695	3.9394194	3.9394693
870	.9397688	.9398187	.9398685	.9399184	.9399683
871	.9402674	.9403172	.9403670	.9404169	.9404667
872	.9407654	.9408152	.9408650	.9409147	.9409645
873	.9412629	.9413126	.9413623	.9414120	.9414617
874	.9417598	.9418095	.9418591	.9419088	.9419584
875	3.9422561	3.9423058	3.9423553	3.9424049	3.9424545
876	.9427519	.9428015	.9429510	.9429005	.9429501
877	.9432471	.9432966	.9433461	.9433956	.9434450
878	.9437418	.9437912	.9438406	.9438900	.9439395
879	.9442358	.9442852	.9443346	.9443840	.9444333
880	.9447294	.9447787	.9448280	.9448773	.9449266
881	3.9452223	3.9452716	3.9453208	3.9453701	3.9454193
882	.9457147	.9457639	.9458131	.9458623	.9459115
883	.9462066	.9462557	.9463048	.9463540	.9464031
884	.9466978	.9467469	.9467960	.9468451	.9468942
885	.9471886	.9472376	.9472866	.9473357	.9473847
886	.9476787	.9477277	.9477767	.9478257	.9478747
887	.9481684	.9482173	.9482662	.9483151	.9483641

A TABLE of Logarithms,

Num.	0	1	2	3	4
888	3.9484130	3.9484619	3.9485108	3.9485597	3.9486085
889	.9489018	.9489507	.9489994	.9490483	.9490971
890	.9493900	.9494388	.9494876	.9495364	.9495851
891	.9498777	.9499264	.9499752	.9500239	.9500726
892	.9503649	.9504135	.9504622	.9505109	.9505596
893	.9508515	.9509001	.9509487	.9509973	.9510459
894	3.9513375	3.9513861	3.9514347	3.9514832	3.9515318
895	.9518230	.9518716	.9519201	.9519686	.9520171
896	.9523080	.9523565	.9524049	.9524534	.9525018
897	.9527924	.9528409	.9528893	.9529377	.9529861
898	.9532763	.9533247	.9533730	.9534214	.9534697
899	.9537597	.9538080	.9538563	.9539046	.9539529
900	3.9542425	3.9542908	3.9543390	3.9543872	3.9544355
901	.9547248	.9547730	.9548212	.9548694	.9549176
902	.9552065	.9552547	.9553028	.9553510	.9553991
903	.9556877	.9557358	.9557839	.9558320	.9558801
904	.9561684	.9562165	.9562645	.9563125	.9563605
905	.9566486	.9566966	.9567445	.9567925	.9568405
906	3.9571282	3.9571761	3.9572241	3.9572720	3.9573199
907	.9576073	.9576552	.9577030	.9577509	.9577988
908	.9580858	.9581337	.9581815	.9582293	.9582771
909	.9585639	.9586117	.9586594	.9587072	.9587546
910	.9590414	.9590891	.9591368	.9591845	.9592322
911	.9595184	.9595660	.9596137	.9596614	.9597090
912	3.9599948	3.9600425	3.9600901	3.9601377	3.9601853
913	.9604708	.9605183	.9605659	.9606135	.9606610
914	.9609462	.9609937	.9610412	.9610887	.9611362
915	.9614211	.9614686	.9615160	.9615635	.9616109
916	.9618955	.9619429	.9619903	.9620377	.9620851
917	.9623693	.9624167	.9624640	.9625114	.9625587
918	3.9628427	3.9628900	3.9629373	3.9629846	3.9630319
919	.9633155	.9633628	.9634100	.9634573	.9635045
920	.9637878	.9638350	.9638822	.9639294	.9639766
921	.9642596	.9643068	.9643539	.9644011	.9644482
922	.9647309	.9647780	.9648251	.9648722	.9649193
923	.9652017	.9652488	.9652958	.9653428	.9653899
924	.9656720	.9657190	.9657660	.9658130	.9658599

from 1 to 10000.

Num	5	6	7	8	9
888	3.9486574	3.9487063	3.9487552	3.9488040	3.9488529
889	.9491460	.9491948	.9492436	.9492924	.9493412
890	.9496339	.9496827	.9497314	.9497802	.9498290
891	.9501213	.9501701	.9502188	.9502675	.9503162
892	.9506081	.9506569	.9507055	.9507542	.9508028
893	.9510946	.9511432	.9511918	.9512404	.9512889
894	3.9515803	3.9516289	3.9516774	3.9517260	3.9517745
895	.9520656	.9521141	.9521626	.9522111	.9522595
896	.9525503	.9525987	.9526472	.9526956	.9527440
897	.9530345	.9530828	.9531312	.9531796	.9532280
898	.9535181	.9535664	.9536147	.9536631	.9537114
899	.9540012	.9540494	.9540977	.9541460	.9541943
900	3.9544837	3.9545319	3.9545802	3.9546284	3.9546766
901	.9549657	.9550139	.9550621	.9551101	.9551584
902	.9554472	.9554953	.9555434	.9555915	.9556397
903	.9559282	.9559762	.9560243	.9560723	.9561204
904	.9564086	.9564566	.9565045	.9565526	.9566006
905	.9568885	.9569364	.9569844	.9570323	.9570803
906	3.9573678	3.9574157	3.9574636	3.9575115	3.9575594
907	.9578466	.9578945	.9579423	.9579902	.9580380
908	.9583249	.9583727	.9584205	.9584683	.9585161
909	.9588027	.9588505	.9588982	.9589459	.9589937
910	.9592799	.9593276	.9593753	.9594230	.9594707
911	.9597567	.9598043	.9598520	.9598996	.9599472
912	3.9602329	3.9602805	3.9603280	3.9603756	3.9604232
913	.9607086	.9607561	.9608036	.9608512	.9608987
914	.9611837	.9612312	.9612787	.9613262	.9613736
915	.9616583	.9617058	.9617532	.9618006	.9618481
916	.9621325	.9621799	.9622272	.9622746	.9623220
917	.9626061	.9626534	.9627007	.9627481	.9627954
918	3.9630792	3.9631264	3.9631737	3.9632210	3.9632683
919	.9635517	.9635990	.9636462	.9636934	.9637406
920	.9640238	.9640710	.9641181	.9641653	.9642125
921	.9644953	.9645425	.9645896	.9646367	.9646838
922	.9649664	.9650134	.9650605	.9651076	.9651546
923	.9654369	.9654839	.9655309	.9655780	.9656250
924	.9659069	.9659539	.9660009	.9660478	.9660948

A T A B L E of Logarithms,

N ^{um} .	0	1	2	3	4
925	3.9661417	3.9661887	3.9662356	3.9662826	3.9663295
926	.9666110	.9666579	.9667048	.9667517	.9667985
927	.9670797	.9671266	.9671734	.9672203	.9672671
928	.9675480	.9675948	.9676416	.9676883	.9677351
929	.9680157	.9680625	.9681092	.9681559	.9682027
930	.9684829	.9685296	.9685763	.9686230	.9686697
931	3.9689497	3.9689963	3.9690430	3.9690895	3.9691362
932	.9694159	.9694625	.9695091	.9695557	.9696023
933	.9698816	.9699282	.9699747	.9700213	.9700678
934	.9703469	.9703934	.9704399	.9704863	.9705328
935	.9708116	.9708581	.9709045	.9709509	.9709974
936	.9712758	.9713222	.9713686	.9714150	.9714614
937	3.9717396	3.9717859	3.9718323	3.9718786	3.9719249
938	.9722028	.9722491	.9722954	.9723417	.9723880
939	.9726656	.9727118	.9727581	.9728043	.9728505
940	.9731278	.9731741	.9732202	.9732664	.9733126
941	.9735896	.9736357	.9736819	.9737281	.9737742
942	.9740509	.9740970	.9741431	.9741892	.9742353
943	3.9745117	3.9745577	3.9746037	3.9746498	3.9746959
944	.9749720	.9750180	.9750640	.9751100	.9751560
945	.9754318	.9754778	.9755237	.9755697	.9756156
946	.9758911	.9759370	.9759829	.9760288	.9760747
947	.9763500	.9763958	.9764417	.9764875	.9765334
948	.9768083	.9768541	.9768999	.9769457	.9769915
949	3.9772662	3.9773120	3.9773577	3.9774035	3.9774492
950	.9777236	.9777693	.9778150	.9778607	.9779064
951	.9781805	.9782262	.9782718	.9783175	.9783631
952	.9786369	.9786826	.9787282	.9787738	.9788194
953	.9790929	.9791385	.9791840	.9792295	.9792751
954	.9795484	.9795939	.9796394	.9796849	.9797304
955	3.9800034	3.9800488	3.9800943	3.9801398	3.9801852
956	.9804579	.9805033	.9805487	.9805942	.9806396
957	.9809119	.9809573	.9810027	.9810481	.9810934
958	.9813655	.9814108	.9814562	.9815015	.9815468
959	.9818185	.9818639	.9819092	.9819544	.9819997
960	.9822712	.9823165	.9823617	.9824069	.9824522
961	.9827234	.9827686	.9828138	.9828589	.9829041

from 1 to 10000.

Num	5	6	7	8	9
925	3.9663764	3.9664133	3.9664703	3.9665172	3.9665641
926	.9668454	.9668923	.9669392	.9669860	3.9670329
927	.9673139	.9673607	.9674076	.9674544	.9675012
928	.9677819	.9678287	.9678754	.9679222	.9679690
929	.9682494	.9682961	.9683428	.9683895	.9684362
930	.9687164	.9687630	.9688097	.9688564	.9689030
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931	3.9691829	3.9692295	3.9692761	3.9693227	3.9693693
932	.9696488	.9696954	.9697420	.9697885	.9698351
933	.9701143	.9701608	.9702074	.9702539	.9703004
934	.9705793	.9706258	.9706722	.9707187	.9707652
935	.9710438	.9710902	.9711366	.9711830	.9712294
936	.9715078	.9715542	.9716005	.9716469	.9716932
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937	3.9719713	3.9720176	3.9720639	3.9721102	3.9721565
938	.9724343	.9724805	.9725268	.9725731	.9726193
939	.9728968	.9729430	.9729892	.9730354	.9730816
840	.9733588	.9734050	.9734511	.9734973	.9735435
941	.9738203	.9738664	.9739126	.9739587	.9740048
942	.9742814	.9743274	.9743735	.9744196	.9744656
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943	3.9747419	3.9747879	3.9748340	3.9748800	3.9749260
944	.9752020	.9752479	.9752939	.9753399	.9753858
945	.9756615	.9757076	.9757534	.9757993	.9758452
946	.9761206	.9761665	.9762124	.9762582	.9763041
947	.9765792	.9766251	.9766709	.9767167	.9767625
948	.9770373	.9770821	.9771289	.9771747	.9772204
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949	3.9774950	3.9775407	3.9775864	3.9776322	3.9776779
950	.9779521	.9779978	.9780435	.9780892	.9781348
951	.9784088	.9784544	.9785001	.9785457	.9785913
952	.9788650	.9789106	.9789562	.9790017	.9790473
953	.9793207	.9793662	.9794118	.9794573	.9795028
954	.9797759	.9798214	.9798669	.9799124	.9799579
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955	3.9802307	3.9802761	3.9803216	3.9803670	3.9804125
956	.9806850	.9807304	.9807758	.9808212	.9808666
957	.9811388	.9811841	.9812295	.9812748	.9813202
958	.9815921	.9816374	.9816827	.9817280	.9817733
959	.9820450	.9820902	.9821355	.9821807	.9822260
960	.9824974	.9825426	.9825878	.9826330	.9826782
961	.9829493	.9829945	.9830396	.9830848	.9831299

A TABLE of Logarithms,

Num.	0	1	2	3	4
962	3.9831751	3.9832202	3.9832654	3.9833105	3.9833556
963	.9836263	.9836714	.9838165	.9837616	.9838066
964	.9840770	.9841221	.9841671	.9842122	.9842572
965	.9845273	.9845723	.9846173	.9846623	.9847073
966	.9849771	.9850221	.9850670	.9851120	.9851569
967	.9854265	.9854714	.9855163	.9855612	.9856061
968	3.9858754	3.9859202	3.9859651	3.9860099	3.9860548
969	.9863238	.9863686	.9864134	.9864582	.9865030
970	.9867717	.9868165	.9868613	.9869060	.9869508
971	.9872192	.9872640	.9873087	.9873534	.9873981
972	.9876663	.9877109	.9877556	.9878003	.9878449
973	.9881128	.9881575	.9882021	.9882467	.9882913
974	3.9885590	3.9886035	3.9886481	3.9886927	3.9887373
975	.9890046	.9890492	.9890937	.9891382	.9891828
976	.9894498	.9894943	.9895388	.9895833	.9896278
977	.9898946	.9899390	.9899835	.9900279	.9900723
978	.9903389	.9903833	.9904277	.9904721	.9905164
979	.9907827	.9908270	.9908714	.9909158	.9909601
980	3.9912261	3.9912704	3.9913147	3.9913590	3.9914033
981	.9916690	.9917133	.9917575	.9918018	.9917461
982	.9921115	.9921557	.9921999	.9922441	.9922884
983	.9925535	.9925977	.9926419	.9926860	.9927302
984	.9930951	.9930392	.9930834	.9931275	.9931716
985	.9934362	.9934803	.9935244	.9935685	.9936126
986	3.9938769	3.9939210	3.9939650	3.9940090	3.9940531
987	.9943172	.9943612	.9944051	.9944491	.9944931
988	.9947569	.9948009	.9948448	.9948888	.9949327
989	.9951963	.9952402	.9952841	.9953280	.9953719
990	.9956352	.9956791	.9957229	.9957668	.9958106
991	.9960737	.9961175	.9961613	.9962051	.9962489
992	3.9965117	3.9965554	3.9965992	3.9966430	3.9966868
993	.9969492	.9969930	.9970367	.9970804	.9971242
994	.9973864	.9974301	.9974738	.9975174	.9975611
995	.9978231	.9978667	.9979104	.9979540	.9979976
996	.9982593	.9983029	.9983465	.9983901	.9984337
997	.9986952	.9987387	.9987823	.9988258	.9988694
998	.9991305	.9991740	.9992176	.9992611	.9993046
999	.9995655	.9996090	.9996524	.9996959	.9997393

from 1 to 10000.

Nun.	5	6	7	8	9
962	3.9834007	3.9834459	3.9834910	3.9835361	3.9835812
963	.9838517	.9838968	.9839419	.9839869	.9840320
964	.9843022	.9843473	.9843924	.9844373	.9844823
965	.9847523	.9847973	.9848422	.9848872	.9849322
966	.9852019	.9852468	.9852917	.9853366	.9853816
967	.9856510	.9856959	.9857407	.9857856	.9858305
968	3.9860996	3.9861445	3.9861893	3.9862341	3.9862790
969	.9865478	.9865926	.9866374	.9866822	.9867270
970	.9869955	.9870403	.9870850	.9871293	.9871745
971	.9874428	.9874875	.9875322	.9875769	.9876216
972	.9878896	.9879343	.9879789	.9880236	.9880682
973	.9883360	.9883806	.9884252	.9884698	.9885144
974	3.9887818	3.9888264	3.9888710	3.9889155	3.9889601
975	.9892273	.9892718	.9893163	.9893608	.9894053
976	.9896722	.9897167	.9897612	.9898056	.9898501
977	.9901168	.9901612	.9902056	.9902500	.9902944
978	.9905608	.9906052	.9906495	.9906940	.9907383
979	.9910044	.9910488	.9910931	.9911374	.9911818
980	3.9914476	3.9914919	3.9915362	3.9915805	3.9916247
981	.9918903	.9919345	.9919788	.9920230	.9920673
982	.9923326	.9923768	.9924210	.9924651	.9925093
983	.9927744	.9928185	.9928627	.9929068	.9929510
984	.9932157	.9932598	.9933039	.9933480	.9933921
985	.9936566	.9937007	.9937448	.9937888	.9938329
986	3.9940971	3.9941411	3.9941851	3.9942291	3.9942731
987	.9945371	.9945811	.9946251	.9946690	.9947130
988	.9949767	.9950206	.9950645	.9951085	.9951524
989	.9954158	.9954597	.9955036	.9955474	.9955913
990	.9958545	.9958983	.9959422	.9959860	.9960298
991	.9962927	.9963365	.9963803	.9964241	.9964679
992	3.9967305	3.9967743	3.9968180	3.9968618	3.9969055
993	.9971679	.9972116	.9972553	.9972990	.9973427
994	.9976048	.9976485	.9976921	.9977358	.9977794
995	.9980413	.9980849	.9981285	.9981721	.9982157
996	.9984773	.9985209	.9985645	.9986080	.9986516
997	.9989129	.9989564	.9990000	.9990435	.9990870
998	.9993481	.9993916	.9994350	.9994785	.9995220
999	.9997828	.9998262	.9998697	.9999131	.9999566

A Table of Artificial Sines,

0 Degrees.

Min.	Sine.		Tang.		Secant.		
0	0.0000000	1.0000000	0.0000000	Infinite.	10.0000000	Infinite.	50
1	6.4637261	9.9999999	6.4637261	13.5362739	10.0000000	13.5362739	59
2	6.7647561	9.9999999	6.7647562	13.2352438	10.0000001	13.2352438	58
3	6.9408473	9.9999998	6.9408475	13.0591525	10.0000002	13.0591527	57
4	7.0657860	9.9999997	7.0657863	12.9342137	10.0000003	12.9342140	56
5	7.1626960	9.9999995	7.1626964	12.8373036	10.0000005	12.8373040	55
6	7.2418771	9.9999993	7.2418778	12.7581222	10.0000007	12.7581229	54
7	7.3088239	9.9999991	7.3088247	12.6911752	10.0000009	12.6911761	53
8	7.3668157	9.9999988	7.3668169	12.6331831	10.0000012	12.6331843	52
9	7.4179681	9.9999985	7.4179696	12.5820304	10.0000015	12.5820319	51
10	7.4637255	9.9999982	7.4637273	12.5362727	10.0000018	12.5362745	50
11	7.5051181	9.9999978	7.5051203	12.4948797	10.0000022	12.4948819	49
12	7.5429065	9.9999974	7.5429091	12.4570909	10.0000026	12.4570935	48
13	7.5776684	9.9999969	7.5776715	12.4223285	10.0000031	12.4223316	47
14	7.6098530	9.9999964	7.6098566	12.3901434	10.0000036	12.3901470	46
15	7.6398160	9.9999959	7.6398201	12.3601799	10.0000041	12.3601840	45
16	7.6678445	9.9999953	7.6678492	12.3321508	10.0000047	12.3321555	44
17	7.6941733	9.9999947	7.6941786	12.3058214	10.0000053	12.3058267	43
18	7.7189966	9.9999940	7.7190026	12.2809974	10.0000060	12.2810034	42
19	7.7424775	9.9999934	7.7424841	12.2575159	10.0000066	12.2575225	41
20	7.7647537	9.9999927	7.7647610	12.2352390	10.0000073	12.2352463	40
21	7.7859427	9.9999919	7.7859508	12.2140492	10.0000081	12.2240573	39
22	7.8061458	9.9999911	7.8061547	12.1938453	10.0000089	12.1938542	38
23	7.8254507	9.9999903	7.8254604	12.1745396	10.0000097	12.1745493	37
24	7.8439338	9.9999894	7.8439444	12.1560556	10.0000106	12.1560662	36
25	7.8616623	9.9999885	7.8616738	12.1383262	10.0000115	12.1383377	35
26	7.8786953	9.9999876	7.8787077	12.1212923	10.0000124	12.1213047	34
27	7.8950854	9.9999866	7.8950988	12.1049012	10.0000134	12.1049146	33
28	7.9108793	9.9999856	7.9108938	12.0891062	10.0000144	12.0891207	32
29	7.9261190	9.9999845	7.9261344	12.0738656	10.0000155	12.0738810	31
30	7.9408419	9.9999835	7.9408584	12.0591416	10.0000165	12.0591581	30
	Sine.		Tang.		Secant.	Min.	

89 Degrees.

Tangents and Secants.

0 Degrees.

Min.	Sine.		Tang.		Secant.	
30	7.9408415	9.9999835	7.9408584	12.0591416	10.0000165	12.0591458
31	7.9550815	9.9999823	7.9550996	12.0449004	10.0000177	12.0449181
32	7.9688698	9.9999812	7.9688886	12.0311114	10.0000188	12.0311303
33	7.9822334	9.9999800	7.9822534	12.0177466	10.0000200	12.0177664
34	7.9951980	9.9999788	7.9952192	12.0047808	10.0000212	12.0048020
35	8.0077786	9.9999775	8.0078092	11.9921908	10.0000225	11.9922132
36	8.0200207	9.9999762	8.0200445	11.9799333	10.0000238	11.9799793
37	8.0319195	9.9999748	8.0319446	11.9680554	10.0000252	11.9680805
38	8.0435009	9.9999735	8.0435274	11.9564726	10.0000265	11.9564991
39	8.0547814	9.9999721	8.0548094	11.9451906	10.0000279	11.9452186
40	8.0657763	9.9999706	8.0658057	11.9341949	10.0000294	11.9342237
41	8.0764997	9.9999691	8.0765306	11.9234694	10.0000309	11.9235003
42	8.0869646	9.9999676	8.0869970	11.9130930	10.0000324	11.9130934
43	8.0971832	9.9999660	8.0972172	11.9027828	10.0000340	11.9028168
44	8.1071669	9.9999644	8.1072025	11.8927975	10.0000356	11.8928337
45	8.1169262	9.9999628	8.1169634	11.8830366	10.0000372	11.8830738
46	8.1264710	9.9999611	8.1265099	11.8734901	10.0000389	11.8735290
47	8.1358104	9.9999594	8.1358510	11.8641490	10.0000406	11.8641896
48	8.1449532	9.9999577	8.1449956	11.8550044	10.0000423	11.8550468
49	8.1539075	9.9999559	8.1539516	11.8460484	10.0000441	11.8460925
50	8.1626808	9.9999541	8.1627267	11.8372733	10.0000459	11.8373192
51	8.1712804	9.9999522	8.1713282	11.8286718	10.0000478	11.8287196
52	8.1797129	9.9999503	8.1797626	11.8202374	10.0000497	11.8202871
53	8.1879848	9.9999484	8.1880364	11.8119636	10.0000516	11.8120152
54	8.1961020	9.9999464	8.1961556	11.8038444	10.0000536	11.8038980
55	8.2040703	9.9999444	8.2041259	11.7958741	10.0000556	11.7959297
56	8.2118949	9.9999424	8.2119526	11.7880474	10.0000576	11.7881051
57	8.2195811	9.9999403	8.2196408	11.7803592	10.0000597	11.7804189
58	8.2271335	9.9999382	8.2271953	11.7728047	10.0000618	11.7728665
59	8.2345568	9.9999360	8.2346208	11.7653792	10.0000640	11.7654432
60	8.2418553	9.9999338	8.2419215	11.7580783	10.0000662	11.7581447
	Sine.		Tang.		Secant.	Min.

89 Degrees.

A Table of Artificial Sines,

1 Degrees.

Min.	Sine.		Tang.		Secant.		
0	8.2418553	9.9999338	8.2419215	11.7580785	10.0000662	11.7581447	00
1	8.2490332	9.9999310	8.2491015	11.7508985	10.0000684	11.7509663	59
2	8.2560943	9.9999294	8.2561649	11.7438351	10.0000705	11.7439057	58
3	8.2630424	9.9999271	8.2631153	11.7368847	10.0000729	11.7369576	57
4	8.2698810	9.9999247	8.2699563	11.7300437	10.0000753	11.7301190	56
5	8.2766136	9.9999224	8.2766912	11.7233288	10.0000776	11.7233864	55
6	8.2832434	9.9999200	8.2833234	11.7166766	10.0000800	11.7167566	54
7	8.2897732	9.9999175	8.2898559	11.7101441	10.0000825	11.7102266	53
8	8.2962067	9.9999150	8.2962917	11.7037083	10.0000850	11.7037933	52
9	8.3025460	9.9999125	8.3026335	11.6973665	10.0000875	11.6974540	51
10	8.3087041	9.9999100	8.3088842	11.6911157	10.0000900	11.6912059	50
11	8.3149536	9.9999074	8.3150462	11.6849538	10.0000926	11.6850464	49
12	8.3210269	9.9999047	8.3211221	11.6788779	10.0000953	11.6789731	48
13	8.3270163	9.9999021	8.3271143	11.6728857	10.0000979	11.6729837	47
14	8.3329243	9.9998994	8.3330249	11.6669751	10.0001006	11.6670757	46
15	8.3387529	9.9998966	8.3388563	11.6611437	10.0001034	11.6612471	45
16	8.3445043	9.9998939	8.3446105	11.6553895	10.0001061	11.6554957	44
17	8.3501869	9.9998911	8.3502895	11.6497105	10.0001089	11.6498195	43
18	8.3557835	9.9998882	8.3558953	11.6441047	10.0001118	11.6442165	42
19	8.3613150	9.9998853	8.3614297	11.6385703	10.0001147	11.6386850	41
20	8.3667769	9.9998824	8.3668945	11.6331055	10.0001176	11.6332231	40
21	8.3721710	9.9998794	8.3722915	11.6277085	10.0001205	11.6278290	39
22	8.3774988	9.9998764	8.3776223	11.6223777	10.0001236	11.6225012	38
23	8.3827620	9.9998734	8.3828886	11.6171114	10.0001266	11.6172380	37
24	8.3879622	9.9998703	8.3880918	11.6119082	10.0001296	11.6120378	36
25	8.3931008	9.9998672	8.3932336	11.6067664	10.0001328	11.6068992	35
26	8.3981793	9.9998641	8.3983152	11.6016848	10.0001359	11.6018207	34
27	8.4031990	9.9998609	8.4033381	11.5966619	10.0001391	11.5968010	33
28	8.4081614	9.9998577	8.4083037	11.5916963	10.0001423	11.5918386	32
29	8.4130676	9.9998544	8.4132132	11.5867868	10.0001456	11.5869324	31
30	8.4179190	9.9998512	8.4180679	11.5819321	10.0001488	11.5820810	30
	Sine.		Tang.		Secant		Min.

88 Degrees.

Tangents and Secants.

1 Degrees.

M.	Sine.	Tang.	Secant.	
30	4179190	9.9998312	3.4180579	11.5819321
31	4227168	9.9998478	3.4228690	11.5771310
32	4274621	9.9998645	3.4276176	11.5723824
33	4321561	9.9998811	3.4323150	11.5676850
34	4367999	9.9998976	3.4369622	11.5630378
35	4413944	9.9999142	3.4415503	11.5584397
36	4459405	9.9999306	3.4461103	11.5538897
37	4504402	9.9999471	3.4506131	11.5493869
38	4548934	9.9999635	3.4550699	11.5449301
39	4593013	9.9999799	3.4594814	11.5405186
40	4636645	9.9999962	3.4638486	11.5361514
41	4679850	9.9999125	3.4681725	11.5318275
42	4722626	9.9999288	3.4724538	11.5275462
43	4764984	9.9999450	3.4766933	11.5233067
44	4806932	9.9999612	3.4808920	11.5191080
45	4848479	9.9999774	3.4850505	11.5149495
46	4889632	9.9999935	3.4891696	11.5108304
47	4930398	9.9999896	3.4932502	11.5067498
48	4970784	9.9999756	3.4972928	11.5027072
49	5010798	9.9999717	3.5012982	11.4987018
50	5050447	9.9999776	3.5052671	11.4947329
51	5089736	9.9999736	3.5092001	11.4907999
52	5128673	9.9999695	3.5130978	11.4869022
53	5167264	9.9999653	3.5169610	11.4830387
54	5205514	9.9999612	3.5207902	11.4792098
55	5243430	9.9999570	3.5245860	11.4754140
56	5281017	9.9999527	3.5283490	11.4716510
57	5318281	9.9999484	3.5320797	11.4679203
58	5355228	9.9999441	3.5357787	11.4642233
59	5391853	9.9999398	3.5394466	11.4605534
60	5428192	9.9999354	3.5430838	11.4569162
	Sine.		Tang.	Secant.

88 Degrees.

A Table of Artificial Sines,

2 Degrees.

Min.	Sine.		Tang.		Secant.	
0	8.5428192	9.9997354	8.5430838	11.4509162	10.0002646	11.4571806
1	8.5404218	9.9997309	8.5466506	11.4533091	10.0002691	11.4535782
2	8.5499948	9.9997265	8.5502683	11.4497317	10.0002735	11.4500052
3	8.5535386	9.9997220	8.5538166	11.4461834	10.0002780	11.4464614
4	8.5570536	9.9997174	8.5573362	11.4426638	10.0002826	11.4429464
5	8.5605404	9.9997128	8.5608276	11.4391724	10.0002872	11.4394596
6	8.5639994	9.9997082	8.5642912	11.4357088	10.0002918	11.4360006
7	8.5674310	9.9997036	8.5677275	11.4322725	10.0002964	11.4325690
8	8.5708357	9.9996989	8.5711368	11.4288632	10.0003011	11.4291643
9	8.5742139	9.9996942	8.5745197	11.4254803	10.0003058	11.4257861
10	8.5775660	9.9996894	8.5778766	11.4221234	10.0003106	11.4224340
11	8.5808923	9.9996846	8.5812077	11.4187923	10.0003154	11.4191077
12	8.5841933	9.9996798	8.5845136	11.4154864	10.0003202	11.4158067
13	8.5874694	9.9996745	8.5877945	11.4122055	10.0003251	11.4125306
14	8.5907209	9.9996706	8.5910569	11.4089498	10.0003300	11.4092791
15	8.5939482	9.9996660	8.5942832	11.4057168	10.0003350	11.4060517
16	8.5971517	9.9996604	8.5974917	11.4025088	10.0003399	11.4028483
17	8.6003317	9.9996550	8.6006767	11.3993233	10.0003450	11.3996683
18	8.6034886	9.9996500	8.6038386	11.3961514	10.0003500	11.3965114
19	8.6066226	9.9996445	8.6069777	11.3930023	10.0003551	11.3933774
20	8.6097341	9.9996398	8.6100943	11.3899057	10.0003602	11.3902659
21	8.6128235	9.9996346	8.6131889	11.3868111	10.0003654	11.3871765
22	8.6158910	9.9996294	8.6162616	11.3837384	10.0003706	11.3841090
23	8.6189369	9.9996242	8.6193127	11.3806873	10.0003758	11.3810631
24	8.6219616	9.9996189	8.6223427	11.3776573	10.0003811	11.3780384
25	8.6249654	9.9996136	8.6253518	11.3746482	10.0003864	11.3750347
26	8.6279484	9.9996082	8.6283402	11.3716598	10.0003918	11.3720512
27	8.6309111	9.9996028	8.6313083	11.3686917	10.0003972	11.3690889
28	8.6338537	9.9995974	8.6342563	11.3657437	10.0004026	11.3661463
29	8.6367764	9.9995919	8.6371845	11.3628155	10.0004081	11.3632236
30	8.6396790	9.9995865	8.6400931	11.3599059	10.0004135	11.3603204
	Sine.		Tang.		Secant.	Min.

87 Degrees.

Tangents and Secants.

2 Degrees.

Min.	Sine.		Tan g.		Secant.	
30	8.6396796	9.9995865	3.6400931	11.3599069	10.0004135	11.3603204 30
31	8.6425634	9.9995809	3.6429825	11.3570175	10.0004191	11.3574366 29
32	8.6454282	9.9995753	3.6458528	11.3541472	10.0004247	11.3545718 28
33	8.6482742	9.9995697	3.6487044	11.3512956	10.0004303	11.3517258 27
34	8.6511016	9.9995641	3.6515375	11.3484821	10.0004359	11.3488984 26
35	8.6539107	9.9995584	3.6543525	11.3456478	10.0004416	11.3460893 25
36	8.6567017	9.9995527	8.6571490	11.3428510	10.0004473	11.3432983 24
37	8.6594748	9.9995469	8.6599279	11.3400721	10.0004530	11.3405252 23
38	8.6622303	9.9995411	8.6626891	11.3373109	10.0004589	11.3377697 22
39	8.6649684	9.9995353	8.6654331	11.3345679	10.0004647	11.3350316 21
40	8.6676893	9.9995294	8.6681598	11.3318402	10.0004705	11.3323107 20
41	8.6703932	9.9995236	8.6708697	11.3291303	10.0004764	11.3296068 19
42	8.6730804	9.9995176	8.6735628	11.3264372	10.0004824	11.3269196 18
43	8.6757510	9.9995116	8.6762393	11.3237607	10.0004884	11.3242490 17
44	8.6784052	9.9995056	8.6788996	11.3211004	10.0004944	11.3215948 16
45	8.6810433	9.9994996	8.6815437	11.3184563	10.0005004	11.3189597 15
46	8.6836654	9.9994935	8.6841719	11.3158281	10.0005065	11.3163346 14
47	8.6862718	9.9994874	8.6867844	11.3132156	10.0005126	11.3137282 13
48	8.6888625	9.9994812	8.6893813	11.3106187	10.0005188	11.3111375 12
49	8.6914379	9.9994750	8.6919629	11.3080371	10.0005250	11.3085621 11
50	8.6939980	9.9994688	8.6945292	11.3054708	10.0005312	11.3060019 10
51	8.6965431	9.9994625	8.6970806	11.3029194	10.0005375	11.3034569 9
52	8.6990734	9.9994562	8.6996172	11.3003828	10.0005438	11.3009266 8
53	8.7015889	9.9994498	8.7021390	11.2978610	10.0005502	11.2984111 7
54	8.7040899	9.9994435	8.7046465	11.2953535	10.0005565	11.2959101 6
55	8.7065766	9.9994370	8.7071395	11.2928605	10.0005630	11.2934234 5
56	8.7090490	9.9994306	8.7096185	11.2903815	10.0005694	11.2909510 4
57	8.7115075	9.9994241	8.7120834	11.2879166	10.0005759	11.2884925 3
58	8.7139520	9.9994176	8.7145344	11.2854655	10.0005824	11.2860480 2
59	8.7163829	9.9994110	8.7169719	11.2830281	10.0005890	11.2836171 1
60	8.7188002	9.9994044	8.7193958	11.2806042	10.0005956	11.2811998 0
	Sine.		Tang.		Secant.	Min.

87 Degrees.

A Table of Artificial Sines,

3 Degrees.

Min.	Sine.		Tang.		Secant.		
0	3.7188002	9.9994044	3.7193958	11.2806042	10.0005956	11.2811998	50
1	8.7212040	9.9993978	8.7218063	11.2781937	10.0006022	11.2787960	59
2	3.7235946	9.9993911	3.7242035	11.2757965	10.0006089	11.2764053	58
3	8.7259721	9.9993844	8.7265877	11.2734123	10.0006156	11.2740279	57
4	8.7283366	9.9993776	8.7289589	11.2710411	10.0006224	11.2716634	56
5	8.7306882	9.9993708	8.7313174	11.2686826	10.0006292	11.2693118	55
6	8.7330272	9.9993640	8.7336631	11.2663369	10.0006360	11.2669728	54
7	8.7353535	9.9993572	8.7359964	11.2640030	10.0006428	11.2646465	53
8	8.7376675	9.9993503	8.7383172	11.2616828	10.0006497	11.2623325	52
9	8.7399691	9.9993433	8.7406258	11.2593742	10.0006567	11.2600309	51
10	8.7422586	9.9993364	8.7429222	11.2570778	10.0006636	11.2577414	50
11	8.7445360	9.9993293	8.7452067	11.2547933	10.0006707	11.2554640	49
12	8.7468015	9.9993223	8.7474792	11.2525208	10.0006777	11.2531985	48
13	8.7490553	9.9993152	8.7497400	11.2502600	10.0006848	11.2509447	47
14	8.7512973	9.9993081	8.7519892	11.2480108	10.0006919	11.2487027	46
15	8.7535278	9.9993009	8.7542269	11.2457731	10.0006991	11.2464722	45
16	8.7557469	9.9992938	8.7564531	11.2435469	10.0007060	11.2442531	44
17	8.7579546	9.9992865	8.7586681	11.2413319	10.0007135	11.2420454	43
18	8.7601512	9.9992793	8.7608719	11.2391281	10.0007207	11.2398488	42
19	8.7623366	9.9992720	8.7630647	11.2369393	10.0007280	11.2376634	41
20	8.7645111	9.9992646	8.7652465	11.2347535	10.0007354	11.2354889	40
21	8.7666747	9.9992572	8.7674175	11.2325825	10.0007428	11.2333253	39
22	8.7688275	9.9992498	8.7695777	11.2304223	10.0007502	11.2311725	38
23	8.7709697	9.9992424	8.7717274	11.2282726	10.0007576	11.2290309	37
24	8.7731014	9.9992349	8.7738665	11.2261335	10.0007651	11.2268986	36
25	8.7752226	9.9992274	8.7759952	11.2240048	10.0007726	11.2247774	35
26	8.7773334	9.9992198	8.7781136	11.2218864	10.0007802	11.2226666	34
27	8.7794340	9.9992122	8.7802218	11.2197782	10.0007878	11.2205660	33
28	8.7815244	9.9992046	8.7823199	11.2176801	10.0007954	11.2184756	32
29	8.7836048	9.9991969	8.7844079	11.2155921	10.0008031	11.2163952	31
30	8.7856753	9.9991892	8.7864861	11.2135139	10.0008108	11.2143247	30
	Sine.		Tang.		Secant.		Min.

86 Degrees.

Tangents and Secants.

3 Degrees.

Min.	Sine.		Tang.		Secant		Min.
30	8.7856753	9.9991892	8.7864861	11.2135139	10.0008108	11.2143247	30
31	8.7877359	9.9991815	8.7885544	11.2114456	10.0008185	11.2122641	29
32	8.7897867	9.9991737	8.7906130	11.2093870	10.0008263	11.2102133	28
33	8.7918278	9.9991659	8.7926620	11.2073380	10.0008341	11.2081722	27
34	8.7938594	9.9991580	8.7947014	11.2052986	10.0008420	11.2061406	26
35	8.7958814	9.9991501	8.7967313	11.2032687	10.0008499	11.2041186	25
36	8.7978941	9.9991422	8.7987519	11.2012481	10.0008578	11.2021059	24
37	8.7998974	9.9991342	8.8007632	11.1992368	10.0008658	11.2001026	23
38	8.8018915	9.9991262	8.8027653	11.1972347	10.0008738	11.1981085	22
39	8.8038764	9.9991182	8.8047583	11.1952417	10.0008818	11.1961236	21
40	8.8058523	9.9991101	8.8067422	11.1932578	10.0008899	11.1941477	20
41	8.8078192	9.9991020	8.8087172	11.1912828	10.0008980	11.1921808	19
42	8.8097772	9.9990938	8.8106834	11.1893166	10.0009062	11.1902223	18
43	8.8117264	9.9990856	8.8126407	11.1873593	10.0009144	11.1882736	17
44	8.8136668	9.9990774	8.8145794	11.1854106	10.0009226	11.1863332	16
45	8.8155985	9.9990691	8.8165294	11.1834706	10.0009309	11.1844015	15
46	8.8175217	9.9990608	8.8184608	11.1815392	10.0009392	11.1824783	14
47	8.8194363	9.9990525	8.8203838	11.1796162	10.0009475	11.1805537	13
48	8.8213425	9.9990441	8.8222984	11.1777016	10.0009559	11.1786375	12
49	8.8232404	9.9990357	8.8242046	11.1757954	10.0009643	11.1767296	11
50	8.8251299	9.9990273	8.8261026	11.1738974	10.0009727	11.1748301	10
51	8.8270112	9.9990188	8.8279924	11.1720076	10.0009812	11.1729388	9
52	8.8288844	9.9990103	8.8298741	11.1701259	10.0009897	11.1711156	8
53	8.8307495	9.9990017	8.8317478	11.1682522	10.0009983	11.1692505	7
54	8.8326066	9.9989931	8.8336134	11.1663866	10.0010069	11.1673934	6
55	8.8344557	9.9989845	8.8354712	11.1645288	10.0010155	11.1655443	5
56	8.8362969	9.9989758	8.8373211	11.1626789	10.0010242	11.1637031	4
57	8.8381304	9.9989671	8.8391633	11.1608367	10.0010329	11.1618696	3
58	8.8399561	9.9989584	8.8409977	11.1590023	10.0010416	11.1600439	2
59	8.8417741	9.9989496	8.8428245	11.1571755	10.0010504	11.1582259	1
60	8.8435845	9.9989408	8.8446437	11.1553563	10.0010592	11.1564155	0
	Sine.		Tang.		Secant.		

86 Degrees.

A Table of Artificial Sines,

4 Degrees.

Min.	Sine.		Tang.		Secant.	
0	8.8435845	9.9989408	3.8446437	11.1553563	10.0010592	11.1564154 60
1	8.8453874	9.9989315	3.8464554	11.1535446	10.0010681	11.1546126 59
2	8.8471827	9.9989230	3.8482597	11.1517403	10.0010770	11.1528173 58
3	8.8489707	9.9989141	3.8500566	11.1499434	10.0010859	11.1510293 57
4	8.8507512	9.9989052	3.8518461	11.1481539	10.0010948	11.1492488 56
5	8.8525245	9.9988962	3.8536283	11.1463717	10.0011038	11.1474755 55
6	8.8542905	9.9988871	3.8554034	11.1445966	10.0011129	11.1457095 54
7	8.8560493	9.9988780	3.8571713	11.1428287	10.0011220	11.1439507 53
8	8.8578010	9.9988689	3.8589321	11.1410679	10.0011311	11.1421990 52
9	8.8595457	9.9988598	3.8606859	11.1393141	10.0011402	11.1404543 51
10	8.8612833	9.9988506	3.8624327	11.1375673	10.0011494	11.1387167 50
11	8.8630139	9.9988414	3.8641725	11.1358275	10.0011586	11.1369861 49
12	8.8647376	9.9988321	3.8659055	11.1340944	10.0011679	11.1352624 48
13	8.8664545	9.9988228	3.8676317	11.1323683	10.0011772	11.1335455 47
14	8.8681646	9.9988135	3.8693511	11.1306489	10.0011865	11.1318354 46
15	8.8698680	9.9988041	3.8710638	11.1289362	10.0011959	11.1301320 45
16	8.8715646	9.9987947	3.8727699	11.1272301	10.0012053	11.1284354 44
17	8.8732546	9.9987853	3.8744694	11.1255306	10.0012147	11.1267454 43
18	8.8749381	9.9987758	3.8761623	11.1238377	10.0012242	11.1250619 42
19	8.8766150	9.9987663	3.8778487	11.1221513	10.0012337	11.1233850 41
20	8.8782854	9.9987567	3.8795286	11.1204714	10.0012433	11.1217146 40
21	8.8799493	9.9987471	3.8812022	11.1187978	10.0012529	11.1200507 39
22	8.8816069	9.9987375	3.8828694	11.1171306	10.0012625	11.1183931 38
23	8.8832581	9.9987278	3.8845303	11.1154697	10.0012722	11.1167419 37
24	8.8849031	9.9987181	3.8861850	11.1138150	10.0012819	11.1150969 36
25	8.8865418	9.9987084	3.8878334	11.1121666	10.0012916	11.1134582 35
26	8.8881743	9.9986986	3.8894757	11.1105243	10.0013014	11.1118257 34
27	8.8898007	9.9986888	3.8911119	11.1088881	10.0013112	11.1101993 33
28	8.8914209	9.9986790	3.8927420	11.1072580	10.0013210	11.1085791 32
29	8.8930351	9.9986691	3.8943660	11.1056340	10.0013309	11.1069649 31
30	8.8946433	9.9986591	3.8959842	11.1040158	10.0013409	11.1053567 30
	Sine.		Tang.		Secant.	

85 Degrees.

Tangents and Secants.

4 Degrees.

Min.	Sine.		Tang.		Seca nt.		
30	8.8946433	9.9986591	8.8959842	11.1040158	10.0013409	11.1053567	30
31	8.8962455	9.9986492	8.8975963	11.1024037	10.0013508	11.1037545	29
32	8.8978418	9.9986392	8.8992026	11.1007974	10.0013608	11.1021582	28
33	8.8994322	9.9986292	8.9008030	11.0991970	10.0013708	11.1005678	27
34	8.9010168	9.9986191	8.9023977	11.0976023	10.0013809	11.0989832	26
35	8.9025955	9.9986090	8.9039866	11.0960134	10.0013910	11.0974045	25
36	8.9041685	9.9985988	8.9055697	11.0944303	10.0014012	11.0958315	24
37	8.9057358	9.9985886	8.9071472	11.0928528	10.0014114	11.0942642	23
38	8.9072975	9.9985784	8.9087190	11.0912810	10.0014216	11.0927025	22
39	8.9088535	9.9985682	8.9102853	11.0897147	10.0014318	11.0911465	21
40	8.9104039	9.9985579	8.9118460	11.0881540	10.0014421	11.0895961	20
41	8.9119487	9.9985475	8.9134012	11.0865988	10.0014525	11.0880513	19
42	8.9134881	9.9985372	8.9149509	11.0850491	10.0014628	11.0865119	18
43	8.9150219	9.9985268	8.9164952	11.0835048	10.0014732	11.0849781	17
44	8.9165504	9.9985163	8.9180340	11.0819660	10.0014837	11.0834496	16
45	8.9180734	9.9985058	8.9195675	11.0804325	10.0014942	11.0819266	15
46	8.9195911	9.9984953	8.9210957	11.0789043	10.0015047	11.0804089	14
47	8.9211034	9.9984848	8.9226186	11.0773814	10.0015152	11.0788966	13
48	8.9226105	9.9984742	8.9241363	11.0758637	10.0015258	11.0773895	12
49	8.9241123	9.9984636	8.9256487	11.0743513	10.0015364	11.0758877	11
50	8.9256089	9.9984529	8.9271560	11.0728440	10.0015471	11.0743911	10
51	8.9271008	9.9984422	8.9286581	11.0713419	10.0015578	11.0728997	9
52	8.9285866	9.9984315	8.9301552	11.0698448	10.0015685	11.0714134	8
53	8.9300678	9.9984207	8.9316471	11.0683529	10.0015793	11.0699322	7
54	8.9315439	9.9984099	8.9331340	11.0668660	10.0015901	11.0684561	6
55	8.9330150	9.9983990	8.9346160	11.0653840	10.0016010	11.0669850	5
56	8.9344811	9.9983881	8.9360929	11.0639071	10.0016119	11.0655189	4
57	8.9359422	9.9983772	8.9375650	11.0624350	10.0016228	11.0640578	3
58	8.9373983	9.9983663	8.9390321	11.0609679	10.0016337	11.0626017	2
59	8.9388496	9.9983553	8.9404944	11.0595056	10.0016447	11.0611504	1
60	8.9402960	9.9983442	8.9419518	11.0580482	10.0016558	11.0597040	0
		Sine.		Tang.		Secant.	Min.

85 Degrees.

A Table of Artificial Sines,

5 Degrees.

Min.	Sine.		Tang.		Secant.		
0	8.9402960	9.9983442	8.9419518	11.0580482	10.0016558	11.059704	6
1	8.9417376	9.9983332	8.9434044	11.0565956	10.0016668	11.0582624	59
2	8.9431743	9.9983220	8.9448523	11.0551477	10.0016780	11.0568257	58
3	8.9446063	9.9983109	8.9462954	11.0537046	10.0016891	11.0553937	57
4	8.9460335	9.9982997	8.9477338	11.0522662	10.0017003	11.0539665	56
5	8.9474561	9.9982885	8.9491676	11.0508324	10.0017115	11.0525439	55
6	8.9488735	9.9982772	8.9505967	11.0494033	10.0017228	11.0511261	54
7	8.9502871	9.9982660	8.9520211	11.0479789	10.0017340	11.0497129	53
8	8.9516957	9.9982546	8.9534410	11.0465590	10.0017454	11.0483043	52
9	8.9530996	9.9982433	8.9548465	11.0451436	10.0017567	11.0469004	51
10	8.9544991	9.9982318	8.9562672	11.0437328	10.0017682	11.0455009	50
11	8.9558960	9.9982204	8.9576735	11.0423265	10.0017796	11.0441060	49
12	8.9572843	9.9982089	8.9590754	11.0409246	10.0017911	11.0427157	48
13	8.9586703	9.9981974	8.9604728	11.0395272	10.0018026	11.0413297	47
14	8.9600517	9.9981859	8.9618659	11.0381341	10.0018141	11.0399483	46
15	8.9614288	9.9981743	8.9632545	11.0367455	10.0018257	11.0385712	45
16	8.9628014	9.9981629	8.9646386	11.0353612	10.0018374	11.0371986	44
17	8.9641697	9.9981510	8.9660188	11.0339812	10.0018490	11.0358363	43
18	8.9655337	9.9981393	8.9673944	11.0326056	10.0018607	11.0344663	42
19	8.9668934	9.9981275	8.9687658	11.0312342	10.0018725	11.0331066	41
20	8.9682487	9.9981158	8.9701330	11.0298670	10.0018842	11.0317513	40
21	8.9695999	9.9981040	8.9714959	11.0285040	10.0018960	11.0304001	39
22	8.9709468	9.9980921	8.9728547	11.0271453	10.0019079	11.0290532	38
23	8.9722895	9.9980802	8.9742092	11.0257908	10.0019198	11.0277105	37
24	8.9736280	9.9980683	8.9755597	11.0244403	10.0019317	11.0263720	36
25	8.9749624	9.9980563	8.9769060	11.0230940	10.0019437	11.0250376	35
26	8.9762926	9.9980443	8.9782483	11.0217517	10.0019557	11.0237074	34
27	8.9776188	9.9980323	8.9795865	11.0204135	10.0019677	11.0223812	33
28	8.9789408	9.9980202	8.9809206	11.0190794	10.0019798	11.0210592	32
29	8.9802589	9.9980081	8.9822507	11.0177493	10.0019919	11.0197411	31
30	8.9815729	9.9989960	8.9835769	11.0164231	10.0020040	11.0184271	30
	Sine.		Tang.		Secant.		Min.

84 Degrees.

Tangents and Secants.

5 Degrees.

Min.	Sine.		Tang.		Secant		Min.
30	3.9815729	9.9979960	8.9835769	11.0164231	10.0020040	11.0184271	30
31	3.9828829	9.9979838	8.9848991	11.0151009	10.0020162	11.0171171	29
32	3.9841889	9.9979716	8.9862173	11.0137827	10.0020284	11.0158111	28
33	3.9854910	9.9979593	8.9875317	11.0124683	10.0020407	11.0145090	27
34	3.9867891	9.9979470	8.9888421	11.0111579	10.0020530	11.0132119	26
35	3.9880834	9.9979347	8.9901487	11.0098513	10.0020653	11.0119166	25
36	3.9893737	9.9979223	8.9914514	11.0085486	10.0020777	11.0106263	24
37	3.9906602	9.9979099	8.9927503	11.0072497	10.0020909	11.0093398	23
38	3.9919429	9.9978975	8.9940454	11.0059546	10.0021025	11.0080572	22
39	3.9932217	9.9978850	8.9953367	11.0046633	10.0021150	11.0067783	21
40	3.9944968	9.9978725	8.9966243	11.0033757	10.0021275	11.0055032	20
41	3.9957681	9.9978590	8.9979081	11.0020919	10.0021401	11.0042319	19
42	3.9970357	9.9978473	8.9991883	11.0008117	10.0021527	11.0029644	18
43	3.9982994	9.9978347	9.0004647	10.9995353	10.0021653	11.0017006	17
44	3.9995595	9.9978220	9.0017375	10.9982625	10.0021780	11.0004405	16
45	4.0008160	9.9978093	9.0030066	10.9969934	10.0021907	10.9991840	15
46	4.0020687	9.9977966	9.0042721	10.9957279	10.0022034	10.9979313	14
47	4.0033179	9.9977838	9.0055340	10.9944660	10.0022162	10.9966821	13
48	4.0045634	9.9977710	9.0067924	10.9932076	10.0022290	10.9954366	12
49	4.0058053	9.9977582	9.0080471	10.9919529	10.0022418	10.9941947	11
50	4.0070436	9.9977453	9.0092984	10.9907016	10.0022547	10.9929564	10
51	4.0082784	9.9977323	9.0105461	10.9894539	10.0022677	10.9917216	9
52	4.0095096	9.9977194	9.0117903	10.9882097	10.0022806	10.9904904	8
53	4.0107374	9.9977064	9.0130310	10.9869690	10.0022936	10.9892626	7
54	4.0119616	9.9976933	9.0142682	10.9857318	10.0023067	10.9880384	6
55	4.0131823	9.9976803	9.0155021	10.9844979	10.0023197	10.9868177	5
56	4.0143996	9.9976672	9.0167325	10.9832675	10.0023328	10.9856004	4
57	4.0156135	9.9976540	9.0179594	10.9820406	10.0023460	10.9843865	3
58	4.0168239	9.9976408	9.0191831	10.9808169	10.0023592	10.9831761	2
59	4.0180300	9.9976276	9.0204033	10.9795967	10.0023724	10.9819691	1
60	4.0192346	9.9976143	9.0216202	10.9783798	10.0023857	10.9807654	0
	Sine.		Tang.		Secant.		Min.

84 Degrees.

A Table of Artificial Sines,

6 Degrees.

Min.	Sine.		Tan g.		Secant.	
0	9.0192346	9.9976143	9.0216202	10.9783798	10.0023857	10.9807654
1	9.0204348	9.9976011	9.0228333	10.9771626	10.0023989	10.9795652
2	9.0216312	9.9975877	9.0240441	10.9759559	10.0024123	10.9783682
3	9.0228254	9.9975743	9.0252510	10.9747490	10.0024257	10.9771746
4	9.0240157	9.9975609	9.0264548	10.9735452	10.0024391	10.9759844
5	9.0252027	9.9975475	9.0276552	10.9723448	10.0024525	10.9747973
6	9.0263865	9.9975340	9.0288524	10.9711476	10.0024660	10.9736135
7	9.0275669	9.9975205	9.0300464	10.9699536	10.0024795	10.9724331
8	9.0287442	9.9975069	9.0312373	10.9687627	10.0024931	10.9712558
9	9.0299182	9.9974933	9.0324249	10.9675751	10.0025067	10.9700818
10	9.0310890	9.9974797	9.0336093	10.9663907	10.0025203	10.9689110
11	9.0322567	9.9974660	9.0347906	10.9652094	10.0025340	10.9677433
12	9.0334212	9.9974523	9.0359688	10.9640312	10.0025477	10.9665788
13	9.0345825	9.9974386	9.0371439	10.9628561	10.0025614	10.9654175
14	9.0357407	9.9974248	9.0383159	10.9616841	10.0025752	10.9642593
15	9.0368958	9.9974110	9.0394848	10.9605152	10.0025890	10.9631042
16	9.0380477	9.9973971	9.0406506	10.9593494	10.0026029	10.9619523
17	9.0391966	9.9973833	9.0418134	10.9581866	10.0026167	10.9608034
18	9.0403424	9.9973693	9.0429731	10.9570269	10.0026307	10.9596576
19	9.0414852	9.9973554	9.0441299	10.9558701	10.0026446	10.9585148
20	9.0426249	9.9973414	9.0452836	10.9547164	10.0026586	10.9573751
21	9.0437616	9.9973273	9.0464343	10.9535657	10.0026727	10.9562383
22	9.0448954	9.9973132	9.0475820	10.9524179	10.0026868	10.9551046
23	9.0460261	9.9972991	9.0487270	10.9512730	10.0027009	10.9539739
24	9.0471538	9.9972850	9.0498689	10.9501311	10.0027150	10.9528462
25	9.0482786	9.9972708	9.0510078	10.9489922	10.0027292	10.9517214
26	9.0494005	9.9972566	9.0521439	10.9478561	10.0027434	10.9505995
27	9.0505194	9.9972423	9.0532771	10.9467229	10.0027577	10.9494804
28	9.0516354	9.9972280	9.0544074	10.9455926	10.0027720	10.9483646
29	9.0527485	9.9972137	9.0555349	10.9444651	10.0027863	10.9472515
30	9.0538588	9.9971993	9.0566595	10.9433405	10.0028007	10.9461412
	Sine.		Tang.		Secant.	Min.

83 Degrees.

Tangents and Secants.

6 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.0538588	9.9971993	9.0566595	10.9433405	10.0028007	10.9461412 30
31	9.0549661	9.9971849	9.0577813	10.9422187	10.0028151	10.9450335 29
32	9.0560706	9.9971704	9.0589002	10.9410998	10.0028296	10.9439294 28
33	9.0571723	9.9971559	9.0600164	10.9399836	10.0028441	10.9428277 27
34	9.0582711	9.9971414	9.0611297	10.9388703	10.0028586	10.9417289 26
35	9.0593672	9.9971268	9.0622403	10.9377597	10.0028732	10.9406328 25
36	9.0604604	9.9971122	9.0633482	10.9366518	10.0028878	10.9395396 24
37	9.0615505	9.9970976	9.0644533	10.9355467	10.0029024	10.9384491 23
38	9.0626386	9.9970829	9.0655556	10.9344444	10.0029171	10.9373614 22
39	9.0637235	9.9970682	9.0666553	10.9333447	10.0029318	10.9362765 21
40	9.0648057	9.9970535	9.0677522	10.9322478	10.0029465	10.9351943 20
41	9.0658852	9.9970387	9.0688465	10.9311535	10.0029613	10.9341148 19
42	9.0669619	9.9970239	9.0699381	10.9300619	10.0029761	10.9330381 18
43	9.0680360	9.9970090	9.0710270	10.9289730	10.0029910	10.9319640 17
44	9.0691074	9.9969941	9.0721133	10.9278867	10.0030059	10.9308926 16
45	9.0701761	9.9969792	9.0731969	10.9268031	10.0030208	10.9298239 15
46	9.0712421	9.9969642	9.0742779	10.9257221	10.0030358	10.9287579 14
47	9.0723055	9.9969492	9.0753563	10.9246437	10.0030508	10.9276945 13
48	9.0733663	9.9969342	9.0764321	10.9235679	10.0030658	10.9266337 12
49	9.0744244	9.9969191	9.0775053	10.9224947	10.0030809	10.9255756 11
50	9.0754799	9.9969040	9.0785760	10.9214240	10.0030960	10.9245201 10
51	9.0765329	9.9968888	9.0796441	10.9203559	10.0031112	10.9234671 9
52	9.0775832	9.9968736	9.0807096	10.9192904	10.0031264	10.9224168 8
53	9.0786310	9.9968584	9.0817726	10.9182274	10.0031416	10.9213690 7
54	9.0796762	9.9968431	9.0828331	10.9171669	10.0031569	10.9203238 6
55	9.0807189	9.9968278	9.0838911	10.9161089	10.0031722	10.9192811 5
56	9.0817590	9.9968121	9.0849466	10.9150534	10.0031875	10.9182410 4
57	9.0827966	9.9967971	9.0859996	10.9140004	10.0032029	10.9172034 3
58	9.0838317	9.9967817	9.0870501	10.9129495	10.0032183	10.9161683 2
59	9.0848643	9.9967662	9.0880981	10.9119010	10.0032338	10.9151357 1
60	9.0858945	9.9967507	9.0891438	10.9108562	10.0032493	10.9141057
	Sine.		Tang.		Secant.	

83 Degrees.

A Table of Artificial Sines,

7 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.0858945	9.9967507	9.0891438	10.9108562	10.0032493	10.9141055	60
1	9.0869221	9.9967352	9.0901869	10.9098131	10.0032648	10.9130779	59
2	9.0879473	9.9967196	9.0912277	10.9087723	10.0032804	10.9120527	58
3	9.0889700	9.9967040	9.0922660	10.9077340	10.0032960	10.9110300	57
4	9.0899903	9.9966884	9.0933020	10.9066980	10.0033116	10.9100097	56
5	9.0910082	9.9966727	9.0943355	10.9056645	10.0033273	10.9089918	55
6	9.0920237	9.9966570	9.0953667	10.9046333	10.0033430	10.9079763	54
7	9.0930367	9.9966412	9.0963955	10.9036045	10.0033588	10.9069533	53
8	9.0940474	9.9966254	9.0974219	10.9025781	10.0033746	10.9059526	52
9	9.0950556	9.9966096	9.0984460	10.9015540	10.0033904	10.9049444	51
10	9.0960615	9.9965937	9.0994678	10.9005322	10.0034063	10.9039385	50
11	9.0970651	9.9965778	9.1004872	10.8995128	10.0034222	10.9029349	49
12	9.0980662	9.9965619	9.1015044	10.8984956	10.0034381	10.9019338	48
13	9.0990651	9.9965459	9.1025192	10.8974808	10.0034541	10.9009349	47
14	9.0000616	9.9965299	9.1035317	10.8964683	10.0034701	10.8999384	46
15	9.0010558	9.9965138	9.1045420	10.8954580	10.0034862	10.8989442	45
16	9.1020477	9.9964977	9.1055500	10.8944500	10.0035023	10.8979523	44
17	9.1030373	9.9964816	9.1065557	10.8934443	10.0035184	10.8969627	43
18	9.1040246	9.9964655	9.1075591	10.8924409	10.0035345	10.8959754	42
19	9.1050096	9.9964493	9.1085604	10.8914396	10.0035507	10.8949904	41
20	9.1059924	9.9964330	9.1095594	10.8904406	10.0035670	10.8940076	40
21	9.1069729	9.9964167	9.1105562	10.8894438	10.0035833	10.8930271	39
22	9.1079512	9.9964004	9.1115508	10.8884492	10.0035996	10.8920488	38
23	9.1089272	9.9963841	9.1125431	10.8874569	10.0036159	10.8910728	37
24	9.1099010	9.9963677	9.1135333	10.8864657	10.0036323	10.8900990	36
25	9.1108726	9.9963513	9.1145213	10.8854787	10.0036487	10.8891274	35
26	9.1118420	9.9963348	9.1155072	10.8844928	10.0036652	10.8881580	34
27	9.1128092	9.9963183	9.1164909	10.8835091	10.0036817	10.8871908	33
28	9.1137742	9.9963018	9.1174724	10.8825276	10.0036982	10.8862258	32
29	9.1147370	9.9962852	9.1184518	10.8815482	10.0037148	10.8852630	31
30	9.1156977	9.9962686	9.1194291	10.8805709	10.0037314	10.8843023	30
		Sine.		Tang.		Secan.	Min.

82 Degrees.

Tangents and Secants.

7 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.1156977	9.9962686	9.1194291	10.8805709	10.0037314	10.8843022
31	9.1166562	9.9962519	9.1204043	10.8795974	10.0037481	10.8833438
32	9.1176125	9.9962352	9.1213773	10.8786227	10.0037648	10.8823875
33	9.1185667	9.9962185	9.1223482	10.8776518	10.0037815	10.8814333
34	9.1195188	9.9962017	9.1233171	10.8766829	10.0037983	10.8804812
35	9.1204688	9.9961849	9.1242839	10.8757161	10.0038151	10.8795312
36	9.1214167	9.9961681	9.1252486	10.8747514	10.0038319	10.8785833
37	9.1223624	9.9961512	9.1262112	10.8737888	10.0038488	10.8776376
38	9.1233061	9.9961343	9.1271718	10.8728282	10.0038657	10.8766939
39	9.1242477	9.9961174	9.1281303	10.8718697	10.0038826	10.8757523
40	9.1251872	9.9961004	9.1290868	10.8709132	10.0038996	10.8748128
41	9.1261246	9.9960834	9.1300413	10.8699587	10.0039166	10.8738754
42	9.1270600	9.9960663	9.1309937	10.8690063	10.0039337	10.8729400
43	9.1279934	9.9960492	9.1319442	10.8680558	10.0039508	10.8720066
44	9.1289247	9.9960321	9.1328926	10.8671074	10.0039679	10.8710753
45	9.1298539	9.9960149	9.1338390	10.8661609	10.0039851	10.8701461
46	9.1307812	9.9959977	9.1347835	10.8652165	10.0040023	10.8692188
47	9.1317064	9.9959804	9.1357260	10.8642740	10.0040196	10.8682936
48	9.1326297	9.9959631	9.1366665	10.8633335	10.0040369	10.8673703
49	9.1335509	9.9959458	9.1376051	10.8623949	10.0040542	10.8664491
50	9.1344702	9.9959284	9.1385417	10.8614583	10.0040716	10.8655298
51	9.1353875	9.9959111	9.1394764	10.8605236	10.0040889	10.8646125
52	9.1363028	9.9958936	9.1404092	10.8595908	10.0041064	10.8636972
53	9.1372161	9.9958761	9.1413400	10.8586600	10.0041239	10.8627839
54	9.1381275	9.9958586	9.1422689	10.8577311	10.0041414	10.8618725
55	9.1390370	9.9958411	9.1431959	10.8568041	10.0041589	10.8609630
56	9.1399445	9.9958235	9.1441210	10.8558790	10.0041765	10.8600555
57	9.1408501	9.9958059	9.1450442	10.8549558	10.0041941	10.8591499
58	9.1417537	9.9957882	9.1459655	10.8540345	10.0042118	10.8582463
59	9.1426555	9.9957705	9.1468850	10.8531150	10.0042295	10.8573445
60	9.1435553	9.9957528	9.1478025	10.8521975	10.0042472	10.8564447
	Sine.		Tang.		Secant.	

83 Degrees.

A Table of Artificial Sines,

8 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.1435553	9.9957528	9.1478025	10.8521975	10.0042472	10.856444760
1	9.1444532	9.9957350	9.1487182	10.8512818	10.0042650	10.855546859
2	9.1453493	9.9957172	9.1496321	10.8503679	10.0042828	10.854650758
3	9.1462435	9.9956993	9.1505441	10.8494559	10.0043007	10.853756557
4	9.1471358	9.9956815	9.1514543	10.8485457	10.0043185	10.852864256
5	9.1480262	9.9956635	9.1523627	10.8475373	10.0043365	10.851973855
6	9.1489148	9.9956456	9.1532692	10.8467308	10.0043544	10.851085254
7	9.1498015	9.9956276	9.1541739	10.8458261	10.0043724	10.850198553
8	9.1506864	9.9956095	9.1550769	10.8449231	10.0043905	10.849313652
9	9.1515694	9.9955915	9.1559780	10.8440220	10.0044085	10.848430651
10	9.1524507	9.9955734	9.1568873	10.8431227	10.0044266	10.847549350
11	9.1533301	9.9955552	9.1577748	10.8422252	10.0044448	10.846669949
12	9.1542076	9.9955370	9.1586706	10.8413294	10.0044630	10.845792448
13	9.1550834	9.9955188	9.1595646	10.8404354	10.0044812	10.844916647
14	9.1559574	9.9955005	9.1604569	10.8395431	10.0044995	10.844042646
15	9.1568296	9.9954822	9.1613473	10.8386527	10.0045178	10.843170445
16	9.1577000	9.9954639	9.1622361	10.8377639	10.0045361	10.842300044
17	9.1585686	9.9954453	9.1631231	10.8368769	10.0045545	10.841431443
18	9.1594354	9.9954271	9.1640083	10.8359917	10.0045729	10.840564642
19	9.1603005	9.9954087	9.1648919	10.8351081	10.0045913	10.839699541
20	9.1611639	9.9953902	9.1657737	10.8342263	10.0046098	10.838836140
21	9.1620254	9.9953717	9.1666538	10.8333462	10.0046283	10.837974639
22	9.1628853	9.9953531	9.1675322	10.8324678	10.0046469	10.837114738
23	9.1637434	9.9953345	9.1684989	10.8315911	10.0046655	10.836256637
24	9.1645998	9.9953159	9.1692839	10.8307161	10.0046841	10.835400236
25	9.1654554	9.9952972	9.1701572	10.8298428	10.0047028	10.834545635
26	9.1663073	9.9952785	9.1710289	10.8289711	10.0047215	10.833692634
27	9.1671586	9.9952597	9.1718989	10.8281011	10.0047403	10.832841433
28	9.1680082	9.9952409	9.1727672	10.8272328	10.0047591	10.831991932
29	9.1688559	9.9952221	9.1736338	10.8263662	10.0047779	10.831144131
30	9.1697021	9.9952033	9.1744988	10.8255012	10.0047967	10.830297930
	Sine.		Tang.		Secant.	Min.

81 Degrees.

Tangents and Secants.

8 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.1697021	9.9952033	9.1744980	10.8255012	10.0047967	10.8302975	30
31	9.1705465	9.9951844	9.1753622	10.8246378	10.0048156	10.8294534	29
32	9.1713893	9.9951654	9.1762239	10.8237761	10.0048346	10.8286107	28
33	9.1722305	9.9951464	9.1770840	10.8229160	10.0048536	10.8277695	27
34	9.1730699	9.9951274	9.1779425	10.8220575	10.0048726	10.8269301	26
35	9.1739077	9.9951084	9.1787993	10.8212007	10.0048916	10.8260923	25
36	9.1747439	9.9950893	9.1796546	10.8103454	10.0049107	10.8252561	24
37	9.1755784	9.9950702	9.1805082	10.8194918	10.0049298	10.8244216	23
38	9.1764112	9.9950510	9.1813602	10.8186398	10.0049490	10.8235888	22
39	9.1772425	9.9950318	9.1822106	10.8177894	10.0049682	10.8227575	21
40	9.1780721	9.9950126	9.1830595	10.8169405	10.0049874	10.8219279	20
41	9.1789001	9.9949933	9.1839068	10.8160932	10.0050067	10.8210999	19
42	9.1797265	9.9949740	9.1847525	10.8152475	10.0050262	10.8202735	18
43	9.1805512	9.9949546	9.1855966	10.8144034	10.0050454	10.8194488	17
44	9.1813744	9.9949352	9.1864392	10.8135608	10.0050648	10.8186256	16
45	9.1821960	9.9949158	9.1872806	10.8127198	10.0050842	10.8178040	15
46	9.1830160	9.9948964	9.1881196	10.8118804	10.0051035	10.8169840	14
47	9.1838344	9.9948769	9.1889575	10.8110425	10.0051231	10.8161656	13
48	9.1846512	9.9948573	9.1897939	10.8102061	10.0051427	10.8153488	12
49	9.1854665	9.9948377	9.1906287	10.8093713	10.0051623	10.8145335	11
50	9.1862802	9.9948181	9.1914621	10.8085379	10.0051819	10.8137199	10
51	9.1870923	9.9947985	9.1922939	10.8077061	10.0052015	10.8129077	9
52	9.1879029	9.9947788	9.1931241	10.8068759	10.0052212	10.8120971	8
53	9.1887120	9.9947591	9.1939529	10.8060471	10.0052409	10.8112880	7
54	9.1895195	9.9947393	9.1947802	10.8052198	10.0052607	10.8104805	6
55	9.1903254	9.9947195	9.1956059	10.8043941	10.0052805	10.8096746	5
56	9.1911299	9.9946997	9.1964302	10.8035698	10.0053003	10.8088701	4
57	9.1919328	9.9946798	9.1972530	10.8027470	10.0053202	10.8080671	3
58	9.1927342	9.9946599	9.1980742	10.8019257	10.0053401	10.8072658	2
59	9.1935341	9.9946399	9.1988942	10.8011055	10.0053601	10.8064659	1
60	9.1943324	9.9946195	9.1997125	10.8002875	10.0053801	10.8056676	0
		Sine.		Tang.		Secant.	Min.

81 Degrees.

A Table of Artificial Sines,

9 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.1943324	9.9946190	9.1997125	10.8002875	10.0053801	10.8056679	60
1	9.1951293	9.9945999	9.2005294	10.7994706	10.0054001	10.8048707	59
2	9.1959247	9.9945798	9.2013449	10.7986551	10.0054202	10.8040753	58
3	9.1967186	9.9945597	9.2021588	10.7978411	10.0054403	10.8032814	57
4	9.1975110	9.9945396	9.2029714	10.7975286	10.0054604	10.8024860	56
5	9.1983019	9.9945194	9.2037825	10.7962175	10.0054806	10.8016981	55
6	9.1990913	9.9944992	9.2045922	10.7954078	10.0055008	10.8009087	54
7	9.1998793	9.9944789	9.2054004	10.7945996	10.0055211	10.8001207	53
8	9.2006658	9.9944587	9.2062072	10.7937928	10.0055413	10.7993342	52
9	9.2014509	9.9944383	9.2070126	10.7929874	10.0055617	10.7985491	51
10	9.2022345	9.9944180	9.2078165	10.7921835	10.0055820	10.7977655	50
11	9.2030167	9.9943975	9.2086191	10.7913809	10.0056025	10.7968633	49
12	9.2037974	9.9943771	9.2094203	10.7905797	10.0056229	10.7960206	48
13	9.2045767	9.9943566	9.2102200	10.7897800	10.0056434	10.7954234	47
14	9.2053545	9.9943361	9.2110184	10.7889816	10.0056639	10.7946455	46
15	9.2061309	9.9943156	9.2118153	10.7881847	10.0056844	10.7938691	45
16	9.2069059	9.9942950	9.2126109	10.7873891	10.0057050	10.7930941	44
17	9.2076795	9.9942743	9.2134051	10.7865949	10.0057257	10.7923205	43
18	9.2084516	9.9942537	9.2141980	10.7858020	10.0057463	10.7915484	42
19	9.2092224	9.9942330	9.2149894	10.7850106	10.0057670	10.7907776	41
20	9.2099917	9.9942122	9.2157795	10.7842205	10.0057878	10.7900083	40
21	9.2107597	9.9941914	9.2165683	10.7834317	10.0058086	10.7892403	39
22	9.2115263	9.9941706	9.2173556	10.7826444	10.0058294	10.7884737	38
23	9.2122914	9.9941498	9.2181417	10.7818583	10.0058502	10.7877086	37
24	9.2130552	9.9941289	9.2189264	10.7810736	10.0058711	10.7869448	36
25	9.2138176	9.9941079	9.2197097	10.7802903	10.0058921	10.7861824	35
26	9.2145787	9.9940870	9.2204917	10.7795083	10.0059130	10.7854213	34
27	9.2153384	9.9940659	9.2212724	10.7787277	10.0059341	10.7846616	33
28	9.2160967	9.9940449	9.2220518	10.7779482	10.0059551	10.7839033	32
29	9.2168536	9.9940238	9.2228298	10.7771702	10.0059762	10.7831464	31
30	9.2176092	9.9940027	9.2236065	10.7763935	10.0059973	10.7823908	30
	Sine.		Tang.		Secant.		Min.

80 Degrees.

Tangents and Secants.

9 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.2176092	9.9940027	9.2236065	10.7763935	10.0050973	10.7823908	30
31	9.2183635	9.9939815	9.2243819	10.7756181	10.0050185	10.7816365	29
32	9.2191164	9.9939603	9.2251561	10.7748439	10.0050397	10.7808836	28
33	9.2198680	9.9939391	9.2259289	10.7740711	10.0050609	10.7801320	27
34	9.2206182	9.9939178	9.2267004	10.7732996	10.0050822	10.7793818	26
35	9.2213671	9.9938965	9.2274706	10.7725294	10.0051035	10.7786329	25
36	9.2221147	9.9938752	9.2282395	10.7717605	10.0051248	10.7778853	24
37	9.2228609	9.9938538	9.2290071	10.7709929	10.0051467	10.7771391	23
38	9.2236059	9.9938324	9.2297735	10.7702265	10.0051676	10.7763941	22
39	9.2243495	9.9938109	9.2305386	10.7694614	10.0051891	10.7756505	21
40	9.2250918	9.9937894	9.2313024	10.7686976	10.0052106	10.7749082	20
41	9.2258328	9.9937679	9.2320650	10.7679350	10.0052321	10.7741672	19
42	9.2265725	9.9937463	9.2328262	10.7671738	10.0052537	10.7734275	18
43	9.2273110	9.9937247	9.2335863	10.7664137	10.0052753	10.7726890	17
44	9.2280481	9.9937030	9.2343451	10.7656549	10.0052970	10.7719519	16
45	9.2287839	9.9936813	9.2351026	10.7648974	10.0053187	10.7712161	15
46	9.2295185	9.9936596	9.2358589	10.7641411	10.0053404	10.7704815	14
47	9.2302518	9.9936378	9.2366139	10.7633861	10.0053622	10.7697482	13
48	9.2309838	9.9936160	9.2373678	10.7626322	10.0053840	10.7690162	12
49	9.2317145	9.9935942	9.2381203	10.7618797	10.0054058	10.7682855	11
50	9.2324440	9.9935723	9.2388717	10.7611283	10.0054277	10.7675560	10
51	9.2331722	9.9935504	9.2396218	10.7603782	10.0054496	10.7668278	9
52	9.2338992	9.9935285	9.2403708	10.7596292	10.0054715	10.7661008	8
53	9.2346249	9.9935065	9.2411185	10.7588815	10.0054935	10.7653751	7
54	9.2353494	9.9934844	9.2418650	10.7581350	10.0055156	10.7646506	6
55	9.2360726	9.9934624	9.2426103	10.7573897	10.0055376	10.7639274	5
56	9.2367946	9.9934403	9.2433543	10.7566457	10.0055597	10.7632054	4
57	9.2375153	9.9934181	9.2440972	10.7559028	10.0055819	10.7624847	3
58	9.2382349	9.9933959	9.2448389	10.7551611	10.0056041	10.7617651	2
59	9.2389532	9.9933737	9.2455794	10.7544206	10.0056263	10.7610468	1
60	9.2396702	9.9933515	9.2463188	10.7536812	10.0056485	10.7603298	0
	Sine.		Tang.		Secant.		Min.

80 Degrees.

A Table of Artificial Sines,

10 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.2396702	9.9933515	9.2463188	10.7536812	10.0066485	10.7603298	60
1	9.2403861	9.9933292	9.2470569	10.7529431	10.0066708	10.7596139	59
2	9.2411007	9.9933068	9.2477939	10.7522061	10.0066932	10.7588993	58
3	9.2418141	9.9932845	9.2485297	10.7514703	10.0067155	10.7581859	57
4	9.2425264	9.9932621	9.2492643	10.7507357	10.0067379	10.7574736	56
5	9.2432374	9.9932396	9.2499978	10.7500022	10.0067604	10.7567626	55
6	9.2439472	9.9932171	9.2507301	10.7492699	10.0067829	10.7560528	54
7	9.2446558	9.9931946	9.2514612	10.7485388	10.0068054	10.7553442	53
8	9.2453632	9.9931720	9.2521912	10.7478088	10.0068280	10.7546368	52
9	9.2460695	9.9931494	9.2529200	10.7470800	10.0068506	10.7539305	51
10	9.2467746	9.9931268	9.2536477	10.7463523	10.0068732	10.7532254	50
11	9.2474784	9.9931041	9.2543742	10.7456257	10.0068959	10.7525216	49
12	9.2481811	9.9930814	9.2550997	10.7449003	10.0069186	10.7518189	48
13	9.2488827	9.9930587	9.2558240	10.7441760	10.0069413	10.7511173	47
14	9.2495836	9.9930359	9.2565472	10.7434528	10.0069641	10.7504170	46
15	9.2502822	9.9930131	9.2572692	10.7427308	10.0069869	10.7497178	45
16	9.2509803	9.9929902	9.2579901	10.7420099	10.0070098	10.7490197	44
17	9.2516772	9.9929673	9.2587099	10.7412901	10.0070327	10.7483228	43
18	9.2523729	9.9929444	9.2594285	10.7405715	10.0070556	10.7476271	42
19	9.2530675	9.9929214	9.2601461	10.7398539	10.0070786	10.7469325	41
20	9.2537609	9.9928984	9.2608625	10.7391375	10.0071016	10.7462391	40
21	9.2544531	9.9928753	9.2615779	10.7384221	10.0071247	10.7455468	39
22	9.2551444	9.9928522	9.2622921	10.7377079	10.0071478	10.7448556	38
23	9.2558344	9.9928291	9.2630053	10.7369947	10.0071709	10.7441656	37
24	9.2565233	9.9928059	9.2637173	10.7362827	10.0071941	10.7434767	36
25	9.2572110	9.9927827	9.2644283	10.7355717	10.0072173	10.7427890	35
26	9.2578977	9.9927595	9.2651382	10.7348618	10.0072405	10.7421023	34
27	9.2585832	9.9927362	9.2658470	10.7341530	10.0072638	10.7414168	33
28	9.2592676	9.9927129	9.2665547	10.7334453	10.0072871	10.7407342	32
29	9.2599509	9.9926895	9.2672613	10.7327387	10.0073105	10.7400491	31
30	9.2606300	9.9926661	9.2679699	10.7320331	10.0073339	10.7393670	30
	Sine.		Tang.		Secant.		Min.

79 Degrees.

Tangents and Secants.

10 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.2606330	9.9926661	9.2679669	10.7320331	10.0073339	10.739367030
31	9.2613141	9.9926427	9.2686714	10.7313286	10.0073573	10.738685929
32	9.2619941	9.9926192	9.2693749	10.7306251	10.0073808	10.738005928
33	9.2626729	9.9925957	9.2700772	10.7299228	10.0074043	10.737327127
34	9.2633507	9.9925722	9.2707786	10.7292214	10.0074278	10.736649326
35	9.2640274	9.9925486	9.2714788	10.7285212	10.0074514	10.735972925
36	9.2647030	9.9925250	9.2721780	10.7278220	10.0074750	10.735297024
37	9.2653775	9.9925013	9.2728762	10.7271238	10.0074987	10.734622523
38	9.2660509	9.9924776	9.2735733	10.7264267	10.0075224	10.733949122
39	9.2667232	9.9924539	9.2742694	10.7257306	10.0075461	10.733276821
40	9.2673945	9.9924301	9.2749644	10.7250356	10.0075699	10.732605520
41	9.2680647	9.9924063	9.2756584	10.7243416	10.0075937	10.731935319
42	9.2687338	9.9923824	9.2763514	10.7236486	10.0076176	10.731266218
43	9.2694019	9.9923585	9.2770434	10.7229566	10.0076415	10.730598117
44	9.2700689	9.9923346	9.2777343	10.7222657	10.0076654	10.729931116
45	9.2707348	9.9923106	9.2784242	10.7215758	10.0076894	10.729265215
46	9.2713997	9.9922866	9.2791130	10.7208869	10.0077134	10.728600314
47	9.2720635	9.9922626	9.2798009	10.7201991	10.0077374	10.727936513
48	9.2727263	9.9922385	9.2804878	10.7195122	10.0077615	10.727273712
49	9.2733880	9.9922144	9.2811736	10.7188264	10.0077856	10.726612011
50	9.2740487	9.9921902	9.2818585	10.7181415	10.0078098	10.725951310
51	9.2747083	9.9921660	9.2825423	10.7174577	10.0078340	10.72529179
52	9.2753665	9.9921418	9.2832251	10.7167749	10.0078582	10.72463318
53	9.2760245	9.9921175	9.2839069	10.7160930	10.0078825	10.72397557
54	9.2766811	9.9920932	9.2845878	10.7154122	10.0079068	10.72331896
55	9.2773366	9.9920689	9.2852677	10.7147323	10.0079311	10.72266345
56	9.2779911	9.9920445	9.2859466	10.7140534	10.0079554	10.72200894
57	9.2786445	9.9920201	9.2866245	10.7133755	10.0079799	10.72135593
58	9.2792970	9.9919956	9.2873014	10.7126986	10.0080044	10.72070302
59	9.2799484	9.9919711	9.2879773	10.7120227	10.0080289	10.72005161
60	9.2805988	9.9919466	9.2886523	10.7113477	10.0080534	10.71940100
	Sine.		Tang.		Secant.	Min.

79 Degrees.

A Table of Artificial Sines,

11 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.2805988	9.9919460	9.2886523	10.7113477	10.0080534	10.7194012	60
1	9.2812483	9.9919220	9.2892363	10.7106737	10.0080780	10.7187517	59
2	9.2818967	9.9918974	9.2899993	10.7100007	10.0081026	10.7181033	58
3	9.2825441	9.9918727	9.2906713	10.7093287	10.0081273	10.7174559	57
4	9.2831905	9.9918480	9.2913424	10.7086576	10.0081520	10.7168095	56
5	9.2838359	9.9918233	9.2920126	10.7079874	10.0081767	10.7161641	55
6	9.2844803	9.9917986	9.2926817	10.7073183	10.0082014	10.7155197	54
7	9.2851237	9.9917737	9.2933509	10.7066500	10.0082263	10.7148763	53
8	9.2857661	9.9917489	9.2940172	10.7059828	10.0082511	10.7142339	52
9	9.2864076	9.9917240	9.2946836	10.7053164	10.0082760	10.7135924	51
10	9.2870480	9.9916991	9.2953489	10.7046511	10.0083009	10.7129520	50
11	9.2876875	9.9916741	9.2960134	10.7039866	10.0083259	10.7123125	49
12	9.2883260	9.9916492	9.2966769	10.7033231	10.0083508	10.7116840	48
13	9.2889636	9.9916241	9.2973395	10.7026605	10.0083759	10.7110364	47
14	9.2896001	9.9915990	9.2980011	10.7019989	10.0084010	10.7103999	46
15	9.2902357	9.9915739	9.2986618	10.7013382	10.0084261	10.7097643	45
16	9.2908704	9.9915488	9.2993216	10.7006784	10.0084512	10.7091296	44
17	9.2915040	9.9915236	9.2999804	10.7000196	10.0084764	10.7084960	43
18	9.2921367	9.9914984	9.3006383	10.6993617	10.0085016	10.7078633	42
19	9.2927685	9.9914731	9.3012954	10.6987046	10.0085269	10.7072315	41
20	9.2933992	9.9914478	9.3019514	10.6980486	10.0085522	10.7066007	40
21	9.2940291	9.9914225	9.3026066	10.6973934	10.0085775	10.7059709	39
22	9.2946580	9.9913971	9.3032609	10.6967391	10.0086029	10.7053420	38
23	9.2952859	9.9913717	9.3039143	10.6960857	10.0086283	10.7047141	37
24	9.2959129	9.9913462	9.3045667	10.6954333	10.0086538	10.7040871	36
25	9.2965390	9.9913207	9.3052183	10.6947817	10.0086793	10.7034610	35
26	9.2971641	9.9912952	9.3058689	10.6941311	10.0087048	10.7028359	34
27	9.2977883	9.9912696	9.3065187	10.6934813	10.0087304	10.7022117	33
28	9.2984116	9.9912440	9.3071675	10.6928325	10.0087560	10.7015884	32
29	9.2990339	9.9912184	9.3078155	10.6921845	10.0087816	10.7009666	31
30	9.2996553	9.9911927	9.3084626	10.6915374	10.0088073	10.7003447	30
	Sine.		Tang.		Secant.		Min.

78 Degrees.

Tangents and Secants.

11 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.2996553	9.9911927	9.3084626	10.6915374	10.0088073	10.7003442	30
31	9.3002758	9.9911670	9.3091088	10.6908912	10.0088330	10.6997242	29
32	9.3008953	9.9911412	9.3097551	10.6902459	10.0088588	10.6991047	28
33	9.3015140	9.9911154	9.3103985	10.6896015	10.0088846	10.6984860	27
34	9.3021317	9.9910896	9.3110421	10.6889579	10.0089104	10.6978683	26
35	9.3027485	9.9910637	9.3116848	10.6883152	10.0089362	10.6972515	25
36	9.3033644	9.9910378	9.3123266	10.6876734	10.0089622	10.6966356	24
37	9.3039794	9.9910119	9.3129675	10.6870325	10.0089881	10.6960206	23
38	9.3045934	9.9909859	9.3136076	10.6863924	10.0090141	10.6954066	22
39	9.3052066	9.9909598	9.3142468	10.6857532	10.0090402	10.6947934	21
40	9.3058189	9.9909338	9.3148851	10.6851149	10.0090662	10.6941811	20
41	9.3064303	9.9909077	9.3155226	10.6844774	10.0090923	10.6935697	19
42	9.3070407	9.9908815	9.3161592	10.6838408	10.0091185	10.6929593	18
43	9.3076503	9.9908553	9.3167950	10.6832050	10.0091447	10.6923497	17
44	9.3082590	9.9908291	9.3174299	10.6825701	10.0091709	10.6917410	16
45	9.3088668	9.9908029	9.3180640	10.6819360	10.0091971	10.6911332	15
46	9.3094737	9.9907766	9.3186972	10.6813028	10.0092234	10.6905263	14
47	9.3100798	9.9907502	9.3193295	10.6806705	10.0092498	10.6899202	13
48	9.3106849	9.9907239	9.3199611	10.6800389	10.0092761	10.6893151	12
49	9.3112892	9.9906974	9.3205918	10.6794082	10.0093026	10.6887108	11
50	9.3118962	9.9906710	9.3212216	10.6787784	10.0093290	10.6881074	10
51	9.3124951	9.9906445	9.3218506	10.6781494	10.0093555	10.6875049	9
52	9.3130968	9.9906180	9.3224788	10.6775212	10.0093820	10.6869032	8
53	9.3136976	9.9905914	9.3231061	10.6768939	10.0094086	10.6863024	7
54	9.3142975	9.9905648	9.3237327	10.6762673	10.0094352	10.6857025	6
55	9.3148965	9.9905382	9.3243584	10.6756416	10.0094618	10.6851035	5
56	9.3154947	9.9905115	9.3249832	10.6750168	10.0094885	10.6845053	4
57	9.3160921	9.9904848	9.3256073	10.6743927	10.0095152	10.6839079	3
58	9.3166885	9.9904580	9.3262305	10.6737695	10.0095420	10.6833115	2
59	9.3172841	9.9904312	9.3268529	10.6731471	10.0095638	10.6827129	1
60	9.3178789	9.9904044	9.3274745	10.6725255	10.0095956	10.6821211	0
	Sine.		Tang.		Secant.		Min.

78 Degrees.

A Table of Artificial Sines,

12 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.3178789	9.9904044	9.3274745	10.6725255	10.0095956	10.6821211	60
1	9.3184728	9.9903775	9.3280953	10.6719047	10.0096225	10.6815272	59
2	9.3190659	9.9903506	9.3287153	10.6712847	10.0096494	10.6809341	58
3	9.3196581	9.9903237	9.3293345	10.6706654	10.0096763	10.6803419	57
4	9.3202495	9.9902967	9.3299528	10.6700472	10.0097033	10.6797505	56
5	9.3208400	9.9902697	9.3305704	10.6694294	10.0097303	10.6791600	55
6	9.3214297	9.9902426	9.3311872	10.6688128	10.0097574	10.6785703	54
7	9.3220186	9.9902155	9.3318031	10.6681969	10.0097845	10.6779814	53
8	9.3226066	9.9901883	9.3324183	10.6675816	10.0098117	10.6773934	52
9	9.3231938	9.9901612	9.3330327	10.6669673	10.0098388	10.6768062	51
10	9.3237802	9.9901339	9.3336463	10.6663537	10.0098661	10.6762198	50
11	9.3243657	9.9901067	9.3342591	10.6657409	10.0098933	10.6756343	49
12	9.3249505	9.9900794	9.3348711	10.6651289	10.0099206	10.6750495	48
13	9.3255344	9.9900521	9.3354823	10.6645177	10.0099479	10.6744656	47
14	9.3261174	9.9900247	9.3360927	10.6639073	10.0099753	10.6738826	46
15	9.3266997	9.9899973	9.3367024	10.6632967	10.0100027	10.6733003	45
16	9.3272811	9.9899698	9.3373113	10.6626887	10.0100302	10.6727189	44
17	9.3278617	9.9899423	9.3379194	10.6620806	10.0100577	10.6721383	43
18	9.3284416	9.9899148	9.3385267	10.6614743	10.0100852	10.6715584	42
19	9.3290206	9.9898873	9.3391333	10.6608667	10.0101127	10.6709794	41
20	9.3295988	9.9898597	9.3397391	10.6602609	10.0101403	10.6704012	40
21	9.3301761	9.9898320	9.3403441	10.6596559	10.0101680	10.6698239	39
22	9.3307527	9.9898043	9.3409484	10.6590516	10.0101957	10.6692473	38
23	9.3313285	9.9897766	9.3415519	10.6584481	10.0102234	10.6686715	37
24	9.3319035	9.9897489	9.3421546	10.6578454	10.0102511	10.6680965	36
25	9.3324777	9.9897211	9.3427566	10.6572434	10.0102789	10.6675223	35
26	9.3330511	9.9896932	9.3433578	10.6566422	10.0103068	10.6669489	34
27	9.3336237	9.9896654	9.3439583	10.6560417	10.0103346	10.6663763	33
28	9.3341955	9.9896374	9.3445580	10.6554420	10.0103626	10.6658045	32
29	9.3347665	9.9896095	9.3451570	10.6548430	10.0103905	10.6652335	31
30	9.3353368	9.9895815	9.3457552	10.6542448	10.0104185	10.6646632	30
	Sine.		Tang.		Secant.		Min.

77 Degrees.

Tangents and Secants.

12 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.3353368	9.9895815	9.3457552	10.6542448	10.0104185	10.6646632	30
31	9.3359062	9.9895535	9.3463527	10.6536473	10.0104465	10.6640938	29
32	9.3364749	9.9895254	9.3469494	10.6530506	10.0104746	10.6635251	28
33	9.3370428	9.9894973	9.3475454	10.6524546	10.0105027	10.6629572	27
34	9.3376099	9.9894692	9.3481407	10.6518593	10.0105308	10.6623901	26
35	9.3381762	9.9894410	9.3487352	10.6512648	10.0105590	10.6618274	25
36	9.3387418	9.9894128	9.3493290	10.6506710	10.0105872	10.6612582	24
37	9.3393065	9.9893845	9.3499220	10.6500780	10.0106155	10.6606935	23
38	9.3398706	9.9893562	9.3505143	10.6494857	10.0106438	10.6601294	22
39	9.3404338	9.9893279	9.3511050	10.6488941	10.0106721	10.6595662	21
40	9.3409963	9.9892995	9.3516968	10.6483032	10.0107004	10.6590037	20
41	9.3415580	9.9892711	9.3522869	10.6477131	10.0107289	10.6584420	19
42	9.3421190	9.9892427	9.3528763	10.6471237	10.0107573	10.6578810	18
43	9.3426792	9.9892142	9.3534650	10.6465350	10.0107858	10.6573208	17
44	9.3432386	9.9891856	9.3540530	10.6459470	10.0108144	10.6567614	16
45	9.3437973	9.9891571	9.3546402	10.6453598	10.0108429	10.6562027	15
46	9.3443552	9.9891285	9.3552267	10.6447733	10.0108716	10.6556448	14
47	9.3449124	9.9890998	9.3558126	10.6441874	10.0109002	10.6550876	13
48	9.3454688	9.9890711	9.3563977	10.6436023	10.0109289	10.6545312	12
49	9.3460240	9.9890424	9.3569821	10.6430179	10.0109576	10.6539755	11
50	9.3465794	9.9890137	9.3575658	10.6424342	10.0109863	10.6534206	10
51	9.3471336	9.9889849	9.3581487	10.6418513	10.0110151	10.6528664	9
52	9.3476870	9.9889560	9.3587310	10.6412690	10.0110440	10.6523130	8
53	9.3482397	9.9889271	9.3593126	10.6406874	10.0110729	10.6517603	7
54	9.3487917	9.9888982	9.3598935	10.6401065	10.0111018	10.6512083	6
55	9.3493429	9.9888693	9.3604736	10.6395264	10.0111307	10.6506571	5
56	9.3498934	9.9888403	9.3610537	10.6389469	10.0111597	10.6501066	4
57	9.3504432	9.9888113	9.3616319	10.6383681	10.0111887	10.6495568	3
58	9.3509922	9.9887822	9.3622100	10.6377900	10.0112178	10.6490078	2
59	9.3515405	9.9887531	9.3627872	10.6372126	10.0112469	10.6484495	1
60	9.3520880	9.9887239	9.3633641	10.6366359	10.0112761	10.6479120	0
	Sine.		Tang.		Secant.		Min.

79 Degrees.

A Table of Artificial Sines,

13 Degrees.

Min.	Sine.		Tang.		Secant.		
C	9.3520880	9.9887239	9.3633641	10.6366359	10.0112761	10.6479120	60
1	9.3526349	9.9886847	9.3639401	10.6300599	10.0113053	10.6473651	59
2	9.3531810	9.9886655	9.3645155	10.6354840	10.0113345	10.6468190	58
3	9.3537264	9.9886365	9.3650901	10.6349099	10.0113637	10.6462736	57
4	9.3542710	9.9886070	9.3656641	10.6343359	10.0113930	10.6457290	56
5	9.3548150	9.9885776	9.3662374	10.6337626	10.0114224	10.6451850	55
6	9.3553582	9.9885482	9.3668100	10.6331900	10.0114518	10.6446418	54
7	9.3559008	9.9885188	9.3673819	10.6326181	10.0114812	10.6440993	53
8	9.3564426	9.9884894	9.3679532	10.6320468	10.0115106	10.6435574	52
9	9.3569836	9.9884599	9.3685238	10.6314762	10.0115401	10.6430164	51
10	9.3575240	9.9884303	9.3690937	10.6309063	10.0115697	10.6424760	50
11	9.3580637	9.9884008	9.3696629	10.6303371	10.0115992	10.6419362	49
12	9.3586027	9.9883712	9.3702315	10.6297685	10.0116288	10.6413973	48
13	9.3591409	9.9883415	9.3707994	10.6292006	10.0116585	10.6408591	47
14	9.3596785	9.9883118	9.3713667	10.6286333	10.0116882	10.6403215	46
15	9.3602154	9.9882821	9.3719333	10.6280667	10.0117179	10.6397846	45
16	9.3607515	9.9882523	9.3724992	10.6275008	10.0117477	10.6392485	44
17	9.3612870	9.9882225	9.3730645	10.6269355	10.0117775	10.6387130	43
18	9.3618217	9.9881927	9.3736291	10.6263709	10.0118073	10.6381783	42
19	9.3623558	9.9881628	9.3741930	10.6258070	10.0118372	10.6376442	41
20	9.3628892	9.9881329	9.3747563	10.6252437	10.0118671	10.6371108	40
21	9.3634219	9.9881029	9.3753190	10.6246810	10.0118971	10.6365781	39
22	9.3639539	9.9880729	9.3758810	10.6241190	10.0119271	10.6360461	38
23	9.3644852	9.9880429	9.3764423	10.6235577	10.0119571	10.6355148	37
24	9.3650158	9.9880128	9.3770030	10.6229970	10.0119872	10.6349842	36
25	9.3655458	9.9879827	9.3775631	10.6224369	10.0120173	10.6344542	35
26	9.3660750	9.9879525	9.3781225	10.6218775	10.0120475	10.6339250	34
27	9.3666036	9.9879223	9.3786813	10.6213187	10.0120777	10.6333964	33
28	9.3671315	9.9878921	9.3792394	10.6207606	10.0121079	10.6328685	32
29	9.3676587	9.9878618	9.3797969	10.6202031	10.0121382	10.6323413	31
30	9.3681853	9.9878315	9.3803537	10.6196463	10.0121685	10.6318147	30
	Sine.		Tang.		Secant.		Min.

76 Degrees.

Tangents and Secants.

13 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.3681853	9.9878315	9.3803537	10.6196463	10.0121685	10.6318147	30
31	9.3687111	9.9878012	9.3809100	10.6190900	10.0121988	10.6312889	29
32	9.3692363	9.9877708	9.3814655	10.6185345	10.0122292	10.6307637	28
33	9.3697608	9.9877404	9.3820205	10.6179795	10.0122596	10.6302392	27
34	9.3702847	9.9877099	9.3825784	10.6174252	10.0122901	10.6297153	26
35	9.3708079	9.9876794	9.3831285	10.6168715	10.0123206	10.6291921	25
36	9.3713304	9.9876488	9.3836816	10.6163184	10.0123512	10.6286696	24
37	9.3718523	9.9876183	9.3842340	10.6157660	10.0123817	10.6281477	23
38	9.3723735	9.9875876	9.3847858	10.6152142	10.0124124	10.6276265	22
39	9.3728940	9.9875570	9.3853370	10.6146630	10.0124430	10.6271060	21
40	9.3734139	9.9875263	9.3858876	10.6141124	10.0124737	10.6265861	20
41	9.3739331	9.9874955	9.3864376	10.6135624	10.0125045	10.6260669	19
42	9.3744517	9.9874648	9.3869869	10.6130131	10.0125352	10.6255483	18
43	9.3749696	9.9874339	9.3875356	10.6124644	10.0125661	10.6250304	17
44	9.3754868	9.9874031	9.3880837	10.6119163	10.0125969	10.6245132	16
45	9.3760034	9.9873722	9.3886312	10.6113688	10.0126278	10.6239966	15
46	9.3765194	9.9873413	9.3891781	10.6108219	10.0126587	10.6234806	14
47	9.3770347	9.9873103	9.3897244	10.6102756	10.0126897	10.6229653	13
48	9.3775493	9.9872793	9.3902700	10.6097300	10.0127207	10.6224507	12
49	9.3780633	9.9872482	9.3908155	10.6091849	10.0127518	10.6219367	11
50	9.3785767	9.9872171	9.3913595	10.6086405	10.0127829	10.6214233	10
51	9.3790894	9.9871860	9.3919034	10.6080966	10.0128140	10.6209106	9
52	9.3796015	9.9871549	9.3924466	10.6075534	10.0128451	10.6203985	8
53	9.3801129	9.9871236	9.3929893	10.6070107	10.0128764	10.6198871	7
54	9.3806237	9.9870924	9.3935313	10.6064687	10.0129076	10.6193763	6
55	9.3811339	9.9870611	9.3940727	10.6059273	10.0129389	10.6188661	5
56	9.3816434	9.9870298	9.3946136	10.6053864	10.0129702	10.6183566	4
57	9.3821523	9.9869984	9.3951538	10.6048462	10.0130016	10.6178477	3
58	9.3826605	9.9869670	9.3956935	10.6043065	10.0130330	10.6173395	2
59	9.3831682	9.9869356	9.3962326	10.6037674	10.0130644	10.6168318	1
60	9.3836752	9.9869041	9.3967711	10.6032289	10.0130959	10.6163248	0
	Sine.		Tang.		Secant.		Min.

76 Degrees.

A Table of Artificial Sines,

14 Degrees.

Mins.	Sine.		Tang.		Secant.		
0	9.3836752	9.9869041	9.3967311	10.6032289	10.0130959	10.6163248	60
1	9.3841815	9.9868726	9.3973089	10.6026911	10.0131274	10.6158185	59
2	9.3846873	9.9868410	9.3978463	10.6021537	10.0131590	10.6153127	58
3	9.3851924	9.9868094	9.3983830	10.6016170	10.0131906	10.6148076	57
4	9.3856969	9.9867778	9.3989191	10.6010809	10.0132222	10.6143031	56
5	9.3862008	9.9867461	9.3994547	10.6005453	10.0132530	10.6137992	55
6	9.3867070	9.9867144	9.3999896	10.6000104	10.0132856	10.6132960	54
7	9.3872067	9.9866827	9.4005240	10.5994760	10.0133173	10.6127933	53
8	9.3877087	9.9866509	9.4010578	10.5989422	10.0133491	10.6122913	52
9	9.3882101	9.9866191	9.4015910	10.5984090	10.0133806	10.6117899	51
10	9.3887109	9.9865872	9.4021237	10.5978763	10.0134128	10.6112891	50
11	9.3892111	9.9865553	9.4026558	10.5973442	10.0134447	10.6107889	49
12	9.3897106	9.9865233	9.4031873	10.5968127	10.0134767	10.6102894	48
13	9.3902096	9.9864913	9.4037182	10.5962818	10.0135087	10.6097904	47
14	9.3907079	9.9864593	9.4042486	10.5957514	10.0135407	10.6092921	46
15	9.3912057	9.9864273	9.4047784	10.5952216	10.0135727	10.6087943	45
16	9.3917028	9.9863952	9.4053076	10.5946924	10.0136048	10.6082972	44
17	9.3921993	9.9863630	9.4058363	10.5941637	10.0136370	10.6078007	43
18	9.3926952	9.9863308	9.4063644	10.5936356	10.0136692	10.6073048	42
19	9.3931905	9.9862986	9.4068919	10.5931081	10.0137014	10.6068095	41
20	9.3936852	9.9862663	9.4074189	10.5925811	10.0137337	10.6063148	40
21	9.3941744	9.9862340	9.4079453	10.5920547	10.0137660	10.6058206	39
22	9.3946729	9.9862017	9.4084712	10.5915288	10.0137983	10.6053271	38
23	9.3951658	9.9861693	9.4089965	10.5910035	10.0138307	10.6048342	37
24	9.3956581	9.9861369	9.4095212	10.5904788	10.0138631	10.6043419	36
25	9.3961499	9.9861045	9.4100454	10.5899546	10.0138955	10.6038501	35
26	9.3966410	9.9860720	9.4105690	10.5894310	10.0139280	10.6033590	34
27	9.3971315	9.9860394	9.4110921	10.5889079	10.0139606	10.6028685	33
28	9.3976215	9.9860069	9.4116146	10.5883854	10.0139931	10.6023785	32
29	9.3981109	9.9859742	9.4121366	10.5878634	10.0140258	10.6018891	31
30	9.3985996	9.9859416	9.4126581	10.5873419	10.0140584	10.6014004	30
	Sine.		Tang.		Secant.		Mins.

77 Degrees.

Tangents and Secants.

14 Degrees.

M. n.	Sine.		Tang.		Secant.		
30	9.3985996	9.9859416	9.4126581	10.5873419	10.0140584	10.6014004	30
31	9.3990878	9.9859089	9.4131789	10.5868211	10.0140911	10.6009122	29
32	9.3995754	9.9858762	9.4136993	10.5863007	10.0141238	10.6004246	28
33	9.4000925	9.9858434	9.4142191	10.5857809	10.0141526	10.5999375	27
34	9.4005489	9.9858106	9.4147383	10.5852617	10.0141894	10.5994511	26
35	9.4010348	9.9857777	9.4152570	10.5847430	10.0142223	10.5989652	25
36	9.4015201	9.9857449	9.4157752	10.5842248	10.0142551	10.5984799	24
37	9.4020048	9.9857119	9.4162928	10.5837072	10.0142881	10.5979952	23
38	9.4024889	9.9856790	9.4168099	10.5831901	10.0143210	10.5975111	22
39	9.4029734	9.9856460	9.4173265	10.5826735	10.0143540	10.5970276	21
40	9.4034554	9.9856129	9.4178425	10.5821575	10.0143871	10.5965446	20
41	9.4039378	9.9855798	9.4183580	10.5816420	10.0144202	10.5960622	19
42	9.4044196	9.9855467	9.4188729	10.5811271	10.0144533	10.5955804	18
43	9.4049009	9.9855135	9.4193874	10.5806126	10.0144865	10.5950991	17
44	9.4053816	9.9854803	9.4199013	10.5800987	10.0145197	10.5946184	16
45	9.4058617	9.9854471	9.4204146	10.5795854	10.0145529	10.5941383	15
46	9.4063413	9.9854138	9.4209275	10.5790725	10.0145862	10.5936587	14
47	9.4068203	9.9853805	9.4214398	10.5785602	10.0146195	10.5931797	13
48	9.4072987	9.9853471	9.4219515	10.5780485	10.0146529	10.5927013	12
49	9.4077766	9.9853138	9.4224628	10.5775372	10.0146862	10.5922234	11
50	9.4082539	9.9852803	9.4229735	10.5770265	10.0147197	10.5917461	10
51	9.4087306	9.9852468	9.4234838	10.5765162	10.0147532	10.5912694	9
52	9.4092068	9.9852133	9.4239935	10.5760065	10.0147867	10.5907932	8
53	9.4096824	9.9851798	9.4245026	10.5754974	10.0148202	10.5903176	7
54	9.4101575	9.9851462	9.4250113	10.5749887	10.0148538	10.5898425	6
55	9.4106320	9.9851125	9.4255194	10.5744806	10.0148875	10.5893680	5
56	9.4111059	9.9850789	9.4260271	10.5739729	10.0149211	10.5888941	4
57	9.4115793	9.9850452	9.4265342	10.5734658	10.0149548	10.5884207	3
58	9.4120522	9.9850114	9.4270408	10.5729592	10.0149886	10.5879478	2
59	9.4125245	9.9849776	9.4275469	10.5724532	10.0150224	10.5874755	1
60	9.4129962	9.9849438	9.4280525	10.5719475	10.0150562	10.5870038	0
	Sine.		Tang.		Secant.		Min.

75 Degrees.

A Table of Artificial Sines,

15 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.4129962	9.9849438	9.4280525	10.5719475	10.0150562	10.5870038 60
1	9.4134674	9.9849099	9.4285575	10.5714425	10.0150901	10.5865326 59
2	9.4139381	9.9848760	9.4290621	10.5709379	10.0151240	10.5860619 58
3	9.4144081	9.9848420	9.4295661	10.5704339	10.0151580	10.5855918 57
4	9.4148778	9.9848081	9.4300697	10.5699303	10.0151919	10.5851222 56
5	9.4153468	9.9847740	9.4305727	10.5694273	10.0152260	10.5846532 55
6	9.4158152	9.9847400	9.4310753	10.5689247	10.0152600	10.5841848 54
7	9.4162832	9.9847059	9.4315773	10.5684227	10.0152941	10.5837168 53
8	9.4167506	9.9846717	9.4320789	10.5679211	10.0153283	10.5832494 52
9	9.4172174	9.9846375	9.4325789	10.5674201	10.0153625	10.5827826 51
10	9.4176837	9.9846033	9.4330804	10.5669196	10.0153967	10.5823163 50
11	9.4181495	9.9845690	9.4335805	10.5664195	10.0154310	10.5818505 49
12	9.4186148	9.9845347	9.4340800	10.5659200	10.0154653	10.5813852 48
13	9.4190795	9.9845004	9.4345791	10.5654209	10.0154996	10.5809205 47
14	9.4195436	9.9844660	9.4350776	10.5649224	10.0155340	10.5804564 46
15	9.4200073	9.9844316	9.4355757	10.5644243	10.0155684	10.5799927 45
16	9.4204704	9.9843971	9.4360733	10.5639267	10.0156029	10.5795296 44
17	9.4209330	9.9843626	9.4365704	10.5634296	10.0156374	10.5790670 43
18	9.4213950	9.9843281	9.4370670	10.5629330	10.0156719	10.5786050 42
19	9.4218566	9.9842935	9.4375631	10.5624309	10.0157065	10.5781434 41
20	9.4223176	9.9842589	9.4380587	10.5619413	10.0157411	10.5776824 40
21	9.4227780	9.9842242	9.4385538	10.5614462	10.0157758	10.5772220 39
22	9.4232380	9.9841895	9.4390485	10.5609515	10.0158105	10.5767620 38
23	9.4236974	9.9841548	9.4395426	10.5604574	10.0158452	10.5763026 37
24	9.4241563	9.9841200	9.4400363	10.5599637	10.0158800	10.5758437 36
25	9.4246147	9.9840852	9.4405295	10.5594705	10.0159148	10.5753853 35
26	9.4250726	9.9840503	9.4410222	10.5589778	10.0159497	10.5749274 34
27	9.4255299	9.9840154	9.4415145	10.5584855	10.0159846	10.5744701 33
28	9.4259867	9.9839805	9.4420062	10.5579938	10.0160195	10.5740133 32
29	9.4264430	9.9839455	9.4424975	10.5575025	10.0160545	10.5735570 31
30	9.4268988	9.9839105	9.4429883	10.5570117	10.0160896	10.5731012 30
	Sine.		Tang.		Secant.	Min.

74 Degrees.

Tangents and Secants.

15 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.4268988	9.9839105	9.4429883	10.5570117	10.0160895	10.5731012	30
31	9.4273541	9.9838755	9.4434786	10.5565214	10.0161245	10.5726459	29
32	9.4278098	9.9838404	9.4439685	10.5560315	10.0161596	10.5721911	28
33	9.4282631	9.9838052	9.4444579	10.5555421	10.0161948	10.5717369	27
34	9.4287169	9.9837701	9.4449468	10.5550532	10.0162299	10.5712831	26
35	9.4291701	9.9837348	9.4454352	10.5545648	10.0162652	10.5708299	25
36	9.4296228	9.9836996	9.4459232	10.5540768	10.0163004	10.5703772	24
37	9.4300750	9.9836643	9.4464107	10.5535893	10.0163357	10.5699250	23
38	9.4305267	9.9836290	9.4468978	10.5531022	10.0163710	10.5694733	22
39	9.4309779	9.9835936	9.4473843	10.5526157	10.0164064	10.5690221	21
40	9.4314286	9.9835582	9.4478704	10.5521296	10.0164418	10.5685714	20
41	9.4318788	9.9835227	9.4483561	10.5516439	10.0164773	10.5681212	19
42	9.4323285	9.9834872	9.4488413	10.5511587	10.0165128	10.5676715	18
43	9.4327777	9.9834517	9.4493260	10.5506740	10.0165483	10.5672223	17
44	9.4332264	9.9834161	9.4498102	10.5501898	10.0165834	10.5667736	16
45	9.4336746	9.9833805	9.4502940	10.5497060	10.0166195	10.5663254	15
46	9.4341223	9.9833449	9.4507774	10.5492226	10.0166551	10.5658777	14
47	9.4345694	9.9833092	9.4512602	10.5487398	10.0166908	10.5654306	13
48	9.4350161	9.9832735	9.4517427	10.5482573	10.0167265	10.5649839	12
49	9.4354623	9.9832377	9.4522246	10.5477754	10.0167623	10.5645377	11
50	9.4359080	9.9832019	9.4527061	10.5472939	10.0167981	10.5640920	10
51	9.4363532	9.9831661	9.4531872	10.5468128	10.0168339	10.5636468	9
52	9.4367980	9.9831302	9.4536678	10.5463322	10.0168698	10.5632020	8
53	9.4372422	9.9830942	9.4541479	10.5458521	10.0169058	10.5627578	7
54	9.4376859	9.9830583	9.4546276	10.5453724	10.0169417	10.5623141	6
55	9.4381292	9.9830228	9.4551069	10.5448931	10.0169777	10.5618708	5
56	9.4385719	9.9829862	9.4555857	10.5444143	10.0170138	10.5614281	4
57	9.4390142	9.9829501	9.4560641	10.5439359	10.0170499	10.5609858	3
58	9.4394560	9.9829140	9.4565420	10.5434580	10.0170860	10.5605440	2
59	9.4398973	9.9828778	9.4570194	10.5429806	10.0171222	10.5601027	1
60	9.4403381	9.9828416	9.4574964	10.5425036	10.0171586	10.5596619	0
		Sine.		Tang.		Secant.	Min.

74 Degrees.

A Table of Artificial Sines,

16 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.4403381	9.9828416	9.4574964	10.5425036	10.0171584	10.559661960
1	9.4407784	9.9828054	9.4579730	10.5420270	10.0171946	10.559221659
2	9.4412182	9.9827691	9.4584491	10.5415509	10.0172309	10.558781858
3	9.4416576	9.9827328	9.4589248	10.5410752	10.0172672	10.558342457
4	9.4420965	9.9826964	9.4594001	10.5405995	10.0173036	10.557903556
5	9.4425349	9.9826600	9.4598749	10.5401251	10.0173400	10.557465155
6	9.4429728	9.9826236	9.4603492	10.5396508	10.0173764	10.557027254
7	9.4434103	9.9825871	9.4608232	10.5391768	10.0174129	10.556589753
8	9.4438472	9.9825506	9.4612967	10.5387033	10.0174494	10.556152852
9	9.4442837	9.9825140	9.4617697	10.5382303	10.0174860	10.555716351
10	9.4447197	9.9824774	9.4622423	10.5377577	10.0175226	10.555280350
11	9.4451553	9.9824408	9.4627145	10.5372855	10.0175592	10.554844749
12	9.4455904	9.9824041	9.4631863	10.5368137	10.0175959	10.554409648
13	9.4460250	9.9823674	9.4636576	10.5363424	10.0176326	10.553975047
14	9.4464591	9.9823306	9.4641285	10.5358715	10.0176694	10.553540946
15	9.4468927	9.9822938	9.4645990	10.5354010	10.0177062	10.553107345
16	9.4473259	9.9822569	9.4650690	10.5349310	10.0177431	10.552674144
17	9.4477586	9.9822201	9.4655386	10.5344614	10.0177799	10.552241443
18	9.4481909	9.9821831	9.4660078	10.5339922	10.0178169	10.551809142
19	9.4486227	9.9821462	9.4664765	10.5335235	10.0178538	10.551377341
20	9.4490540	9.9821092	9.4669448	10.5330552	10.0178908	10.550946040
21	9.4494849	9.9820721	9.4674127	10.5325873	10.0179279	10.550515139
22	9.4499153	9.9820351	9.4678802	10.5321198	10.0179649	10.550084738
23	9.4503452	9.9819979	9.4683473	10.5316527	10.0180021	10.549654837
24	9.4507747	9.9819608	9.4688139	10.5311861	10.0180392	10.549225336
25	9.4512037	9.9819236	9.4692801	10.5307195	10.0180764	10.548796335
26	9.4516322	9.9818863	9.4697459	10.5302541	10.0181137	10.548367834
27	9.4520603	9.9818490	9.4702112	10.5297888	10.0181510	10.547939733
28	9.4524879	9.9818117	9.4706762	10.5293238	10.0181883	10.547512132
29	9.4529151	9.9817744	9.4711407	10.5288593	10.0182256	10.547084931
30	9.4533418	9.9817370	9.4716048	10.5283952	10.0182630	10.546658230
	Sine.		Tang.		Secant.	Min.

73 Degrees.

Tangents and Secants.

16 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.4533418	9.9817370	9.4716048	10.5283952	10.0182630	10.546658230
31	9.4537681	9.9816995	9.4720685	10.5279315	10.0183005	10.546231929
32	9.4541939	9.9816620	9.4725318	10.5274682	10.0183380	10.545806128
33	9.4546192	9.9816245	9.4729947	10.5270053	10.0183755	10.545380827
34	9.4550441	9.9815870	9.4734571	10.5265428	10.0184130	10.544955526
35	9.4554686	9.9815494	9.4739192	10.5260808	10.0184506	10.544531425
36	9.4558926	9.9815117	9.4743808	10.5256192	10.0184883	10.544107424
37	9.4563161	9.9814740	9.4748421	10.5251579	10.0185260	10.543683923
38	9.4567392	9.9814363	9.4753029	10.5246971	10.0185637	10.543260822
39	9.4571618	9.9813986	9.4757633	10.5242367	10.0186014	10.542838221
40	9.4575840	9.9813608	9.4762233	10.5237767	10.0186392	10.542416020
41	9.4580058	9.9813229	9.4766829	10.5233171	10.0186771	10.541994219
42	9.4584271	9.9812850	9.4771421	10.5228579	10.0187150	10.541572918
43	9.4588480	9.9812471	9.4776009	10.5223991	10.0187529	10.541152017
44	9.4592684	9.9812091	9.4780592	10.5219408	10.0187909	10.540731616
45	9.4596884	9.9811711	9.4785172	10.5214828	10.0188289	10.540311615
46	9.4601079	9.9811331	9.4789748	10.5210251	10.0188669	10.539892114
47	9.4605270	9.9810950	9.4794319	10.5205681	10.0189050	10.539473013
48	9.4609456	9.9810569	9.4798887	10.5201113	10.0189431	10.539054412
49	9.4613638	9.9810187	9.4803451	10.5196549	10.0189813	10.538636211
50	9.4617816	9.9809805	9.4808011	10.5191989	10.0190195	10.538218410
51	9.4621989	9.9809423	9.4812566	10.5187434	10.0190578	10.53780119
52	9.4626158	9.9809040	9.4817118	10.5182882	10.0190960	10.53738428
53	9.4630323	9.9808657	9.4821666	10.5178334	10.0191343	10.53696777
54	9.4634483	9.9808273	9.4826210	10.5173790	10.0191727	10.53655176
55	9.4638639	9.9807889	9.4830750	10.5169250	10.0192111	10.53613615
56	9.4642790	9.9807505	9.4835286	10.5164714	10.0192495	10.53572104
57	9.4646938	9.9807120	9.4839818	10.5160182	10.0192880	10.53530623
58	9.4651081	9.9806735	9.4844346	10.5155654	10.0193265	10.53489192
59	9.4655219	9.9806349	9.4848870	10.5151130	10.0193651	10.53447811
60	9.4659353	9.9805963	9.4853390	10.5146610	10.0194037	10.53406470
		Sine.		Tang.		Secant.

74 Degrees.

A Table of Artificial Sines,

17 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.4659353	9.9805963	9.4853390	10.5146610	10.0194037	10.5340647 60
1	9.4663483	9.9805577	9.4857907	10.5142093	10.0194423	10.5336517 59
2	9.4667609	9.9805190	9.4862419	10.5137581	10.0194810	10.5332391 58
3	9.4671730	9.9804803	9.4866928	10.5133072	10.0195197	10.5328270 57
4	9.4675848	9.9804415	9.4871433	10.5128567	10.0195585	10.5324152 56
5	9.4679960	9.9804027	9.4875933	10.5124067	10.0195973	10.5320040 55
6	9.4684069	9.9803639	9.4880430	10.5119570	10.0196361	10.5315931 54
7	9.4688173	9.9803250	9.4884924	10.5115076	10.0196750	10.5311827 53
8	9.4692273	9.9802860	9.4889413	10.5110587	10.0197140	10.5307727 52
9	9.4696369	9.9802471	9.4893898	10.5106102	10.0197529	10.5303631 51
10	9.4700461	9.9802081	9.4898380	10.5101620	10.0197919	10.5299539 50
11	9.4704548	9.9801690	9.4902858	10.5097142	10.0198310	10.5295452 49
12	9.4708631	9.9801299	9.4907332	10.5092668	10.0198701	10.5291369 48
13	9.4712710	9.9800908	9.4911802	10.5088198	10.0199092	10.5287290 47
14	9.4716785	9.9800516	9.4916269	10.5083731	10.0199484	10.5283215 46
15	9.4720856	9.9800124	9.4920731	10.5079269	10.0199876	10.5279144 45
16	9.4724922	9.9799732	9.4925190	10.5074810	10.0200268	10.5275078 44
17	9.4728985	9.9799339	9.4929646	10.5070354	10.0200661	10.5271015 43
18	9.4733043	9.9798946	9.4934097	10.5065903	10.0201054	10.5266957 42
19	9.4737097	9.9798552	9.4938545	10.5061455	10.0201448	10.5262903 41
20	9.4741146	9.9798158	9.4942988	10.5057012	10.0201842	10.5258844 40
21	9.4745192	9.9797764	9.4947429	10.5052571	10.0202236	10.5254808 39
22	9.4749234	9.9797369	9.4951865	10.5048135	10.0202631	10.5250766 38
23	9.4753271	9.9796973	9.4956298	10.5043702	10.0203027	10.5246729 37
24	9.4757304	9.9796578	9.4960727	10.5039273	10.0203422	10.5242696 36
25	9.4761334	9.9796182	9.4965152	10.5034848	10.0203818	10.5238666 35
26	9.4765359	9.9795785	9.4969574	10.5030426	10.0204215	10.5234641 34
27	9.4769380	9.9795388	9.4973991	10.5026009	10.0204612	10.5230620 33
28	9.4773396	9.9794991	9.4978406	10.5021594	10.0205009	10.5226644 32
29	9.4777409	9.9794593	9.4982816	10.5017184	10.0205407	10.5222591 31
30	9.4781418	9.9794195	9.4987223	10.5012777	10.0205805	10.5218582 30
	Sine.		Tang.		Secant.	Min.

72 Degrees.

Tangents, and Secants.

17 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.4781418	9.9794195	9.4987223	10.5012777	10.0205805	10.5218582	30
31	9.4785423	9.9793796	9.4991626	10.5008374	10.0206204	10.5214577	29
32	9.4789423	9.9793398	9.4996026	10.5003974	10.0206602	10.5210577	28
33	9.4793420	9.9792998	9.5000422	10.4999578	10.0207002	10.5206580	27
34	9.4797412	9.9792599	9.5004814	10.4995186	10.0207462	10.5202586	26
35	9.4801401	9.9792198	9.5009203	10.4990997	10.0207802	10.5198599	25
36	9.4805385	9.9791798	9.5013588	10.4986412	10.0208202	10.5194615	24
37	9.4809360	9.9791397	9.5017969	10.4982031	10.0208603	10.5190634	23
38	9.4813342	9.9790996	9.5022347	10.4977653	10.0209004	10.5186653	22
39	9.4817315	9.9790594	9.5026721	10.4973279	10.0209406	10.5182685	21
40	9.4821283	9.9790192	9.5031092	10.4968908	10.0209808	10.5178717	20
41	9.4825248	9.9789789	9.5035459	10.4964541	10.0210211	10.5174752	19
42	9.4829208	9.9789388	9.5039822	10.4960178	10.0210614	10.5170792	18
43	9.4833165	9.9788983	9.5044182	10.4955818	10.0211017	10.5166835	17
44	9.4837117	9.9788579	9.5048538	10.4951462	10.0211421	10.5162883	16
45	9.4841066	9.9788175	9.5052891	10.4947109	10.0211825	10.5158934	15
46	9.4845010	9.9787770	9.5057240	10.4942760	10.0212230	10.5154990	14
47	9.4848951	9.9787365	9.5061586	10.4938414	10.0212635	10.5151049	13
48	9.4852888	9.9786960	9.5065928	10.4934072	10.0213040	10.5147112	12
49	9.4856820	9.9786554	9.5070267	10.4929733	10.0213446	10.5143180	11
50	9.4860749	9.9786148	9.5074602	10.4925398	10.0213852	10.5139251	10
51	9.4864674	9.9785741	9.5078933	10.4921067	10.0214259	10.5135326	9
52	9.4868595	9.9785334	9.5083261	10.4916739	10.0214666	10.5131405	8
53	9.4872512	9.9784927	9.5087586	10.4912414	10.0215073	10.5127488	7
54	9.4876426	9.9784519	9.5091907	10.4908093	10.0215481	10.5123574	6
55	9.4880335	9.9784111	9.5096224	10.4903776	10.0215889	10.5119665	5
56	9.4884240	9.9783702	9.5100539	10.4899461	10.0216298	10.5115760	4
57	9.4888142	9.9783293	9.5104849	10.4895151	10.0216707	10.5111858	3
58	9.4892040	9.9782883	9.5109156	10.4890844	10.0217117	10.5107960	2
59	9.4895934	9.9782474	9.5113460	10.4886540	10.0217526	10.5104066	1
60	9.4899824	9.9782063	9.5117760	10.4882240	10.0217937	10.5100176	0
		Sine.		Tang.		Secant.	Min.

72 Degrees.

A Table of Artificial Sines,

18 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.4899824	9.9782062	9.5117760	10.4882240	10.0217930	10.510017650
1	9.4903710	9.9781653	9.5122057	10.4877943	10.0218347	10.509629059
2	9.4907592	9.9781241	9.5126351	10.4873649	10.0218759	10.509240858
3	9.4911471	9.9780830	9.5130641	10.4869359	10.0219170	10.508852957
4	9.4915345	9.9780418	9.5134927	10.4865073	10.0219583	10.508465556
5	9.4919216	9.9780006	9.5139210	10.4860790	10.0219994	10.508078455
6	9.4923083	9.9779593	9.5143490	10.4856510	10.0220407	10.507691754
7	9.4926946	9.9779180	9.5147766	10.4852234	10.0220820	10.507305453
8	9.4930806	9.9778766	9.5152039	10.4847961	10.0221233	10.506919452
9	9.4934661	9.9778353	9.5156309	10.4843691	10.0221647	10.506533951
10	9.4938513	9.9777938	9.5160575	10.4839425	10.0222062	10.506148750
11	9.4942361	9.9777523	9.5164838	10.4835162	10.0222477	10.505763949
12	9.4946205	9.9777108	9.5169097	10.4830903	10.0222892	10.505379548
13	9.4950047	9.9776693	9.5173353	10.4826647	10.0223307	10.504995447
14	9.4953883	9.9776277	9.5177606	10.4822394	10.0223723	10.504611746
15	9.4957716	9.9775860	9.5181855	10.4818145	10.0224140	10.504228445
16	9.4961545	9.9775444	9.5186101	10.4813899	10.0224556	10.503845544
17	9.4965370	9.9775026	9.5190344	10.4809656	10.0224974	10.503463043
18	9.4969192	9.9774609	9.5194583	10.4805417	10.0225391	10.503080842
19	9.4973010	9.9774191	9.5198819	10.4801181	10.0225809	10.502699041
20	9.4976824	9.9773772	9.5203052	10.4796948	10.0226228	10.502317240
21	9.4980635	9.9773354	9.5207282	10.4792718	10.0226646	10.501936539
22	9.4984442	9.9772934	9.5211508	10.4788492	10.0227066	10.501555838
23	9.4988245	9.9772515	9.5215730	10.4784270	10.0227485	10.501175537
24	9.4992045	9.9772095	9.5219950	10.4780050	10.0227905	10.500795536
25	9.4995840	9.9771674	9.5224166	10.4775834	10.0228326	10.500416035
26	9.4999633	9.9771253	9.5228379	10.4771621	10.0228747	10.500036734
27	9.5003421	9.9770832	9.5232589	10.4767411	10.0229168	10.499657933
28	9.5007206	9.9770410	9.5236795	10.4763205	10.0229590	10.499279432
29	9.5010987	9.9769988	9.5240999	10.4759001	10.0230012	10.498901331
30	9.5014764	9.9769566	9.5245199	10.4754801	10.0230434	10.498523630
	Sine.		Tang.		Secant.	Min.

71 Degrees.

Tangents and Secants.

18 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.5014764	9.9769566	9.5245199	10.4754801	10.0230434	10.4985236	30
31	9.5018538	9.9769143	9.5249395	10.4750605	10.0230853	10.4981462	29
32	9.5022308	9.9768720	9.5253589	10.4746411	10.0231280	10.4977692	28
33	9.5026075	9.9768296	9.5257779	10.4742221	10.0231704	10.4973925	27
34	9.5029838	9.9767872	9.5261966	10.4738034	10.0232128	10.4970162	26
35	9.5033598	9.9767447	9.5266150	10.4733850	10.0232553	10.4966403	25
36	9.5037353	9.9767022	9.5270331	10.4729667	10.0232978	10.4962647	24
37	9.5041105	9.9766597	9.5274508	10.4725492	10.0233403	10.4958895	23
38	9.5044853	9.9766171	9.5278682	10.4721318	10.0233829	10.4955147	22
39	9.5048598	9.9765745	9.5282853	10.4717147	10.0234255	10.4951402	21
40	9.5052339	9.9765318	9.5287021	10.4712979	10.0234682	10.4947661	20
41	9.5056077	9.9764891	9.5291186	10.4708814	10.0235109	10.4943923	19
42	9.5059811	9.9764464	9.5295347	10.4704653	10.0235536	10.4940185	18
43	9.5063542	9.9764036	9.5299505	10.4700495	10.0235964	10.4936447	17
44	9.5067265	9.9763608	9.5303661	10.4696339	10.0236392	10.4932731	16
45	9.5070992	9.9763179	9.5307813	10.4692187	10.0236821	10.4929008	15
46	9.5074712	9.9762750	9.5311961	10.4688039	10.0237250	10.4925288	14
47	9.5078428	9.9762321	9.5316107	10.4683893	10.0237679	10.4921572	13
48	9.5082141	9.9761891	9.5320250	10.4679750	10.0238109	10.4917855	12
49	9.5085850	9.9761461	9.5324389	10.4675611	10.0238539	10.4914150	11
50	9.5089556	9.9761030	9.5328526	10.4671474	10.0238970	10.4910444	10
51	9.5093258	9.9760599	9.5332659	10.4667341	10.0239401	10.4906742	9
52	9.5096956	9.9760167	9.5336789	10.4663211	10.0239833	10.4903044	8
53	9.5100651	9.9759736	9.5340916	10.4659084	10.0240264	10.4899349	7
54	9.5104343	9.9759303	9.5345040	10.4654960	10.0240697	10.4895657	6
55	9.5108031	9.9758870	9.5349161	10.4650839	10.0241130	10.4891969	5
56	9.5111716	9.9758433	9.5353278	10.4646722	10.0241563	10.4888284	4
57	9.5115397	9.9758004	9.5357393	10.4642607	10.0241996	10.4884603	3
58	9.5119074	9.9757570	9.5361505	10.4638495	10.0242430	10.4880926	2
59	9.5122749	9.9757135	9.5365613	10.4634387	10.0242865	10.4877251	1
60	9.5126419	9.9756701	9.5369719	10.4630281	10.0243299	10.4873581	0
	Sine.		Tang.		Secant.		Min.

71 Degrees.

A Table of Artificial Sines,

19 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.5126419	9.9756701	9.5369719	10.4630281	10.0243299	10.4873581
1	9.5130086	9.9756265	9.5373821	10.4626179	10.0243735	10.4869914
2	9.5133750	9.9755830	9.5377920	10.4622080	10.0244170	10.4866250
3	9.5137410	9.9755394	9.5382017	10.4617983	10.0244606	10.4862590
4	9.5141067	9.9754957	9.5386110	10.4613809	10.0245043	10.4858933
5	9.5144721	9.9754521	9.5390200	10.4609800	10.0245479	10.4855279
6	9.5148371	9.9754083	9.5394287	10.4605713	10.0245917	10.4851629
7	9.5152017	9.9753646	9.5398371	10.4601629	10.0246354	10.4847983
8	9.5155060	9.9753208	9.5402453	10.4597547	10.0246792	10.4844340
9	9.5159300	9.9752769	9.5406534	10.4593469	10.0247231	10.4840700
10	9.5162936	9.9752330	9.5410605	10.4589394	10.0247670	10.4837064
11	9.5166569	9.9751891	9.5414678	10.4585322	10.0248109	10.4833431
12	9.5170198	9.9751451	9.5418747	10.4581253	10.0248549	10.4829802
13	9.5173824	9.9751011	9.5422813	10.4577187	10.0248989	10.4826176
14	9.5177447	9.9750570	9.5426877	10.4573123	10.0249430	10.4822553
15	9.5181066	9.9750129	9.5430937	10.4569063	10.0249871	10.4818934
16	9.5184682	9.9749688	9.5434994	10.4565006	10.0250312	10.4815318
17	9.5188295	9.9749246	9.5439048	10.4560952	10.0250754	10.4811705
18	9.5191904	9.9748804	9.5443100	10.4556900	10.0251196	10.4808096
19	9.5195510	9.9748361	9.5447148	10.4552852	10.0251639	10.4804490
20	9.5199112	9.9747918	9.5451193	10.4548807	10.0252082	10.4800888
21	9.5202711	9.9747475	9.5455236	10.4544764	10.0252525	10.4797289
22	9.5206307	9.9747031	9.5459276	10.4540724	10.0252969	10.4793693
23	9.5209899	9.9746587	9.5463312	10.4536688	10.0253412	10.4790101
24	9.5213488	9.9746142	9.5467346	10.4532654	10.0253858	10.4786512
25	9.5217074	9.9745697	9.5471377	10.4528623	10.0254303	10.4782926
26	9.5220656	9.9745252	9.5475405	10.4524594	10.0254748	10.4779344
27	9.5224235	9.9744806	9.5479430	10.4520570	10.0255194	10.4775765
28	9.5227811	9.9744359	9.5483452	10.4516548	10.0255641	10.4772189
29	9.5231383	9.9743913	9.5487471	10.4512529	10.0256087	10.4768617
30	9.5234953	9.9743465	9.5491487	10.4508513	10.0256534	10.4765047
	Sine.		Tang.		Secant.	Min.

70 Degrees.

Tan gents, and Secants.

19 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.5234953	9.9743466	9.5491487	10.4508513	10.0256534	10.4765047	30
31	9.5238518	9.9743018	9.5495500	10.4504500	10.0256982	10.4761482	29
32	9.5242081	9.9742570	9.5499511	10.4500489	10.0257430	10.4757919	28
33	9.5245640	9.9742122	9.5503519	10.4496481	10.0257878	10.4754360	27
34	9.5249196	9.9741664	9.5507523	10.4492477	10.0258327	10.4750804	26
35	9.5252749	9.9741224	9.5511525	10.4488475	10.0258776	10.4747251	25
36	9.5256298	9.9740774	9.5515524	10.4484476	10.0259226	10.4743702	24
37	9.5259844	9.9740324	9.5519524	10.4480479	10.0259676	10.4740156	23
38	9.5263387	9.9739873	9.5523514	10.4476486	10.0260127	10.4736613	22
39	9.5266927	9.9739422	9.5527504	10.4472496	10.0260578	10.4733073	21
40	9.5270463	9.9738971	9.5531492	10.4468506	10.0261029	10.4729537	20
41	9.5273997	9.9738519	9.5535477	10.4464523	10.0261481	10.4726003	19
42	9.5277526	9.9738067	9.5539459	10.4460541	10.0261933	10.4722474	18
43	9.5281053	9.9737615	9.5543438	10.4456562	10.0262385	10.4718947	17
44	9.5284577	9.9737162	9.5547415	10.4452585	10.0262838	10.4715423	16
45	9.5288097	9.9736709	9.5551388	10.4448612	10.0263291	10.4711903	15
46	9.5291614	9.9736255	9.5555359	10.4444641	10.0263745	10.4708386	14
47	9.5295128	9.9735801	9.5559327	10.4440673	10.0264199	10.4704872	13
48	9.5298638	9.9735346	9.5563292	10.4436708	10.0264654	10.4701362	12
49	9.5302146	9.9734891	9.5567255	10.4432745	10.0265109	10.4697854	11
50	9.5305650	9.9734435	9.5571214	10.4428786	10.0265565	10.4694350	10
51	9.5309151	9.9733980	9.5575171	10.4424829	10.0266020	10.4690849	9
52	9.5312649	9.9733523	9.5579125	10.4420875	10.0266477	10.4687351	8
53	9.5316143	9.9733067	9.5583077	10.4416923	10.0266933	10.4683857	7
54	9.5319635	9.9732610	9.5587025	10.4412975	10.0267390	10.4680365	6
55	9.5323123	9.9732152	9.5590971	10.4409029	10.0267848	10.4676877	5
56	9.5326608	9.9731694	9.5594914	10.4405086	10.0268306	10.4673392	4
57	9.5330090	9.9731236	9.5598854	10.4401146	10.0268764	10.4669910	3
58	9.5333569	9.9730777	9.5602792	10.4397608	10.0269223	10.4666431	2
59	9.5337244	9.9730318	9.5606727	10.4393273	10.0269682	10.4662956	1
60	9.5340517	9.9729858	9.5610659	10.4389029	10.0270142	10.4659483	0
	Sine.		Tang.		Secant.	Min.	

70 Degrees.

A Table of Artificial Sines,

20 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.5340517	9.9729858	9.5610650	10.4389341	10.0270142	10.4659483 60
1	9.5343986	9.9729398	9.5614588	10.4385412	10.0270602	10.4656014 59
2	9.5347452	9.9728938	9.5618515	10.4381485	10.0271062	10.4652548 58
3	9.5350915	9.9728477	9.5622439	10.4377561	10.0271523	10.4649085 57
4	9.5354375	9.9728016	9.5626360	10.4373640	10.0271984	10.4645625 56
5	9.5357832	9.9727554	9.5630278	10.4369722	10.0272446	10.4642168 55
6	9.5361286	9.9727092	9.5634194	10.4365806	10.0272908	10.4638714 54
7	9.5364737	9.9726629	9.5638107	10.4361893	10.0273371	10.4635263 53
8	9.5368184	9.9726166	9.5642018	10.4357982	10.0273834	10.4631816 52
9	9.5371628	9.9725703	9.5645925	10.4354075	10.0274297	10.4628372 51
10	9.5375070	9.9725339	9.5649831	10.4350169	10.0274761	10.4624930 50
11	9.5378508	9.9724775	9.5653733	10.4346267	10.0275225	10.4621492 49
12	9.5381943	9.9724310	9.5657633	10.4342367	10.0275690	10.4618057 48
13	9.5385375	9.9723845	9.5661530	10.4338470	10.0276155	10.4614625 47
14	9.5388804	9.9723380	9.5665424	10.4334576	10.0276620	10.4611196 46
15	9.5392230	9.9722914	9.5669316	10.4330684	10.0277086	10.4607770 45
16	9.5395653	9.9722448	9.5673205	10.4326725	10.0277552	10.4604347 44
17	9.5399073	9.9721981	9.5677091	10.4322909	10.0278019	10.4600927 43
18	9.5402489	9.9721514	9.5680975	10.4319025	10.0278486	10.4597511 42
19	9.5405903	9.9721047	9.5684856	10.4315144	10.0278952	10.4594097 41
20	9.5409314	9.9720579	9.5688735	10.4311265	10.0279421	10.4590686 40
21	9.5412721	9.9720110	9.5692611	10.4307389	10.0279890	10.4587279 39
22	9.5416126	9.9719642	9.5696484	10.4303516	10.0280358	10.4583874 38
23	9.5419527	9.9719172	9.5700355	10.4299645	10.0280828	10.4580473 37
24	9.5422926	9.9718703	9.5704223	10.4295777	10.0281297	10.4577074 36
25	9.5426321	9.9718233	9.5708088	10.4291912	10.0281767	10.4573679 35
26	9.5429713	9.9717762	9.5711951	10.4288049	10.0282238	10.4570287 34
27	9.5433103	9.9717291	9.5715811	10.4284189	10.0282709	10.4566897 33
28	9.5436489	9.9716820	9.5719669	10.4280331	10.0283180	10.4563511 32
29	9.5439873	9.9716348	9.5723524	10.4276476	10.0283652	10.4560127 31
30	9.5443253	9.9715876	9.5727377	10.4272623	10.0284124	10.4556747 30
	Sine.		Tang.		Secant.	Min.

69 Degrees.

Tangents, and Secants.

20 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.5443253	9.9715876	9.5727377	10.4272623	10.0284124	10.4556747 30
31	9.5440630	9.9715405	9.5731227	10.4268773	10.0284596	10.4553370 29
32	9.5450005	9.9714931	9.5735074	10.4264926	10.0285069	10.4549995 28
33	9.5453376	9.9714457	9.5738919	10.4261081	10.0285543	10.4546624 27
34	9.5456745	9.9713984	9.5742761	10.4257239	10.0286016	10.4543255 26
35	9.5460110	9.9713509	9.5746601	10.4253399	10.0286491	10.4539890 25
36	9.5463472	9.9713035	9.5750438	10.4249562	10.0286965	10.4536528 24
37	9.5466832	9.9712560	9.5754292	10.4245728	10.0287440	10.4533168 23
38	9.5470189	9.9712084	9.5758104	10.4241896	10.0287916	10.4529811 22
39	9.5473542	9.9711608	9.5761934	10.4238066	10.0288392	10.4526458 21
40	9.5476893	9.9711132	9.5765761	10.4234239	10.0288868	10.4523107 20
41	9.5480240	9.9710655	9.5769585	10.4230415	10.0289345	10.4519760 19
42	9.5483585	9.9710178	9.5773407	10.4226593	10.0289822	10.4516415 18
43	9.5486929	9.9709701	9.5777226	10.4222774	10.0290299	10.4513073 17
44	9.5490266	9.9709223	9.5781043	10.4218957	10.0290777	10.4509734 16
45	9.5493602	9.9708744	9.5784858	10.4215142	10.0291256	10.4506398 15
46	9.5496935	9.9708265	9.5788669	10.4211331	10.0291735	10.4503065 14
47	9.5500265	9.9707786	9.5792479	10.4207521	10.0292214	10.4499735 13
48	9.5503592	9.9707306	9.5796286	10.4203714	10.0292694	10.4496408 12
49	9.5506916	9.9706826	9.5800090	10.4199910	10.0293174	10.4493084 11
50	9.5510237	9.9706346	9.5803892	10.4196108	10.0293654	10.4489763 10
51	9.5513556	9.9705865	9.5807691	10.4192309	10.0294135	10.4486444 9
52	9.5516871	9.9705383	9.5811488	10.4188512	10.0294617	10.4483129 8
53	9.5520184	9.9704902	9.5815282	10.4184718	10.0295098	10.4479816 7
54	9.5523494	9.9704419	9.5819074	10.4180926	10.0295581	10.4476506 6
55	9.5526801	9.9703937	9.5822864	10.4177136	10.0296063	10.4473199 5
56	9.5530105	9.9703454	9.5826651	10.4173349	10.0296540	10.4469895 4
57	9.5533406	9.9702970	9.5830435	10.4169565	10.0297030	10.4466594 3
58	9.5536704	9.9702486	9.5834217	10.4165783	10.0297514	10.4463296 2
59	9.5539999	9.9702002	9.5837997	10.4162003	10.0297998	10.4460001 1
60	9.5543292	9.9701517	9.5841774	10.4158226	10.0298482	10.4456708 0
	Sine.		Tang.		Seca nt.	Min.

69 Degrees.

A Table of Artificial Sines,

21 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.5543292	9.9701517	9.5841774	10.4158226	10.0298485	10.4456708 60
1	9.5546581	9.9701032	9.5845549	10.4154451	10.0298968	10.4453419 59
2	9.5549868	9.9700547	9.5849321	10.4150679	10.0299453	10.4450132 58
3	9.5553152	9.9700061	9.5853098	10.4146909	10.0299939	10.4446848 57
4	9.5556433	9.9699574	9.5856859	10.4143141	10.0300426	10.4443567 56
5	9.5559711	9.9699087	9.5860624	10.4139376	10.0300913	10.4440289 55
6	9.5562987	9.9698600	9.5864386	10.4135614	10.0301400	10.4437013 54
7	9.5566259	9.9698112	9.5868147	10.4131853	10.0301888	10.4433741 53
8	9.5569529	9.9697624	9.5871904	10.4128096	10.0302376	10.4430471 52
9	9.5572796	9.9697136	9.5875660	10.4124340	10.0302864	10.4427204 51
10	9.5576061	9.9696647	9.5879413	10.4120587	10.0303353	10.4423940 50
11	9.5579321	9.9696158	9.5883163	10.4116837	10.0303842	10.4420679 49
12	9.5582579	9.9695668	9.5886912	10.4113088	10.0304332	10.4417421 48
13	9.5585839	9.9695177	9.5890657	10.4109343	10.0304823	10.4414165 47
14	9.5589088	9.9694687	9.5894401	10.4105599	10.0305313	10.4410912 46
15	9.5592338	9.9694196	9.5898142	10.4101858	10.0305804	10.4407662 45
16	9.5595585	9.9693704	9.5901881	10.4098119	10.0306296	10.4404415 44
17	9.5598829	9.9693212	9.5905617	10.4094383	10.0306788	10.4401171 43
18	9.5602071	9.9692720	9.5909351	10.4090649	10.0307280	10.4397929 42
19	9.5605310	9.9692227	9.5913082	10.4086918	10.0307773	10.4394690 41
20	9.5608546	9.9691734	9.5916812	10.4083188	10.0308266	10.4391454 40
21	9.5611779	9.9691240	9.5920539	10.4079461	10.0308759	10.4388221 39
22	9.5615010	9.9690746	9.5924263	10.4075737	10.0309254	10.4384990 38
23	9.5618237	9.9690252	9.5927985	10.4072015	10.0309748	10.4381763 37
24	9.5621462	9.9689757	9.5931705	10.4068295	10.0310243	10.4378538 36
25	9.5624685	9.9689262	9.5935423	10.4064577	10.0310738	10.4375315 35
26	9.5627904	9.9688766	9.5939138	10.4060862	10.0311234	10.4372096 34
27	9.5631121	9.9688270	9.5942851	10.4057149	10.0311730	10.4368879 33
28	9.5634335	9.9687773	9.5946561	10.4053439	10.0312227	10.4365665 32
29	9.5637546	9.9687276	9.5950269	10.4049731	10.0312724	10.4362454 31
30	9.5640754	9.9686779	9.5953975	10.4046025	10.0313221	10.4359246 30
	Sine.		Tang.		Secant.	Min.

68 Degrees.

Tangents and Secants.

21 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.5640754	9.9686779	9.5953975	10.4046025	10.0313221	10.4359240	30
31	9.5643960	9.9686281	9.5957679	10.4042321	10.0313719	10.4356040	29
32	9.5647163	9.9685783	9.5961380	10.4038620	10.0314217	10.4352837	28
33	9.5650363	9.9685284	9.5965079	10.4034921	10.0314716	10.4349637	27
34	9.5653561	9.9684785	9.5968776	10.4031224	10.0315215	10.4346434	26
35	9.5656756	9.9684286	9.5972470	10.4027530	10.0315714	10.4343244	25
36	9.5659948	9.9683786	9.5976162	10.4023838	10.0316214	10.4340052	24
37	9.5663137	9.9683285	9.5979852	10.4020148	10.0316715	10.4336863	23
38	9.5666324	9.9682784	9.5983540	10.4016460	10.0317216	10.4333676	22
39	9.5669508	9.9682283	9.5987225	10.4012775	10.0317717	10.4330492	21
40	9.5672689	9.9681781	9.5990908	10.4009092	10.0318219	10.4327311	20
41	9.5675868	9.9681279	9.5994588	10.4005412	10.0318721	10.4324132	19
42	9.5679044	9.9680777	9.5998267	10.4001733	10.0319223	10.4320956	18
43	9.5682217	9.9680274	9.6001943	10.3998057	10.0319726	10.4317783	17
44	9.5685387	9.9679771	9.6005617	10.3994383	10.0320229	10.4314613	16
45	9.5688555	9.9679267	9.6009289	10.3990711	10.0320733	10.4311445	15
46	9.5691721	9.9678763	9.6012958	10.3987042	10.0321237	10.4308279	14
47	9.5694883	9.9678258	9.6016625	10.3983375	10.0321742	10.4305117	13
48	9.5698043	9.9677753	9.6020290	10.3979710	10.0322247	10.4301957	12
49	9.5701200	9.9677247	9.6023953	10.3976047	10.0322753	10.4298800	11
50	9.5704355	9.9676741	9.6027613	10.3972387	10.0323259	10.4295645	10
51	9.5707506	9.9676235	9.6031271	10.3968729	10.0323765	10.4292494	9
52	9.5710656	9.9675728	9.6034927	10.3965073	10.0324272	10.4289348	8
53	9.5713802	9.9675221	9.6038581	10.3961419	10.0324779	10.4286198	7
54	9.5716946	9.9674713	9.6042233	10.3957767	10.0325287	10.4283054	6
55	9.5720087	9.9674205	9.6045882	10.3954118	10.0325795	10.4279913	5
56	9.5723226	9.9673698	9.6049529	10.3950471	10.0326303	10.4276774	4
57	9.5726362	9.9673188	9.6053174	10.3946826	10.0326812	10.4273638	3
58	9.5729495	9.9672679	9.6056817	10.3943183	10.0327321	10.4270505	2
59	9.5732626	9.9672169	9.6060457	10.3939543	10.0327831	10.4267374	1
60	9.5735754	9.9671659	9.6064096	10.3935904	10.0328341	10.4264246	0
	Sine.		Tang.		Secant.		Min.

68 Degrees.

A Table of Artificial Sines,

22 Degrees.

Min.	Sine.		Tang.		Secant.	
c	9.5735754	9.9671659	9.6064096	10.3935904	10.0328341	10.426424660
1	9.5738880	9.9671143	9.6067732	10.3932268	10.0328852	10.426112059
2	9.5742003	9.9670637	9.6071366	10.3928634	10.0329363	10.425799758
3	9.5745123	9.9670125	9.6074997	10.3925003	10.0329875	10.425487757
4	9.5748240	9.9669614	9.6078627	10.3921373	10.0330386	10.425176056
5	9.5751356	9.9669101	9.6082254	10.3917746	10.0330899	10.424864455
6	9.5754468	9.9668588	9.6085880	10.3914120	10.0331412	10.424553254
7	9.5757578	9.9668075	9.6089503	10.3910497	10.0331925	10.424242253
8	9.5760685	9.9667562	9.6093123	10.3906876	10.0332438	10.423931552
9	9.5763790	9.9667048	9.6096742	10.3903258	10.0332952	10.423621051
10	9.5766892	9.9666533	9.6100359	10.3899641	10.0333467	10.423310850
11	9.5769991	9.9666018	9.6103973	10.3896027	10.0333982	10.423000949
12	9.5773088	9.9665503	9.6107586	10.3892414	10.0334497	10.422691248
13	9.5776183	9.9664986	9.6111196	10.3888804	10.0335013	10.422381747
14	9.5779275	9.9664471	9.6114804	10.3885196	10.0335529	10.422072546
15	9.5782364	9.9663954	9.6118409	10.3881591	10.0336046	10.421763645
16	9.5785450	9.9663437	9.6122013	10.3877987	10.0336563	10.421455044
17	9.5788535	9.9662920	9.6125615	10.3874385	10.0337080	10.421146543
18	9.5791616	9.9662402	9.6129214	10.3870786	10.0337598	10.420838442
19	9.5794695	9.9661884	9.6132812	10.3867188	10.0338116	10.420530541
20	9.5797772	9.9661365	9.6136407	10.3863593	10.0338635	10.420222840
21	9.5800845	9.9660846	9.6140000	10.3860000	10.0339154	10.419915539
22	9.5803917	9.9660326	9.6143591	10.3856409	10.0339674	10.419608338
23	9.5806986	9.9659806	9.6147180	10.3852820	10.0340194	10.419301437
24	9.5810052	9.9659285	9.6150766	10.3849234	10.0340715	10.418994836
25	9.5813116	9.9658764	9.6154351	10.3845649	10.0341236	10.418688435
26	9.5816177	9.9658243	9.6157934	10.3842066	10.0341757	10.418382334
27	9.5819236	9.9657721	9.6161514	10.3838480	10.0342245	10.418076433
28	9.5822292	9.9657199	9.6165093	10.3834907	10.0342801	10.417770832
29	9.5825345	9.9656677	9.6168669	10.3831331	10.0343323	10.417465531
30	9.5828397	9.9656153	9.6172242	10.3827757	10.0343847	10.417160330
	Sine.		Tang.		Secant.	Min.

67 Degrees.

Tangents and Secants.

22 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.5828397	9.9656153	9.6172243	10.3827757	10.0343847	10.417160530
31	9.5831445	9.9655630	9.6175815	10.3824185	10.0344370	10.416855529
32	9.5834491	9.9655106	9.6179385	10.3820615	10.0344894	10.416550928
33	9.5837535	9.9654582	9.6182953	10.3817047	10.0345418	10.416246927
34	9.5840576	9.9654057	9.6186515	10.3813481	10.0345943	10.415942426
35	9.5843615	9.9653532	9.6190083	10.3809917	10.0346468	10.415638525
36	9.5846651	9.9653006	9.6193645	10.3806355	10.0346994	10.415334924
37	9.5849686	9.9652480	9.6197205	10.3802795	10.0347520	10.415031923
38	9.5852716	9.9651953	9.6200762	10.3799238	10.0348047	10.414728422
39	9.5855745	9.9651426	9.6204318	10.3795682	10.0348574	10.414425521
40	9.5858771	9.9650899	9.6207872	10.3792128	10.0349101	10.414122920
41	9.5861795	9.9650371	9.6211423	10.3788577	10.0349629	10.413820519
42	9.5864816	9.9649843	9.6214974	10.3785026	10.0350157	10.413518418
43	9.5867835	9.9649314	9.6218520	10.3781480	10.0350686	10.413216517
44	9.5870851	9.9648785	9.6222066	10.3777934	10.0351215	10.412914916
45	9.5873865	9.9648256	9.6225609	10.3774391	10.0351744	10.412613515
46	9.5876876	9.9647726	9.6229150	10.3770850	10.0352274	10.412312414
47	9.5879885	9.9647195	9.6232690	10.3767310	10.0352805	10.412011513
48	9.5882892	9.9646665	9.6236227	10.3763773	10.0353335	10.411710812
49	9.5885896	9.9646133	9.6239763	10.3760237	10.0353867	10.411410411
50	9.5888397	9.9645602	9.6243296	10.3756704	10.0354398	10.411110310
51	9.5891897	9.9645069	9.6246827	10.3753173	10.0354931	10.41081039
52	9.5894803	9.9644537	9.6250356	10.3749644	10.0355463	10.41051078
53	9.5897888	9.9644004	9.6253884	10.3746116	10.0355996	10.41021127
54	9.5900880	9.9643470	9.6257409	10.3742591	10.0356530	10.40991206
55	9.5903865	9.9642937	9.6260932	10.3739068	10.0357063	10.40961305
56	9.5906856	9.9642402	9.6264454	10.3735546	10.0357598	10.40931444
57	9.5909841	9.9641868	9.6267973	10.3732027	10.0358132	10.40901593
58	9.5912823	9.9641332	9.6271491	10.3728509	10.0358668	10.40871772
59	9.5915803	9.9640797	9.6275006	10.3724994	10.0359203	10.40841971
60	9.5918780	9.9640261	9.6278519	10.3721481	10.0359739	10.40812200
	Sine.		Tang.		Secant.	Min.

67 Degrees.

A Table of Artificial Sines,

23 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.5918780	9.9640261	9.6278319	10.3721481	10.0359739	10.4081220	60
1	9.5921755	9.9639724	9.6282031	10.3717969	10.0360276	10.4078245	59
2	9.5924728	9.9639187	9.6285540	10.3714460	10.0360813	10.4075272	58
3	9.5927698	9.9638650	9.6289048	10.3710952	10.0361350	10.4072302	57
4	9.5930666	9.9638112	9.6292553	10.3707447	10.0361888	10.4069334	56
5	9.5933661	9.9637574	9.6296057	10.3703943	10.0362426	10.4066369	55
6	9.5936594	9.9637036	9.6299558	10.3700442	10.0362964	10.4063406	54
7	9.5939555	9.9636496	9.6303058	10.3696942	10.0363504	10.4060445	53
8	9.5942513	9.9635957	9.6306556	10.3693444	10.0364043	10.4057487	52
9	9.5945469	9.9635417	9.6310052	10.3689948	10.0364583	10.4054531	51
10	9.5948422	9.9634877	9.6313542	10.3686455	10.0365123	10.4051578	50
11	9.5951373	9.9634336	9.6317037	10.3682963	10.0365664	10.4048627	49
12	9.5954322	9.9633795	9.6320527	10.3679473	10.0366205	10.4045678	48
13	9.5957268	9.9633253	9.6324015	10.3675985	10.0366747	10.4042732	47
14	9.5960212	9.9632711	9.6327501	10.3672499	10.0367289	10.4039788	46
15	9.5963154	9.9632168	9.6330985	10.3669015	10.0367832	10.4036846	45
16	9.5966093	9.9631625	9.6334468	10.3665532	10.0368375	10.4033907	44
17	9.5969030	9.9631082	9.6337948	10.3662052	10.0368918	10.4030970	43
18	9.5971965	9.9630538	9.6341426	10.3658574	10.0369462	10.4028035	42
19	9.5974897	9.9629994	9.6344903	10.3655097	10.0370006	10.4025103	41
20	9.5977827	9.9629449	9.6348378	10.3651622	10.0370551	10.4022173	40
21	9.5980754	9.9628904	9.6351850	10.3648150	10.0371096	10.4019246	39
22	9.5983680	9.9628358	9.6355321	10.3644679	10.0371642	10.4016321	38
23	9.5986602	9.9627812	9.6358790	10.3641210	10.0372188	10.4013398	37
24	9.5989523	9.9627266	9.6362257	10.3637743	10.0372734	10.4010477	36
25	9.5992441	9.9626719	9.6365722	10.3634278	10.0373281	10.4007559	35
26	9.5995357	9.9626172	9.6369185	10.3630815	10.0373828	10.4004643	34
27	9.5998270	9.9625624	9.6372646	10.3627354	10.0374376	10.4001730	33
28	9.6001181	9.9625076	9.6376106	10.3623894	10.0374924	10.3998819	32
29	9.6004090	9.9624527	9.6379563	10.3620437	10.0375473	10.3995910	31
30	9.6006997	9.9623978	9.6383019	10.3616981	10.0376022	10.3993003	30
		Sine.		Tang.		Secant.	Min.

66 Degrees.

Tangents, and Secants.

23 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.6006997	9.9623978	9.6383019	10.3616981	10.0376022	10.3993003	30
31	9.6009901	9.9623428	9.6386473	10.3613527	10.0376572	10.3990095	29
32	9.6012803	9.9622878	9.6389925	10.3610075	10.0377122	10.3987197	28
33	9.6015703	9.9622328	9.6393375	10.3606625	10.0377672	10.3984297	27
34	9.6018600	9.9621777	9.6396823	10.3603177	10.0378223	10.3981400	26
35	9.6021495	9.9621226	9.6400269	10.3599731	10.0378774	10.3978505	25
36	9.6024388	9.9620674	9.6403714	10.3596286	10.0379326	10.3975612	24
37	9.6027278	9.9620122	9.6407156	10.3592844	10.0379878	10.3972722	23
38	9.6030165	9.9619569	9.6410597	10.3589403	10.0380431	10.3969834	22
39	9.6033052	9.9619016	9.6414036	10.3585964	10.0380984	10.3966948	21
40	9.6035936	9.9618463	9.6417473	10.3582527	10.0381537	10.3964064	20
41	9.6038817	9.9617909	9.6420908	10.3579092	10.0382091	10.3961183	19
42	9.6041696	9.9617355	9.6424342	10.3575658	10.0382645	10.3958304	18
43	9.6044573	9.9616800	9.6427773	10.3572227	10.0383200	10.3955427	17
44	9.6047448	9.9616245	9.6431283	10.3568797	10.0383755	10.3952552	16
45	9.6050320	9.9615689	9.6434631	10.3565370	10.0384311	10.3949680	15
46	9.6053190	9.9615133	9.6438057	10.3561943	10.0384867	10.3946810	14
47	9.6056057	9.9614576	9.6441481	10.3558519	10.0385424	10.3943943	13
48	9.6058923	9.9614020	9.6444903	10.3555097	10.0385980	10.3941077	12
49	9.6061786	9.9613463	9.6448324	10.3551676	10.0386538	10.3938214	11
50	9.6064647	9.9612904	9.6451743	10.3548257	10.0387096	10.3935353	10
51	9.6067506	9.9612346	9.6455160	10.3544840	10.0387654	10.3932494	9
52	9.6070362	9.9611787	9.6458575	10.3541425	10.0388213	10.3929638	8
53	9.6073216	9.9611228	9.6461988	10.3538012	10.0388772	10.3926784	7
54	9.6076068	9.9610668	9.6465400	10.3534600	10.0389336	10.3923932	6
55	9.6078918	9.9610108	9.6468810	10.3531190	10.0389892	10.3921082	5
56	9.6081765	9.9609548	9.6472217	10.3527783	10.0390452	10.3918235	4
57	9.6084611	9.9608987	9.6475624	10.3524376	10.0391013	10.3915389	3
58	9.6087454	9.9608426	9.6479028	10.3520972	10.0391574	10.3912545	2
59	9.6090294	9.9607864	9.6482431	10.3517569	10.0392136	10.3909706	1
60	9.6093133	9.9607302	9.6485831	10.3514169	10.0392698	10.3906867	0
	Sine.		Tang.		Secant.		Min.

66 Degrees.

A Table of Artificial Sines,

24 Degrees.

Min.	Sine.		Tang.		Secant.		
	9.6093133	9.9607302	9.6485831	10.3514169	10.0392698	10.3906867	60
1	9.6095969	9.9606735	9.6489230	10.3510770	10.0393261	10.3904031	59
2	9.6098803	9.9606176	9.6492628	10.3507372	10.0393824	10.3901197	58
3	9.6101635	9.9605612	9.6496023	10.3503977	10.0394388	10.3898365	57
4	9.6104465	9.9605048	9.6499417	10.3500583	10.0394952	10.3895535	56
5	9.6107293	9.9604484	9.6502809	10.3497191	10.0395516	10.3892707	55
6	9.6110118	9.9603919	9.6506199	10.3493801	10.0396081	10.3889883	54
7	9.6112942	9.9603354	9.6509587	10.3490413	10.0396646	10.3887059	53
8	9.6115762	9.9602788	9.6512974	10.3487026	10.0397212	10.3884238	52
9	9.6118580	9.9602222	9.6516359	10.3483641	10.0397778	10.3881420	51
10	9.6121397	9.9601655	9.6519743	10.3480258	10.0398345	10.3878603	50
11	9.6124211	9.9601088	9.6523123	10.3476877	10.0398912	10.3875489	49
12	9.6127023	9.9600520	9.6526503	10.3473497	10.0399480	10.3872977	48
13	9.6129833	9.9599952	9.6529881	10.3470119	10.0400048	10.3870167	47
14	9.6132641	9.9599384	9.6533257	10.3466743	10.0400616	10.3867359	46
15	9.6135446	9.9598815	9.6536631	10.3463369	10.0401185	10.3864554	45
16	9.6138250	9.9598246	9.6540004	10.3459996	10.0401754	10.3861750	44
17	9.6141051	9.9597676	9.6543375	10.3456625	10.0402324	10.3858949	43
18	9.6143850	9.9597106	9.6546744	10.3453256	10.0402894	10.3856150	42
19	9.6146647	9.9596535	9.6550112	10.3449888	10.0403465	10.3853353	41
20	9.6149441	9.9595964	9.6553477	10.3446523	10.0404036	10.3850559	40
21	9.6152234	9.9595393	9.6556841	10.3443159	10.0404607	10.3847766	39
22	9.6155024	9.9594821	9.6560204	10.3439796	10.0405179	10.3844976	38
23	9.6157812	9.9594248	9.6563564	10.3436436	10.0405752	10.3842188	37
24	9.6160598	9.9593675	9.6566923	10.3433077	10.0406325	10.3839401	36
25	9.6163382	9.9593102	9.6570280	10.3429720	10.0406898	10.3836618	35
26	9.6166164	9.9592528	9.6573636	10.3426364	10.0407472	10.3833836	34
27	9.6168944	9.9591954	9.6576989	10.3423011	10.0408046	10.3831056	33
28	9.6171721	9.9591380	9.6580341	10.3419659	10.0408620	10.3828279	32
29	9.6174496	9.9590805	9.6583692	10.3416308	10.0409195	10.3825504	31
30	9.6177270	9.9590229	9.6587041	10.3412960	10.0409771	10.3822730	30
		Sine.		Tang		Secant.	Min.

65 Degrees.

Tangents, and Secants.

24 Degrees.

Mil.	Sine.		Tang.		Secant.	
30	9.6177270	9.9590229	9.6587041	10.3412960	10.0409771	10.3822730
31	9.6180041	9.9589653	9.6590387	10.3409613	10.0410347	10.3819959
32	9.6182809	9.9589077	9.6593733	10.3406267	10.0410923	10.3817191
33	9.6185576	9.9588500	9.6597076	10.3402924	10.0411500	10.3814424
34	9.6188341	9.9587923	9.6600418	10.3399582	10.0412077	10.3811659
35	9.6191103	9.9587345	9.6603758	10.3396242	10.0412655	10.3808897
36	9.6193864	9.9586767	9.6607097	10.3392903	10.0413233	10.3806136
37	9.6196622	9.9586188	9.6610434	10.3389560	10.0413812	10.3803378
38	9.6199378	9.9585609	9.6613769	10.3386231	10.0414391	10.3800622
39	9.6202132	9.9585030	9.6617103	10.3382897	10.0414970	10.3797868
40	9.6204884	9.9584450	9.6620434	10.3379566	10.0415550	10.3795116
41	9.6207634	9.9583869	9.6623765	10.3376235	10.0416131	10.3792366
42	9.6210382	9.9583288	9.6627093	10.3372907	10.0416712	10.3789618
43	9.6213127	9.9582707	9.6630420	10.3369580	10.0417293	10.3786873
44	9.6215871	9.9582125	9.6633745	10.3366255	10.0417875	10.3784129
45	9.6218612	9.9581543	9.6637065	10.3362931	10.0418457	10.3781388
46	9.6221351	9.9580961	9.6640391	10.3359609	10.0419039	10.3778649
47	9.6224088	9.9580378	9.6643711	10.3356289	10.0419622	10.3775912
48	9.6226824	9.9579794	9.6647030	10.3352970	10.0420206	10.3773176
49	9.6229557	9.9579210	9.6650346	10.3349654	10.0420790	10.3770443
50	9.6232287	9.9578626	9.6653662	10.3346338	10.0421374	10.3767713
51	9.6235016	9.9578041	9.6656975	10.3343025	10.0421959	10.3764984
52	9.6237743	9.9577456	9.6660288	10.3339712	10.0422544	10.3762257
53	9.6240468	9.9576870	9.6663598	10.3336402	10.0423130	10.3759532
54	9.6243190	9.9576284	9.6666907	10.3333093	10.0423716	10.3756810
55	9.6245911	9.9575697	9.6670214	10.3329786	10.0424303	10.3754089
56	9.6248629	9.9575110	9.6673519	10.3326481	10.0424890	10.3751371
57	9.6251346	9.9574522	9.6676823	10.3323177	10.0425478	10.3748654
58	9.6254060	9.9573934	9.6680126	10.3319874	10.0426066	10.3745940
59	9.6256772	9.9573346	9.6683426	10.3316574	10.0426654	10.3743228
60	9.6259483	9.9572757	9.6286725	10.3313275	10.0427243	10.3740517
	Sine		Tang.		Secant.	

65 Degrees.

A Table of Artificial Sines,

25 Degrees.

M.n.	Sine.		Tang.		Secant.		
C	9.6259483	9.9572757	9.6686725	10.3313275	10.0427243	10.3740517	50
1	9.6262191	9.9572168	9.6690023	10.3309977	10.0427832	10.3737809	59
2	9.6264897	9.9571578	9.6693319	10.3306681	10.0428422	10.3735103	58
3	9.6267901	9.9570988	9.6696613	10.3303387	10.0429012	10.3732399	57
4	9.6270308	9.9570397	9.6699906	10.3300094	10.0429603	10.3729697	56
5	9.6273003	9.9569806	9.6703197	10.3296803	10.0430194	10.3726997	55
6	9.6275701	9.9569215	9.6706486	10.3293514	10.0430785	10.3724299	54
7	9.6278397	9.9568623	9.6709774	10.3290226	10.0431377	10.3721603	53
8	9.6281090	9.9568030	9.6713060	10.3286940	10.0431970	10.3718910	52
9	9.6283782	9.9567437	9.6716345	10.3283655	10.0432563	10.3716218	51
10	9.6286472	9.9566844	9.6719628	10.3280372	10.0433156	10.3713528	50
11	9.6289160	9.9566250	9.6723920	10.3277090	10.0433750	10.3710840	49
12	9.6291845	9.9565656	9.6726190	10.3273810	10.0434344	10.3708155	48
13	9.6294529	9.9565061	9.6729468	10.3270632	10.0434939	10.3705471	47
14	9.6297211	9.9564466	9.6732745	10.3267255	10.0435534	10.3702789	46
15	9.6299890	9.9563870	9.6736020	10.3263980	10.0436130	10.3700110	45
16	9.6302568	9.9563274	9.6739294	10.3260706	10.0436726	10.3697432	44
17	9.6305243	9.9562678	9.6742566	10.3257434	10.0437322	10.3694757	43
18	9.6307917	9.9562081	9.6745836	10.3254164	10.0437919	10.3692082	42
19	9.6310589	9.9561483	9.6749109	10.3250895	10.0438517	10.3689411	41
20	9.6313258	9.9560886	9.6752372	10.3247628	10.0439114	10.3686742	40
21	9.6315926	9.9560287	9.6755638	10.3244362	10.0439713	10.3684074	39
22	9.6318591	9.9559689	9.6758903	10.3241097	10.0440311	10.3681409	38
23	9.6321255	9.9559089	9.6762165	10.3237835	10.0440911	10.3678746	37
24	9.6323916	9.9558490	9.6765426	10.3234574	10.0441510	10.3676084	36
25	9.6326576	9.9557890	9.6768686	10.3231314	10.0442110	10.3673424	35
26	9.6329233	9.9557289	9.6771944	10.3228056	10.0442711	10.3670767	39
27	9.6331889	9.9556688	9.6775201	10.3224799	10.0443312	10.3668111	34
28	9.6334542	9.9556087	9.6778456	10.3221544	10.0443913	10.3665454	32
29	9.6337294	9.9555485	9.6781709	10.3218291	10.0444515	10.3662806	31
30	9.6339844	9.9554882	9.6784961	10.3215039	10.0445118	10.3660155	30
	Sine.		Tang.		Secant.	M.n.	

64 Degrees.

Tangents and Secants.

25 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.6339844	9.9554882	9.6784961	10.3215039	10.0445118	10.3660156	30
31	9.6342491	9.9554280	9.6788211	10.3211789	10.0445720	10.3657509	29
32	9.6345137	9.9553676	9.6791460	10.3208540	10.0446324	10.3654863	28
33	9.6347780	9.9553073	9.6794708	10.3205292	10.0446927	10.3652220	27
34	9.6350422	9.9552489	9.6797953	10.3202047	10.0447531	10.3649578	26
35	9.6353062	9.9551864	9.6801198	10.3198802	10.0448136	10.3646938	25
36	9.6355699	9.9551259	9.6804440	10.3195560	10.0448741	10.3644301	24
37	9.6358335	9.9550653	9.6807682	10.3192318	10.0449347	10.3641665	23
38	9.6360969	9.9550047	9.6810921	10.3189079	10.0449953	10.3639031	22
39	9.6363601	9.9559441	9.6814160	10.3185840	10.0450559	10.3636399	21
40	9.6366231	9.9558834	9.6817396	10.3182604	10.0451166	10.3633709	20
41	9.6368859	9.9548227	9.6820632	10.3179368	10.0451773	10.3631141	19
42	9.6371484	9.9547619	9.6823865	10.3176135	10.0452381	10.3628516	18
43	9.6374108	9.9547011	9.6827098	10.3172902	10.0452989	10.3625892	17
44	9.6376731	9.9546402	9.6830328	10.3169672	10.0453598	10.3623269	16
45	9.6379351	9.9545793	9.6833557	10.3166443	10.0454207	10.3620649	15
46	9.6381969	9.9545184	9.6836785	10.3163215	10.0454816	10.3618031	14
47	9.6384585	9.9544574	9.6840011	10.3159989	10.0455426	10.3615415	13
48	9.6387199	9.9543963	9.6843236	10.3156764	10.0456037	10.3612801	12
49	9.6389812	9.9543352	9.6846459	10.3153541	10.0456648	10.3610188	11
50	9.6392422	9.9542741	9.6849681	10.3150319	10.0457259	10.3607578	10
51	9.6395030	9.9542129	9.6852901	10.3147099	10.0457871	10.3604970	9
52	9.6397639	9.9541517	9.6856120	10.3143880	10.0458483	10.3602363	8
53	9.6400241	9.9540904	9.6859338	10.3140662	10.0459096	10.3599759	7
54	9.6402844	9.9540291	9.6862553	10.3137447	10.0459709	10.3597156	6
55	9.6405445	9.9539677	9.6865768	10.3134232	10.0460323	10.3594555	5
56	9.6408044	9.9539063	9.6868961	10.3131019	10.0460937	10.3591956	4
57	9.6410640	9.9538448	9.6872192	10.3127808	10.0461552	10.3589360	3
58	9.6413235	9.9537833	9.6875402	10.3124598	10.0462167	10.3586765	2
59	9.6415828	9.9537218	9.6878611	10.3121389	10.0462782	10.3584172	1
60	9.6418420	9.9536602	9.6881818	10.3118182	10.0463398	10.3581580	0
	Sine.		Tang.		Secant.		Min.

64 Degrees.

A Table of Artificial Sines,

26 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.6418420	9.9536602	9.6881818	10.3118182	10.0463398	10.3581580
1	9.6421009	9.9535985	9.6885023	10.3114977	10.0464015	10.3578991
2	9.6423596	9.9535369	9.6888227	10.3111773	10.0464631	10.3576404
3	9.6426182	9.9534751	9.6891430	10.3108570	10.0465249	10.3573818
4	9.6428765	9.9534134	9.6894631	10.3105365	10.0465866	10.3571235
5	9.6431347	9.9533515	9.6897831	10.3102165	10.0466485	10.3568653
6	9.6433926	9.9532879	9.6901030	10.3098970	10.0467103	10.3566074
7	9.6436504	9.9532278	9.6904226	10.3095774	10.0467722	10.3563496
8	9.6439080	9.9531658	9.6907422	10.3092578	10.0468342	10.3560920
9	9.6441654	9.9531038	9.6910616	10.3089384	10.0468962	10.3558346
10	9.6444226	9.9530418	9.6913809	10.3086191	10.0469582	10.3555774
11	9.6446796	9.9529797	9.6917000	10.3083000	10.0470203	10.3553204
12	9.6449365	9.9529175	9.6920189	10.3079811	10.0470823	10.3550635
13	9.6451931	9.9528553	9.6923378	10.3076622	10.0471447	10.3548069
14	9.6454496	9.9527931	9.6926565	10.3073435	10.0472069	10.3545504
15	9.6457058	9.9527308	9.6929750	10.3070250	10.0472692	10.3542942
16	9.6459619	9.9526685	9.6932934	10.3067066	10.0473315	10.3540381
17	9.6462178	9.9526061	9.6936117	10.3063883	10.0473939	10.3537822
18	9.6464735	9.9525437	9.6939298	10.3060702	10.0474563	10.3535265
19	9.6467290	9.9524813	9.6942478	10.3057522	10.0475187	10.3532710
20	9.6469844	9.9524188	9.6945656	10.3054344	10.0475812	10.3530156
21	9.6472395	9.9523562	9.6948833	10.3051167	10.0476438	10.3527605
22	9.6474945	9.9522936	9.6952009	10.3047991	10.0477064	10.3525055
23	9.6477492	9.9522310	9.6955183	10.3044817	10.0477690	10.3522508
24	9.6480038	9.9521683	9.6958355	10.3041645	10.0478317	10.3519962
25	9.6482582	9.9521055	9.6961527	10.3038473	10.0478945	10.3517478
26	9.6485124	9.9520428	9.6964697	10.3035303	10.0479572	10.3514876
27	9.6487665	9.9519799	9.6967865	10.3032135	10.0480201	10.3512335
28	9.6490203	9.9519171	9.6971032	10.3028968	10.0480829	10.3509797
29	9.6492740	9.9518541	9.6974198	10.3025802	10.0481459	10.3507260
30	9.6495274	9.9517912	9.6977363	10.3022637	10.0482088	10.3504726
	Sine.		Tang.		Secant.	Min.

63 Degrees.

Tangents, and Secants.

26 Degrees.

Min.	Sine.		Targ.		Secant.	
30	9.6495274	9.9517912	9.6977363	10.3022637	10.0482088	10.3504726 30
31	9.6497807	9.9517282	9.6980526	10.3019474	10.0482718	10.3502193 29
32	9.6500338	9.9516651	9.6983687	10.3016313	10.0483349	10.3499662 28
33	9.6502868	9.9516020	9.6986847	10.3013153	10.0483980	10.3497132 27
34	9.6505395	9.9515389	9.6990006	10.3009994	10.0484611	10.3494605 26
35	9.6507920	9.9514757	9.6993164	10.3006836	10.0485243	10.3492080 25
36	9.6510444	9.9514124	9.6996320	10.3003680	10.0485876	10.3489556 24
37	9.6512966	9.9513492	9.6999474	10.3000526	10.0486508	10.3487034 23
38	9.6515486	9.9512858	9.7002628	10.2997372	10.0487142	10.3484514 22
39	9.6518004	9.9512224	9.7005780	10.2994220	10.0487776	10.3481996 21
40	9.6520521	9.9511590	9.7008930	10.2991070	10.0488410	10.3479479 20
41	9.6523035	9.9510956	9.7012080	10.2987920	10.0489044	10.3476965 19
42	9.6525548	9.9510320	9.7015227	10.2984773	10.0489680	10.3474452 18
43	9.6528059	9.9509685	9.7018374	10.2981626	10.0490315	10.3471941 17
44	9.6530568	9.9509049	9.7021519	10.2978481	10.0490951	10.3469432 16
45	9.6533075	9.9508412	9.7024663	10.2975337	10.0491588	10.3466925 15
46	9.6535581	9.9507775	9.7027805	10.2972195	10.0492225	10.3464419 14
47	9.6538084	9.9507138	9.7030946	10.2969054	10.0492862	10.3461916 13
48	9.6540586	9.9506500	9.7034086	10.2965914	10.0493500	10.3459414 12
49	9.6543086	9.9505861	9.7037225	10.2962775	10.0494139	10.3456914 11
50	9.6545584	9.9505223	9.7040362	10.2959638	10.0494777	10.3454416 10
51	9.6548081	9.9504583	9.7043497	10.2956503	10.0495417	10.3451919 9
52	9.6550575	9.9503944	9.7046632	10.2953368	10.0496056	10.3449425 8
53	9.6553068	9.9503303	9.7049765	10.2950235	10.0496697	10.3446932 7
54	9.6555559	9.9502663	9.7052897	10.2947103	10.0497337	10.3444441 6
55	9.6558048	9.9502022	9.7056027	10.2943973	10.0497978	10.3441952 5
56	9.6560536	9.9501380	9.7059156	10.2940844	10.0498620	10.3439464 4
57	9.6563021	9.9500738	9.7062284	10.2937716	10.0499262	10.3436979 3
58	9.6565505	9.9500095	9.7065410	10.2934590	10.0499905	10.3434495 2
59	9.6567987	9.9499452	9.7068535	10.2931465	10.0500548	10.3432013 1
60	9.6570468	9.9498809	9.7071659	10.2928341	10.0501191	10.3429532 0
	Sine		Tang.		Secant.	Min.

63 Degrees.

A Table of Artificial Sines,

27 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.6570468	9.9498809	9.7071659	10.2928341	10.0501191	10.3429532	50
1	9.6572946	9.9498165	9.7074781	10.2925219	10.0501835	10.3427054	59
2	9.6575423	9.9497521	9.7077902	10.2922098	10.0502479	10.3424577	58
3	9.6577898	9.9496876	9.7081022	10.2918978	10.0503124	10.3422102	57
4	9.6580371	9.9496230	9.7084141	10.2915857	10.0503770	10.3419629	56
5	9.6582842	9.9495585	9.7087258	10.2912742	10.0504415	10.3417158	55
6	9.6585312	9.9494938	9.7090374	10.2909626	10.0505062	10.3414688	54
7	9.6587780	9.9494292	9.7093488	10.2906512	10.0505708	10.3412220	53
8	9.6590246	9.9493645	9.7096601	10.2903399	10.0506355	10.3409754	52
9	9.6592710	9.9492997	9.7099713	10.2900287	10.0507003	10.3407290	51
10	9.6595173	9.9492349	9.7102824	10.2897186	10.0507651	10.3404827	50
11	9.6597634	9.9491700	9.7105933	10.2894067	10.0508300	10.3402367	49
12	9.6600093	9.9491051	9.7109041	10.2890959	10.0508949	10.3399907	48
13	9.6602550	9.9490402	9.7112148	10.2887852	10.0509598	10.3397450	47
14	9.6605005	9.9489752	9.7115254	10.2884746	10.0510248	10.3394995	46
15	9.6607459	9.9489101	9.7118358	10.2881642	10.0510899	10.3392541	45
16	9.6609911	9.9488450	9.7121461	10.2878539	10.0511550	10.3390089	44
17	9.6612361	9.9487799	9.7124562	10.2875438	10.0512201	10.3387639	43
18	9.6614810	9.9487147	9.7127662	10.2872338	10.0512853	10.3385190	42
19	9.6617257	9.9486495	9.7130761	10.2869239	10.0513505	10.3382743	41
20	9.6619701	9.9485842	9.7133859	10.2866141	10.0514158	10.3380298	40
21	9.6622145	9.9485189	9.7136956	10.2863045	10.0514811	10.3377855	39
22	9.6624586	9.9484535	9.7140051	10.2859949	10.0515465	10.3375414	38
23	9.6627026	9.9483881	9.7143145	10.2856855	10.0516119	10.3372974	37
24	9.6629464	9.9483227	9.7146237	10.2853763	10.0516773	10.3370536	36
25	9.6631900	9.9482572	9.7149329	10.2850671	10.0517428	10.3368100	35
26	9.6634335	9.9481917	9.7152419	10.2847581	10.0518084	10.3365665	34
27	9.6636768	9.9481260	9.7155508	10.2844492	10.0518740	10.3363232	33
28	9.6639199	9.9480604	9.7158595	10.2841405	10.0519396	10.3360801	32
29	9.6641628	9.9479947	9.7161682	10.2838318	10.0520053	10.3358372	31
30	9.6644056	9.9479289	9.7164757	10.2835233	10.0520711	10.3355944	30
	Sine.		Tang.		Secant.		Min.

62 Degrees.

Tangents and Secants.

27 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.6644056	9.9479289	9.7164767	10.2835233	10.0520711	10.3355944	30
31	9.6646482	9.9478631	9.7167851	10.2832149	10.0521366	10.3353518	29
32	9.6648906	9.9477973	9.7170933	10.2829067	10.0522027	10.3351094	28
33	9.6651329	9.9477314	9.7174014	10.2825986	10.0522686	10.3348671	27
34	9.6653749	9.9476655	9.7177094	10.2822906	10.0523345	10.3346251	26
35	9.6656168	9.9475995	9.7180173	10.2819827	10.0524005	10.3343832	25
36	9.6658586	9.9475335	9.7183251	10.2816749	10.0524665	10.3341414	24
37	9.6661001	9.9474674	9.7186327	10.2813673	10.0525326	10.3338999	23
38	9.6663415	9.9474013	9.7189402	10.2810598	10.0525987	10.3336585	22
39	9.6665828	9.9473352	9.7192476	10.2807514	10.0526648	10.3334172	21
40	9.6668238	9.9472689	9.7195549	10.2804451	10.0527311	10.3331762	20
41	9.6670647	9.9472027	9.7198620	10.2801380	10.0527973	10.3329353	19
42	9.6673054	9.9471364	9.7201690	10.2798309	10.0528636	10.3326946	18
43	9.6675459	9.9470700	9.7204759	10.2795241	10.0529300	10.3324541	17
44	9.6677863	9.9470036	9.7207827	10.2792173	10.0529964	10.3322137	16
45	9.6680265	9.9469372	9.7210893	10.2789107	10.0530628	10.3319735	15
46	9.6682665	9.9468707	9.7213958	10.2786042	10.0531293	10.3317335	14
47	9.6685064	9.9468042	9.7217022	10.2782978	10.0531958	10.3314936	13
48	9.6687461	9.9467376	9.7220085	10.2779915	10.0532624	10.3312539	12
49	9.6689856	9.9466710	9.7223147	10.2776853	10.0533290	10.3310144	11
50	9.6692250	9.9466043	9.7226207	10.2773793	10.0533957	10.3307750	10
51	9.6694642	9.9465336	9.7229276	10.2770734	10.0534624	10.3305358	9
52	9.6697032	9.9464708	9.7232324	10.2767676	10.0535292	10.3302968	8
53	9.6699420	9.9464040	9.7235381	10.2764619	10.0535960	10.3300580	7
54	9.6701807	9.9463371	9.7238436	10.2761564	10.0536629	10.3298193	6
55	9.6704192	9.9462702	9.7241490	10.2758510	10.0537298	10.3295808	5
56	9.6706576	9.9462032	9.7244543	10.2755457	10.0537968	10.3293424	4
57	9.6708958	9.9461362	9.7247595	10.2752405	10.0538638	10.3291042	3
58	9.6711338	9.9460692	9.7250646	10.2749354	10.0539308	10.3288662	2
59	9.6713716	9.9460021	9.7253695	10.2746305	10.0539979	10.3286284	1
60	9.6716093	9.9459349	9.7256744	10.2743256	10.0540551	10.3283907	0
		Sine.		Tang.		Secant.	Min.

66 Degrees.

A Table of Artificial Sines,

28 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.6716093	9.9459349	9.7256744	10.2743256	10.0540651	10.3283907 60
1	9.6718468	9.9458677	9.7259791	10.2740209	10.0541323	10.3281532 59
2	9.6720841	9.9458005	9.7262836	10.2737163	10.0541995	10.3279159 58
3	9.6723213	9.9457332	9.7265881	10.2734119	10.0542668	10.3276787 57
4	9.6725583	9.9456659	9.7268925	10.2731075	10.0543341	10.3274417 56
5	9.6727952	9.9455985	9.7271967	10.2728033	10.0544015	10.3272048 55
6	9.6730319	9.9455310	9.7275008	10.2724992	10.0544690	10.3269681 54
7	9.6732684	9.9454636	9.7278048	10.2721952	10.0545364	10.3267316 53
8	9.6735047	9.9453960	9.7281087	10.2718913	10.0546040	10.3264953 52
9	9.6737409	9.9453285	9.7284124	10.2715876	10.0546715	10.3262591 51
10	9.6739769	9.9452609	9.7287161	10.2712839	10.0547391	10.3260231 50
11	9.6742128	9.9451932	9.7290196	10.2709804	10.0548068	10.3257872 49
12	9.6744485	9.9451255	9.7293230	10.2706770	10.0548745	10.3255515 48
13	9.6746840	9.9450577	9.7296263	10.2703737	10.0549423	10.3253160 47
14	9.6749194	9.9449899	9.7299295	10.2700705	10.0550101	10.3250806 46
15	9.6751546	9.9449220	9.7302325	10.2697675	10.0550780	10.3248454 45
16	9.6753896	9.9448541	9.7305354	10.2694646	10.0551459	10.3246104 44
17	9.6756245	9.9447862	9.7308383	10.2691617	10.0552138	10.3243756 43
18	9.6758592	9.9447182	9.7311410	10.2688590	10.0552818	10.3241408 42
19	9.6760937	9.9446501	9.7314436	10.2685564	10.0553499	10.3239063 41
20	9.6763281	9.9445821	9.7317460	10.2682540	10.0554179	10.3236719 40
21	9.6765623	9.9445139	9.7320484	10.2679516	10.0554861	10.3234377 39
22	9.6767963	9.9444457	9.7323506	10.2676494	10.0555543	10.3232037 38
23	9.6770302	9.9443775	9.7326527	10.2673473	10.0556225	10.3229698 37
24	9.6772640	9.9443092	9.7329547	10.2670453	10.0556908	10.3227360 36
25	9.6774975	9.9442409	9.7332566	10.2667434	10.0557591	10.3225025 35
26	9.6777309	9.9441725	9.7335584	10.2664416	10.0558275	10.3222691 34
27	9.6779642	9.9441042	9.7338601	10.2661399	10.0558959	10.3220358 33
28	9.6781972	9.9440356	9.7341616	10.2658384	10.0559644	10.3218028 32
29	9.6784301	9.9439671	9.7344631	10.2655369	10.0560329	10.3215699 31
30	9.6786629	9.9438985	9.7347644	10.2652356	10.0561015	10.3213371 30
	Sine.		Tang.		Secant.	n.

61 Degrees.

nts, and Secants.

28 Degrees.

Min.	Sine.	Tang.	Secant.	Min.			
30	9.6786629	9.9438985	9.7347644	10.2652356	10.0561019	10.3213371	30
31	9.6788955	9.9438295	9.7350656	10.2649344	10.0561708	10.3211045	29
32	9.6791279	9.9437612	9.7353667	10.2646333	10.0562388	10.3208721	28
33	9.6793602	9.9436925	9.7356677	10.2643323	10.0563079	10.3206398	27
34	9.6795923	9.9436238	9.7359689	10.2640313	10.0563762	10.3204077	26
35	9.6798243	9.9435549	9.7362699	10.2637307	10.0564451	10.3201757	25
36	9.6800560	9.9434862	9.7365699	10.2634301	10.0565139	10.3199440	24
37	9.6802877	9.9434172	9.7368705	10.2631295	10.0565828	10.3197123	23
38	9.6805191	9.9433482	9.7371709	10.2628291	10.0566518	10.3194809	22
39	9.6807504	9.9432792	9.7374712	10.2625288	10.0567208	10.3192486	21
40	9.6809816	9.9432102	9.7377714	10.2622286	10.0567898	10.3190184	20
41	9.6812126	9.9431413	9.7380715	10.2619285	10.0568589	10.3187874	19
42	9.6814434	9.9430720	9.7383714	10.2616286	10.0569280	10.3185566	18
43	9.6816741	9.9430028	9.7386713	10.2613287	10.0569972	10.3183259	17
44	9.6819046	9.9429335	9.7389710	10.2610290	10.0570665	10.3180954	16
45	9.6821349	9.9428643	9.7392707	10.2607293	10.0571357	10.3178651	15
46	9.6823651	9.9427949	9.7395702	10.2604298	10.0572051	10.3176349	14
47	9.6825952	9.9427255	9.7398696	10.2601304	10.0572745	10.3174048	13
48	9.6828250	9.9426561	9.7401689	10.2598311	10.0573439	10.3171750	12
49	9.6830548	9.9425866	9.7404681	10.2595319	10.0574134	10.3169452	11
50	9.6832843	9.9425171	9.7407672	10.2592328	10.0574829	10.3167157	10
51	9.6835137	9.9424476	9.7410662	10.2589338	10.0575524	10.3164863	9
52	9.6837430	9.9423779	9.7413650	10.2586350	10.0576221	10.3162570	8
53	9.6839720	9.9423083	9.7416638	10.2583362	10.0576917	10.3160280	7
54	9.6842010	9.9422386	9.7419624	10.2580376	10.0577614	10.3157990	6
55	9.6844297	9.9421688	9.7422609	10.2577391	10.0578312	10.3155703	5
56	9.6846583	9.942099	9.7425594	10.2574406	10.0579010	10.3153417	4
57	9.6848868	9.9420291	9.7428577	10.2571403	10.0579709	10.3151132	3
58	9.6851151	9.9419592	9.7431559	10.2568441	10.0580408	10.3148845	2
59	9.6853432	9.9418893	9.7434540	10.2565460	10.0581107	10.3146568	1
60	9.6855712	9.9418195	9.7437520	10.2562480	10.0581807	10.3144288	0
	Sine.	Tang.	Secant.	Min.			

61 Degrees.

61 Degrees.

A Table of Artificial Sines,

29 Degrees.

M.in.	Sine.	Tang.	Secant.				
0	9.6855712	9.9418193	9.7437520	10.2562480	10.0581807	10.3144288	60
1	9.6857991	9.9417492	9.7440499	10.2559501	10.0582508	10.3142009	59
2	9.6860267	9.9416791	9.7443476	10.2556521	10.0583209	10.3139733	58
3	9.6862542	9.9416090	9.7446453	10.2553542	10.0583910	10.3137458	57
4	9.6864816	9.9415388	9.7449428	10.2550572	10.0584612	10.3135184	56
5	9.6867088	9.9414685	9.7452403	10.2547597	10.0585315	10.3132912	55
6	9.6869359	9.9413982	9.7455376	10.2544624	10.0586018	10.3130641	54
7	9.6871628	9.9413297	9.7458349	10.2541651	10.0586721	10.3128372	53
8	9.6873895	9.9412575	9.7461320	10.2538680	10.0587425	10.3126105	52
9	9.6876161	9.9411871	9.7464290	10.2535700	10.0588129	10.3123839	51
10	9.6878425	9.9411166	9.7467259	10.2532741	10.0588834	10.3121575	50
11	9.6880688	9.9410461	9.7470227	10.2529773	10.0589539	10.3119312	49
12	9.6882949	9.9409755	9.7473194	10.2526806	10.0590245	10.3117051	48
13	9.6885209	9.9409048	9.7476160	10.2523840	10.0590952	10.3114791	47
14	9.6887467	9.9408342	9.7479125	10.2520875	10.0591658	10.3112533	46
15	9.6889723	9.9407634	9.7482089	10.2517911	10.0592366	10.3110277	45
16	9.6891978	9.9406927	9.7485052	10.2514948	10.0593073	10.3108022	44
17	9.6894232	9.9406219	9.7488013	10.2511987	10.0593781	10.3105768	43
18	9.6896484	9.9405510	9.7490974	10.2509026	10.0594490	10.3103516	42
19	9.6898734	9.9404801	9.7493934	10.2506066	10.0595199	10.3101266	41
20	9.6900983	9.9404091	9.7496892	10.2503108	10.0595909	10.3099017	40
21	9.6903231	9.9403381	9.7499850	10.2500150	10.0596619	10.3096769	39
22	9.6905476	9.9402670	9.7502806	10.2497194	10.0597330	10.3094524	38
23	9.6907721	9.9401959	9.7505762	10.2494238	10.0598041	10.3092279	37
24	9.6909964	9.9401248	9.7508716	10.2491284	10.0598752	10.3090036	36
25	9.6912205	9.9400535	9.7511669	10.2488331	10.0599463	10.3087795	35
26	9.6914445	9.9399823	9.7514622	10.2485378	10.0600177	10.3085555	34
27	9.6916683	9.9399110	9.7517573	10.2482427	10.0600890	10.3083317	33
28	9.6918919	9.9398396	9.7520523	10.2479477	10.0601604	10.3081081	32
29	9.6921155	9.9397681	9.7523472	10.2476528	10.0602318	10.3078845	31
30	9.6923388	9.9396958	9.7526420	10.2473580	10.0603032	10.3076612	30
	Sine	Tang.	Secant.	Min.			

60 Degrees.

Tangents and Secants.

29 Degrees.

Min.	Sine.	Tang.	Secant.	
30	9.6923388	9.9396968	9.7526420	10.2473580
31	9.6923620	9.9396753	9.7529368	10.2470632
32	9.6923781	9.9396557	9.7532314	10.2467686
33	9.6923908	9.9396321	9.7535259	10.2464741
34	9.6924008	9.9396105	9.7538203	10.2461797
35	9.6924134	9.9395888	9.7541146	10.2458854
36	9.6924258	9.9395671	9.7544088	10.2455912
37	9.6924381	9.9395453	9.7547029	10.2452971
38	9.6924483	9.9395234	9.7549969	10.2450031
39	9.6924564	9.9395015	9.7552908	10.2447091
40	9.6924642	9.9394796	9.7555846	10.2444145
41	9.6924718	9.9394576	9.7558783	10.2441217
42	9.6924794	9.9394356	9.7561718	10.2438282
43	9.6924868	9.9394135	9.7564653	10.2435347
44	9.6924940	9.9393914	9.7567587	10.2432413
45	9.6925012	9.9393692	9.7570520	10.2429480
46	9.6925082	9.9393470	9.7573452	10.2426548
47	9.6925150	9.9393247	9.7576383	10.2423617
48	9.6925218	9.9393024	9.7579313	10.2420687
49	9.6925284	9.9392800	9.7582242	10.2417758
50	9.6925349	9.9392576	9.7585170	10.2414830
51	9.6925413	9.9392351	9.7588096	10.2411904
52	9.6925476	9.9392127	9.7591022	10.2408978
53	9.6925538	9.9391900	9.7593947	10.2406053
54	9.6925599	9.9391674	9.7596871	10.2403129
55	9.6925659	9.9391447	9.7599794	10.2400206
56	9.6925718	9.9391220	9.7602716	10.2397284
57	9.6925776	9.9390992	9.7605637	10.2394363
58	9.6925833	9.9390764	9.7608557	10.2391443
59	9.6925889	9.9390535	9.7611476	10.2388524
60	9.6925944	9.9390306	9.7614394	10.2385606
	Sine.	Tang.	Secant.	Min.

60 Degrees.

A Table of Artificial Sines,

30 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.6989700	9.9375306	9.7614394	10.2385606	10.0624694	10.3010300	50
1	9.6991887	9.9374577	9.7617311	10.2382689	10.0625423	10.3008113	59
2	9.6994073	9.9373847	9.7620227	10.2379793	10.0626153	10.3005927	58
3	9.6996258	9.9373116	9.7623142	10.2376858	10.0626884	10.3003742	57
4	9.6998441	9.9372385	9.7626056	10.2373944	10.0627615	10.3001559	56
5	9.7000622	9.9371653	9.7628969	10.2371031	10.0628347	10.2999378	55
6	9.7002802	9.9370921	9.7631881	10.2368119	10.0629079	10.2997198	54
7	9.7004981	9.9370189	9.7634792	10.2365208	10.0629811	10.2995019	53
8	9.7007158	9.9369456	9.7637702	10.2362298	10.0630544	10.2992842	52
9	9.7009334	9.9368722	9.7640612	10.2359388	10.0631278	10.2990666	51
10	9.7011508	9.9367988	9.7643520	10.2356480	10.0632012	10.2988492	50
11	9.7013681	9.9367254	9.7646427	10.2353573	10.0632746	10.2986315	49
12	9.7015852	9.9366519	9.7649334	10.2350666	10.0633481	10.2984148	48
13	9.7018022	9.9365783	9.7652239	10.2347761	10.0634217	10.2981978	47
14	9.7020190	9.9365047	9.7655143	10.2344857	10.0634953	10.2979810	46
15	9.7022357	9.9364311	9.7658047	10.2341953	10.0635689	10.2977663	45
16	9.7024523	9.9363574	9.7660949	10.2339051	10.0636426	10.2975477	44
17	9.7026687	9.9362836	9.7663851	10.2336149	10.0637164	10.2973313	43
18	9.7028849	9.9362098	9.7666751	10.2333249	10.0637902	10.2971151	42
19	9.7031011	9.9361360	9.7669651	10.2330349	10.0638640	10.2968989	41
20	9.7033170	9.9360621	9.7672550	10.2327450	10.0639379	10.2966830	40
21	9.7035329	9.9359881	9.7675448	10.2324552	10.0640116	10.2964671	39
22	9.7037486	9.9359141	9.7678344	10.2321656	10.0640859	10.2962514	38
23	9.7039641	9.9358403	9.7681240	10.2318760	10.0641599	10.2960359	37
24	9.7041795	9.9357666	9.7684135	10.2315865	10.0642340	10.2958205	36
25	9.7043947	9.9356918	9.7687029	10.2312971	10.0643082	10.2956052	35
26	9.7046099	9.9356177	9.7689922	10.2310078	10.0643823	10.2953901	34
27	9.7048248	9.9355434	9.7692814	10.2307186	10.0644566	10.2951752	33
28	9.7050397	9.9354691	9.7695705	10.2304295	10.0645309	10.2949603	32
29	9.7052543	9.9353948	9.7698596	10.2301404	10.0646052	10.2947457	31
30	9.7054689	9.9353204	9.7701485	10.2298515	10.0646796	10.2945311	30
	Sine.		Tang.		Secant.	Min.	

59 Degrees.

Tangents, and Secants.

30 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
30	9.705468	9.9353204	9.7701485	10.2298515	10.0646796	10.2945311	30
31	9.705683	9.9352455	9.7704373	10.2295627	10.0647541	10.2943167	29
32	9.705875	9.9351719	9.7707261	10.2292739	10.0648285	10.2941023	28
33	9.706116	9.9350966	9.7710147	10.2289853	10.0649031	10.2938884	27
34	9.7063256	9.9350223	9.7713033	10.2286967	10.0649777	10.2936744	26
35	9.7065394	9.9349477	9.7715917	10.2284083	10.0650523	10.2934606	25
36	9.7067531	9.9348730	9.7718801	10.2281199	10.0651270	10.2932469	24
37	9.7069667	9.9347983	9.7721684	10.2278316	10.0652017	10.2930333	23
38	9.7071801	9.9347235	9.7724566	10.2275434	10.0652765	10.2928199	22
39	9.7073933	9.9346486	9.7727447	10.2272553	10.0653514	10.2926067	21
40	9.7076064	9.9345738	9.7730327	10.2269673	10.0654262	10.2923936	20
41	9.7078194	9.9344988	9.7733206	10.2266794	10.0655012	10.2921806	19
42	9.7080323	9.9344238	9.7736084	10.2263916	10.0655762	10.2919677	18
43	9.7082450	9.9343488	9.7738961	10.2261039	10.0656512	10.2917550	17
44	9.7084575	9.9342737	9.7741838	10.2258162	10.0657263	10.2915425	16
45	9.7086699	9.9341986	9.7744713	10.2255282	10.0658014	10.2913301	15
46	9.7088822	9.9341234	9.7747588	10.2252412	10.0658766	10.2911178	14
47	9.7090943	9.9340482	9.7750462	10.2249538	10.0659518	10.2909057	13
48	9.7093063	9.9339728	9.7753334	10.2246666	10.0660271	10.2906937	12
49	9.7095182	9.9338976	9.7756206	10.2243794	10.0661024	10.2904818	11
50	9.7097299	9.9338222	9.7759077	10.2240923	10.0661778	10.2902701	10
51	9.7099415	9.9337467	9.7761947	10.2238053	10.0662532	10.2900585	9
52	9.7101529	9.9336713	9.7764816	10.2235184	10.0663287	10.2898471	8
53	9.7103642	9.9335957	9.7767685	10.2232315	10.0664043	10.2896358	7
54	9.7105753	9.9335201	9.7770552	10.2229448	10.0664799	10.2894247	6
55	9.7107863	9.9334445	9.7773418	10.2226582	10.0665555	10.2892137	5
56	9.7109972	9.9333688	9.7776284	10.2223716	10.0666312	10.2890028	4
57	9.7112080	9.9332931	9.7779149	10.2220851	10.0667069	10.2887920	3
58	9.7114186	9.9332173	9.7782012	10.2217988	10.0667827	10.2885814	2
59	9.7116290	9.9331415	9.7784875	10.2215125	10.0668585	10.2883710	1
60	9.7118393	9.9330658	9.7787737	10.2212263	10.0669344	10.2881607	0
	Sine.		Tang.		Secant.		

59 Degrees.

A Table of Artificial Sines,

3. Degrees.

Min.	Sine.	Tang.	Secant.	Min.
0	9.7118293	9.9330651	9.7787787	10.2212263
1	9.7120495	9.9330897	9.7790599	10.2209401
2	9.7122696	9.9331137	9.7793459	10.2206541
3	9.7124896	9.9331376	9.7796218	10.2203682
4	9.7127093	9.9331616	9.7798977	10.2200823
5	9.7129288	9.9331854	9.7801734	10.2197966
6	9.7131482	9.9332092	9.7804491	10.2195109
7	9.7133673	9.9332330	9.7807247	10.2192253
8	9.7135863	9.9332567	9.7810002	10.2189398
9	9.7138052	9.9332804	9.7812756	10.2186544
10	9.7140239	9.9333041	9.7815509	10.2183691
11	9.7142423	9.9333276	9.7818261	10.2180838
12	9.7144605	9.9333511	9.7821013	10.2177987
13	9.7146786	9.9333746	9.7823764	10.2175136
14	9.7148963	9.9333980	9.7826513	10.2172287
15	9.7151139	9.9334213	9.7829261	10.2169438
16	9.7153312	9.9334447	9.7832008	10.2166589
17	9.7155483	9.9334679	9.7834754	10.2163742
18	9.7157651	9.9334911	9.7837500	10.2160896
19	9.7159817	9.9335143	9.7840244	10.2158051
20	9.7161981	9.9335374	9.7842987	10.2155206
21	9.7164142	9.9335605	9.7845728	10.2152362
22	9.7166301	9.9335835	9.7848468	10.2149519
23	9.7168458	9.9336065	9.7851207	10.2146677
24	9.7170612	9.9336294	9.7853944	10.2143836
25	9.7172764	9.9336522	9.7856680	10.2140996
26	9.7174913	9.9336750	9.7859414	10.2138156
27	9.7177060	9.9336978	9.7862147	10.2135318
28	9.7179205	9.9337205	9.7864879	10.2132480
29	9.7181348	9.9337432	9.7867610	10.2129643
30	9.7183488	9.9337658	9.7870340	10.2126807
31	9.7185625	9.9337884	9.7873068	10.2123972
32	9.7187760	9.9338109	9.7875795	10.2121138
33	9.7189892	9.9338333	9.7878521	10.2118305
34	9.7192022	9.9338557	9.7881246	10.2115473
35	9.7194149	9.9338780	9.7883969	10.2112642
36	9.7196273	9.9338999	9.7886691	10.2109812
37	9.7198394	9.9339218	9.7889412	10.2106983
38	9.7200512	9.9339436	9.7892132	10.2104155
39	9.7202628	9.9339653	9.7894851	10.2101328
40	9.7204741	9.9339869	9.7897569	10.2098502
41	9.7206852	9.9340084	9.7899986	10.2095677
42	9.7208960	9.9340298	9.7902401	10.2092853
43	9.7211065	9.9340511	9.7904815	10.2090030
44	9.7213168	9.9340723	9.7907228	10.2087208
45	9.7215268	9.9340934	9.7909639	10.2084387
46	9.7217365	9.9341144	9.7912049	10.2081567
47	9.7219459	9.9341353	9.7914458	10.2078748
48	9.7221550	9.9341561	9.7916866	10.2075930
49	9.7223638	9.9341768	9.7919273	10.2073113
50	9.7225723	9.9341974	9.7921679	10.2070297
51	9.7227805	9.9342179	9.7924083	10.2067482
52	9.7229884	9.9342383	9.7926486	10.2064668
53	9.7231960	9.9342586	9.7928888	10.2061855
54	9.7234033	9.9342788	9.7931289	10.2059043
55	9.7236103	9.9342989	9.7933689	10.2056232
56	9.7238170	9.9343189	9.7936088	10.2053422
57	9.7240234	9.9343388	9.7938486	10.2050613
58	9.7242295	9.9343586	9.7940883	10.2047805
59	9.7244353	9.9343783	9.7943279	10.2045000
60	9.7246408	9.9343979	9.7945674	10.2042195
61	9.7248460	9.9344174	9.7948068	10.2039392
62	9.7250509	9.9344368	9.7950461	10.2036590
63	9.7252555	9.9344561	9.7952853	10.2033789
64	9.7254598	9.9344753	9.7955244	10.2030989
65	9.7256638	9.9344944	9.7957634	10.2028190
66	9.7258675	9.9345134	9.7960023	10.2025392
67	9.7260709	9.9345323	9.7962411	10.2022595
68	9.7262740	9.9345511	9.7964798	10.2019799
69	9.7264768	9.9345698	9.7967184	10.2016999
70	9.7266793	9.9345884	9.7969569	10.2014200
71	9.7268815	9.9346069	9.7971953	10.2011402
72	9.7270834	9.9346253	9.7974336	10.2008605
73	9.7272850	9.9346436	9.7976718	10.2005809
74	9.7274863	9.9346618	9.7979099	10.2003014
75	9.7276873	9.9346799	9.7981479	10.2000220
76	9.7278880	9.9346979	9.7983858	10.1997427
77	9.7280884	9.9347158	9.7986236	10.1994635
78	9.7282885	9.9347336	9.7988613	10.1991843
79	9.7284883	9.9347513	9.7990989	10.1989052
80	9.7286878	9.9347689	9.7993364	10.1986262
81	9.7288870	9.9347864	9.7995738	10.1983473
82	9.7290859	9.9348038	9.7998111	10.1980685
83	9.7292845	9.9348211	9.8000483	10.1977897
84	9.7294828	9.9348383	9.8002854	10.1975110
85	9.7296808	9.9348554	9.8005224	10.1972324
86	9.7298785	9.9348724	9.8007593	10.1969539
87	9.7300759	9.9348893	9.8009961	10.1966755
88	9.7302730	9.9349061	9.8012328	10.1963972
89	9.7304698	9.9349228	9.8014694	10.1961190
90	9.7306663	9.9349394	9.8017059	10.1958409
91	9.7308625	9.9349559	9.8019423	10.1955629
92	9.7310584	9.9349723	9.8021786	10.1952850
93	9.7312540	9.9349886	9.8024148	10.1950072
94	9.7314493	9.9350048	9.8026509	10.1947295
95	9.7316443	9.9350209	9.8028869	10.1944519
96	9.7318390	9.9350369	9.8031228	10.1941744
97	9.7320334	9.9350528	9.8033586	10.1938970
98	9.7322275	9.9350686	9.8035943	10.1936197
99	9.7324213	9.9350843	9.8038299	10.1933425
100	9.7326148	9.9350999	9.8040654	10.1930654

58 Degrees.

Tangents and Secants,

31 Degrees.

Min.	Sine.		Tang.		Secant.	
30	0.50000	0.9307658	0.7873193	10.2125607	10.0692342	10.2181914930
31	0.7182912	0.9306883	0.7876028	10.2123972	10.0693117	10.2181708829
32	0.7184971	0.9306109	0.7878863	10.2121137	10.0693891	10.2181503928
33	0.7187039	0.9305333	0.7881696	10.2118304	10.0694667	10.2181299027
34	0.7189086	0.9304559	0.7884529	10.2115471	10.0695443	10.2181094126
35	0.7191142	0.9303781	0.7887361	10.2112639	10.0696219	10.2180885825
36	0.7193196	0.9303004	0.7890192	10.2109808	10.0696990	10.2180680424
37	0.7195249	0.9302226	0.7893023	10.2106977	10.0697774	10.2180475123
38	0.7197300	0.9301448	0.7895854	10.2104148	10.0698552	10.2180270022
39	0.7199350	0.9300670	0.7898681	10.2101319	10.0699330	10.2180065021
40	0.7201399	0.9299881	0.7901508	10.2098492	10.0700109	10.2179860120
41	0.7203447	0.9299112	0.7904335	10.2095665	10.0700888	10.2179655319
42	0.7205492	0.9298332	0.7907161	10.2092833	10.0701668	10.2179450718
43	0.7207538	0.9297551	0.7909987	10.2090003	10.0702449	10.2179245217
44	0.7209581	0.9296770	0.7912811	10.2087189	10.0703230	10.2179041916
45	0.7211622	0.9295989	0.7915635	10.2084365	10.0704011	10.2178837715
46	0.7213664	0.9295207	0.7918458	10.2081542	10.0704793	10.2178633614
47	0.7215704	0.9294414	0.7921280	10.2078720	10.0705576	10.2178429613
48	0.7217742	0.9293621	0.7924101	10.2075899	10.0706359	10.2178225812
49	0.7219779	0.9292837	0.7926921	10.2073079	10.0707143	10.2178022111
50	0.7221814	0.9292073	0.7929741	10.2070259	10.0707927	10.2177818610
51	0.7223848	0.9291287	0.7932560	10.2067470	10.0708711	10.217761529
52	0.7225881	0.9290504	0.7935378	10.2064622	10.0709496	10.217741198
53	0.7227913	0.9289718	0.7938195	10.2061805	10.0710283	10.217720877
54	0.7229943	0.9288932	0.7941011	10.2058989	10.0711068	10.217700576
55	0.7231972	0.9288145	0.7943827	10.2056173	10.0711855	10.217680285
56	0.7234000	0.9287358	0.7946641	10.2053359	10.0712642	10.217659000
57	0.7236026	0.9286571	0.7949455	10.2050545	10.0713429	10.217637743
58	0.7238051	0.9285783	0.7952268	10.2047732	10.0714217	10.217616492
59	0.7240075	0.9284994	0.7955081	10.2044919	10.0715006	10.217595215
60	0.7242097	0.9284205	0.7957892	10.2042108	10.0715795	10.217573903
	Sine.		Tang.		Secant.	Min.

58 Degrees.

A Table of Artificial Sines,

32 Degrees.

Min.	Sine.		Tang.		Sec ant.	
0	9.7242097	9.9284205	9.7957892	10.2042108	10.0715795	10.2757903 60
1	9.7244128	9.9283415	9.7960703	10.2039207	10.0716585	10.2755882 59
2	9.7246138	9.9282625	9.7963513	10.2036487	10.0717375	10.2753862 58
3	9.7248156	9.9281834	9.7966322	10.2033678	10.0718166	10.2751844 57
4	9.7250174	9.9281043	9.7969130	10.2030870	10.0718957	10.2749826 56
5	9.7252189	9.9280251	9.7971938	10.2028062	10.0719745	10.2747811 55
6	9.7254204	9.9279459	9.7974745	10.2025255	10.0720541	10.2745796 54
7	9.7256217	9.9278666	9.7977552	10.2022449	10.0721334	10.2743783 53
8	9.7258229	9.9277873	9.7980356	10.2019644	10.0722127	10.2741771 52
9	9.7260240	9.9277079	9.7983160	10.2016840	10.0722921	10.2739760 51
10	9.7262249	9.9276285	9.7985964	10.2014036	10.0723715	10.2737751 50
11	9.7264257	9.9275490	9.7988767	10.2011233	10.0724510	10.2735743 49
12	9.7266264	9.9274695	9.7991569	10.2008431	10.0725305	10.2733736 48
13	9.7268269	9.9273899	9.7994370	10.2005630	10.0726101	10.2731731 47
14	9.7270273	9.9273103	9.7997170	10.2002830	10.0726897	10.2729727 46
15	9.7272276	9.9272306	9.7999970	10.2000030	10.0727694	10.2727724 45
16	9.7274278	9.9271509	9.8002769	10.1997231	10.0728491	10.2725722 44
17	9.7276278	9.9270711	9.8005567	10.1994433	10.0729289	10.2723722 43
18	9.7278277	9.9269913	9.8008365	10.1991635	10.0730087	10.2721723 42
19	9.7280275	9.9269114	9.8011161	10.1988839	10.0730886	10.2719725 41
20	9.7282271	9.9268314	9.8013957	10.1986043	10.0731686	10.2717729 40
21	9.7284267	9.9267514	9.8016752	10.1983248	10.0732486	10.2715733 39
22	9.7286260	9.9266714	9.8019546	10.1980454	10.0733286	10.2713740 38
23	9.7288253	9.9265913	9.8022340	10.1977660	10.0734087	10.2711747 37
24	9.7290245	9.9265112	9.8025133	10.1974867	10.0734888	10.2709756 36
25	9.7292234	9.9264310	9.8027925	10.1972075	10.0735690	10.2707766 35
26	9.7294223	9.9263507	9.8030716	10.1969284	10.0736493	10.2705777 34
27	9.7296211	9.9262704	9.8033506	10.1966494	10.0737296	10.2703790 33
28	9.7298197	9.9261901	9.8036296	10.1963704	10.0738099	10.2701803 32
29	9.7300182	9.9261096	9.8039085	10.1960915	10.0738904	10.2699818 31
30	9.7302165	9.9260292	9.8041873	10.1958127	10.0739708	10.2697835 30
	Sine.		Tang.		Secant.	Min.

57 Degrees.

Tangents, and Secants.

32 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.7302165	9.9240292	9.8041873	10.1958127	10.0739708	10.2697835
31	9.7304148	9.9239487	9.8044661	10.1955339	10.0740513	10.2695852
32	9.7306129	9.9238681	9.8047447	10.1952553	10.0741319	10.2693871
33	9.7308109	9.9237875	9.8050233	10.1949767	10.0742125	10.2691891
34	9.7310087	9.9237069	9.8053019	10.1946981	10.0742931	10.2689913
35	9.7312064	9.9236261	9.8055803	10.1944197	10.0743739	10.2687936
36	9.7314040	9.9235454	9.8058587	10.1941413	10.0744546	10.2685960
37	9.7316015	9.9234646	9.8061370	10.1938630	10.0745354	10.2683985
38	9.7317989	9.9233837	9.8064152	10.1935848	10.0746163	10.2682011
39	9.7319961	9.9233028	9.8066933	10.1933067	10.0746972	10.2680039
40	9.7321932	9.9232218	9.8069714	10.1930286	10.0747780	10.2678066
41	9.7323902	9.9231408	9.8072494	10.1927506	10.0748592	10.2676098
42	9.7325870	9.9230597	9.8075273	10.1924727	10.0749403	10.2674130
43	9.7327837	9.9229786	9.8078052	10.1921948	10.0750214	10.2672163
44	9.7329803	9.9228974	9.8080829	10.1919171	10.0751026	10.2670197
45	9.7331768	9.9228161	9.8083606	10.1916394	10.0751839	10.2668232
46	9.7333731	9.9227349	9.8086383	10.1913617	10.0752651	10.2666264
47	9.7335693	9.9226535	9.8089158	10.1910842	10.0753463	10.2664307
48	9.7337654	9.9225721	9.8091933	10.1908067	10.0754279	10.2662346
49	9.7339614	9.9224907	9.8094707	10.1905293	10.0755093	10.2660386
50	9.7341572	9.9224092	9.8097480	10.1902520	10.0755908	10.2658428
51	9.7343529	9.9223277	9.8100253	10.1899747	10.0756723	10.2656471
52	9.7345485	9.9222461	9.8103025	10.1896975	10.0757539	10.2654515
53	9.7347440	9.9221644	9.8105796	10.1894204	10.0758356	10.2652560
54	9.7349393	9.9220827	9.8108566	10.1891434	10.0759173	10.2650607
55	9.7351345	9.9220010	9.8111336	10.1888664	10.0759990	10.2648655
56	9.7353296	9.9239191	9.8114105	10.1885895	10.0760809	10.2646704
57	9.7355246	9.9238373	9.8116873	10.1883127	10.0761627	10.2644754
58	9.7357195	9.9237554	9.8119641	10.1880359	10.0762446	10.2642805
59	9.7359142	9.9236734	9.8122408	10.1877592	10.0763266	10.2640858
60	9.7361088	9.9235914	9.8125174	10.1874826	10.0764086	10.2638912
	Sine.		Tang.		Secant.	Min.

57 Degrees.

A Table of Artificial Sines,

33 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.7361088	9.9235914	9.8125174	10.1874826	10.0764086	10.263891250
1	9.7363032	9.9235093	9.8127939	10.1872061	10.0764907	10.263696359
2	9.7364976	9.9234272	9.8130704	10.1869296	10.0765728	10.263502458
3	9.7366918	9.9233450	9.8133468	10.1866532	10.0766550	10.263308257
4	9.7368859	9.9232628	9.8136231	10.1863769	10.0767372	10.263114156
5	9.7370799	9.9231865	9.8138993	10.1861007	10.0768195	10.262920155
6	9.7372737	9.9230982	9.8141755	10.1858245	10.0769018	10.262726354
7	9.7374675	9.9230158	9.8144516	10.1855484	10.0769842	10.262532553
8	9.7376611	9.9229334	9.8147277	10.1852723	10.0770666	10.262338952
9	9.7378546	9.9228509	9.8150036	10.1849964	10.0771491	10.262145451
10	9.7380479	9.9227684	9.8152795	10.1847205	10.0772316	10.261952150
11	9.7382412	9.9226858	9.8155554	10.1844446	10.0773142	10.261758849
12	9.7384343	9.9226032	9.8158311	10.1841689	10.0773969	10.261565748
13	9.7386273	9.9225205	9.8161068	10.1838932	10.0774795	10.261372747
14	9.7388201	9.9224377	9.8163824	10.1836176	10.0775623	10.261179946
15	9.7390129	9.9223549	9.8166580	10.1833420	10.0776451	10.260987145
16	9.7392055	9.9222721	9.8169335	10.1830665	10.0777279	10.260794544
17	9.7393980	9.9221891	9.8172089	10.1827911	10.0778109	10.260602043
18	9.7395904	9.9221062	9.8174842	10.1825158	10.0778938	10.260409642
19	9.7397827	9.9220232	9.8177595	10.1822405	10.0779768	10.260217341
20	9.7399748	9.9219401	9.8180347	10.1819653	10.0780599	10.260025240
21	9.7401668	9.9218570	9.8183098	10.1816902	10.0781430	10.259833239
22	9.7403587	9.9217738	9.8185849	10.1814151	10.0782262	10.259641338
23	9.7405505	9.9216906	9.8188599	10.1811401	10.0783094	10.259449537
24	9.7407421	9.9216073	9.8191348	10.1808652	10.0783927	10.259257936
25	9.7409337	9.9215240	9.8194096	10.1805904	10.0784762	10.259066335
26	9.7411251	9.9214406	9.8196844	10.1803156	10.0785594	10.258874934
27	9.7413164	9.9213572	9.8199592	10.1800408	10.0786428	10.258683633
28	9.7415075	9.9212737	9.8202338	10.1797662	10.0787263	10.258492532
29	9.7416986	9.9211902	9.8205084	10.1794916	10.0788098	10.258301431
30	9.7418895	9.9211066	9.8207829	10.1792171	10.0788934	10.258110530
		Sine		Tang.		Secant.
						Min.

56 Degrees.

Tangents and Secants.

33 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.741885	9.9211066	9.8207829	10.1792171	10.0788934	10.2581105	30
31	9.7420803	9.9210229	9.8210574	10.1789426	10.0789771	10.2579197	29
32	9.7422710	9.9209393	9.8213317	10.1786683	10.0790607	10.2577290	28
33	9.7424616	9.9208555	9.8216060	10.1783946	10.0791445	10.2575384	27
34	9.7426520	9.9207717	9.8218803	10.1781197	10.0792283	10.2573480	26
35	9.7428423	9.9206878	9.8221545	10.1778455	10.0793122	10.2571577	25
36	9.7430325	9.9206039	9.8224286	10.1775714	10.0793961	10.2569675	24
37	9.7432226	9.9205200	9.8227026	10.1772974	10.0794800	10.2567774	23
38	9.7434126	9.9204360	9.8229766	10.1770234	10.0795640	10.2565874	22
39	9.7436024	9.9203519	9.8232505	10.1767495	10.0796481	10.2563976	21
40	9.7437921	9.9202678	9.8235244	10.1764756	10.0797322	10.2562079	20
41	9.7439817	9.9201836	9.8237981	10.1762019	10.0798164	10.2560183	19
42	9.7441712	9.9200994	9.8240719	10.1759281	10.0799006	10.2558288	18
43	9.7443606	9.9200151	9.8243455	10.1756545	10.0799849	10.2556394	17
44	9.7445498	9.9199308	9.8246191	10.1753809	10.0800692	10.2554502	16
45	9.7447390	9.9198464	9.8248926	10.1751074	10.0801536	10.2552610	15
46	9.7449280	9.9197619	9.8251660	10.1748340	10.0802381	10.2550720	14
47	9.7451169	9.9196775	9.8254394	10.1745606	10.0803225	10.2548831	13
48	9.7453056	9.9195929	9.8257127	10.1742873	10.0804071	10.2546944	12
49	9.7454953	9.9195083	9.8259860	10.1740140	10.0804917	10.2545057	11
50	9.7456828	9.9194237	9.8262592	10.1737408	10.0805763	10.2543172	10
51	9.7458712	9.9193390	9.8265323	10.1734677	10.0806610	10.2541288	9
52	9.7460595	9.9192542	9.8268053	10.1731947	10.0807458	10.2539405	8
53	9.7462477	9.9191694	9.8270783	10.1729217	10.0808306	10.2537523	7
54	9.7464358	9.9190845	9.8273513	10.1726487	10.0809155	10.2535642	6
55	9.7466237	9.9189996	9.8276241	10.1723759	10.0810004	10.2533763	5
56	9.7468115	9.9189146	9.8278965	10.1721031	10.0810854	10.2531885	4
57	9.7469992	9.9188296	9.8281656	10.1718304	10.0811704	10.2530008	3
58	9.7471868	9.9187445	9.8284423	10.1715577	10.0812555	10.2528132	2
59	9.7473743	9.9186594	9.8287149	10.1712851	10.0813406	10.2526257	1
60	9.7475617	9.9185742	9.8289874	10.1710126	10.0814258	10.2524383	0
	Sine.		Tang.		Secant.		Min.

56 Degrees.

A Table of Artificial Sines,

34 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.7475617	9.9185742	9.8289874	10.1710126	10.0814258	10.2524383 60
1	9.7477489	9.9184890	9.8292599	10.1707401	10.0815110	10.2522511 59
2	9.7479360	9.9184037	9.8295323	10.1704677	10.0815963	10.2520640 58
3	9.7481230	9.9183183	9.8298047	10.1701953	10.0816817	10.2518770 57
4	9.7483099	9.9182329	9.8300769	10.1799231	10.0817671	10.2516901 56
5	9.7484967	9.9181475	9.8303492	10.1696508	10.0818525	10.2515033 55
6	9.7486833	9.9180620	9.8306213	10.1693787	10.0819380	10.2513167 54
7	9.7488699	9.9179764	9.8308934	10.1691066	10.0820236	10.2511302 53
8	9.7490562	9.9178908	9.8311654	10.1688346	10.0821092	10.2509438 52
9	9.7492425	9.9178051	9.8314374	10.1685626	10.0821948	10.2507579 51
10	9.7494287	9.9177194	9.8317093	10.1682907	10.0822806	10.2505713 50
11	9.7496148	9.9176336	9.8319811	10.1680189	10.0823664	10.2503852 49
12	9.7498007	9.9175478	9.8322525	10.1677471	10.0824522	10.2501993 48
13	9.7499866	9.9174619	9.8325246	10.1674754	10.0825381	10.2500134 47
14	9.7501723	9.9173760	9.8327963	10.1672037	10.0826240	10.2498277 46
15	9.7503579	9.9172900	9.8330679	10.1669321	10.0827100	10.2496421 45
16	9.7505434	9.9172040	9.8333394	10.1666606	10.0827960	10.2494566 44
17	9.7507287	9.9171179	9.8336109	10.1663891	10.0828821	10.2492713 43
18	9.7509140	9.9170317	9.8338823	10.1661177	10.0829683	10.2490860 42
19	9.7510991	9.9169455	9.8341536	10.1658464	10.0830545	10.2489009 41
20	9.7512842	9.9168593	9.8344249	10.1655751	10.0831407	10.2487158 40
21	9.7514691	9.9167730	9.8346961	10.1653039	10.0832270	10.2485305 39
22	9.7516538	9.9166866	9.8349673	10.1650327	10.0833134	10.2483462 38
23	9.7518385	9.9166002	9.8352384	10.1647616	10.0833998	10.2481615 37
24	9.7520231	9.9165137	9.8355094	10.1644906	10.0834863	10.2479769 36
25	9.7522075	9.9164272	9.8357804	10.1642196	10.0835728	10.2477925 35
26	9.7523919	9.9163406	9.8360513	10.1639487	10.0836594	10.2476081 34
27	9.7525761	9.9162539	9.8363221	10.1636779	10.0837461	10.2474238 33
28	9.7527602	9.9161673	9.8365929	10.1634071	10.0838327	10.2472398 32
29	9.7529442	9.9160805	9.8368636	10.1631364	10.0839195	10.2470558 31
30	9.7531280	9.9159937	9.8371342	10.1628657	10.0840063	10.2468720 30
	Sine.		Tang.		Secant.	Min.

55 Degrees.

Tangents, and Secants.

34 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.7531280	9.9159937	9.8371343	10.1628657	10.0840063	10.2467203	0
31	9.7533118	9.9159069	9.8374049	10.1625951	10.0840931	10.2466882	29
32	9.7534954	9.9158200	9.8376755	10.1623245	10.0841800	10.2466562	28
33	9.7536790	9.9157330	9.8379460	10.1620540	10.0842670	10.2466241	27
34	9.7538624	9.9156460	9.8382164	10.1617836	10.0843540	10.2465920	26
35	9.7540457	9.9155589	9.8384867	10.1615133	10.0844411	10.2465599	25
36	9.7542288	9.9154718	9.8387571	10.1612429	10.0845282	10.2465278	24
37	9.7544119	9.9153846	9.8390273	10.1609727	10.0846154	10.2464957	23
38	9.7545949	9.9152974	9.8392975	10.1607025	10.0846026	10.2464636	22
39	9.7547777	9.9152101	9.8395676	10.1604324	10.0847899	10.2464315	21
40	9.7549604	9.9151228	9.8398377	10.1601623	10.0848772	10.2463994	20
41	9.7551431	9.9150354	9.8401077	10.1598923	10.0849646	10.2463673	19
42	9.7553256	9.9149479	9.8403776	10.1596224	10.0850521	10.2463352	18
43	9.7555080	9.9148604	9.8406475	10.1593525	10.0851396	10.2463031	17
44	9.7556902	9.9147729	9.8409174	10.1590826	10.0852271	10.2462710	16
45	9.7558724	9.9146852	9.8411871	10.1588129	10.0853148	10.2462389	15
46	9.7560544	9.9145976	9.8414569	10.1585431	10.0854024	10.2462068	14
47	9.7562364	9.9145098	9.8417265	10.1582735	10.0854901	10.2461747	13
48	9.7564182	9.9144221	9.8419961	10.1580039	10.0855779	10.2461426	12
49	9.7565999	9.9143342	9.8422657	10.1577343	10.0856658	10.2461105	11
50	9.7567815	9.9142464	9.8425351	10.1574649	10.0857536	10.2460784	10
51	9.7569630	9.9141584	9.8428046	10.1571954	10.0858416	10.2460463	9
52	9.7571444	9.9140704	9.8430739	10.1569261	10.0859296	10.2460142	8
53	9.7573256	9.9139824	9.8433432	10.1566568	10.0860176	10.2459821	7
54	9.7575068	9.9138943	9.8436125	10.1563875	10.0861057	10.2459500	6
55	9.7576878	9.9138061	9.8438817	10.1561183	10.0861939	10.2459179	5
56	9.7578687	9.9137175	9.8441508	10.1558492	10.0862821	10.2458858	4
57	9.7580495	9.9136296	9.8444199	10.1555801	10.0863704	10.2458537	3
58	9.7582302	9.9135413	9.8446889	10.1553111	10.0864587	10.2458216	2
59	9.7584108	9.9134530	9.8449579	10.1550421	10.0865471	10.2457895	1
60	9.7585913	9.9133645	9.8452268	10.1547732	10.0866355	10.2457574	0
	Sine.		Tang.		Secant.		Min.

55 Degrees.

A Table of Artificial Sines,

35 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.7585913	9.9133645	9.8452268	10.1547732	10.0866355	10.2414087	60
1	9.7587717	9.9132760	9.8454956	10.1545044	10.0867240	10.24 2283	59
2	9.7589519	9.913 875	9.8457644	10.1542356	10.0868125	10.2410481	58
3	9.7591321	9.9130989	9.8460332	10.1539668	10.0869011	10.2408679	57
4	9.7593121	9.9130102	9.8463018	10.1536982	10.0869898	10.2406879	56
5	9.7594920	9.9129215	9.8465705	10.1534295	10.0870785	10.2405080	55
6	9.7596718	9.9128328	9.8468390	10.1531610	10.0871672	10.2403282	54
7	9.7598515	9.9127440	9.8471075	10.1528925	10.0872560	10.2401485	53
8	9.7600311	9.9126551	9.8473760	10.1526240	10.0873449	10.2399689	52
9	9.7602106	9.9125662	9.8476444	10.1523556	10.0874338	10.2397894	51
10	9.7603899	9.9124773	9.8479127	10.1520873	10.0875228	10.2396091	50
11	9.7605693	9.9123882	9.8481810	10.1518190	10.0876118	10.2394288	49
12	9.7607483	9.9122991	9.8484492	10.1515508	10.0877009	10.2392485	48
13	9.7609274	9.9122099	9.8487174	10.1512826	10.0877901	10.2390682	47
14	9.7611063	9.9121207	9.8489855	10.1510145	10.0878793	10.2388879	46
15	9.7612851	9.9120315	9.8492536	10.1507464	10.0879685	10.2387076	45
16	9.7614638	9.9119423	9.8495216	10.1504784	10.0880578	10.2385273	44
17	9.7616424	9.9118530	9.8497896	10.1502104	10.0881472	10.2383470	43
18	9.7618208	9.9117634	9.8500575	10.1499425	10.0882366	10.2381667	42
19	9.7619990	9.9116739	9.8503253	10.1496747	10.0883261	10.2379864	41
20	9.7621775	9.9115844	9.8505931	10.1494069	10.0884156	10.2378061	40
21	9.7623556	9.9114948	9.8508608	10.1491392	10.0885052	10.2376258	39
22	9.7625337	9.9114051	9.8511285	10.1488715	10.0885949	10.2374455	38
23	9.7627116	9.9113155	9.8513961	10.1486039	10.0886845	10.2372652	37
24	9.7628894	9.9112257	9.8516637	10.1483362	10.0887743	10.2370849	36
25	9.7630671	9.9111359	9.8519312	10.1480688	10.0888641	10.2369046	35
26	9.7632447	9.9110460	9.8521987	10.1478013	10.0889540	10.2367243	34
27	9.7634222	9.9109561	9.8524661	10.1475339	10.0890439	10.2365440	33
28	9.7635996	9.9108661	9.8527335	10.1472665	10.0891339	10.2363637	32
29	9.7637769	9.9107761	9.8530008	10.1469992	10.0892239	10.2361834	31
30	9.7639540	9.9106860	9.8532680	10.1467320	10.0893140	10.2360031	30
	Sine		Tang		Secant.		Min.

54 Degrees.

Tangents and Secants.

35 Degrees.

Min.	Sine.		Tang.		Secant.	
30	0.7639540	0.9106860	0.8532680	10.1467320	10.0893140	10.2350460
31	0.7641311	0.9105959	0.8535352	10.1464648	10.0894041	10.2358689
32	0.7643080	0.9105057	0.8538023	10.1461977	10.0894942	10.2366920
33	0.7644849	0.9104155	0.8540694	10.1459306	10.0895846	10.2375151
34	0.7646618	0.9103251	0.8543365	10.1456635	10.0896749	10.2383384
35	0.7648382	0.9102348	0.8546034	10.1453966	10.0897652	10.2391618
36	0.7650147	0.9101444	0.8548704	10.1451296	10.0898556	10.2400853
37	0.7651911	0.9100539	0.8551372	10.1448626	10.0899461	10.2410089
38	0.7653674	0.9099633	0.8554041	10.1445955	10.0900366	10.2419326
39	0.7655436	0.9098728	0.8556708	10.1443282	10.0901272	10.2428564
40	0.7657097	0.9097821	0.8559376	10.1440624	10.0902179	10.2437802
41	0.7658857	0.9096919	0.8562042	10.1437958	10.0903085	10.2447041
42	0.7660615	0.9096007	0.8564708	10.1435292	10.0903993	10.2456281
43	0.7662373	0.9095099	0.8567374	10.1432626	10.0904901	10.2465522
44	0.7664129	0.9094190	0.8570036	10.1429961	10.0905810	10.2474764
45	0.7665885	0.9093281	0.8572704	10.1427296	10.0906719	10.2484006
46	0.7667639	0.9092371	0.8575368	10.1424632	10.0907629	10.2493249
47	0.7669392	0.9091461	0.8578021	10.1421969	10.0908539	10.2502493
48	0.7671144	0.9090550	0.8580674	10.1419306	10.0909450	10.2511738
49	0.7672896	0.9089639	0.8583327	10.1416643	10.0910361	10.2520984
50	0.7674646	0.9088727	0.8585979	10.1413981	10.0911272	10.2530230
51	0.7676404	0.9087814	0.8588630	10.1411320	10.0912186	10.2539478
52	0.7678162	0.9086901	0.8591281	10.1408659	10.0913099	10.2548728
53	0.7679919	0.9085988	0.8593932	10.1405998	10.0914012	10.2557980
54	0.7681675	0.9085073	0.8596583	10.1403339	10.0914927	10.2567234
55	0.7683430	0.9084159	0.8599234	10.1400679	10.0915841	10.2576490
56	0.7685183	0.9083243	0.8601885	10.1398020	10.0916757	10.2585748
57	0.7686936	0.9082327	0.8604536	10.1395362	10.0917672	10.2595008
58	0.7688687	0.9081411	0.8607187	10.1392704	10.0918589	10.2604270
59	0.7690438	0.9080494	0.8609838	10.1390046	10.0919506	10.2613534
60	0.7692187	0.9079576	0.8612489	10.1387388	10.0920424	10.2622800
	Sine.		Tang.		Secant.	Min.

54 Degrees.

A Table of Artificial Sines,

36 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.7692187	9.9079576	9.8612610	10.1387390	10.0920424	10.230781360
1	9.7693925	9.9078658	9.8615267	10.1384733	10.0921342	10.230607559
2	9.7695662	9.9077740	9.8617923	10.1382077	10.0922260	10.230433858
3	9.7697398	9.9076820	9.8620578	10.1379422	0.0923180	10.230260257
4	9.7699134	9.9075901	9.8623233	10.1376767	10.0924099	10.230086656
5	9.7700868	9.9074980	9.8625887	10.1374113	10.0925020	10.229913255
6	9.7702601	9.9074059	9.8628541	10.1371459	10.0925941	10.229739954
7	9.7704332	9.9073138	9.8631195	10.1368803	10.0926862	10.229566853
8	9.7706063	9.9072216	9.8633848	10.1366152	10.0927784	10.229393752
9	9.7707793	9.9071293	9.8636500	10.1363500	10.0928707	10.229220751
10	9.7709522	9.9070370	9.8639152	10.1360848	10.0929630	10.229047850
11	9.7711249	9.9069446	9.8641803	10.1358197	10.0930554	10.228875149
12	9.7712976	9.9068522	9.8644454	10.1355546	10.0931478	10.228702448
13	9.7714702	9.9067597	9.8647105	10.1352895	10.0932403	10.228529847
14	9.7716426	9.9066671	9.8649755	10.1350245	10.0933329	10.228357446
15	9.7718150	9.9065745	9.8652404	10.1347596	10.0934255	10.228185045
16	9.7719872	9.9064819	9.8655053	10.1344947	10.0935181	10.228012844
17	9.7721593	9.9063892	9.8657702	10.1342298	10.0936108	10.227840743
18	9.7723314	9.9062964	9.8660350	10.1339650	10.0937036	10.227668642
19	9.7725033	9.9062036	9.8662997	10.1337003	10.0937964	10.227496341
20	9.7726751	9.9061107	9.8665644	10.1334356	10.0938893	10.227324940
21	9.7728468	9.9060177	9.8668291	10.1331709	10.0939823	10.227153239
22	9.7730185	9.9059247	9.8670937	10.1329063	10.0940753	10.226981538
23	9.7731900	9.9058317	9.8673583	10.1326417	10.0941683	10.226810037
24	9.7733614	9.9057386	9.8676228	10.1323772	10.0942614	10.226638636
25	9.7735327	9.9056454	9.8678873	10.1321127	10.0943546	10.226467335
26	9.7737039	9.9055522	9.8681517	10.1318483	10.0944478	10.226292134
27	9.7738749	9.9054589	9.8684160	10.1315840	10.0945411	10.226125133
28	9.7740459	9.9053656	9.8686804	10.1313196	10.0946344	10.225954132
29	9.7742168	9.9052722	9.8689446	10.1310554	10.0947278	10.225783231
30	9.7743876	9.9051787	9.8692089	10.1307911	10.0948213	10.225612430
	Sine.		Tang.		Secant.	Min.

53 Degrees.

Tangents and Secants.

36 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
30	9.7743876	9.9051787	9.8692089	10.1307921	10.0948413	10.2256124	30
31	9.7745583	9.9050852	9.8694731	10.1305269	10.0949148	10.2254417	29
32	9.7747288	9.9049916	9.8697372	10.1302628	10.0950084	10.2252712	28
33	9.7748993	9.9048980	9.8700013	10.1299987	10.0951020	10.2251007	27
34	9.7750697	9.9048043	9.8702653	10.1297347	10.0951957	10.2249303	26
35	9.7752399	9.9047106	9.8705293	10.1294707	10.0952894	10.2247601	25
36	9.7754101	9.9046168	9.8707933	10.1292067	10.0953832	10.2245895	24
37	9.7755801	9.9045230	9.8710572	10.1289428	10.0954770	10.2244195	23
38	9.7757501	9.9044291	9.8713210	10.1286790	10.0955709	10.2242495	22
39	9.7759199	9.9043351	9.8715848	10.1284152	10.0956649	10.2240801	21
40	9.7760897	9.9042411	9.8718486	10.1281514	10.0957589	10.2239103	20
41	9.7762593	9.9041470	9.8721123	10.1278837	10.0958530	10.2237407	19
42	9.7764289	9.9040529	9.8723760	10.1276240	10.0959471	10.2235711	18
43	9.7765983	9.9039587	9.8726396	10.1273604	10.0960413	10.2234017	17
44	9.7767676	9.9038644	9.8729032	10.1270968	10.0961356	10.2232324	16
45	9.7769369	9.9037701	9.8731668	10.1268332	10.0962299	10.2230631	15
46	9.7771060	9.9036757	9.8734302	10.1265698	10.0963243	10.2228940	14
47	9.7772750	9.9035813	9.8736937	10.1263063	10.0964187	10.2227250	13
48	9.7774439	9.9034868	9.8739571	10.1260429	10.0965132	10.2225561	12
49	9.7776128	9.9033923	9.8742204	10.1257796	10.0966077	10.2223872	11
50	9.7777815	9.9032977	9.8744838	10.1255162	10.0967023	10.2222185	10
51	9.7779501	9.9032031	9.8747470	10.1252530	10.0967969	10.2220499	9
52	9.7781186	9.9031084	9.8750102	10.1249898	10.0968916	10.2218814	8
53	9.7782870	9.9030136	9.8752734	10.1247266	10.0969864	10.2217130	7
54	9.7784553	9.9029188	9.8755365	10.1244635	10.0970812	10.2215447	6
55	9.7786235	9.9028239	9.8757996	10.1242004	10.0971761	10.2213765	5
56	9.7787916	9.9027289	9.8760627	10.1239373	10.0972711	10.2212084	4
57	9.7789596	9.9026339	9.8763257	10.1236743	10.0973661	10.2210404	3
58	9.7791275	9.9025389	9.8765886	10.1234114	10.0974611	10.2208725	2
59	9.7792953	9.9024438	9.8768515	10.1231485	10.0975562	10.2207047	1
60	9.7794630	9.9023486	9.8771144	10.1228856	10.0976514	10.2205370	0
	Sine.		Tang.		Secant.		Min.

53 Degrees.

A Table of Artificial Sines,

37 Degrees.

Min.	Sine.	Tang.	Secant.	Min.
0	9.7794630	9.8771144	10.1228856	0
1	9.7796500	9.8773772	10.1226228	1
2	9.7797981	9.8776400	10.1223600	2
3	9.7799655	9.8779027	10.1220973	3
4	9.7801328	9.8781654	10.1218346	4
5	9.7803000	9.8784281	10.1215719	5
6	9.7804671	9.8786907	10.1213093	6
7	9.7806341	9.8789533	10.1210467	7
8	9.7808010	9.8792158	10.1207841	8
9	9.7809677	9.8794782	10.1205218	9
10	9.7811344	9.8797407	10.1202593	10
11	9.7813010	9.8800031	10.1199969	11
12	9.7814675	9.8802654	10.1197346	12
13	9.7816339	9.8805277	10.1194723	13
14	9.7818002	9.8807900	10.1192100	14
15	9.7819664	9.8810522	10.1189478	15
16	9.7821324	9.8813144	10.1186856	16
17	9.7822984	9.8815765	10.1184233	17
18	9.7824643	9.8818386	10.1181614	18
19	9.7826301	9.8821007	10.1178993	19
20	9.7827958	9.8823627	10.1176373	20
21	9.7829614	9.8826246	10.1173754	21
22	9.7831268	9.8828866	10.1171134	22
23	9.7832922	9.8831484	10.1168516	23
24	9.7834575	9.8834103	10.1165897	24
25	9.7836227	9.8836721	10.1163279	25
26	9.7837878	9.8839338	10.1160662	26
27	9.7839528	9.8841956	10.1158044	27
28	9.7841177	9.8844572	10.1155428	28
29	9.7842824	9.8847189	10.1152811	29
30	9.7844471	9.8849805	10.1150195	30
	Sine.	Tang.	Secant.	Min.

52 Degrees.

Tangents and Secants.

37 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.7844 71	9.8994667	9.8849805	10.1150195	10.1005333	10.215552930
31	9.7846117	9.8993697	9.8852421	10.1147579	10.1006303	10.215388329
32	9.7847762	9.8992727	9.8855035	10.1144965	10.1007273	10.215223828
33	9.7849406	9.8991756	9.8857650	10.1142350	10.1008244	10.215059427
34	9.7851049	9.8990784	9.8860264	10.1139737	10.1009216	10.214895126
35	9.7852691	9.8989812	9.8862878	10.1137122	10.1010188	10.214730925
36	9.7854332	9.8988840	9.8865492	10.1134508	0.1011160	10.214566824
37	9.7855972	9.8987867	9.8868105	10.1131895	10.1012133	10.214402823
38	9.7857611	9.8986893	9.8870718	10.1129282	10.1013107	10.214238522
39	9.7859249	9.8985919	9.8873330	10.1126670	10.1014081	10.214075121
40	9.7860886	9.8984944	9.8875942	10.1124058	10.1015056	10.213911420
41	9.7862522	9.8983968	9.8878554	10.1121446	10.1016032	10.213747819
42	9.7864157	9.8982992	9.8881165	10.1118835	10.1017008	10.213584318
43	9.7865791	9.8982015	9.8883775	10.1116225	10.1017985	10.213420917
44	9.7867424	9.8981038	9.8886386	10.1113614	10.1018962	10.213257416
45	9.7869056	9.8980060	9.8888996	10.1111004	10.1019940	10.213094415
46	9.7870687	9.8979082	9.8891605	10.1108395	10.1020918	10.212931314
47	9.7872317	9.8978103	9.8894214	10.1105786	10.1021897	10.212768313
48	9.7873946	9.8977123	9.8896823	10.1103177	10.1022877	10.212605412
49	9.7875574	9.8976143	9.8899432	10.1100568	10.1023857	10.212442611
50	9.7877202	9.8975162	9.8902040	10.1097959	10.1024838	10.212279810
51	9.7878828	9.8974181	9.8904647	10.1095353	10.1025819	10.21211729
52	9.7880453	9.8973199	9.8907254	10.1092746	10.1026801	10.21195478
53	9.7882077	9.8972216	9.8909861	10.1090139	10.1027784	10.21179237
54	9.7883701	9.8971233	9.8912468	10.1087532	10.1028767	10.21162996
55	9.7885323	9.8970249	9.8915074	10.1084926	10.1029751	10.21146775
56	9.7886944	9.8969265	9.8917679	10.1082321	10.1030735	10.21130564
57	9.7888565	9.8968286	9.8920285	10.1079715	10.1031720	10.21114353
58	9.7890184	9.8967294	9.8922890	10.1077110	10.1032706	10.21098162
59	9.7891802	9.8966308	9.8925494	10.1074506	10.1033692	10.21081981
60	9.7893420	9.8965321	9.8928098	10.1071902	10.1034679	10.21065800
	Sine		Tang.		Secant.	Min.

52 Degrees.

A Table of Artificial Sines,

38 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
0	9.7893420	9.8965321	9.8928098	10.1071902	10.1034679	10.2106580	60
1	9.7895036	9.8964334	9.8930702	10.1069298	10.1035666	10.2104964	59
2	9.7896652	9.8963346	9.8933206	10.1066694	10.1036654	10.2103348	58
3	9.7898266	9.8962358	9.8935909	10.1064091	10.1037642	10.2101734	57
4	9.7899880	9.8961369	9.8938511	10.1061489	10.1038631	10.2100120	56
5	9.7901493	9.8960379	9.8941114	10.1058886	10.1039621	10.2098507	55
6	9.7903104	9.8959389	9.8943715	10.1056285	10.1040611	10.2096896	54
7	9.7904715	9.8958398	9.8946317	10.1053683	10.1041602	10.2095285	53
8	9.7906325	9.8957406	9.8948918	10.1051082	10.1042594	10.2093675	52
9	9.7907933	9.8956414	9.8951519	10.1048481	10.1043586	10.2092067	51
10	9.7909541	9.8955422	9.8954119	10.1045881	10.1044578	10.2090459	50
11	9.7911146	9.8954429	9.8956719	10.1043281	10.1045572	10.2088852	49
12	9.7912754	9.8953435	9.8959319	10.1040681	10.1046565	10.2087246	48
13	9.7914359	9.8952440	9.8961918	10.1038082	10.1047560	10.2085641	47
14	9.7915963	9.8951445	9.8964517	10.1035483	10.1048555	10.2084037	46
15	9.7917560	9.8950450	9.8967116	10.1032884	10.1049550	10.2082434	45
16	9.7919168	9.8949453	9.8969714	10.1030286	10.1050547	10.2080832	44
17	9.7920769	9.8948457	9.8972312	10.1027688	10.1051543	10.2079231	43
18	9.7922369	9.8947459	9.8974910	10.1025090	10.1052541	10.2077631	42
19	9.7923968	9.8946461	9.8977507	10.1022493	10.1053539	10.2076032	41
20	9.7925566	9.8945463	9.8980104	10.1019896	10.1054537	10.2074434	40
21	9.7927163	9.8944463	9.8982700	10.1017300	10.2055537	10.2072837	39
22	9.7928760	9.8943454	9.8985296	10.1014704	10.1056536	10.2071240	38
23	9.7930355	9.8942463	9.8987892	10.1012108	10.1057537	10.2069645	37
24	9.7931949	9.8941462	9.8990487	10.1009513	10.1058538	10.2068051	36
25	9.7933543	9.8940461	9.8993082	10.1006918	10.1059539	10.2066457	35
26	9.7935135	9.8939458	9.8995677	10.1004323	10.1060542	10.2064865	34
27	9.7936727	9.8938456	9.8998271	10.1001729	10.1061544	10.2063273	33
28	9.7938317	9.8937452	9.9000865	10.0999135	10.1062548	10.2061683	32
29	9.7939907	9.8936448	9.9003459	10.0996541	10.1063552	10.2060093	31
30	9.7941496	9.8935444	9.9006052	10.0993948	10.1064556	10.2058504	30
	Sine.		Tang.		Secant.		Min.

51 Degrees.

Tangents and Secants.

38 Degrees.

Min.	Sine.		Tang.		Secant.		
30	9.7941496	9.8935444	9.9086052	10.0993948	10.1064556	10.2058504	30
31	9.7943083	9.8934439	9.908645	10.0991355	10.1065561	10.2056917	29
32	9.7944670	9.8933433	9.9011237	10.0988763	10.1066567	10.2055330	28
33	9.7946256	9.8932426	9.9013830	10.0986170	10.1067574	10.2053744	27
34	9.7947841	9.8931419	9.9016422	10.0983578	10.1068581	10.2052159	26
35	9.7949425	9.8930412	9.9019013	10.0980987	10.1069588	10.2050575	25
36	9.7951008	9.8929404	9.9021604	10.0978396	10.1070596	10.2048992	24
37	9.7952590	9.8928395	9.9024195	10.0975805	10.1071605	10.2047410	23
38	9.7954171	9.8927385	9.9026786	10.0973214	10.1072615	10.2045825	22
39	9.7955751	9.8926375	9.9029376	10.0970624	10.1073625	10.2044245	21
40	9.7957330	9.8925365	9.9031966	10.0968034	10.1074635	10.2042670	20
41	9.7958909	9.8924354	9.9034555	10.0965445	10.1075646	10.2041091	19
42	9.7960486	9.8923342	9.9037144	10.0962856	10.1076658	10.2039514	18
43	9.7962062	9.8922329	9.9039733	10.0960267	10.1077671	10.2037938	17
44	9.7963638	9.8921316	9.9042321	10.0957679	10.1078684	10.2036362	16
45	9.7965212	9.8920303	9.9044910	10.0955090	10.1079697	10.2034788	15
46	9.7966786	9.8919289	9.9047497	10.0952503	10.1080711	10.2033214	14
47	9.7968359	9.8918274	9.9050085	10.0949915	10.1081726	10.2031641	13
48	9.7969930	9.8917258	9.9052672	10.0947328	10.1082742	10.2030070	12
49	9.7971501	9.8916242	9.9055259	10.0944741	10.1083758	10.2028499	11
50	9.7973071	9.8915226	9.9057845	10.0942255	10.1084774	10.2026929	10
51	9.7974640	9.8914208	9.9060431	10.0939569	10.1085792	10.2025360	9
52	9.7976208	9.8913191	9.9063017	10.0936983	10.1086809	10.2023792	8
53	9.7977775	9.8912172	9.9065603	10.0934397	10.1087828	10.2022225	7
54	9.7979341	9.8911153	9.9068188	10.0931812	10.1088847	10.2020659	6
55	9.7980906	9.8910133	9.9070773	10.0929227	10.1089867	10.2019094	5
56	9.7982470	9.8909113	9.9073357	10.0926643	10.1090887	10.2017530	4
57	9.7984034	9.8908092	9.907594	10.0924059	10.1091908	10.2015966	3
58	9.7985596	9.8907071	9.9078525	10.0921475	10.1092929	10.2014404	2
59	9.7987158	9.8906049	9.9081109	10.0918891	10.1093951	10.2012842	1
60	9.7988718	9.8905026	9.9083692	10.0916308	10.1094974	10.2011282	0
	Sine.		Tang.		Secant.		Min.

51 Degrees.

A Table of Artificial Sines,

39 Degrees.

Min.	Sine.		Tang.				
0	9.7988718	9.8905021	9.9083692	10.0916308	10.1094974	10.2011282	60
1	9.7990278	9.8904003	9.9086275	10.0913725	10.1095997	10.2009722	59
2	9.7991836	9.8902979	9.9088858	10.0911142	10.1097021	10.2008164	58
3	9.7993394	9.8901954	9.9091440	10.0908560	10.1098046	10.2006606	57
4	9.7994951	9.8900929	9.9094022	10.0905978	10.1099071	10.2005049	56
5	9.7996507	9.8899903	9.9096603	10.0903397	10.1100097	10.2003493	55
6	9.7998062	9.8898877	9.9099185	10.0900815	10.1101122	10.2001938	54
7	9.7999616	9.8897850	9.9101766	10.0898234	10.1102150	10.2000384	53
8	9.8001169	9.8896822	9.9104347	10.0895653	10.1103178	10.1998831	52
9	9.8002721	9.8895794	9.9106927	10.0893073	10.1104206	10.1997279	51
10	9.8004272	9.8894765	9.9109507	10.0890493	10.1105235	10.1995728	50
11	9.8005823	9.8893736	9.9112087	10.0887913	10.1106264	10.1994177	49
12	9.8007372	9.8892706	9.9114666	10.0885334	10.1107294	10.1992628	48
13	9.8008921	9.8891675	9.9117245	10.0882755	10.1108325	10.1991079	47
14	9.8010468	9.8890644	9.9119824	10.0880176	10.1109356	10.1989532	46
15	9.8012015	9.8889612	9.9122402	10.0877597	10.1110388	10.1987985	45
16	9.8013561	9.8888580	9.9124981	10.0875019	10.1111420	10.1986439	44
17	9.8015106	9.8887547	9.9127559	10.0872441	10.1112453	10.1984894	43
18	9.8016649	9.8886513	9.9130137	10.0869863	10.1113487	10.1983351	42
19	9.8018192	9.8885479	9.9132714	10.0867286	10.1114521	10.1981808	41
20	9.8019735	9.8884444	9.9135291	10.0864709	10.1115556	10.1980265	40
21	9.8021276	9.8883408	9.9137868	10.0862132	10.1116592	10.1978724	39
22	9.8022816	9.8882372	9.9140444	10.0859556	10.1117627	10.1977184	38
23	9.8024355	9.8881335	9.9143020	10.0856980	10.1118665	10.1975645	37
24	9.8025894	9.8880298	9.9145595	10.0854404	10.1119702	10.1974106	36
25	9.8027431	9.8879260	9.9148171	10.0851829	10.1120740	10.1972569	35
26	9.8028968	9.8878221	9.9150747	10.0849253	10.1121779	10.1971032	34
27	9.8030504	9.8877182	9.9153322	10.0846678	10.1122818	10.1969496	33
28	9.8032038	9.8876142	9.9155896	10.0844104	10.1123858	10.1967962	32
29	9.8033572	9.8875102	9.9158471	10.0841529	10.1124898	10.1966428	31
30	9.8035105	9.8874061	9.9161045	10.0838955	10.1125939	10.1964895	30
	Sine.		Tang.		Secant.	Min.	

50 Degrees.

Tangents and Secants.

39 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
30	9.8035105	9.8874061	9.9161045	10.0838955	10.1125939	10.1964895	30
31	9.8036637	9.8873019	9.9163618	10.0836382	10.1126981	10.1963363	29
32	9.8038168	9.8871977	9.9166192	10.0833808	10.1128023	10.1961832	28
33	9.8039699	9.8870934	9.9168765	10.0831235	10.1129066	10.1960301	27
34	9.8041228	9.8869890	9.9171338	10.0828662	10.1130110	10.1958772	26
35	9.8042757	9.8868846	9.9173911	10.0826089	10.1131154	10.1957243	25
36	9.8044284	9.8867801	9.9176483	10.0823517	10.1132199	10.1955716	24
37	9.8045811	9.8866756	9.9179055	10.0820945	10.1133244	10.1954189	23
38	9.8047336	9.8865710	9.9181627	10.0818373	10.1134290	10.1952664	22
39	9.8048861	9.8864663	9.9184198	10.0815802	10.1135337	10.1951139	21
40	9.8050385	9.8863616	9.9186769	10.0813231	10.1136384	10.1949615	20
41	9.8051908	9.8862568	9.9189340	10.0810660	10.1137432	10.1948092	19
42	9.8053430	9.8861519	9.9191911	10.0808089	10.1138481	10.1946570	18
43	9.8054951	9.8860470	9.9194481	10.0805519	10.1139530	10.1945049	17
44	9.8056472	9.8859420	9.9197051	10.0802949	10.1140580	10.1943528	16
45	9.8057991	9.8858370	9.9199621	10.0800379	10.1141630	10.1942008	15
46	9.8059510	9.8857319	9.9202191	10.0797809	10.1142681	10.1940490	14
47	9.8061027	9.8856267	9.9204760	10.0795240	10.1143733	10.1938973	13
48	9.8062544	9.8855215	9.9207329	10.0792671	10.1144785	10.1937456	12
49	9.8064060	9.8854162	9.9209898	10.0790102	10.1145838	10.1935940	11
50	9.8065575	9.8853109	9.9212466	10.0787534	10.1146891	10.1934425	10
51	9.8067089	9.8852055	9.9215034	10.0784966	10.1147945	10.1932911	9
52	9.8068602	9.8851000	9.9217602	10.0782398	10.1149000	10.1931398	8
53	9.8070114	9.8849945	9.9220170	10.0779830	10.1150055	10.1929886	7
54	9.8071626	9.8848889	9.9222737	10.0777263	10.1151111	10.1928374	6
55	9.8073136	9.8847832	9.9225304	10.0774696	10.1152168	10.1926864	5
56	9.8074646	9.8846775	9.9227871	10.0772129	10.1153225	10.1925354	4
57	9.8076154	9.8845717	9.9230437	10.0769563	10.1154283	10.1923846	3
58	9.8077662	9.8844659	9.9233004	10.0766996	10.1155341	10.1922338	2
59	9.8079169	9.8843599	9.9235570	10.0764430	10.1156401	10.1920831	1
60	9.8080675	9.8842540	9.9238135	10.0761865	10.1157460	10.1919325	0
	Sine		Tang.		Secant.		Min.

50 Degrees.

A Table of Artificial Sines,

40 Degrees.

Min.	Sine.	Tang.	Secant.	
0	9.8080675	9.8842540	9.9238135	10.0761865
1	9.8082180	9.8841479	9.9240701	10.0759299
2	9.8083684	9.8840418	9.9243266	10.0756734
3	9.8085188	9.8839357	9.9245831	10.0754169
4	9.8086690	9.8838294	9.9248396	10.0751604
5	9.8088192	9.8837232	9.9250960	10.0749040
6	9.8089692	9.8836168	9.9253524	10.0746476
7	9.8091192	9.8835104	9.9256088	10.0743912
8	9.8092691	9.8834039	9.9258652	10.0741348
9	9.8094189	9.8832974	9.9261215	10.0738785
10	9.8095686	9.8831908	9.9263778	10.0736222
11	9.8097182	9.8830841	9.9266341	10.0733659
12	9.8098678	9.8829774	9.9268904	10.0731096
13	9.8100172	9.8828706	9.9271466	10.0728534
14	9.8101666	9.8827638	9.9274028	10.0725972
15	9.8103159	9.8826568	9.9276590	10.0723410
16	9.8104650	9.8825499	9.9279152	10.0720848
17	9.8106141	9.8824428	9.9281713	10.0718287
18	9.8107631	9.8823357	9.9284274	10.0715726
19	9.8109121	9.8822285	9.9286835	10.0713165
20	9.8110609	9.8821213	9.9289396	10.0710604
21	9.8112096	9.8820140	9.9291956	10.0708044
22	9.8113583	9.8819067	9.9294516	10.0705484
23	9.8115069	9.8817992	9.9297076	10.0702924
24	9.8116554	9.8816918	9.9299636	10.0700364
25	9.8118038	9.8815842	9.9302195	10.0697805
26	9.8119521	9.8814756	9.9304755	10.0695245
27	9.8121003	9.8813689	9.9307310	10.0692686
28	9.8122484	9.8812612	9.9309872	10.0690128
29	9.8123965	9.8811534	9.9312431	10.0687569
30	9.8125444	9.8810455	9.9314989	10.0685011
	Sine.		Tang.	
				Secant.
				Min.

49 Degrees.

Tangents and Secants.

40 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.8125444	9.8810455	9.9314985	10.0685011	10.1189545	10.1874556 30
31	9.8126923	9.8809376	9.9317547	10.0682453	10.1190624	10.1873077 29
32	9.8128401	9.8808296	9.9320105	10.0679895	10.1191704	10.1871599 28
33	9.8129878	9.8807215	9.9322662	10.0677338	10.1192785	10.1870122 27
34	9.8131354	9.8806134	9.9325220	10.0674780	10.1193866	10.1868646 26
35	9.8132829	9.8805052	9.9327777	10.0672223	10.1194948	10.1867171 25
36	9.8134303	9.8803970	9.9330334	10.0669666	10.1196030	10.1865697 24
37	9.8135777	9.8802887	9.9332890	10.0667110	10.1197113	10.1864223 23
38	9.8137250	9.8801803	9.9335446	10.0664554	10.1198197	10.1862750 22
39	9.8138721	9.8800719	9.9338003	10.0661997	10.1199281	10.1861275 21
40	9.8140192	9.8799634	9.9340559	10.0659441	10.1200366	10.1859808 20
41	9.8141662	9.8798548	9.9343114	10.0656886	10.1201452	10.1858338 19
42	9.8143131	9.8797462	9.9345670	10.0654330	10.1202538	10.1856869 18
43	9.8144600	9.8796375	9.9348225	10.0651775	10.1203625	10.1855400 17
44	9.8146067	9.8795287	9.9350780	10.0649220	10.1204712	10.1853933 16
45	9.8147534	9.8794199	9.9353335	10.0646665	10.1205801	10.1852466 15
46	9.8148999	9.8793110	9.9355889	10.0644111	10.1206890	10.1851001 14
47	9.8150464	9.8792021	9.9358444	10.0641556	10.1207979	10.1849536 13
48	9.8151928	9.8790930	9.9360998	10.0639002	10.1209070	10.1848072 12
49	9.8153391	9.8789840	9.9363552	10.0636448	10.1210160	10.1846609 11
50	9.8154854	9.8788748	9.9366105	10.0633895	10.1211252	10.1845146 10
51	9.8156315	9.8787656	9.9368659	10.0631341	10.1212344	10.1843685 9
52	9.8157776	9.8786563	9.9371212	10.0628788	10.1213437	10.1842226 8
53	9.8159235	9.8785470	9.9373765	10.0626235	10.1214530	10.1840769 7
54	9.8160694	9.8784376	9.9376318	10.0623682	10.1215624	10.1839306 6
55	9.8162152	9.8783281	9.9378871	10.0621129	10.1216719	10.1837848 5
56	9.8163609	9.8782186	9.9381423	10.0618577	10.1217814	10.1836391 4
57	9.8165066	9.8781090	9.9383975	10.0616025	10.1218910	10.1834934 3
58	9.8166521	9.8779994	9.9386527	10.0613473	10.1220006	10.1833475 2
59	9.8167975	9.8778896	9.9389079	10.0610921	10.1221104	10.1832025 1
60	9.8169429	9.8777799	9.9391631	10.0608369	10.1222201	10.1830570 0
	Sine.		Tang.		Secant.	Min.

49 Degrees.

A Table of Artificial Sines,

41 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.8169429	9.8777799	9.9391630	10.0608359	10.1222201	10.1830571 60
1	9.8170882	9.8776700	9.9394182	10.0605818	10.1223300	10.1829118 59
2	9.8172334	9.8775601	9.9396733	10.0603267	10.1224399	10.1827665 58
3	9.8173785	9.8774501	9.9399284	10.0600716	10.1225499	10.1826215 57
4	9.8175235	9.8773401	9.9401835	10.0598165	10.1226599	10.1824765 56
5	9.8176685	9.8772300	9.9404385	10.0595615	10.1227700	10.1823315 55
6	9.8178133	9.8771198	9.9406936	10.0593064	10.1228802	10.1821867 54
7	9.8179581	9.8770096	9.9409486	10.0590514	10.1229904	10.1820419 53
8	9.8181028	9.8768993	9.9412036	10.0587964	10.1231007	10.1818972 52
9	9.8182474	9.8767889	9.9414585	10.0585415	10.1232111	10.1817526 51
10	9.8183919	9.8766785	9.9417135	10.0582865	10.1233215	10.1816081 50
11	9.8185364	9.8765680	9.9419684	10.0580316	10.1234320	10.1814636 49
12	9.8186807	9.8764574	9.9422233	10.0577767	10.1235426	10.1813193 48
13	9.8188250	9.8763468	9.9424782	10.0575218	10.1236532	10.1811750 47
14	9.8189692	9.8762361	9.9427331	10.0572669	10.1237639	10.1810308 46
15	9.8191133	9.8761253	9.9429879	10.0570121	10.1238747	10.1808867 45
16	9.8192573	9.8760145	9.9432428	10.0567572	10.1239855	10.1807427 44
17	9.8194012	9.8759036	9.9434976	10.0565024	10.1240964	10.1805988 43
18	9.8195450	9.8757927	9.9437524	10.0562476	10.1242073	10.1804550 42
19	9.8196888	9.8756816	9.9440072	10.0559928	10.1243184	10.1803112 41
20	9.8198325	9.8755706	9.9442619	10.0557381	10.1244294	10.1801675 40
21	9.8199761	9.8754594	9.9445166	10.0554834	10.1245406	10.1800239 39
22	9.8201196	9.8753482	9.9447714	10.0552286	10.1246518	10.1798804 38
23	9.8202630	9.8752369	9.9450261	10.0549739	10.1247631	10.1797370 37
24	9.8204063	9.8751256	9.9452807	10.0547193	10.1248744	10.1795937 36
25	9.8205496	9.8750142	9.9455354	10.0544646	10.1249858	10.1794504 35
26	9.8206927	9.8749027	9.9457900	10.0542100	10.1250973	10.1793073 34
27	9.8208358	9.8747912	9.9460447	10.0539553	10.1252088	10.1791642 33
28	9.8209788	9.8746795	9.9462993	10.0537007	10.1253203	10.1790212 32
29	9.8211217	9.8745679	9.9465539	10.0534461	10.1254321	10.1788783 31
30	9.8212646	9.8744561	9.9468084	10.0531916	10.1255439	10.1787354 30
		Sine.		Tang.		Secant. Min.

48 Degrees.

Tangents and Secants.

41 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
30	9.8212646	9.8744561	9.9468084	10.0531916	10.1255439	10.1787354	30
31	9.8214073	9.8743443	9.9470630	10.0529370	10.1256357	10.1785927	29
32	9.8215500	9.8742325	9.9473175	10.0526825	10.1257265	10.1784500	28
33	9.8216926	9.8741205	9.9475720	10.0524280	10.1258173	10.1783074	27
34	9.8218351	9.8740085	9.9478265	10.0521735	10.1259081	10.1781649	26
35	9.8219775	9.8738965	9.9480810	10.0519190	10.1260035	10.1780225	25
36	9.8221198	9.8737844	9.9483355	10.0516645	10.1261036	10.1778802	24
37	9.8222621	9.8736722	9.9485899	10.0514101	10.1262037	10.1777379	23
38	9.8224042	9.8735599	9.9488443	10.0511557	10.1263038	10.1775958	22
39	9.8225463	9.8734476	9.9490987	10.0509013	10.1264039	10.1774537	21
40	9.8226883	9.8733352	9.9493531	10.0506469	10.1265040	10.1773117	20
41	9.8228302	9.8732227	9.9496075	10.0503925	10.1266041	10.1771698	19
42	9.8229721	9.8731102	9.9498619	10.0501381	10.1267042	10.1770279	18
43	9.8231138	9.8729976	9.9501162	10.0498838	10.1268043	10.1768862	17
44	9.8232555	9.8728849	9.9503705	10.0496293	10.1269044	10.1767445	16
45	9.8233971	9.8727722	9.9506248	10.0493752	10.1270045	10.1766029	15
46	9.8235386	9.8726594	9.9508791	10.0491207	10.1271046	10.1764614	14
47	9.8236800	9.8725466	9.9511334	10.0488665	10.1272047	10.1763200	13
48	9.8238213	9.8724337	9.9513876	10.0486123	10.1273048	10.1761787	12
49	9.8239626	9.8723207	9.9516419	10.0483582	10.1274049	10.1760374	11
50	9.8241037	9.8722076	9.9518951	10.0481040	10.1275050	10.1758963	10
51	9.8242448	9.8720945	9.9521503	10.0478497	10.1276051	10.1757552	9
52	9.8243858	9.8719813	9.9524045	10.0475955	10.1277052	10.1756142	8
53	9.8245267	9.8718681	9.9526587	10.0473413	10.1278053	10.1754733	7
54	9.8246676	9.8717548	9.9529128	10.0470872	10.1279054	10.1753324	6
55	9.8248083	9.8716414	9.9531670	10.0468330	10.1280055	10.1751917	5
56	9.8249490	9.8715279	9.9534211	10.0465789	10.1281056	10.1750510	4
57	9.8250896	9.8714144	9.9536752	10.0463248	10.1282057	10.1749104	3
58	9.8252301	9.8713008	9.9539293	10.0460707	10.1283058	10.1747699	2
59	9.8253705	9.8711872	9.9541834	10.0458166	10.1284059	10.1746295	1
60	9.8255109	9.8710735	9.9544374	10.0455626	10.1285060	10.1744891	0
	Sine.		Tang.		Secant.		

48 Degrees.

A Table of Artificial Sines,

42 Degrees.

Min.	Sine.		Tang.		Secant.		
0	9.8255109	9.8710735	9.9544374	10.0455626	10.1289265	10.1744891	60
1	9.8256512	9.8709597	9.9546915	10.0453085	10.1290403	10.1743488	59
2	9.8257913	9.8708458	9.9549455	10.0450545	10.1291542	10.1742087	58
3	9.8259314	9.8707319	9.9551997	10.0448005	10.1292681	10.1740686	57
4	9.8260715	9.8706179	9.9554535	10.0445465	10.1293821	10.1739285	56
5	9.8262114	9.8705039	9.9557075	10.0442925	10.1294961	10.1737886	55
6	9.8263512	9.8703898	9.9559615	10.0440385	10.1296102	10.1736488	54
7	9.8264910	9.8702756	9.9562154	10.0437846	10.1297244	10.1735090	53
8	9.8266307	9.8701613	9.9564694	10.0435307	10.1298387	10.1733693	52
9	9.8267703	9.8700470	9.9567233	10.0432767	10.1299530	10.1732297	51
10	9.8269098	9.8699326	9.9569772	10.0430228	10.1300674	10.1730902	50
11	9.8270493	9.8698182	9.9572312	10.0427689	10.1301818	10.1729507	49
12	9.8271887	9.8697037	9.9574850	10.0425150	10.1302963	10.1728113	48
13	9.8273279	9.8695891	9.9577389	10.0422611	10.1304109	10.1726721	47
14	9.8274671	9.8694744	9.9579927	10.0420073	10.1305256	10.1725329	46
15	9.8276063	9.8693597	9.9582465	10.0417535	10.1306403	10.1723937	45
16	9.8277453	9.8692449	9.9585004	10.0414996	10.1307551	10.1722547	44
17	9.8278843	9.8691301	9.9587542	10.0412458	10.1308699	10.1721157	43
18	9.8280231	9.8690152	9.9590080	10.0409920	10.1309848	10.1719769	42
19	9.8281619	9.8689002	9.9592628	10.0407382	10.1310998	10.1718381	41
20	9.8283006	9.8687851	9.9595155	10.0404845	10.1312149	10.1716994	40
21	9.8284393	9.8686700	9.9597693	10.0402307	10.1313300	10.1715607	39
22	9.8285778	9.8685548	9.9600230	10.0399770	10.1314452	10.1714222	38
23	9.8287163	9.8684396	9.9602767	10.0397233	10.1315604	10.1712837	37
24	9.8288547	9.8683242	9.9605305	10.0394695	10.1316758	10.1711453	36
25	9.8289930	9.8682088	9.9607842	10.0392158	10.1317912	10.1710070	35
26	9.8291312	9.8680934	9.9610378	10.0389622	10.1319066	10.1708688	34
27	9.8292694	9.8679779	9.9612915	10.0387085	10.1320221	10.1707306	33
28	9.8294075	9.8678623	9.9615452	10.0384548	10.1321377	10.1705925	32
29	9.8295454	9.8677466	9.9617988	10.0382012	10.1322534	10.1704546	31
30	9.8296833	9.8676309	9.9620525	10.0379475	10.1323691	10.1703167	30
	Sine		Tang.		Secant.		Min.

47 Degrees.

Tangents and Secants.

42 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
30	9.8296833	9.8676309	9.9620525	10.0379475	10.1323691	10.1703167	30
31	9.8298212	9.8675151	9.9623061	10.0376939	10.1324849	10.1701788	29
32	9.8299589	9.8673992	9.9625597	10.0374403	10.1326008	10.1700411	28
33	9.8300966	9.8672833	9.9628133	10.0371867	10.1327167	10.1699034	27
34	9.8302342	9.8671673	9.9630669	10.0369331	10.1328327	10.1697658	26
35	9.8303717	9.8670512	9.9633204	10.0366796	10.1329488	10.1696283	25
36	9.8305091	9.8669351	9.9635740	10.0364260	10.1330649	10.1694909	24
37	9.8306464	9.8668189	9.9638275	10.0361725	10.1331811	10.1693536	23
38	9.8307837	9.8667026	9.9640811	10.0359189	10.1332974	10.1692163	22
39	9.8309209	9.8665863	9.9643346	10.0356654	10.1334137	10.1690791	21
40	9.8310580	9.8664699	9.9645881	10.0354119	10.1335301	10.1689420	20
41	9.8311950	9.8663534	9.9648416	10.0351584	10.1336466	10.1688050	19
42	9.8313320	9.8662369	9.9650951	10.0349049	10.1337631	10.1686680	18
43	9.8314688	9.8661203	9.9653486	10.0346514	10.1338797	10.1685312	17
44	9.8316056	9.8660036	9.9656020	10.0343980	10.1339964	10.1683944	16
45	9.8317423	9.8658868	9.9658555	10.0341445	10.1341132	10.1682577	15
46	9.8318789	9.8657700	9.9661089	10.0338911	10.1342300	10.1681211	14
47	9.8320155	9.8656531	9.9663623	10.0336377	10.1343469	10.1679845	13
48	9.8321519	9.8655362	9.9666157	10.0333843	10.1344638	10.1678481	12
49	9.8322883	9.8654192	9.9668692	10.0331308	10.1345808	10.1677117	11
50	9.8324246	9.8653021	9.9671225	10.0328775	10.1346979	10.1675754	10
51	9.8325609	9.8651849	9.9673759	10.0326241	10.1348151	10.1674391	9
52	9.8326970	9.8650677	9.9676293	10.0323707	10.1349323	10.1673030	8
53	9.8328331	9.8649504	9.9678827	10.0321173	10.1350496	10.1671669	7
54	9.8329691	9.8648331	9.9681360	10.0318640	10.1351669	10.1670309	6
55	9.8331050	9.8647156	9.9683893	10.0316107	10.1352844	10.1668950	5
56	9.8332408	9.8645981	9.9686427	10.0313573	10.1354019	10.1667592	4
57	9.8333766	9.8644806	9.9688960	10.0311040	10.1355194	10.1666234	3
58	9.8335122	9.8643629	9.9691493	10.0308507	10.1356371	10.1664878	2
59	9.8336478	9.8642452	9.9694026	10.0305974	10.1357548	10.1663522	1
60	9.8337833	9.8641275	9.9696559	10.0303441	10.1358725	10.1662167	0
	Sine.		Tang.		Secant.		

47 Degrees.

A Table of Artificial Sines,

43 Degrees.

Min.	Sine.		Tang.		Secant.	
0	9.8337833	9.8641275	9.9696559	10.0303441	10.1358725	10.1662167 60
1	9.8339188	9.8640091	9.9699091	10.0300909	10.1359904	10.16608 2 59
2	9.8340541	9.8638917	9.9701624	10.0298376	10.1361083	10.1659459 58
3	9.8341894	9.8637737	9.9704157	10.0295843	10.1362263	10.1658106 57
4	9.8343246	9.8636557	9.9706689	10.0293311	10.1363443	10.1656754 56
5	9.8344597	9.8635376	9.9709221	10.0290779	10.1364624	10.1655403 55
6	9.8345948	9.8634194	9.9711754	10.0288246	10.1365806	10.1654052 54
7	9.8347297	9.8633011	9.9714286	10.0285714	10.1366989	10.1652703 53
8	9.8348646	9.8631828	9.9716818	10.0283182	10.1368172	10.1651354 52
9	9.8349994	9.8630644	9.9719350	10.0280650	10.1369356	10.1650006 51
10	9.8351341	9.8629460	9.9721882	10.0278118	10.1370540	10.1648659 50
11	9.8352688	9.8628274	9.9724413	10.0275587	10.1371726	10.1647312 49
12	9.8354033	9.8627088	9.9726945	10.0273055	10.1372912	10.1645967 48
13	9.8355378	9.8625902	9.9729477	10.0270523	10.1374098	10.1644622 47
14	9.8356722	9.8624714	9.9732008	10.0267992	10.1375285	10.1643278 46
15	9.8358066	9.8623526	9.9734539	10.0265461	10.1376474	10.1641934 45
16	9.8359408	9.8622338	9.9737071	10.0262929	10.1377662	10.1640592 44
17	9.8360750	9.8621148	9.9739602	10.0260398	10.1378852	10.1639250 43
18	9.8362091	9.8619958	9.9742133	10.0257867	10.1380042	10.1637909 42
19	9.8363431	9.8618767	9.9744664	10.0255336	10.1381233	10.1636569 41
20	9.8364771	9.8617576	9.9747195	10.0252805	10.1382424	10.1635229 40
21	9.8366109	9.8616383	9.9749726	10.0250274	10.1383617	10.1633891 39
22	9.8367447	9.8615190	9.9752257	10.0247743	10.1384810	10.1632553 38
23	9.8368784	9.8613997	9.9754787	10.0245213	10.1386003	10.1631216 37
24	9.8370121	9.8612803	9.9757318	10.0242682	10.1387197	10.1629879 36
25	9.8371456	9.8611608	9.9759849	10.0240151	10.1388392	10.1628544 35
26	9.8372791	9.8610412	9.9762379	10.0237621	10.1389588	10.1627209 34
27	9.8374125	9.8609215	9.9764509	10.0235091	10.1390785	10.1625875 33
28	9.8375458	9.8608018	9.9766740	10.0232560	10.1391982	10.1624542 32
29	9.8376790	9.8606821	9.9769970	10.0230030	10.1393179	10.1623210 31
30	9.8378122	9.8605622	9.9772500	10.0227500	10.1394378	10.1621878 30
	Sine.		Tang.		Secant.	Min.

46 Degrees.

Tangents and Secants.

43 Degrees.

Min.	Sine.		Tang.		Secant.		Min.
30	9.8378122	9.8605622	9.9772500	10.0227500	10.139437	10.1621878	30
31	9.8379453	9.8604423	9.9775030	10.0224970	10.1395377	10.1620347	29
32	9.8380783	9.8603223	9.9777560	10.0222440	10.1395777	10.1619217	28
33	9.8382112	9.8602022	9.9780090	10.0219910	10.1397978	10.1617888	27
34	9.8383441	9.8600821	9.9782620	10.0217380	10.1399179	10.1616559	26
35	9.8384769	9.8599619	9.9785149	10.0214851	10.1400381	10.1615231	25
36	9.8386096	9.8598416	9.9787679	10.0212321	10.1401584	10.1613904	24
37	9.8387422	9.8597213	9.9790209	10.0209791	10.1402787	10.1612578	23
38	9.8388747	9.8596009	9.9792738	10.0207262	10.1403991	10.1611253	22
39	9.8390072	9.8594804	9.9795268	10.0204732	10.1405196	10.1609928	21
40	9.8391396	9.8593599	9.9797797	10.0202203	10.1406401	10.1608604	20
41	9.8392719	9.8592393	9.9800326	10.0199674	10.1407607	10.1607281	19
42	9.8394041	9.8591186	9.9802856	10.0197144	10.1408814	10.1605959	18
43	9.8395363	9.8589978	9.9805385	10.0194615	10.1410022	10.1604637	17
44	9.8396684	9.8588770	9.9807914	10.0192086	10.1411230	10.1603316	16
45	9.8398004	9.8587561	9.9810443	10.0189557	10.1412439	10.1601996	15
46	9.8399323	9.8586351	9.9812972	10.0187028	10.1413649	10.1600677	14
47	9.8400642	9.8585141	9.9815501	10.0184499	10.1414859	10.1599358	13
48	9.8401959	9.8583929	9.9818030	10.0181970	10.1416071	10.1598041	12
49	9.8403276	9.8582718	9.9820559	10.0179441	10.1417282	10.1596724	11
50	9.8404593	9.8581505	9.9824087	10.0176913	10.1418495	10.1595407	10
51	9.8405908	9.8580292	9.9825616	10.0174384	10.1419708	10.1594092	9
52	9.8407223	9.8579078	9.9828145	10.0171855	10.1420922	10.1592777	8
53	9.8408537	9.8577863	9.9830673	10.0169327	10.1422137	10.1591463	7
54	9.8409850	9.8576648	9.9833202	10.0166798	10.1423352	10.1590150	6
55	9.8411162	9.8575432	9.9835730	10.0164270	10.1424568	10.1588838	5
56	9.8412474	9.8574215	9.9838259	10.0161741	10.1425785	10.1587526	4
57	9.8413785	9.8572998	9.9840787	10.0159213	10.1427002	10.1586215	3
58	9.8415095	9.8571779	9.9843315	10.0156685	10.1428221	10.1584905	2
59	9.8416404	9.8570561	9.9845844	10.0154156	10.1429439	10.1583596	1
60	9.8417713	9.8569341	9.9848372	10.0151628	10.1430659	10.1582287	0
	Sine.		Tang.		Secant.		Min.

46 Degrees.

A Table of Artificial Sines,

44 Degrees.

N.	Sine.		Tang.		Secant.		N.
0	9.8417713	9.8569341	9.9848972	10.0151628	10.1430655	10.1582287	60
1	9.8419021	9.8568121	9.9850900	10.0149100	10.1431875	10.1580979	59
2	9.8420328	9.8566900	9.9853428	10.0146572	10.1433100	10.1579672	58
3	9.8421634	9.8565678	9.9855956	10.0144044	10.1434322	10.1578366	57
4	9.8422939	9.8564455	9.9858484	10.0141516	10.1435545	10.1577061	56
5	9.8424244	9.8563232	9.9861012	10.0138988	10.1436768	10.1575755	55
6	9.8425548	9.8562008	9.9863540	10.0136460	10.1437992	10.1574452	54
7	9.8426851	9.8560784	9.9866068	10.0133932	10.1439216	10.1573149	53
8	9.8428154	9.8559558	9.9868596	10.0131404	10.1440442	10.1571846	52
9	9.8429456	9.8558332	9.9871123	10.0128877	10.1441668	10.1570544	51
10	9.8430757	9.8557106	9.9873651	10.0126349	10.1442894	10.1569243	50
11	9.8432057	9.8555878	9.9876179	10.0123821	10.1444122	10.1567943	49
12	9.8433356	9.8554650	9.9878706	10.0121294	10.1445350	10.1566644	48
13	9.8434655	9.8553421	9.9881234	10.0118766	10.1446579	10.1565345	47
14	9.8435953	9.8552192	9.9883761	10.0116239	10.1447808	10.1564047	46
15	9.8437250	9.8550961	9.9886289	10.0113711	10.1449039	10.1562750	45
16	9.8438547	9.8549730	9.9888816	10.0111184	10.1450270	10.1561452	44
17	9.8439842	9.8548499	9.9891344	10.0108656	10.1451501	10.1560158	43
18	9.8441137	9.8547266	9.9893871	10.0106129	10.1452734	10.1558863	42
19	9.8442432	9.8546033	9.9896399	10.0103601	10.1453967	10.1557568	41
20	9.8443725	9.8544799	9.9898926	10.0101074	10.1455200	10.1556273	40
21	9.8445018	9.8543564	9.9901453	10.0098547	10.1456436	10.1554982	39
22	9.8446310	9.8542329	9.9903981	10.0096019	10.1457671	10.1553690	38
23	9.8447601	9.8541093	9.9906508	10.0093492	10.1458907	10.1552399	37
24	9.8448891	9.8539856	9.9909035	10.0090965	10.1460144	10.1551109	36
25	9.8450181	9.8538619	9.9911562	10.0088438	10.1461381	10.1549819	35
26	9.8451470	9.8537381	9.9914089	10.0085911	10.1462619	10.1548530	34
27	9.8452758	9.8536142	9.9916616	10.0083384	10.1463858	10.1547242	33
28	9.8454045	9.8534902	9.9919143	10.0080857	10.1465098	10.1545955	32
29	9.8455332	9.8533660	9.9921670	10.0078330	10.1466338	10.1544668	31
30	9.8456618	9.8532418	9.9924197	10.0075803	10.1467579	10.1543382	30
	Sine.		Tang.		Secant.		N.

45 Degrees.

Tangents and Secants.

44 Degrees.

Min.	Sine.		Tang.		Secant.	
30	9.8456618	9.8532421	9.9924197	10.0075803	10.1467579	10.1543382 30
31	9.8457903	9.8531179	9.9926724	10.0073276	10.1468821	10.1542097 29
32	9.8459188	9.8529936	9.9929251	10.0070749	10.1470064	10.1540812 28
33	9.8460471	9.8528693	9.9931778	10.0068222	10.1471307	10.1539529 27
34	9.8461754	9.8527449	9.9934305	10.0065695	10.1472551	10.1538240 26
35	9.8463036	9.8526204	9.9936832	10.0063168	10.1473796	10.1536964 25
36	9.8464318	9.8524959	9.9939359	10.0060641	10.1475041	10.1535682 24
37	9.8465599	9.8523713	9.9941886	10.0058114	10.1476287	10.1534401 23
38	9.8466879	9.8522466	9.9944413	10.0055587	10.1477534	10.1533121 22
39	9.8468158	9.8521218	9.9946940	10.0053060	10.1478782	10.1531842 21
40	9.8469436	9.8519970	9.9949466	10.0050534	10.1480030	10.1530564 20
41	9.8470714	9.8518721	9.9951993	10.0048007	10.1481279	10.1529286 19
42	9.8471991	9.8517471	9.9954520	10.0045480	10.1482529	10.1528009 18
43	9.8473267	9.8516220	9.9957047	10.0042953	10.1483780	10.1526733 17
44	9.8474543	9.8514969	9.9959573	10.0040427	10.1485031	10.1525457 16
45	9.8475817	9.8513717	9.9962100	10.0037900	10.1486283	10.1524183 15
46	9.8477091	9.8512465	9.9964627	10.0035373	10.1487539	10.1522909 14
47	9.8478365	9.8511211	9.9967154	10.0032846	10.1488789	10.1521635 13
48	9.8479637	9.8509957	9.9969680	10.0030320	10.1490043	10.1520363 12
49	9.8480909	9.8508702	9.9972207	10.0027793	10.1491298	10.1519091 11
50	9.8482180	9.8507446	9.9974734	10.0025266	10.1492554	10.1517820 10
51	9.8483450	9.8506190	9.9977260	10.0022740	10.1493810	10.1516550 9
52	9.8484720	9.8504933	9.9979787	10.0020213	10.1495067	10.1515280 8
53	9.8485989	9.8503675	9.9982314	10.0017686	10.1496325	10.1514011 7
54	9.8487257	9.8502417	9.9984840	10.0015160	10.1497583	10.1512743 6
55	9.8488524	9.8501157	9.9987367	10.0012633	10.1498843	10.1511476 5
56	9.8489791	9.8499897	9.9989893	10.0010107	10.1500163	10.1510209 4
57	9.8491057	9.8498637	9.9992420	10.0007580	10.1501363	10.1508943 3
58	9.8492322	9.8497375	9.9994947	10.0005053	10.1502625	10.1507678 2
59	9.8493585	9.8496113	9.9997473	10.0002527	10.1503887	10.1506414 1
60	9.8494850	9.8494850	10.0000000	10.0000000	10.1505150	10.1505150 0
	Sine.		Tang.		Secant.	Min.

45 Degrees.

A Table of Angles, which every Rhomb (or Point of the
the Compass) maketh with the Meridian.

North.	South.	Points.	D.	M.	North.	South.
		$\frac{1}{4}$	02	49		
		$\frac{1}{2}$	05	37		
		$\frac{3}{4}$	08	26		
<u>N. by E.</u>	<u>S. by East</u>	1	11	15	<u>N. by W.</u>	<u>S. by W.</u>
		$\frac{1}{4}$	14	04		
		$\frac{1}{2}$	16	52		
		$\frac{3}{4}$	19	41		
<u>N. N. E.</u>	<u>S. S. E.</u>	2	22	30	<u>N. N. W.</u>	<u>S. S. W.</u>
		$\frac{1}{4}$	25	19		
		$\frac{1}{2}$	28	07		
		$\frac{3}{4}$	30	56		
<u>N. E. by N.</u>	<u>S. E. by E.</u>	3	33	45	<u>N. W. by N.</u>	<u>S. W. by S.</u>
		$\frac{1}{4}$	36	34		
		$\frac{1}{2}$	39	22		
		$\frac{3}{4}$	42	11		
<u>No. East</u>	<u>So. East.</u>	4	45	00	<u>No. West.</u>	<u>So. West.</u>
		$\frac{1}{4}$	47	49		
		$\frac{1}{2}$	50	37		
		$\frac{3}{4}$	43	26		
<u>N. E. by E.</u>	<u>S. E. by E.</u>	5	56	15	<u>N. W. by W.</u>	<u>S. W. by W.</u>
		$\frac{1}{4}$	59	04		
		$\frac{1}{2}$	61	52		
		$\frac{3}{4}$	64	42		
<u>E. N. E.</u>	<u>E. S. E.</u>	6	67	30	<u>W. N. W.</u>	<u>W. S. W.</u>
		$\frac{1}{4}$	70	19		
		$\frac{1}{2}$	73	07		
		$\frac{3}{4}$	75	56		
<u>E. by N.</u>	<u>E. by S.</u>	7	78	45	<u>W. by N.</u>	<u>W. by S.</u>
		$\frac{1}{4}$	81	34		
		$\frac{1}{2}$	84	22		
		$\frac{3}{4}$	87	11		
<u>East.</u>	<u>East.</u>	8	90	00	<u>West.</u>	<u>West.</u>

P I N T S.